

1 **Suction Caisson Installation in Sand with Isotropic Permeability Varying**  
2 **with Depth**

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## 1 Abstract

Suction-induced seepage is pivotal to the installation of caisson foundations in sand. Indeed, the upward pore water flow on the inner side of the caisson wall causes a release of a fraction of soil resistance due to the reduction of the lateral effective stress. A safe caisson installation requires a reliable prediction of soil conditions, especially soil resistance and critical suction for piping. These soil conditions must be predicted for the whole installation process.

In this paper, we examine the effect of the assumed permeability profile, as a function of depth below the mudline, on such prediction. This study is motivated by the fact that marine sediments generally exhibit a permeability that decreases with depth because of consolidation under gravity. Hence, the question is whether conventional theories based on a constant permeability lead to a conservative prediction of soil conditions. Our conclusion is affirmative only regarding piping condition. As for soil resistance, a prediction based on the assumption of a constant permeability is non conservative. This is due to an overestimated reduction in effective stresses under suction-induced seepage.

## 10 Keywords

Caisson foundation; Installation in sand; Normalised geometry; Piping condition; Permeability varying with depth.

## 19 1. Introduction

20 A Suction caisson consists of a thin-walled upturned ‘bucket’ of cylindrical shape made from  
21 steel. This type of foundation has proven to be efficient and versatile as a support for offshore  
22 structures and appears to be a very attractive option for future use in offshore wind turbines  
23 [1, 2].

1 The installation procedure starts by lowering the caisson into the seabed where an initial  
2 penetration is achieved under caisson self-weight. Seabed material surrounding the caisson  
3 wall above the caisson tip forms a natural seal which is vital to the initial installation stage.  
4 Water trapped inside the caisson cavity is then pumped out, which imposes a suction that  
5 results into a pressure differential on the caisson lid. At mudline level, inside the caisson  
6 cavity, the imposed suction, which will be assumed uniformly distributed in this work,  
7 induces seepage around the caisson wall. For a caisson installation in sand, seepage causes an  
8 overall reduction in soil resistance and facilitates caisson penetration. It is often recognised  
9 that the downward force produced by suction wouldn't overcome soil resistance for  
10 installation in sand if no soil loosening is achieved due to the induced seepage [3-8]. Most  
11 design procedures of caisson installation in sand take into account the role of porewater  
12 seepage induced by suction [9-12]. The role of suction during caisson installation in sand has  
13 also been considered in centrifuge model testing [13] and finite element simulations [14]. The  
14 existence of low permeability silt layers has been considered by Tran et al., [15].

15 During caisson installation in sand, suction must be controlled to avoid the formation of  
16 piping channels which would prevent further penetration and may cause the installation  
17 procedure to fail [16]. The development of design procedures with effective suction control  
18 requires a good understanding of soil conditions and seepage around the caisson wall. Effects  
19 of seepage on soil conditions, such as piping and soil resistance, must be predicted for the  
20 whole installation process to ensure that changes in suction remain within the safety limits.  
21 Using a finite difference procedure applied to the normalised seepage problem of caisson  
22 installation in sand, Harireche et al., [17] described soil conditions and derived criteria for  
23 suction control during caisson installation in sand. The numerical procedure they proposed  
24 takes into account the actual variation in excess pressure gradient over the installation depth.

1 In the present paper, the numerical procedure proposed by Harireche et al., [17] is extended  
2 to take into account a seabed permeability that decreases with depth. Bryan et al. [18]  
3 reported field data for marine sediments in the Gulf of Mexico. Their measurements show  
4 that soil permeability generally decreases with an increasing depth. Bennett et al. [19] have  
5 also performed in-situ measurements of porosity and permeability of selected carbonate  
6 sediments and their reported data provides further evidence for soil permeability varying with  
7 depth. The present study is motivated by the need to assess whether a homogeneous seabed  
8 model is a conservative assumption for caisson installation design.

9

## 10 **2. Normalised seepage problem and permeability profiles**

11 We consider a caisson of radius  $R$ , height  $L$  and we denote  $h$  the depth of caisson penetration  
12 into the seabed. The soil consists of sand with permeability  $k$  decreasing with the depth  $z$   
13 below the mudline. A normalised problem geometry where all dimensions are scaled with  
14 respect to the caisson radius is adopted. Figure 1 shows a vertical section through the  
15 meridian plane of the system caisson-soil where a cylindrical system of coordinates  $r^*$  and  
16  $z^*$  is used. The hydrostatic porewater pressure that exists in the soil before caisson installation  
17 is denoted  $p_0$  and has a magnitude at depth  $z$ ,  $p_0 = p_{at} + \gamma_w h_w + \gamma_w z$ , where  $p_{at}$  is the  
18 atmospheric pressure,  $\gamma_w$  the unit weight of water and  $h_w$  the water height above the mudline.  
19 During caisson installation the imposed suction induces a deviation of porewater pressure  
20 from the hydrostatic value, which will be referred to as excess porewater pressure and will be  
21 denoted  $p$ . The suction magnitude,  $\bar{s}$  imposed over the radial distance  $OC$  (Fig. 1) is  
22 expected to increase during installation. Indeed, as the caisson is pushed into the seabed,  
23 suction must be increased to overcome the increasing soil resistance. On the mudline

1 boundary C<sup>+</sup>F outside the caisson, and on the boundaries FH and BH sufficiently far from the  
 2 zone of significant pressure disturbance, the initial hydrostatic pressure  $p_0$  is not affected.

3

4 Figure 1

5

6 In order to describe the variation of permeability with depth, the following expression is  
 7 adopted:

$$8 \quad \bar{k} \equiv \frac{k(z^*)}{k_0} = (1 - \beta)e^{-\alpha z^*} + \beta \quad (1)$$

9 In this equation,  $k \equiv K / n\gamma_w$ , where  $K$  is the absolute permeability and  $n$  denotes the porosity.

10 The coefficient  $k_0$  denotes the permeability at the seabed surface,  $z^* = z/R$  the normalised  
 11 depth and  $\alpha, \beta$  are two constants such that:

$$12 \quad \alpha > 0; \quad \beta = \frac{k_\infty}{k_0}, \quad 0 \leq \beta \leq 1 \quad (2)$$

13 Note that for  $\beta = 1$ , the case of a homogeneous seabed with a constant permeability  $k_0$  is  
 14 recovered. A value  $\beta = 0$  corresponds to an impervious condition at large depth, i.e.,  $k_\infty = 0$ .

15 In order to identify the constants  $\alpha$  and  $\beta$  for a given seabed profile,  $k_\infty, k_0$  and  $\bar{k}_1 = \bar{k}(z_1^*)$ , for  
 16 a given normalised depth  $z_1^*$ , must be specified. The coefficient  $\beta$  can be calculated using the  
 17 second relation (2) and  $\alpha$  is given by:

$$18 \quad \alpha = \frac{1}{z_1^*} \text{Ln} \left( \frac{1 - \beta}{\bar{k}_1 - \beta} \right) \quad (3)$$

1 Figure 2 shows different permeability profiles and the corresponding values of the parameters  
 2  $\alpha$  and  $\beta$ . Three cases have been selected, which will be investigated in the following sections.  
 3 Case A corresponds to a homogeneous seabed profile with constant permeability. In case B,  
 4 the permeability decreases with depth almost linearly. A value  $\bar{k} = 0.75$  is achieved at depth  $z$   
 5  $= R$  using  $\beta = 0$  and  $\alpha = 0.288$ . In case C, permeability has a non-linear profile and decreases  
 6 with depth at a much higher rate compared to case B. At depth  $z = R$ , a value  $\bar{k} = 0.30$  is  
 7 achieved using  $\beta = 0$  and  $\alpha = 1.204$ . Note that in both cases B and C, the soil is assumed to  
 8 become impervious at large depth.

9 Figure 2

10  
 11 The porewater seepage is assumed to obey Laplace's equation:

$$12 \operatorname{div}(-k\nabla p) = 0 \quad (4)$$

13 Where  $\nabla p$  denotes the excess porewater pressure gradient and,

$$14 \operatorname{div} \equiv (1/r)\partial/\partial r + (1/r)\partial/\partial\theta + \partial/\partial z.$$

15 Denoting  $k' \equiv dk/dz$ , equation (4) can be developed in axisymmetric conditions ( $\partial/\partial\theta = 0$ )

16 to give:

$$17 \frac{\partial^2 p}{\partial r^2} + \frac{1}{r} \frac{\partial p}{\partial r} + \frac{\partial^2 p}{\partial z^2} + \frac{k'}{k} \frac{\partial p}{\partial z} = 0 \quad (5)$$

18 In order to draw conclusions that are not affected by the problem dimensions, we adopt the

19 following scaling of the main problem variables:

$$20 p^* = \frac{p}{s}, \quad h^* = \frac{h}{R}, \quad r^* = \frac{r}{R} \quad (0 \leq r^* \leq 1 \text{ on OC and } 1 \leq r^* < \infty \text{ on CF}) \quad (6)$$

1 The scaled porewater pressure  $p^*$  satisfies the dimensionless equation:

$$2 \frac{\partial^2 p^*}{\partial r^{*2}} + \frac{1}{r^*} \frac{\partial p^*}{\partial r^*} + \frac{\partial^2 p^*}{\partial z^{*2}} + f^*(z^*) \frac{\partial p^*}{\partial z^*} = 0 \quad (7)$$

3 Where:

$$4 f^*(z^*) \equiv \frac{-\alpha(1-\beta)}{1-\beta + \beta e^{\alpha z^*}} \quad (8)$$

5 As the caisson penetrates into the seabed, radial porewater flow across the caisson wall is  
6 prevented, which is described by the boundary condition on CD:  $\partial p / \partial r = 0$  and due to  
7 symmetry, this condition must also be satisfied on the z-axis (i.e., for  $r = 0$ ). As shown in  
8 Figure 1, the soil domain is divided into four regions. Region ( $\Omega_1$ ) represents soil inside the  
9 caisson, ( $\Omega_2$ ) is the region occupied by soil which passes inside the caisson after further  
10 penetration and regions ( $\Omega_3$ ) and ( $\Omega_4$ ) are the complementary soil regions outside the caisson,  
11 surrounding ( $\Omega_2$ ) and ( $\Omega_1$ ) respectively. In addition to equation (7), the scaled excess  
12 porewater pressure  $p^*$  must satisfy the boundary conditions:

$$13 p^* = -1 \text{ on } OC^-, \quad p^* = 0 \text{ on } C^+F, FH, BH \text{ and } \frac{\partial p^*}{\partial r^*} = 0 \text{ on } CD \text{ and } OB \quad (9)$$

14

### 15 **3. Finite difference solution of the normalised problem**

16 A simple finite difference scheme is used to solve the model problem presented in the  
17 previous section. The coordinates  $r^*$  and  $z^*$  are discretised into constant increments  $\Delta r^*$  and  
18  $\Delta z^*$  and the following approximations are adopted:

$$\begin{aligned}
\text{1} \quad \left. \frac{\partial p^*}{\partial r^*} \right|_{i,j} &\cong \frac{p_{i,j+1}^* - p_{i,j}^*}{\Delta r^*} \\
\text{2} \quad \left. \frac{\partial p^*}{\partial z^*} \right|_{i,j} &\cong \frac{p_{i+1,j}^* - p_{i,j}^*}{\Delta z^*} \\
\text{3} \quad \left. \frac{\partial^2 p^*}{\partial r^{*2}} \right|_{i,j} &\cong \frac{p_{i,j+1}^* - 2p_{i,j}^* + p_{i,j-1}^*}{\Delta r^{*2}} \\
\text{4} \quad \left. \frac{\partial^2 p^*}{\partial z^{*2}} \right|_{i,j} &\cong \frac{p_{i+1,j}^* - 2p_{i,j}^* + p_{i-1,j}^*}{\Delta z^{*2}}
\end{aligned} \tag{10}$$

5 Where  $i=1$  on the mudline (OF) and  $j=1$  on the vertical axis (OB).

6 Using the finite difference scheme above, equation (7) is approximated by:

$$\begin{aligned}
\text{7} \quad &\left[ 2 \left( \frac{1}{\Delta r^{*2}} + \frac{1}{\Delta z^{*2}} \right) + \frac{1}{r^* \Delta r^*} + \frac{f_i^*}{\Delta z^*} \right] p_{i,j}^* - \\
&\left( \frac{1}{\Delta r^{*2}} + \frac{1}{r^* \Delta r^*} \right) p_{i,j+1}^* - \frac{1}{\Delta r^{*2}} p_{i,j-1}^* - \left( \frac{1}{\Delta z^{*2}} + \frac{f_i^*}{\Delta z^*} \right) p_{i+1,j}^* - \frac{1}{\Delta z^{*2}} p_{i-1,j}^* = 0
\end{aligned} \tag{11}$$

8 Where  $f_i^* \equiv f^*((i-1) \times \Delta z^*)$  and  $f^*(z^*)$  is defined by (8).

9 On the z-axis, the condition

$$\text{10} \quad \lim_{r^* \rightarrow 0} \frac{1}{r^*} \frac{\partial p^*}{\partial r^*} = \frac{\partial^2 p^*}{\partial r^{*2}} \tag{12}$$

11 leads to the approximation form:

$$\text{12} \quad \left. \frac{1}{r^*} \frac{\partial p^*}{\partial r^*} \right|_{i,j} \cong \frac{2(p_{i,j+1}^* - p_{i,j}^*)}{\Delta r^{*2}} \tag{13}$$



1 An important aspect of the present numerical procedure is to enforce the continuity of excess  
 2 pore water pressure  $p^*$  at point D (Fig.1).

$$3 \quad p^*(D)|_{\Omega_1} = p^*(D)|_{\Omega_4} \quad (14)$$

4 Applying equation (11) to point D, separately in domains ( $\Omega_1$ ) and ( $\Omega_4$ ), taking into account  
 5 condition (14) and the third boundary condition (9), leads to the approximation below:

$$6 \quad 2 \left( \frac{1}{\Delta r^{*2}} + \frac{2}{\Delta z^{*2}} + \frac{f^*(D)}{\Delta z^*} \right) p_D^* - \frac{1}{\Delta r^{*2}} p_{DL}^* - \frac{1}{\Delta r^{*2}} p_{DR}^* - \frac{1}{\Delta z^{*2}} p_{I^-}^* - \frac{1}{\Delta z^{*2}} p_{I^+}^* \\
 7 \quad - 2 \left( \frac{1}{\Delta z^{*2}} + \frac{f^*(D)}{\Delta z^*} \right) p_J^* = 0 \quad (15)$$

8 Where points D,  $D_L$ ,  $D_R$ , I,  $I^+$  and J are shown in Figure 1.

9 The finite difference approximations presented in this section have been implemented in a  
 10 computer program which has been used to analyse seepage around a suction caisson as  
 11 installation progresses in sand with a permeability decreasing with depth. This analysis is  
 12 performed to study the effects of suction induced seepage on soil resistance for the different  
 13 permeability profiles described in section 2. Critical conditions for piping are also considered  
 14 within this extended context of permeability varying with depth. These aspects are reported  
 15 and discussed in the following sections.

16

17

#### 18 **4. Soil resistance to caisson penetration**

19 Water seepage caused by suction produces a hydraulic gradient which, on both faces of the  
 20 caisson wall, varies with depth. Figures 3a, 3c and 3e show the contours of normalised excess

1 pore pressure  $p^*$  for values of the scaled penetration depth  $h^* = 0.2$  (typical of self-weight  
2 penetration), 1 and 2. These figures correspond to a homogeneous seabed with constant  
3 permeability. For comparison, figures 3b, 3d and 3f show similar contours for a seabed  
4 profile that corresponds to case C described in section 2. These figures show clearly that the  
5 pressure distribution is affected by the permeability profile, although this effect is not  
6 noticeable at the early stage where the installation depth is typical of self-weight penetration  
7 (Fig. 3b).

### 8 Figure 3

9

10  
11 Figure 4 shows the vertical component of the normalised pressure gradient  $g^* \equiv \partial p^* / \partial z^*$  on  
12 both sides of the caisson wall as a function of scaled depth  $z^*$  for the three permeability  
13 profiles (cases A, B and C). Values of scaled penetration depth  $h^* = 0.2, 1$  and 2 have been  
14 considered.

15 It can be seen that the pressure gradient on each side of the caisson wall is higher at the early  
16 stages of the installation process. Maximum values of the gradient occur at the caisson tip.

17 For the homogeneous seabed profile with constant permeability (case A), the gradient  
18 distribution over the caisson embedment tends to become uniform over a significant depth as  
19 the installation proceeds. A gradient of higher magnitude tends to localise around the caisson  
20 tip. For seabed profiles where the permeability decreases with depth (cases B and C), such a  
21 uniformity is less pronounced, especially for the gradient on the inner side. By comparing the  
22 normalised gradients for the three different cases A, B and C, on both sides of the caisson  
23 wall, it can be observed that the effect of permeability profile becomes more important as the  
24 penetration depth increases. For the normalised gradient on the outer side, the difference in

1 gradient magnitude for the three permeability profiles is not significant at shallow depths.  
2 However, such a difference increases with depth, which is likely to affect soil resistance  
3 through the increase in effective stress and this will be more noticeable at later stages during  
4 the caisson installation process. On the inner side of the caisson wall, the normalised gradient  
5 magnitude is affected in a different way. Up to a scaled depth which can be estimated to 3/4  
6 of the scaled penetration depth, the normalised gradient magnitude is lower for a higher rate  
7 of variability in the permeability profile. Below such depth, the opposite trend is observed.  
8 This behaviour suggests that soil is less prone to piping for a permeability that has a higher  
9 variability profile. In terms of soil resistance to caisson penetration, it can be anticipated that  
10 a higher variability profile is likely to correspond to less reduction in soil resistance due to  
11 seepage. If this is the case, then we would conclude that soil resistance estimations based on a  
12 constant permeability assumption are not conservative.

13

14 Figure 4

15

16 These effects are now studied in more detail in order to withdraw final conclusions regarding  
17 soil resistance against caisson penetration and critical condition for piping.

18

#### 19 **4.1 Lateral frictional resistance on caisson wall**

20 In the absence of seepage, the lateral effective pressure on the caisson wall has the  
21 expression:

$$22 \sigma'_h = K(\gamma'z + \tilde{\sigma}) \quad (16)$$

23 Where  $K$  is a lateral earth pressure coefficient. The vertical effective stress near the caisson  
24 wall is enhanced by the magnitude  $\tilde{\sigma}$  due to the effect of shear resistance that develops on the

1 interface soil-caisson. Under seepage conditions produced by an applied suction, the lateral  
 2 effective pressure acting on the caisson wall at depth  $z$ , inside and outside the caisson is  
 3 respectively expressed as follows:

$$4 \quad \sigma'_{hi}(R, z) = K \left( \gamma' z - \int_0^z g_i(R, \zeta) d\zeta + \tilde{\sigma}_i(R, z) \right) \quad (17)$$

$$5 \quad \sigma'_{ho}(R, z) = K \left( \gamma' z - \int_0^z g_o(R, \zeta) d\zeta + \tilde{\sigma}_o(R, z) \right) \quad (18)$$

6 Where  $g_i(R, \zeta)$  and  $g_o(R, \zeta)$  denote the vertical component of the pressure gradient on the  
 7 inner and the outer sides of the caisson wall respectively. Assuming that the enhanced  
 8 effective stresses  $\tilde{\sigma}_i$  and  $\tilde{\sigma}_o$  are not affected by seepage conditions, the reduction at depth  $z$  in  
 9 the lateral pressure acting on the caisson wall caused by seepage is given by:

$$10 \quad \Delta\sigma'_h(R, z) = K \left( \int_0^z g_i(R, \zeta) d\zeta + \int_0^z g_o(R, \zeta) d\zeta \right) \quad (19)$$

11 The pressure gradients can be expressed as follows:

$$12 \quad g_o = \frac{\bar{s}}{R} g_o^*; \quad g_i = \frac{\bar{s}}{R} g_i^* \quad (20)$$

13 Where  $g_o^* \equiv \partial p^* / \partial z^*$  is the normalised pressure gradient in domains  $(\Omega_4)$ ,  $(\Omega_3)$  and

14  $g_i^* \equiv \partial p^* / \partial z^*$  denotes the same quantity when evaluated in domains  $(\Omega_1)$  and  $(\Omega_2)$ . Hence,

15 expression (19) can be rewritten under the following form:

$$16 \quad \frac{\Delta\sigma'_h(R, z)}{K\bar{s}} = L_i^*(z^*) + L_o^*(z^*) \quad (21)$$

17 Where, as can be seen from Figure 4:

$$L_i^*(z^*) \equiv \int_0^{z^*} g_i^*(1, \zeta^*) d\zeta^* > 0, L_o^*(z^*) \equiv \int_0^{z^*} g_o^*(1, \zeta^*) d\zeta^* < 0 \text{ and } |L_i^*(z^*)| > |L_o^*(z^*)| \quad (22)$$

Using a numerical calculation of the integrals in (22) on the normalised finite difference mesh, we obtain the scaled reduction of the lateral effective stress expressed in (21) as a function of the normalised depth  $z^*$ , which is shown in Figure 5. It can be observed that such a reduction increases with depth and is clearly affected by the permeability profile. A higher rate of variability in the permeability corresponds to a lower reduction in the lateral effective stress. Although this effect is quite limited at shallow penetration depths (Fig. 5a), it is clearly more pronounced at larger penetration depths (Figs. 5b-c). This shows clearly that the assumption of a homogeneous seabed is not in favour of a conservative estimation of soil resistance to caisson penetration as it overestimates the effect of seepage on the reduction of the lateral effective stress.

Figure 5

As a consequence, seepage causes the frictional resisting force acting on the caisson wall to decrease by a magnitude  $\Delta F_s$  given as a function of the scaled penetration depth  $h^*$  by the expression:

$$\frac{\Delta F_s}{2\pi R^2 K_s} = \int_0^{h^*} [L_i^*(z^*) + L_o^*(z^*)] dz^* \quad (23)$$

## 4.2 Tip resistance

Seepage also causes the vertical effective stress at the caisson tip to decrease, thereby leading to further reduction in the total resisting force. The resisting force at the caisson tip can be expressed under the form:

$$F_t = 2\pi R N_q \int_{R_i}^{R_o} \sigma'_v dr \quad (24)$$

Where  $N_q$  is a bearing capacity factor and  $\sigma'_v$  the vertical effective stress at the caisson tip, which is assumed to vary linearly from  $\sigma'_{vi}$  inside the caisson (radius  $R_i$ ) to  $\sigma'_{vo}$  outside (radius  $R_o$ ), and these stresses have the expressions:

$$\sigma'_{vi}(R, h) = \gamma' h - \int_0^h g_i(R, \zeta) d\zeta + \tilde{\sigma}'_i(R, h) \quad (25)$$

$$\sigma'_{vo}(R, h) = \gamma' h - \int_0^h g_o(R, \zeta) d\zeta + \tilde{\sigma}'_o(R, h) \quad (26)$$

Assuming that seepage does not affect the enhanced vertical stress, the resisting force at the caisson tip decreases by the magnitude  $\Delta F_t$  such that:

$$\frac{\Delta F_t}{2\pi R t N_q \bar{s}} = \frac{1}{2} (L_i^*(h^*) + L_o^*(h^*)) \quad (27)$$

where functions  $L_i^*(z^*)$  and  $L_o^*(z^*)$  are defined by expressions (22).

Figure 6 shows the expression  $(L_i^*(h^*) + L_o^*(h^*))$  as a function of penetration depth  $(h^*)$  for the three permeability profiles considered in this study. Figure 6 and expression (27) show clearly that the reduction in the magnitude of tip resistance is maximum when permeability is assumed constant (case A). Hence, constant permeability profile is not a conservative assumption when estimating tip resistance to caisson penetration.

## 5. Critical suction for piping condition

During caisson installation in sand, suction magnitude must be controlled to avoid the formation of piping channels around the caisson wall, which may cause the installation procedure to fail [16].

At a generic material point of normalised coordinates  $r^*$ ,  $z^*$  within the soil in contact with the inner side of the caisson wall, piping takes place when the vertical effective stress becomes zero. This is expressed by the equation:

$$\sigma'_v = \gamma' z - \int_0^z g_i(R, \zeta) d\zeta = 0 \quad (28)$$

Hence, the suction magnitude that causes such condition is given by:

$$\frac{s_{cr}}{\gamma' R} = \frac{z^*}{L_i^*(1, z^*)} \quad (29)$$

$$\text{Where } L_i^*(1, z^*) \equiv \int_0^{z^*} g_i^*(1, \zeta^*) d\zeta^* .$$

Note that expression (29) is similar to the one derived by Houlsby and Byrne [10] under the form  $s_{cr}/(\gamma' R) = h^*/(1-a)$  where  $a$  is the magnitude of the normalised pressure at the caisson tip on the inner side; i.e.  $a \equiv -p^*(h^*)$ .

The present criterion extends the expression proposed by Houlsby and Byrne [10], taking into account the actual variation of the pressure gradient as a function of depth. At the caisson tip,

it has the expression:  $s_{cr}/(\gamma' R) = \frac{h^*}{L_i^*(1, h^*)}$ . Note that, in addition to the variable pressure

gradient, the present criterion also takes into consideration a permeability varying with depth,

which is implicitly accounted for in the expression of  $L_i^*(1, h^*)$ .

1 Figure 7 shows the variation of the normalised magnitude of critical suction,  $s_{cr}/(\gamma'R)$  as a  
2 function of depth at three different stages of the installation process where the scaled  
3 penetration depth is 0.2, 1 and 2. The three permeability profiles have been considered at  
4 each stage for comparison. It can be observed that the assumption of a homogeneous soil  
5 (case A) leads to the estimation of a minimum critical suction. Hence, as far as the condition  
6 for piping is concerned, such an assumption is conservative. It can be observed from Figure 7  
7 that, while the effect of the variability with depth of permeability is less pronounced around  
8 the caisson tip, it becomes very significant at shallow depth.

9  
10 Figure 7

## 11 12 **6. Conclusion**

13 In this study we have considered the effect of a permeability varying with depth on the  
14 prediction of soil resistance to caisson penetration and critical suction for piping condition.

15 Three permeability profiles have been considered, namely: constant permeability,  
16 permeability slowly varying with depth ( $\alpha = 0.288$ ), permeability with a high variability with  
17 depth ( $\alpha = 1.204$ ). These profiles have been motivated by the fact that marine sediments are  
18 expected to exhibit a permeability that decreases with depth at a rate that must also be taken  
19 into consideration as it may vary from one type of soil to another. The effect of suction  
20 induced seepage on soil resistance to caisson penetration has been investigated using the  
21 normalised solution of seepage around the caisson wall. It has been observed that a constant  
22 permeability profile leads to an under-estimation of soil resistance to caisson penetration.  
23 This highlights the importance of taking into account a permeability profile with certain



1 variability with depth for a more accurate prediction of the required suction throughout the  
2 installation process. The investigation of piping on the inner side of the caisson wall revealed  
3 that the constant permeability assumption under-estimates the critical suction for piping. As  
4 far as the formation of piping channels is concerned, the assumption of homogeneous seabed  
5 with constant permeability is conservative. However, taking into account the actual  
6 variability with depth of the permeability may lead to a more accurate estimation of the  
7 critical suction with significantly less restriction on the safe suction profile throughout the  
8 installation process.

9

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7 **Figure Captions**

8 **Figure 1.**

9 Normalised geometry and finite difference mesh

10 **Figure 2.**

11 Permeability profiles: Case A (constant permeability), case B ( $\alpha = 0.288$ ) and case C ( $\alpha =$   
12 1.204)

13 **Figure 3.**

14 Normalised excess porewater pressure contours for scaled penetration depths  $h^*=0.2, 1, 2$ .

15 a, c, e: constant permeability (case A); b, d, f: permeability with a high variability profile  
16 (case C,  $\alpha = 1.204$ ).

17 **Figure 4.**

18 Dimensionless pressure gradient as a function of scaled depth for different  
19 permeability profiles (cases A, B and C). a/  $h^* = 0.2$ ; b/  $h^* = 1$ ; c/  $h^* = 2$ .

20 **Figure 5.**

21 Reduction in the normalised lateral effective stress on caisson wall due to suction-induced  
22 seepage. a/  $h^* = 0.2$ ; b/  $h^* = 1$ ; c/  $h^* = 2$ .

23 **Figure 6.**

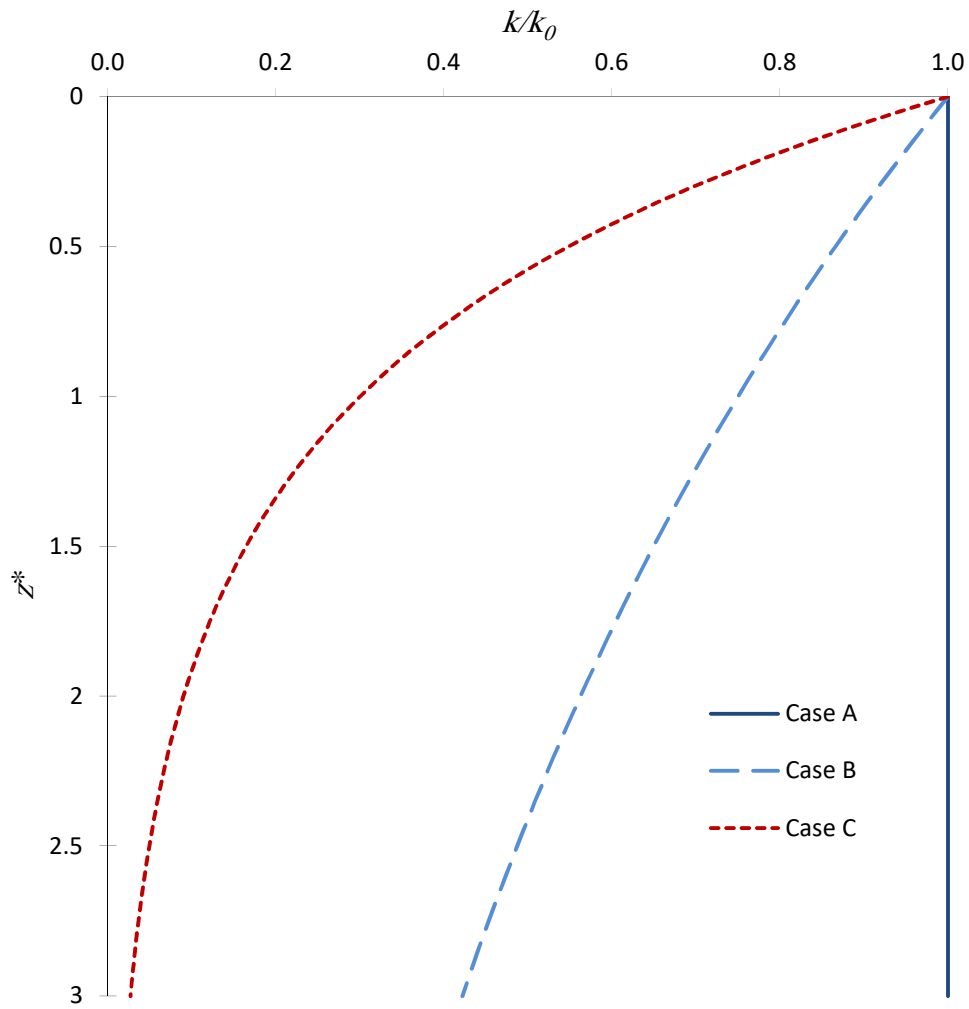
24 Effect of suction-induced seepage on soil resistance at caisson tip.

25 **Figure 7.**

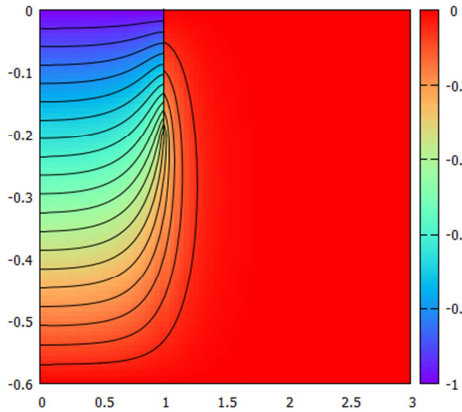
26 Critical suction for piping on the inner caisson wall. a/  $h^* = 0.2$ ; b/  $h^* = 1$ ; c/  $h^* = 2$ .

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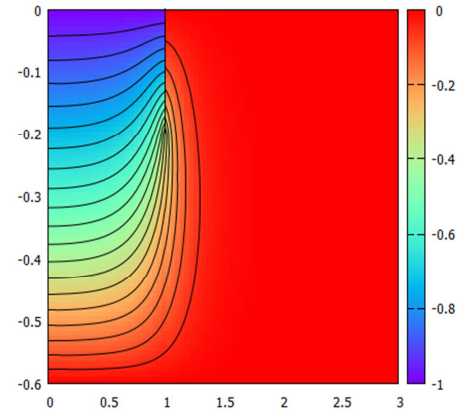




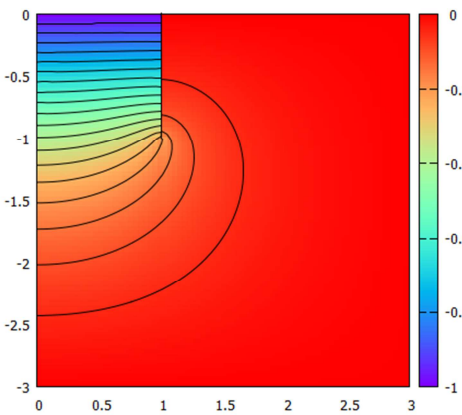
**Figure 2.**  
(Colour on the Web)



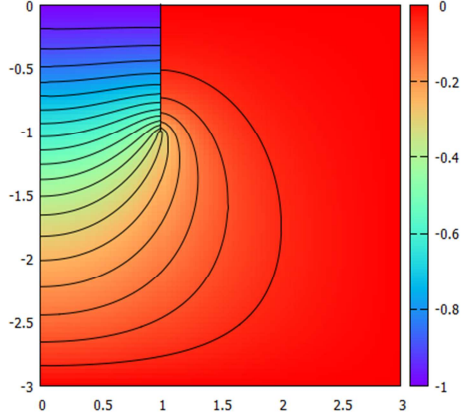
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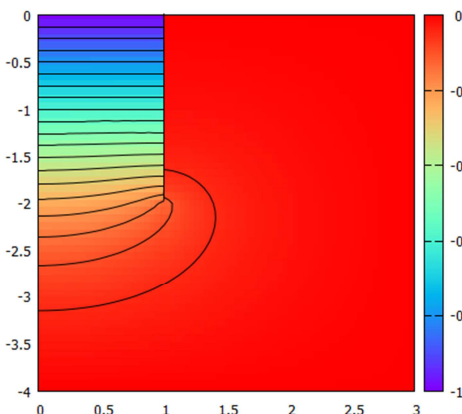
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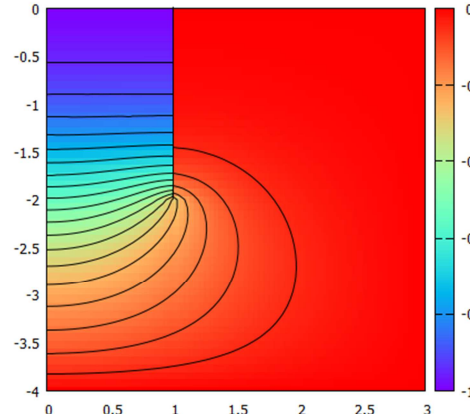
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(d)



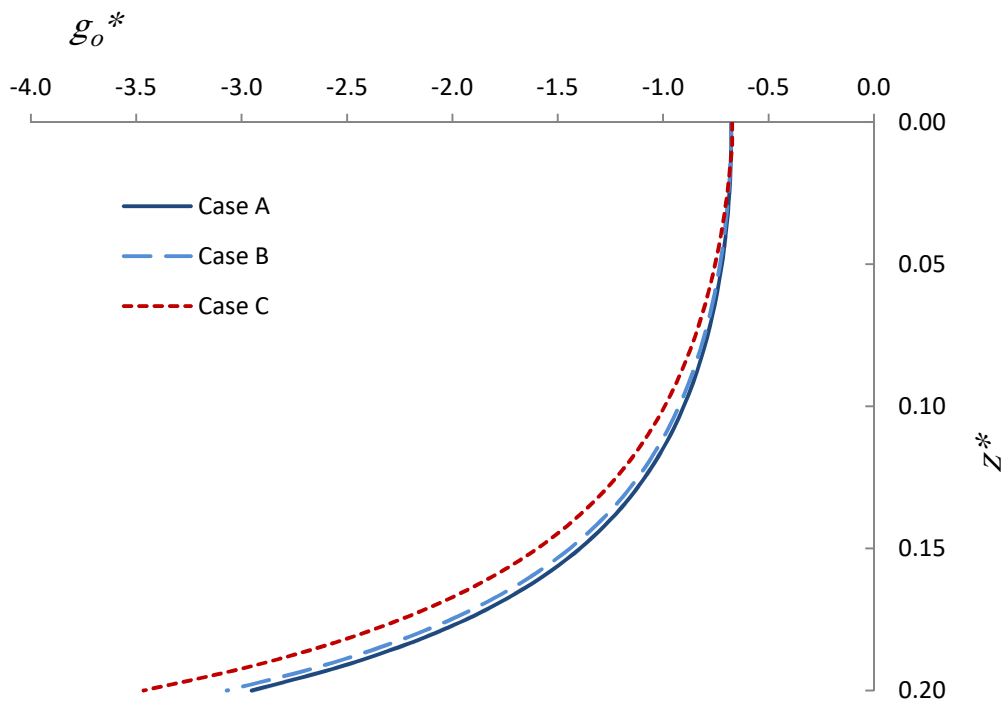
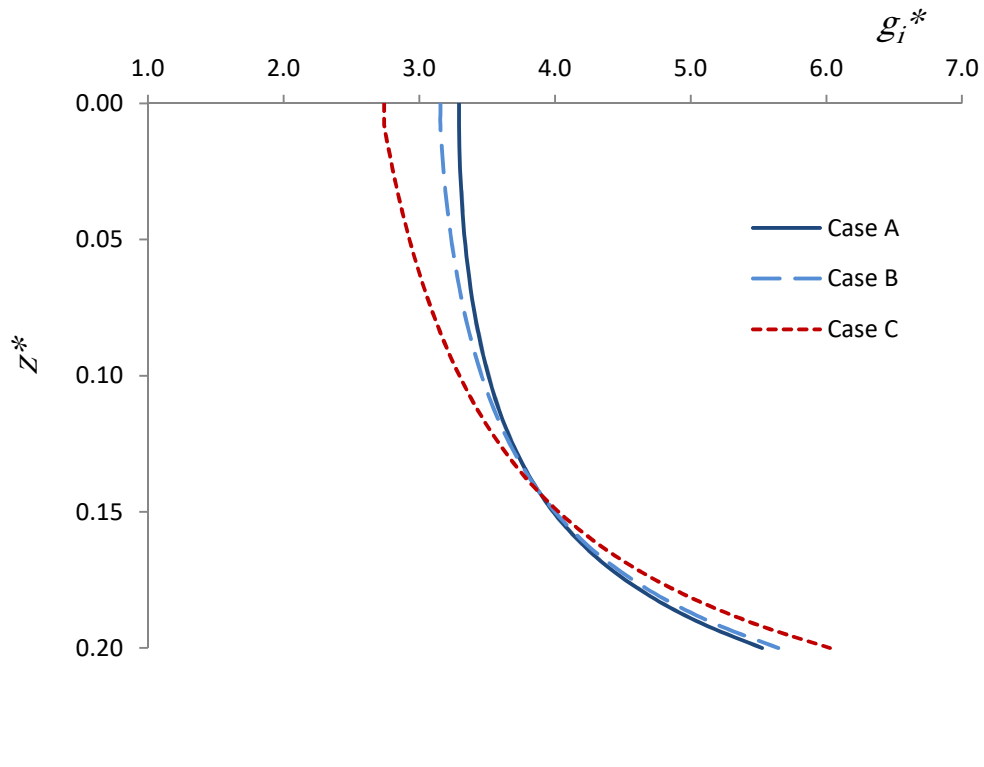
(e)



(f)

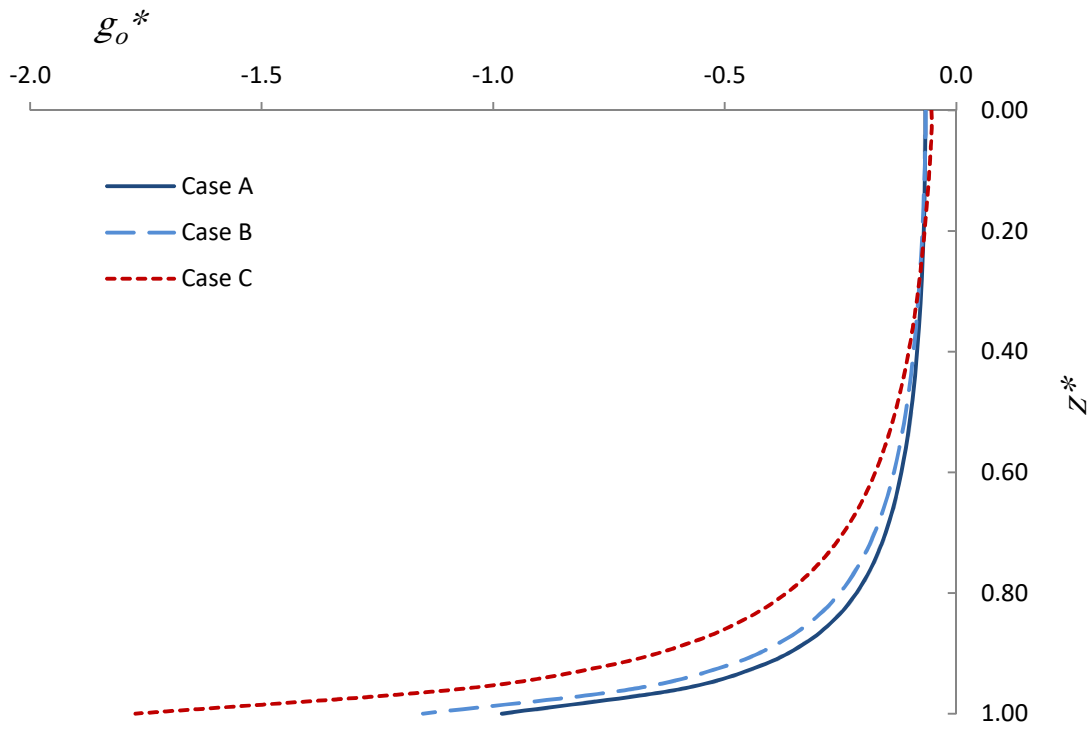
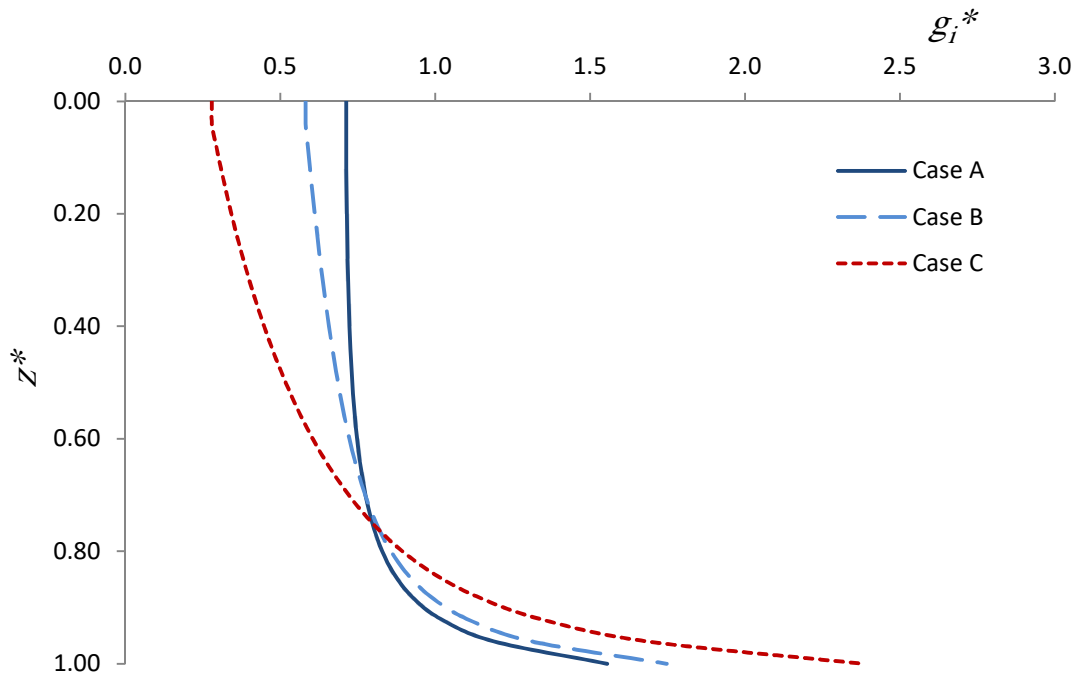
**Figure 3.**

(Colour on the Web)

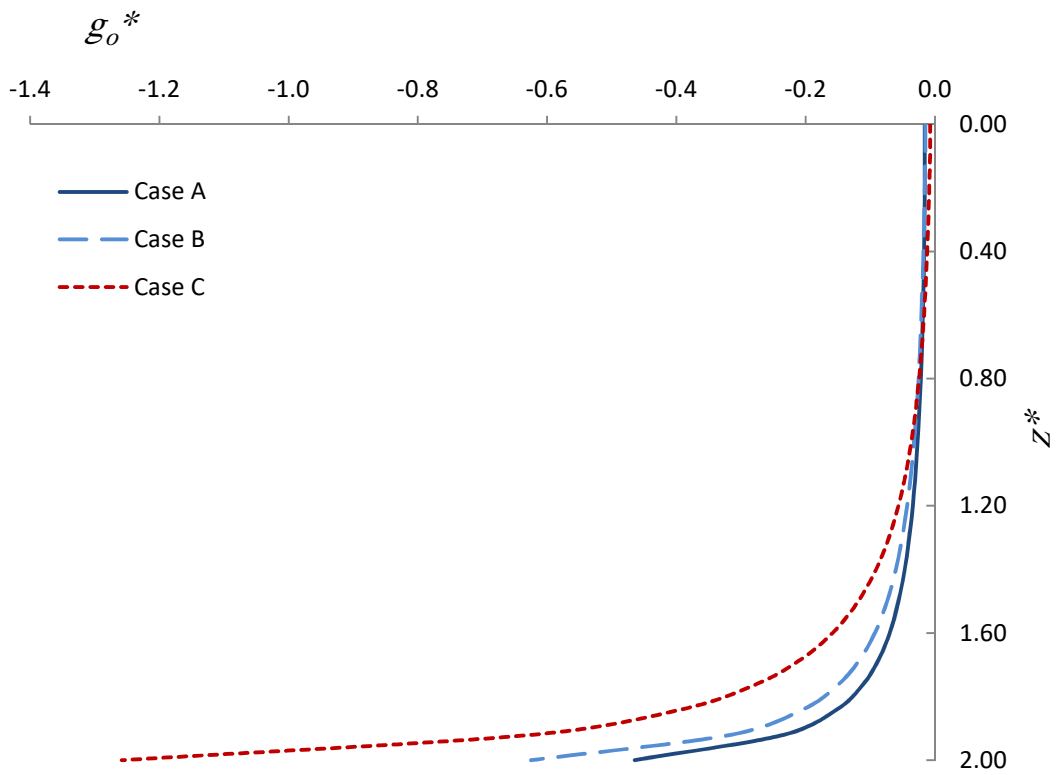
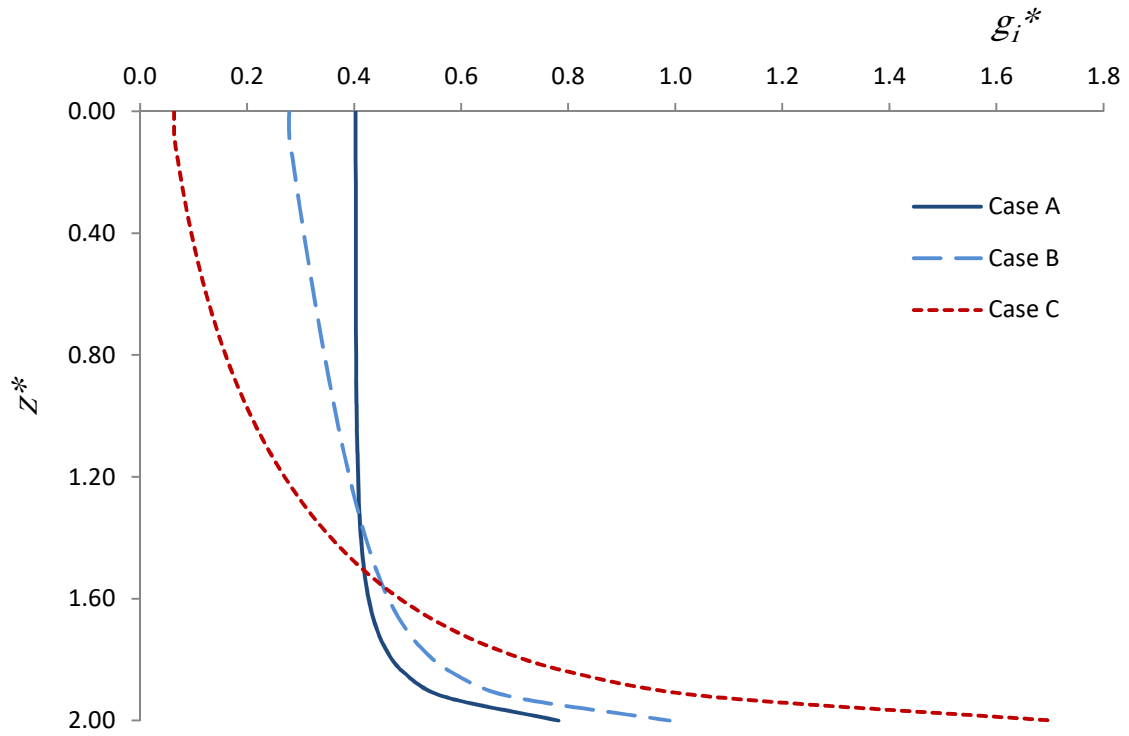


(a)





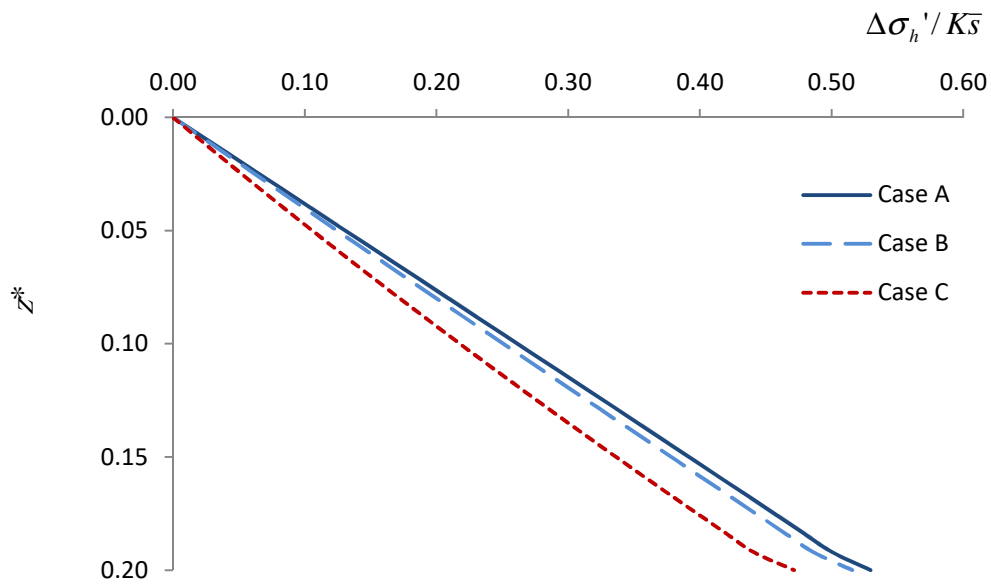
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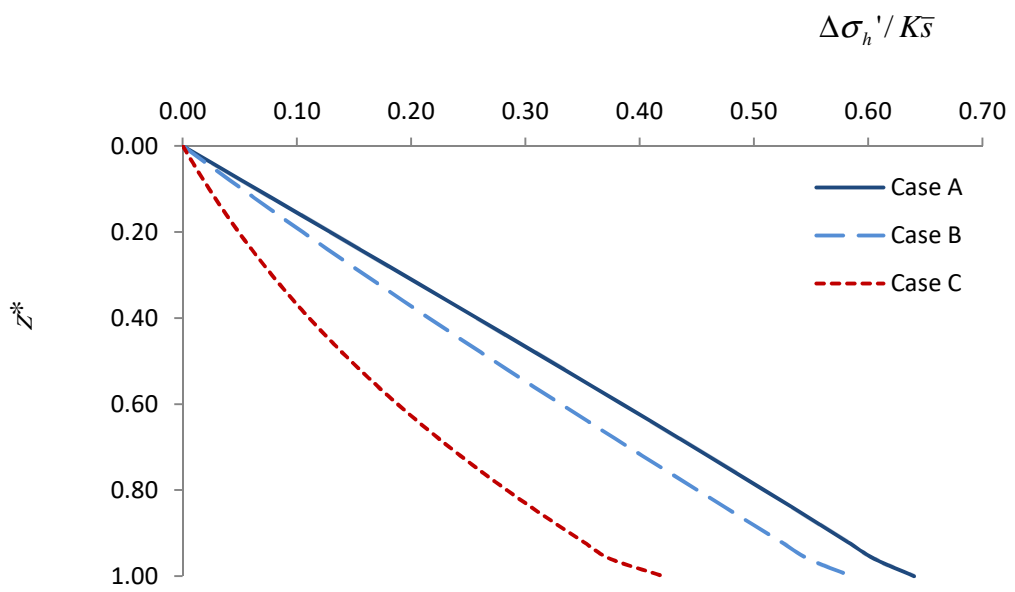
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Figure 4.

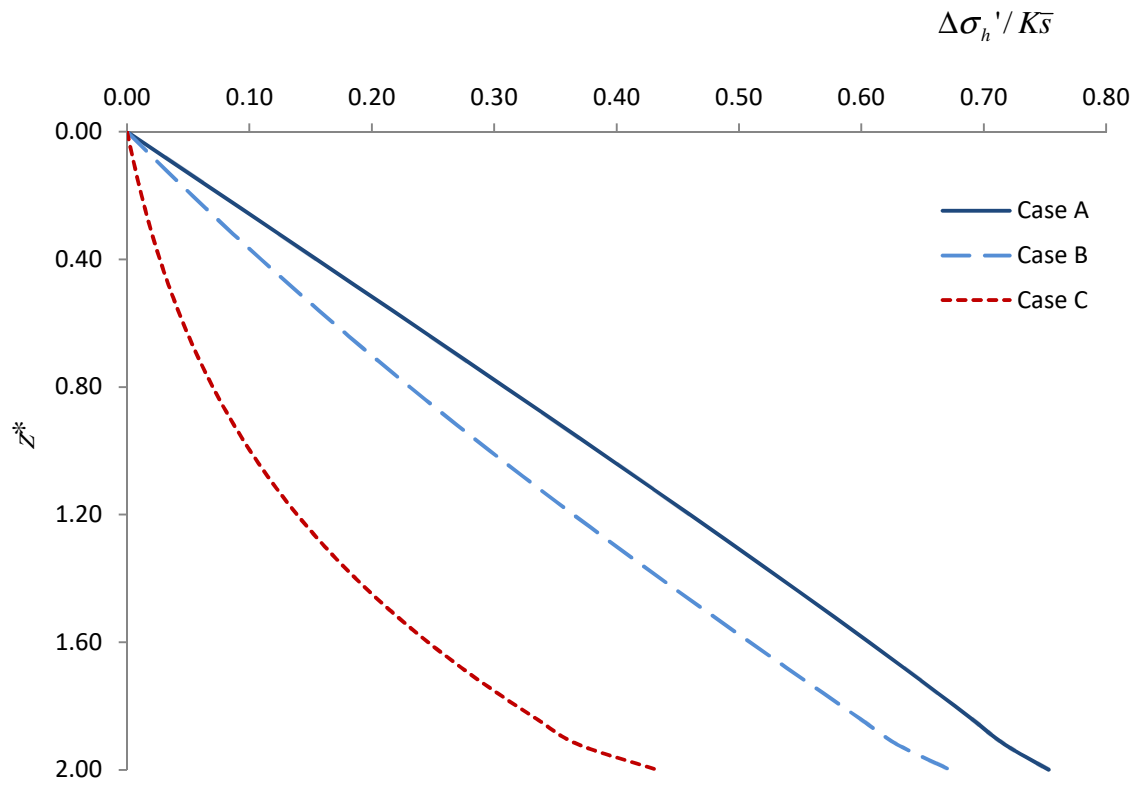
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(a)



(b)

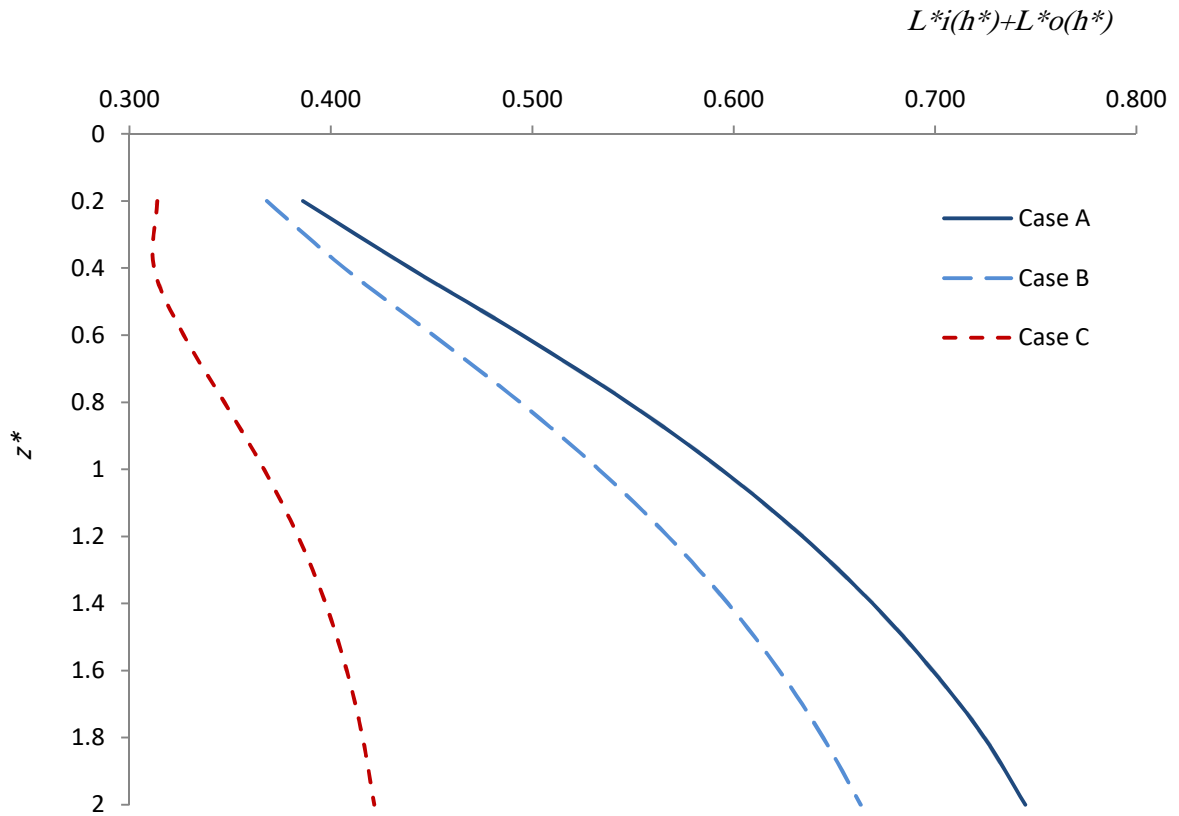


(c)

**Figure 5.**

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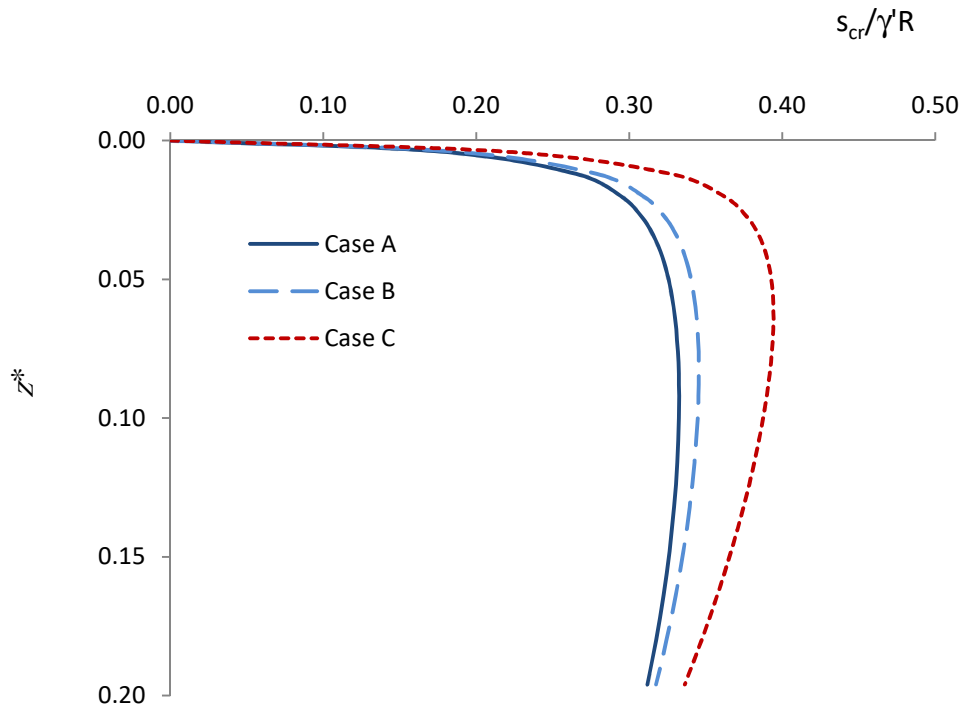
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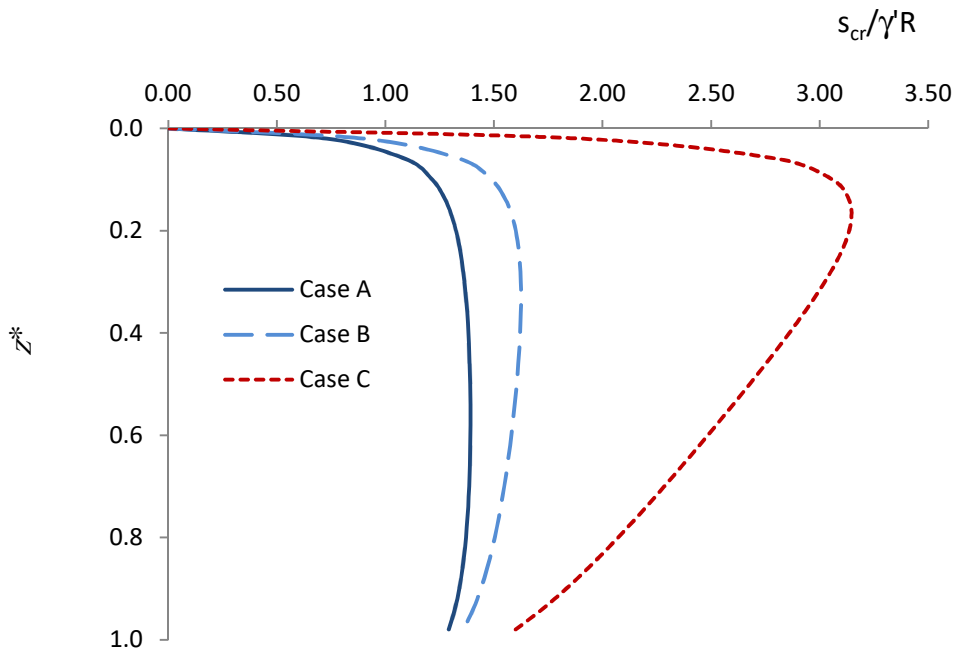
**Figure 6.**

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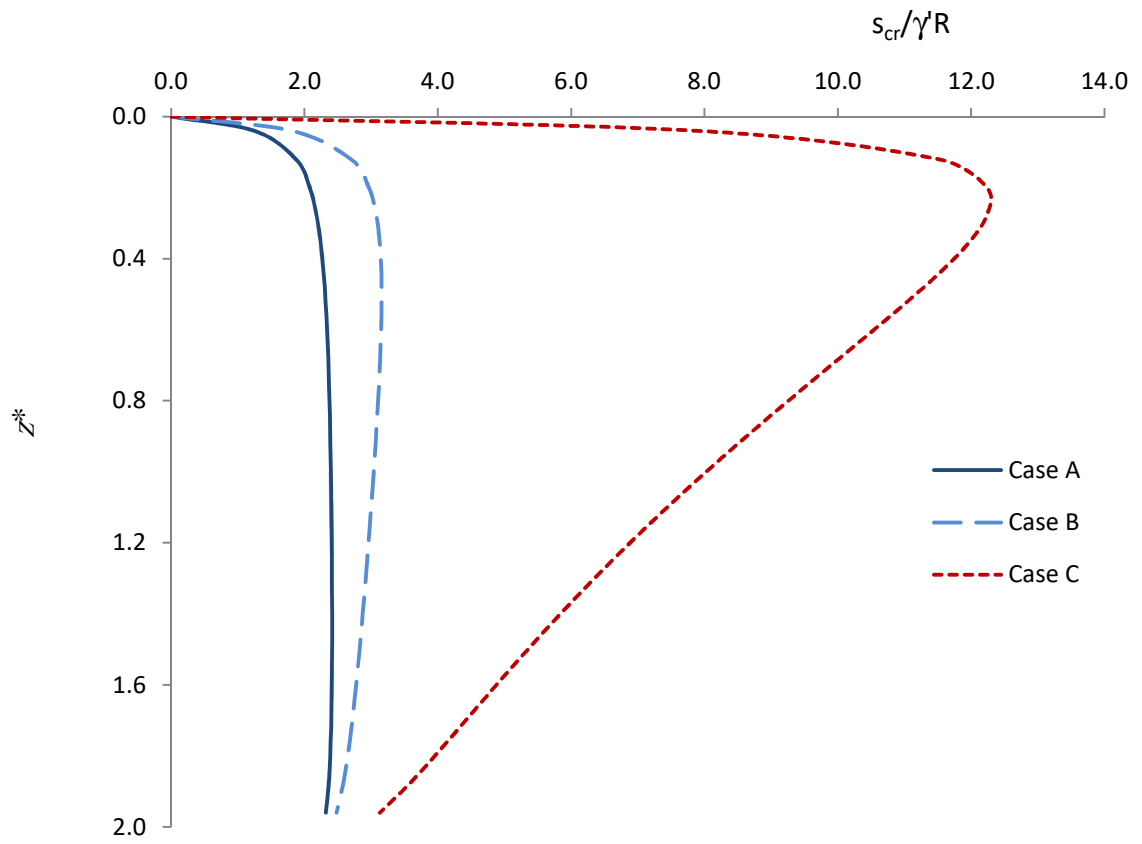
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(a)



(b)



(c)

**Figure 7.**

(Colour on the web)