

# Energy Forward Price Prediction with a Hybrid Adaptive Model

Hang T. Nguyen and Ian T. Nabney

**Abstract**—This paper presents a forecasting technique for forward electricity/gas prices, one day ahead. This technique combines a Kalman filter (KF) and a generalised autoregressive conditional heteroschedasticity (GARCH) model (often used in financial forecasting). The GARCH model is used to compute next value of a time series. The KF updates parameters of the GARCH model when the new observation is available. This technique is applied to real data from the UK energy markets to evaluate its performance. The results show that the forecasting accuracy is improved significantly by using this hybrid model. The methodology can be also applied to forecasting market clearing prices and electricity/gas loads.

## I. INTRODUCTION

ACCURATE electricity/gas price forecasting is very important for traders in the energy market, especially energy generators. If an energy generator makes an accurate forecast of the market price, it can develop a strategy to maximise its own profits and minimise risk due to price spikes by appropriate trading in forward contracts. It can also plan its actions to maximise benefits or utilities by reducing/increasing its generation. Energy suppliers can use short-term price forecasts to adjust their bidding strategies to achieve the maximum benefit. In addition, understanding the process of forward price development can help the generators make money on the forward market.

The relevant literature on energy price forecasting issues includes a wide range of methods. Many approaches based on time series models have been used for price forecasting, such as threshold auto-regressive switching (TAR) models [1], AR models [2], autoregressive integrated moving average (ARIMA) models [3], [4], and GARCH [5], [6]. Moreover, neural networks (NNs) are used widely for electricity price forecasting in the literature [7]. Due to the complexity of the environment, the functional relationships we are looking for might be non-linear. Several researchers have proposed additional procedures to improve accuracy. Pre-processing procedures and regularisation methods are used in [7]. Another approach for improving forecasting performance is multiple NNs. The use of a committee of NNs for forecasting is suggested in [8]. Similarly, cascaded neural networks are proposed in [9]. The use of Input/Output Hidden Markov Model (IOHMM) to combine two NNs which estimate underlying market states and observed price respectively are suggested in [10].

However, forecasting energy prices presents a number of challenges because of the volatility characteristic of prices,

especially in competitive environments [5]. To overcome this problem, some researchers have proposed a hybrid form of forecasting models, which are the combination of Kalman filter/Extend Kalman Filter (EKF) and prediction models, such as Radial Basic Function (RBF), Multilayer perceptrons (MLP), linear regression (LR), or financial models. The forecast models are used to forecast next-day price, and KF/EKF updated parameters of these models as the new value of price are observed. Niranjana [11] used EKF algorithm to recursively reestimate parameters of the Black-Scholes model from observations (the Black-Scholes model is well-known financial formula for approximate option price). Nabney et al. [12] showed that an EKF used for online-learning parameters of RBF model give much better tracking of non-stationary data than a fixed RBF model. Some researchers proposed a training method, which used an EKF in order to train MLP network. The simulation results on predicting exchange rate [13], positioning a GSM mobile phone in real-time [14], estimate wind turbine power generation [15], and predicting New England electricity price [16] show that this method is good in the speed of learning and the accuracy of mapping. Parameters of linear models were also estimated using a KF in [17], [18].

This paper uses the combination of KF and GARCH model. This model is applied in forecasting forward electricity/gas price in the UK market. We compare the prediction performance of three methods:

- *Method 1*: a random walk model, which is used as a benchmark.
- *Method 2*: fixed GARCH model, i.e. model whose parameters are fixed after training on a subset of the data set.
- *Method 3*: a combination of KF and GARCH model, where parameters of GARCH model are adapted continuously on the test set using KF.

Compared with previous work, our paper has the following contributions. Firstly, we propose a framework for an adaptive GARCH model and apply it for electricity/gas price forecasting problem. Secondly, besides historical price data, a number of exogenous variables, for example, electricity/gas demand, temperature, exchange rate (USD:GBP) etc, are also considered as candidates for input variables. Some pre-processing procedures are used to choose the relevant input variables for each forecasting model.

This paper is organised as follows. Section II provides the detailed forecasting framework. In Section III, the detail of the hybrid model is presented. The numerical results on data from the UK electricity/gas market are given in Section IV. Section V provides some conclusions.

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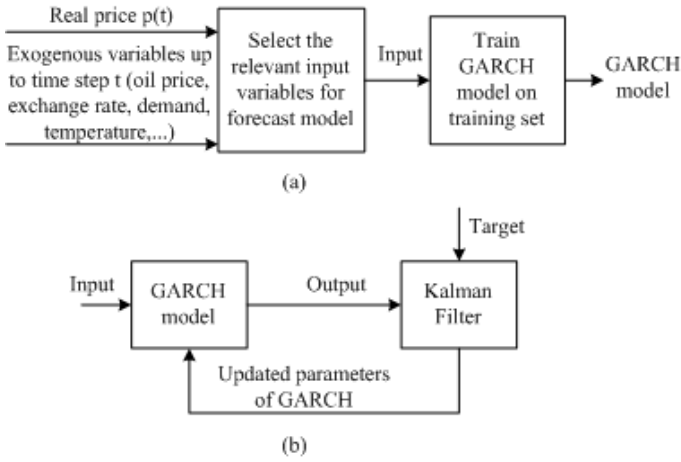


Fig. 1. The combination model of GARCH and KF. (a) Training phase, (b) Test phase.

## II. FORECASTING FRAMEWORK

The framework of Method 3 for forecasting electricity/gas prices of forward contracts is shown in Figure 1. A data set is divided into two subsets: (1) a training set to train the models and (2) a test set to evaluate these models by calculating their errors.

- Training phase:

*Step 1:* Determine the input vectors for GARCH model. In addition to historical price data, there is a large number of observable variables which are potential inputs. However, only some of them are relevant. Using irrelevant variables as inputs might reduce the performance of the forecasting models. Therefore, selecting correct inputs for each type of model is very important. In the this phase, various measures were used to determine the relevant input variables, including the correlation matrix (CM), autocorrelation function (ACF), and partial autocorrelation function (PACF).

*Step 2:* The training sets are used to estimate parameters of GARCH models. We can use maximum likelihood to train the model with an iterative non-linear optimisation algorithm.

- Test phase: Two steps are recursively repeated.

*Step 1:* When the new observation is available, the Kalman Filter updates parameters of the GARCH model.

*Step 2:* Use the GARCH model with the latest estimated parameters to predict the next-day price.

## III. COMBINATION MODEL

### A. GARCH

In several forecast model, such as MLP, RBF or LR, the errors are assumed to be homoscedastic (i.e., the variance of the residual is assumed to be independent of time). GARCH [19] can be used to model changes in the variance of the errors as a function of time. The GARCH( $r, m$ ) model is given by:

$$y_t = \beta_0 + \hat{\beta}x_t + \varepsilon_t \quad (1)$$

$$\varepsilon_t = \sqrt{n_t}e_t, \quad e_t \sim D(0, 1) \quad (2)$$

$$n_t = \alpha_0 + \sum_{i=1}^m \alpha_i \varepsilon_{t-i}^2 + \sum_{j=1}^r \gamma_j n_{t-j}, \quad (3)$$

with constraints:

$$\alpha_i, \gamma_j > 0, \quad \sum_{i=1}^m \alpha_i + \sum_{j=1}^r \gamma_j < 1, \quad (4)$$

where  $x_t$ ,  $y_t$ , and  $\varepsilon_t$  represent the input vector, output vector, and error of the model respectively,  $n_t$  is variance of error  $\varepsilon_t$ ,  $\beta = \{\beta_0, \hat{\beta}\}$  is parameters vector for the AR process,  $m$  and  $r$  are order of ARCH process and AR for the variance  $n_t$  respectively.

$e_t$  is i.i.d, with  $E(e_t) = 0$  and  $var(e_t) = 1$ .  $e_t$  can be a Gaussian or Student-T distribution. GARCH is a generalisation of a linear time series model with homoscedastic disturbances in which the variance  $n_t$  of the noise varies with information about errors and its variance up to time  $t$ .

We can train a GARCH model using maximum likelihood. To deal with the constraints (4), we used penalty function method to optimise the model.

### B. Kalman Model

1) *State space models:* The Kalman Filter is based on a state space model; we assume that the observed time series  $y_t \in R^p$  is a function of random variables  $x_t \in R^k$  which are not observed.

$$y_t = H_t x_t + v_t, \quad (5)$$

where  $v_t \in R^p$  is assumed to be Gaussian noise  $N(0, R)$ ,  $y_t$  is the output of the model,  $x_t$  is the hidden state vector. The  $p \times k$  matrix  $H_t$  is the output matrix. Equation (5) represents the output function. We assume that the dynamics of the hidden state space is given by

$$x_{t+1} = F_t x_t + w_t, \quad (6)$$

where the  $k \times k$  matrix  $F_t$  forms the parameters of the model and  $w_t$  is zero-mean Gaussian noise with covariance  $Q$ . Equation (6) represents the state transition function. The hidden state vector obeys the Markov independence property (i.e. the current state depends only on the previous state).

$x_0$  is the system initial condition, modelled as a Gaussian random vector  $x_0 \sim N(\pi_1, P_1)$ . Equation (6) shows that if  $p(x_t)$  is Gaussian, then so is  $p(x_{t+1})$ .

2) *Kalman Filter:* The Kalman Filter [20] is a recursive algorithm used to compute the probability of the current hidden state space  $x_t$  given the sequence of observations up to time  $t$ . One iteration of the KF is composed of the following consecutive steps:

- Prediction:

$$\begin{aligned} x_t^{t-1} &= F_t x_{t-1}^{t-1} \\ P_t^{t-1} &= F_t P_{t-1}^{t-1} F_t' + Q. \end{aligned}$$

- Update

$$\begin{aligned} K_t &= P_t^{t-1} H_t' (H_t P_t^{t-1} H_t' + R_t)^{-1} \\ x_t^t &= x_t^{t-1} + K_t (y_t - H_t x_t^{t-1}) \\ P_t^t &= (I - K_t H_t) P_t^{t-1}, \end{aligned}$$

where:

$$\begin{aligned} x_t^t &= E[x_t|y_1, \dots, y_t] \\ x_t^{t-1} &= E[x_t|y_1, \dots, y_{t-1}] \\ P_t^t &= E[(x_t - x_t^t)(x_t - x_t^t)'|y_1, \dots, y_t] \\ P_t^{t-1} &= E[(x_t - x_t^{t-1})(x_t - x_t^{t-1})'|y_1, \dots, y_{t-1}], \end{aligned}$$

where  $x_t^{t-1}$  is the *a priori* state estimate at time step  $t$  given knowledge of the process prior to step  $t$ , and  $x_t^t$  is an *a posteriori* state estimate at time step  $t$  given measurement  $y_t$ . The matrices  $P_t^{t-1}$  and  $P_t^t$  are *a priori* estimate error covariance and the *a posteriori* estimate error covariance respectively.

In the prediction phase, the *a priori* state estimate  $x_t^{t-1}$  and the *a priori* estimate error covariance  $P_t^{t-1}$  are computed forward from time step  $t-1$  to step  $t$ . In the update phase, we assume that we have measured the process to obtain  $y_t$ . Firstly, the Kalman gain  $K_t$  is computed. Then the *a posteriori* state estimate  $x_t^t$  and the *a posteriori* estimate error covariance  $P_t^t$  are calculated. The initial values are  $x_1^0 = \pi_1$  and  $P_1^0 = P_1$ .

### C. Combination of GARCH and Kalman filter

In a fixed GARCH model, its parameters are estimated using the training set only, and the test set is not used to adjust parameters. This constraint may reduce the forecast accuracy, especially in predicting non-stationary data. To overcome this, the KF can be used to update parameters of a GARCH model by treating the weights as the states of an unforced linear dynamical system. This can be considered as an estimation problem where the weight values are unknown and have to be estimated. A little noise is added to the existing state estimate. Denote the vector of GARCH parameters which need to be updated by  $\theta$ , then the evolution equation of GARCH parameters is given by

$$\theta_t = \theta_{t-1} + \omega_t, \quad \omega_t \sim N(0, Q).$$

The other parameters of the Kalman filter can be derived from the GARCH model. We consider two solutions of combination of GARCH and Kalman Filter as follows.

1) *Solution 1*: In this solution, all parameters of GARCH model are set on training set, with exception of the bias  $\beta_0$  which is adjusted on-line on the test set. Denote  $\delta = \{\alpha_0, \dots, \alpha_m, \gamma_1, \dots, \gamma_r\}$

- **On the training set**: we use maximum likelihood to compute GARCH parameters, denoted  $\beta(0)$ ,  $\delta(0)$ .
- **On the test set**: two steps are recursively repeated.

*Step 1*: Update parameters of the GARCH model using the KF. We fixed the value  $\delta(t) = \delta(0)$  and  $\hat{\beta}(t) = \hat{\beta}(0)$ , and used a KF to update value of  $\beta_0(t)$ . The KF is given by

$$\begin{aligned} \beta_0(t) &= \beta_0(t-1) + \omega(t), \quad \omega(t) \sim N(0, Q) \\ y_t &= \beta_0(t) + \hat{\beta}(0)x_t + \varepsilon_t \quad \varepsilon_t \sim N(0, n_t) \\ n_t &= \alpha_0(0) + \sum_{i=1}^m \alpha_i(0)\varepsilon_{t-i}^2 + \sum_{j=1}^r \gamma_j(0)n_{t-j}. \end{aligned}$$

Parameters  $\Omega = \{Q, P_1\}$  of the Kalman Filter can be estimated by using maximum log likelihood (using the Kalman

smoother) [21], or just initialised to relatively small values. Other parameters of KF are given by

$$\begin{aligned} \pi_1 &= \beta_0(0) \\ F_t &= I \quad (\text{i.e. identity matrix}) \\ H_t &= 1 \\ R_t &= \alpha_0(0) + \sum_{i=1}^m \alpha_i(0)\varepsilon_{t-i}^2 + \sum_{j=1}^r \gamma_j(0)R_{t-j}. \end{aligned}$$

*Step 2*: Predict next-day price

$$y_t = \beta_0(t) + \hat{\beta}(0)x_t.$$

2) *Solution 2*: In this solution, all parameters of GARCH model are set on training set, with exception of  $\beta = \{\beta_0, \hat{\beta}\}$  which is adjusted on-line on the test set. Denote  $\delta = \{\alpha_0, \dots, \alpha_m, \gamma_1, \dots, \gamma_r\}$

- **On the training set**: we use maximum likelihood to compute GARCH parameters, denoted  $\beta(0)$ ,  $\delta(0)$ .
- **On the test set**: two steps are recursively repeated.

*Step 1*: Update parameters of the GARCH model using the KF. We fixed the value  $\delta(t) = \delta(0)$ , and used a KF to update value of  $\beta(t)$ . The KF is given by

$$\begin{aligned} \beta(t) &= \beta(t-1) + \omega(t), \quad \omega(t) \sim N(0, Q) \\ \beta(t) &= \{\beta_0(t), \hat{\beta}(t)\} \\ y_t &= \beta_0(t) + \hat{\beta}(t)x_t + \varepsilon_t \quad \varepsilon_t \sim N(0, n_t) \\ n_t &= \alpha_0(0) + \sum_{i=1}^m \alpha_i(0)\varepsilon_{t-i}^2 + \sum_{j=1}^r \gamma_j(0)n_{t-j}. \end{aligned}$$

Parameters  $\Omega = \{Q, P_1\}$  of the Kalman Filter can be estimated by using maximum log likelihood (using Kalman smoother) [21], or just initialised to relatively small values. Other parameters of KF are given by

$$\begin{aligned} \pi_1 &= \beta(0) \\ F_t &= I \quad (\text{i.e. identity matrix}) \\ H_t &= [1, x_t] \\ R_t &= \alpha_0(0) + \sum_{i=1}^m \alpha_i(0)\varepsilon_{t-i}^2 + \sum_{j=1}^r \gamma_j(0)R_{t-j}. \end{aligned}$$

*Step 2*: Predict next-day price

$$y_t = \beta_0(t) + \hat{\beta}(t)x_t.$$

## IV. EXPERIMENTAL RESULTS

### A. Data

Two datasets are used in this work: (1) daily price of monthly electricity baseload forward products and (2) daily price of monthly gas forward products. They are taken from the UK energy market, provided by E.ON UK plc. The monthly electricity/gas product is a forward contract for supplying electricity/gas in a single month in the future. In the UK energy market, it is possible to trade gas from one to six month(s) ahead and to trade electricity from one to four month(s) ahead. There is four/six months of daily price data (approximately 90/130 data points) for each monthly electricity/gas product. For example, the July 2006 gas product

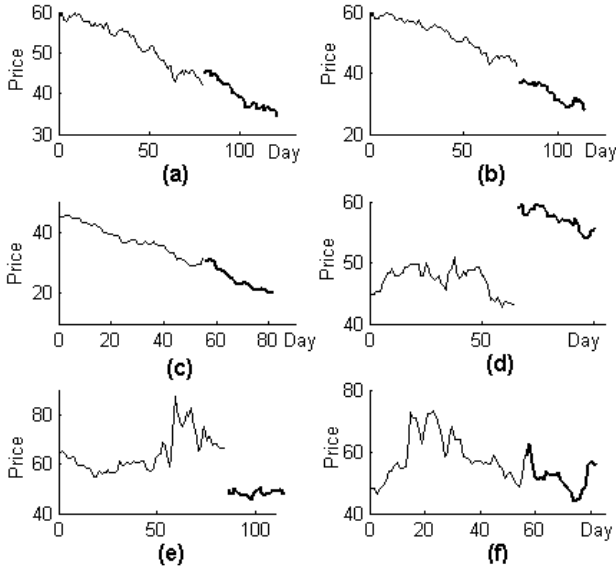


Fig. 2. Six sub-datasets (1-6) of the ELECTRICITY price dataset. The thin lines are the training sets and the bold lines are the test sets.

can be traded from 03 Jan 2006 to 30 Jun 2006. To illustrate the behaviour of the proposed methods, six sub-datasets for each datasets are used. Figure 2 and 3 show six sub-dataset of the electricity dataset (denote sub-datset 1 to 6) and gas dataset (denote sub-datset 7 to 12) respectively. The test sets of the first three sub-datasets of each dataset correspond to the beginning, middle and end of a stable monthly product. The test sets of the last three sub-datasets of each dataset correspond to the beginning, middle and end of a volatile monthly product. If a test set of a sub-dataset is the beginning or middle of a monthly gas product trading period, the training set are data of another monthly product. For example, in sub-dataset 8 in the gas price dataset (Figure 3 (b)), the test set is the middle samples of March 2007 product and the training set is November 2006 product. The prices for different products are different even in the same trading day; for example, the price of a colder month is normally higher than that of a warmer month. This is the reason why there is gap between the training sets and test sets of these sub-datasets in Figure 2 and 3.

We have randomly selected the sub-datasets from tables of price of monthly electricity/gas forward products. The input of the forecast models include historical price of monthly products, seasonal products and weekend ahead products (i.e. contracts for the next Saturday/Sunday.). In this paper, the GARCH models with  $m = 1$  and  $r = 1$  are used.

### B. Model evaluation

The random walk (RW) is used as a benchmark model. This model is given by:

$$y(t+1) = y(t) + \varepsilon(t),$$

where  $\varepsilon$  is a zero-mean noise. The model predicts that the next value of the time series is the same as the current value.

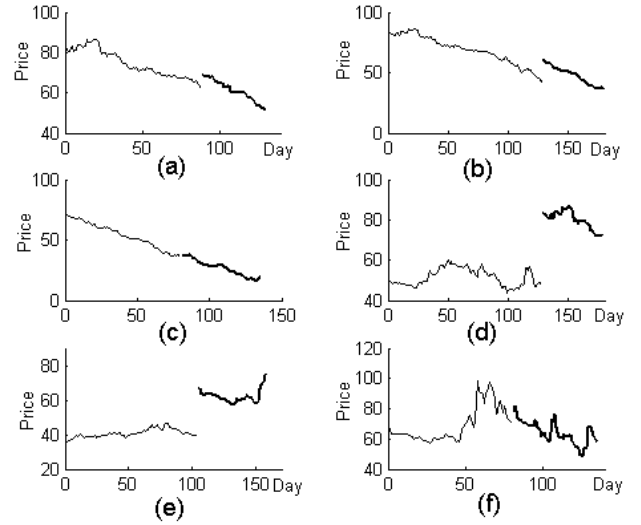


Fig. 3. Six sub-datasets (7-12) of the GAS price dataset. The thin lines are the training sets and the bold lines are the test sets.

To evaluate the prediction performance of these models, three types of prediction errors of the test sets are computed: Mean Squared Error (MSE), Root Mean Squared Error (RMSE), and Mean Absolute Percent Error (MAPE).

$$e_{MSE} = \frac{\sum_1^T (y_{\text{real}} - y_{\text{forecast}})^2}{\sum_1^T (y_{\text{real}} - \bar{y})^2}$$

$$e_{RMSE} = \frac{\sqrt{\sum_1^T (y_{\text{real}} - y_{\text{forecast}})^2}}{\sqrt{\sum_1^T (y_{\text{real}} - \bar{y})^2}}$$

$$e_{MAPE} = \frac{1}{T} \sum_{t=1}^T \left| \frac{y_{\text{real}}(t) - y_{\text{forecast}}(t)}{y_{\text{real}}(t)} \right|$$

where  $y_{\text{real}}$  is the real gas price,  $y_{\text{forecast}}$  is the forecast gas price,  $\bar{y}$  is the mean of  $y_{\text{real}}$ , and  $T$  is the number of data points.

We also compute the improvement ratio (IR) of errors of a method comparing to errors of the RW model. Errors here may be MSE, RMSE or MAPE. For example, the IR of MSE of a model M comparing to MSE of the RW is given by:

$$IR_{MSE}(M) = \frac{e_{MSE}(RW) - e_{MSE}(M)}{e_{MSE}(RW)} \times 100\%$$

### C. Results

The  $IR_{MSE}$ , MSE, MAPE, and RMSE are computed for each sub-dataset and for prediction methods. Their averaged values for the six sub-datasets of electricity and gas dataset of these methods are shown in Table I and Table II respectively. For the purpose of comparison, these errors are computed for four methods, as the follows

- Random walk model, which is used as the bench mark model.
- Fixed GARCH model, whose parameters are computed on the training set.

- Adaptive- $\beta_0$  GARCH model, whose all parameters are set on training set, with exception of the bias  $\beta_0$  which is adjusted on-line on the test set.
- Adaptive- $\beta$  GARCH model, whose all parameters are set on training set, with exception of  $\beta$  which is adjusted on-line on the test set.

It can be noticed that the errors of adaptive models are reduced in comparison with those of the fixed GARCH model. Therefore, the adaptive models do improve the performance of the GARCH model in these datasets. This improvement proves the usefulness of updating parameters using a Kalman filter. MSE of adaptive GARCH models are 0.2155 and 0.0945 for electricity price dataset and gas price dataset respectively, their MSE improves around 15.9% compared to the MSE of the random walk model. There is not much difference between the results of adaptive- $\beta_0$  GARCH and those of adaptive- $\beta$  GARCH.

TABLE I

AVERAGE ERRORS FOR THE SIX SUB-DATASETS IN THE ELECTRICITY DATASET OF THE PREDICTION METHODS.

Model	$IR_{MSE}$ (%)	MSE	MAPE	RMSE
RW	0.00	0.25623	0.01767	0.43623
Fixed GARCH	8.09	0.23551	0.01654	0.41007
Adaptive- $\beta_0$ GARCH	15.89	0.21551	0.01643	0.39828
Adaptive- $\beta$ GARCH	15.88	0.21554	0.01643	0.39832

TABLE II

AVERAGE ERRORS FOR THE SIX SUB-DATASETS IN THE GAS DATASET OF THE PREDICTION METHODS.

Model	$IR_{MSE}$ (%)	MSE	MAPE	RMSE
RW	0.00	0.11238	0.02168	0.29658
Fixed GARCH	12.41	0.09843	0.01983	0.27508
Adaptive- $\beta_0$ GARCH	15.90	0.09451	0.01991	0.27053
Adaptive- $\beta$ GARCH	15.91	0.09450	0.01990	0.27053

Table III, IV, V and VI show the MSE and Improvement ratio (IR) of these forecast models for sub-datasets. It can be seen that the adaptive GARCH models reduce the prediction errors in comparison to fixed GARCH model in case of volatility data (i.e sub-datasets 4, 5, 6, 10 and 12). For example, in the results for sub-dataset 5, the MSE of the adaptive- $\beta_0$  GARCH model and the adaptive- $\beta$  GARCH model improved 15.76% compared to these in the random walk model while the improvement ratio for the fix GARCH model is only 3.42%. However applying the filter has not much effect on stationary data (i.e. sub-datasets 1, 2, 3, 7, 8 and 9).

The adaptive models were also applied for gas quarterly products and achieved comparable but slightly worse results.

## V. CONCLUSION

This paper proposes a new forecast technique which is a combination of GARCH and Kalman filter models. Testing on the UK electricity/gas forward price shows that the GARCH models with online adaptive parameters outperform the normal

TABLE III

MSE OF SIX SUB-DATASETS IN THE ELECTRICITY PRICE DATASET USING DIFFERENT PREDICTION MODELS.

MSE	RW	Fixed GARCH	Adaptive- $\beta_0$	Adaptive- $\beta$
Sd 1	0.05040	0.04240	0.04206	0.04206
Sd 2	0.09456	0.08856	0.08792	0.08794
Sd 3	0.05300	0.03001	0.02969	0.02970
Sd 4	0.12765	0.12698	0.12550	0.12554
Sd 5	0.92351	0.89189	0.77794	0.77796
Sd 6	0.28827	0.23322	0.22995	0.23003
Average	0.25623	0.23551	0.21551	0.21554
Sd: Sub-dataset				
Adaptive- $\beta_0$ : Adaptive- $\beta_0$ GARCH				
Adaptive- $\beta$ : Adaptive- $\beta$ GARCH				

TABLE IV

IMPROVEMENT RATIO OF MSE OF SIX SUB-DATASETS IN THE ELECTRICITY PRICE DATASET USING DIFFERENT PREDICTION MODELS.

$IR_{MSE}$ (%)	Fixed GARCH	Adaptive- $\beta_0$	Adaptive- $\beta$
Sd 1	15.86	16.55	16.54
Sd 2	6.34	7.02	7.00
Sd 3	43.38	43.97	43.95
Sd 4	0.52	1.68	1.65
Sd 5	3.42	15.76	15.76
Sd 6	19.10	20.23	20.20
Average	8.09	15.89	15.88
Sd: Sub-dataset			
Adaptive- $\beta_0$ : Adaptive- $\beta_0$ GARCH			
Adaptive- $\beta$ : Adaptive- $\beta$ GARCH			

GARCH model on volatile data. The framework of this combination model of GARCH can be applied to other prediction models, such as machine learning or financial models.

This paper forecasts daily electricity/gas prices for the monthly forward product as an example to verify the performance of the proposed method. It can be used for forecasting other types of forward products, market clearing prices, and electricity/gas demand forecasts.

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TABLE V  
MSE OF SIX SUB-DATASETS IN THE GAS PRICE DATASET USING  
DIFFERENT PREDICTION MODELS.

MSE	RW	Fixed GARCH	Adaptive- $\beta_0$	Adaptive- $\beta$
Sd 7	0.05584	0.03580	0.03671	0.03671
Sd 8	0.02649	0.01991	0.02000	0.02000
Sd 9	0.03155	0.02973	0.02961	0.02961
Sd 10	0.05374	0.05582	0.04880	0.04880
Sd 11	0.12435	0.10596	0.10706	0.10706
Sd 12	0.38232	0.34338	0.32488	0.32488
Average	0.11238	0.09843	0.09451	0.09450
Sd: Sub-dataset Adaptive- $\beta_0$ : Adaptive- $\beta_0$ GARCH Adaptive- $\beta$ : Adaptive- $\beta$ GARCH				

TABLE VI  
IMPROVEMENT RATIO OF MSE OF SIX SUB-DATASETS IN THE GAS  
PRICE DATASET USING DIFFERENT PREDICTION MODELS.

$IR_{MSE}$ (%)	Fixed GARCH	Adaptive- $\beta_0$	Adaptive- $\beta$
Sd 7	35.88	34.25	34.25
Sd 8	24.85	24.51	24.51
Sd 9	5.77	6.17	6.17
Sd 10	-3.87	9.19	9.19
Sd 11	14.79	13.90	13.90
Sd 12	10.19	15.02	15.02
Average	12.41	15.90	15.91
Sd: Sub-dataset Adaptive- $\beta_0$ : Adaptive- $\beta_0$ GARCH Adaptive- $\beta$ : Adaptive- $\beta$ GARCH			

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