

Vector solitons in harmonic mode-locked erbium-doped fiber lasers

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ABSTRACT

We report experimental study of vector solitons for the fundamental and harmonic mode-locked operation in erbium-doped fiber lasers with carbon nanotubes based saturable absorbers and anomalous dispersion cavities. We measure evolution of the output pulses polarization and demonstrate vector solitons with various polarization attractors, including locked polarization, periodic polarization switching, and polarization precession.

Keywords: Mode locked lasers, solitons, polarization dynamics, fiber lasers

1. INTRODUCTION

To describe a train of short pulses with a specific shape defined by a complex interplay and balance between the effects of gain/loss, dispersion, and nonlinearity in mode-locked fiber lasers (MLFLs), the concept of dissipative solitons has been recently introduced^{1,2}. With an increased gain in active medium, fundamental soliton becomes unstable and more complex waveforms can appear, viz. multi-pulsing^{3,4}, harmonic mode locking⁵, soliton molecules^{1,2,6-13}, and soliton rain^{1,14}. The multi-pulsing and harmonic mode-locking arises as a result of an interplay between the laser cavity bandwidth constraints and the energy quantization associated with the resulting mode-locked pulses^{3,4}.

Harmonic mode-locking provides the technique for high repetition rates pulse generation in passively MLFLs, which is of great interest for telecommunications and sensing applications. Typically MLFLs operate at repetition rates in the order of MHz due to relatively long laser cavities, however, the increase of the pump power results in solitons breakup leading to multi-pulsing and harmonic mode-locking. When compared to active mode-locking techniques, passive mode-locking has reduced complexity and a potential to obtain shorter optical pulses at high repetition rates. Polarization dynamics in MLFLs is important to reveal the pulse train stability, which is vital for fibre optic communications and all-optical clock recovery.

Recently, the vector nature of dissipative solitons has been exploited to reveal polarization dynamics of dissipative solitons or so-called vector dissipative solitons (VDSs)^{4,8,13,15}. Apart from the fundamental interest, VDSs provide a base for advances in increased capacity in fiber optic telecommunications, secure communications, trapping and manipulation of atoms and nanoparticles, control of magnetization in data storage devices and many other areas¹⁶⁻²⁵. In our previous publications we have already studied experimentally conditions for emerging and suppression of VDSs for multi-pulse and bound-states operation^{4,8,13,15}.

In this paper, we address issues related to the noise properties of harmonic mode-locked operation and control of state of polarization (SOPs) in both fundamental and harmonic mode-locked regime. Harmonic MLFLs based on carbon nanotubes (CNTs) demonstrated sub-picosecond pulses at high repetition rates²⁶. We present experimental study of polarization attractors of fundamental and harmonic mode-locked regimes for two fiber lasers with different gain fibers. Unlike polarization dynamics of vector solitons on the Poincaré sphere demonstrated by Akhmediev, Soto-Crespo²⁷ and Komarov et al.²⁸, we demonstrate new insight related to contribution of polarization hole burning in an active medium to the polarization dynamics.

2. EXPERIMENTAL SET-UP AND RESULTS

We used two fiber laser configurations in these studies. The laser 1 ring cavity shown in Fig.1 with a total cavity length of 8 m (a) included high concentration erbium doped fiber (2m of LIEKKITM Er80-8/125), single mode fiber (SMF-28)

with anomalous dispersion, a 99/1 tap, an optical isolator, a polarization controller (PC), a wavelength division multiplexing (WDM) coupler, an output coupler, and a fast (370 fs relaxation time) saturable absorber based on carbon nanotubes (CNTs). The laser 2 configuration was similar to that of the laser 1, but with different erbium doped fiber used as a gain: 40 cm of LIEKKI™ Er110-4/125. In both cases, the gain fiber was pumped at 976 nm by a laser diode via a 980/1550 nm WDM coupler and a PC. The maximum pump laser diode current was about 355 mA, which corresponded to 170 mW of optical power. We used a single-wall CNTs polymer film embedded between standard FC/APC fiber connectors as a saturable absorber. CNTs films preparation and characterization was as described in Ref. 28. In experiments, the pump current of the laser diode was increased and various polarization attractors were obtained by varying both the in-cavity and pump PCs for a given pump power.

The laser outputs were characterized using optical and electronic spectrum analyzers (ANDO AQ6317B and HP8562), an inline polarimeter (Thorlabs, IPM5300) and a fast oscilloscope (Tektronix DPO7254). The dynamics of SOP was characterized using the inline polarimeter, which measured the normalized Stokes parameters s_1, s_2, s_3 , output power and degree of polarization (DOP) producing 1024 samples with 1 μs resolution (25 round-trip times).

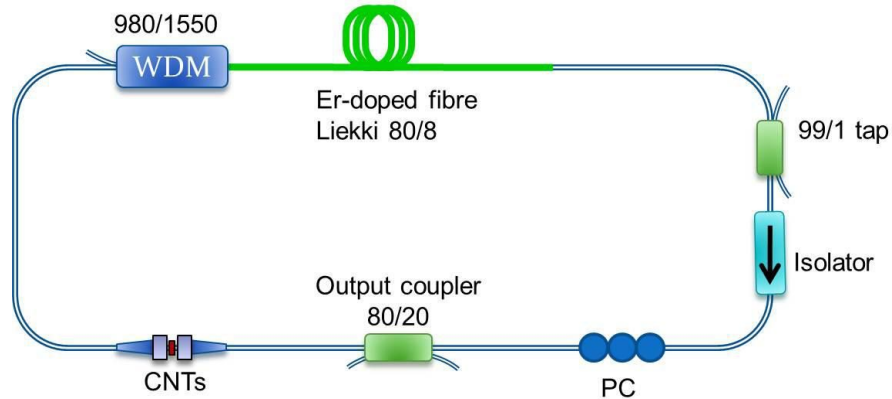


Figure 1. Configuration of Erbium-doped fiber laser with single wall carbon nanotubes (CNTs) saturable absorber. PC -- polarization controller, WDM -- wavelength division multiplexing coupler, CNTs – carbon nanotubes based saturable absorber.

The Stokes parameters are related to the output powers of two linearly cross-polarized SOPs $|u|^2$ and $|v|^2$, and phase difference between them $\Delta\phi$ as follows:

$$S_0 = |u|^2 + |v|^2, S_1 = |u|^2 - |v|^2, S_2 = 2|u||v|\cos\Delta\phi, S_3 = 2|u||v|\sin\Delta\phi \quad (1)$$

The normalized Stokes parameters s_1, s_2, s_3 , and a degree of polarization (DOP) are defined as:

$$s_i = \frac{S_i}{\sqrt{S_1^2 + S_2^2 + S_3^2}}, \quad DOP = \frac{\sqrt{S_1^2 + S_2^2 + S_3^2}}{S_0}, (i = 1, 2, 3) \quad (2)$$

The evolution of normalized Stokes parameters over time produces a track on the Poincarè sphere, which is commonly used to visualize polarization dynamics. In experiments, the pump power was varied and various polarization attractors were obtained by tuning both the intra-cavity and pump laser PCs.

Pump current was tuned between 50 and to 400 mA, and various harmonics were achieved in the laser operation. Pump power increase resulted in the multiple-pulsing and harmonic mode-locking, with a higher pump power leading to a larger number of solitons and higher harmonics. This multi-pulsing arises due to limited cavity bandwidth constraints^{3,5}. Soliton spectral bandwidth increase with the pump power is limited by the cavity gain bandwidth, which forces a single pulse split into two pulses with energy divided between them and spectral bandwidth within the gain

bandwidth window. Low noise harmonic mode-locking was achieved with over 50 dB sidebands suppression ratio up to 10th harmonic. The sidebands increased with harmonic number, as shown in Figure 2. We achieved up to 13th harmonic for both laser 1 and laser 2.

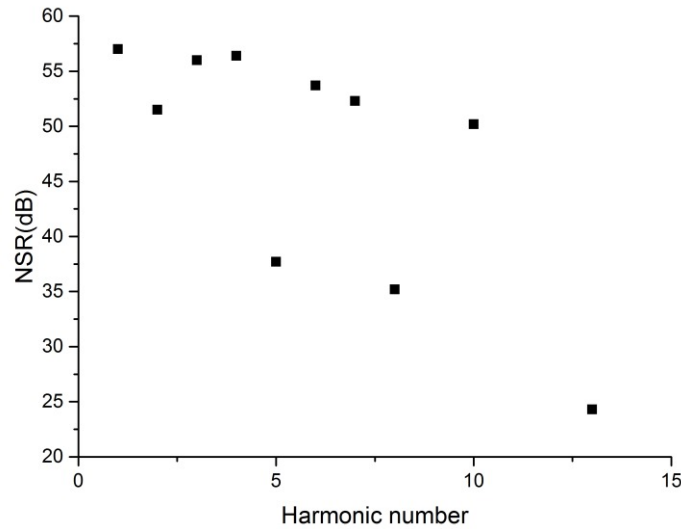


Figure 2. Sidebands suppression ratio versus harmonic number. Laser 1.

3. POLARIZATION ATTRACTORS

Tuning of the both pump and intra-cavity PCs lead to a large diversity of the laser operation regimes, including harmonic mode-locking, bound states and multi-pulsing. By varying the intra-cavity PC we could achieve VDSs with

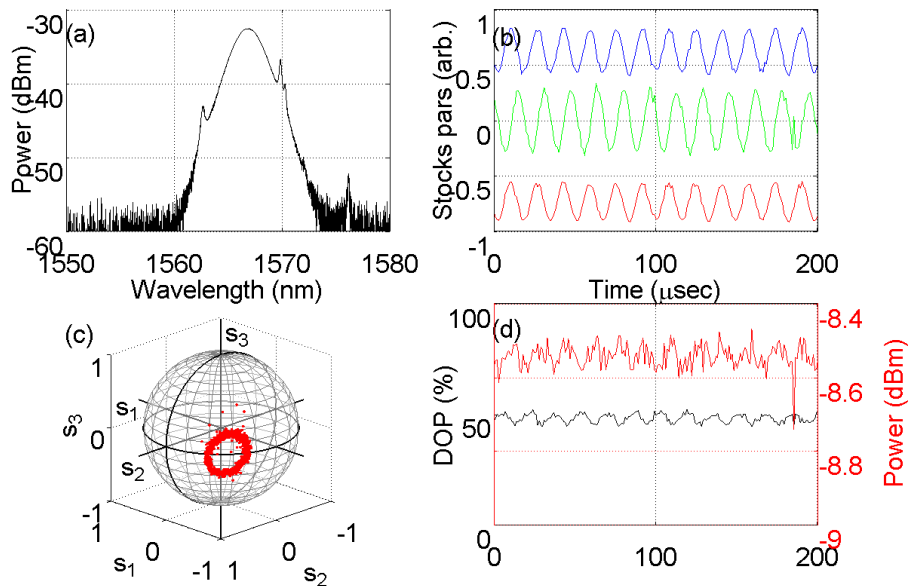


Figure 3. VDSs with circularly evolving SOP. (a) optical spectrum, (b) normalized Stokes parameters s_1 (red), s_2 (blue), s_3 (green), (c) Poincaré sphere, (d) degree of polarization (black) and output power (red). Pump LD current 150 mA.

different polarization dynamics, such as polarization-locked vector solitons, solitons with precessing, switching and chaotic SOP⁴. Polarization attractors measured for fundamental mode-locking for laser 1 are shown in Figs. 3-4. Figure 3 (a) demonstrates a typical spectrum of a soliton operation with Kelly sidebands, the oscilloscope traces and electronic spectrum revealed fundamental mode-locking operation.

Figure 3 (c) demonstrates slow circularly evolving SOP evolution. Similar polarization dynamics was also observed for the second harmonic and multi-pulse operation. The evolution of the Stokes parameters shows periodic dynamics of SOP with a period of $\sim 17\mu\text{s}$. This exotic behavior is described in the next discussion section. Figure 4 shows VDSs at the fundamental harmonic with the sector-type attractor with grouping at two orthogonal SOPs (Fig.4 (c)).

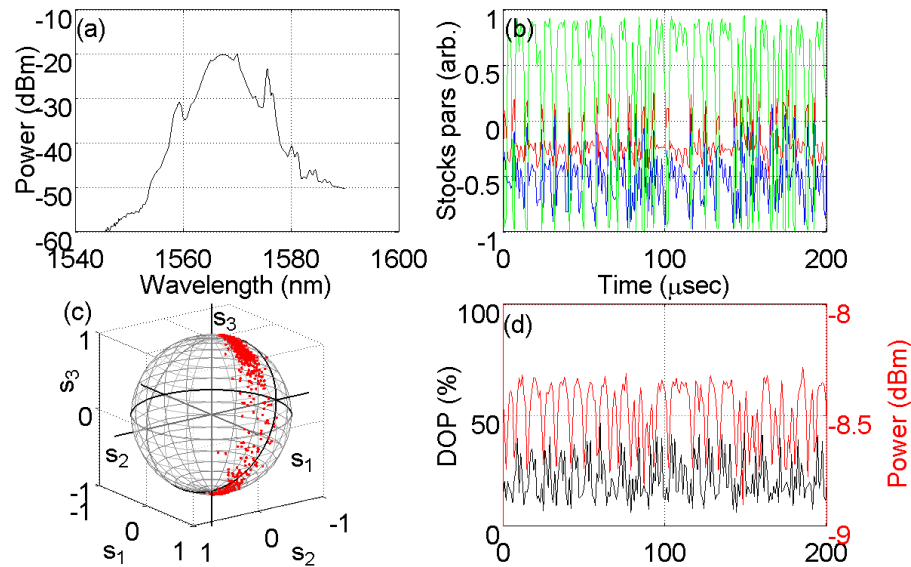


Figure 4. VDSs with conical polarization attractor. (a) optical spectrum, (b) normalized Stokes parameters s_1 (red), s_2 (blue), s_3 (green), (c) Poincaré sphere, (d) degree of polarization (black) and output power (red).

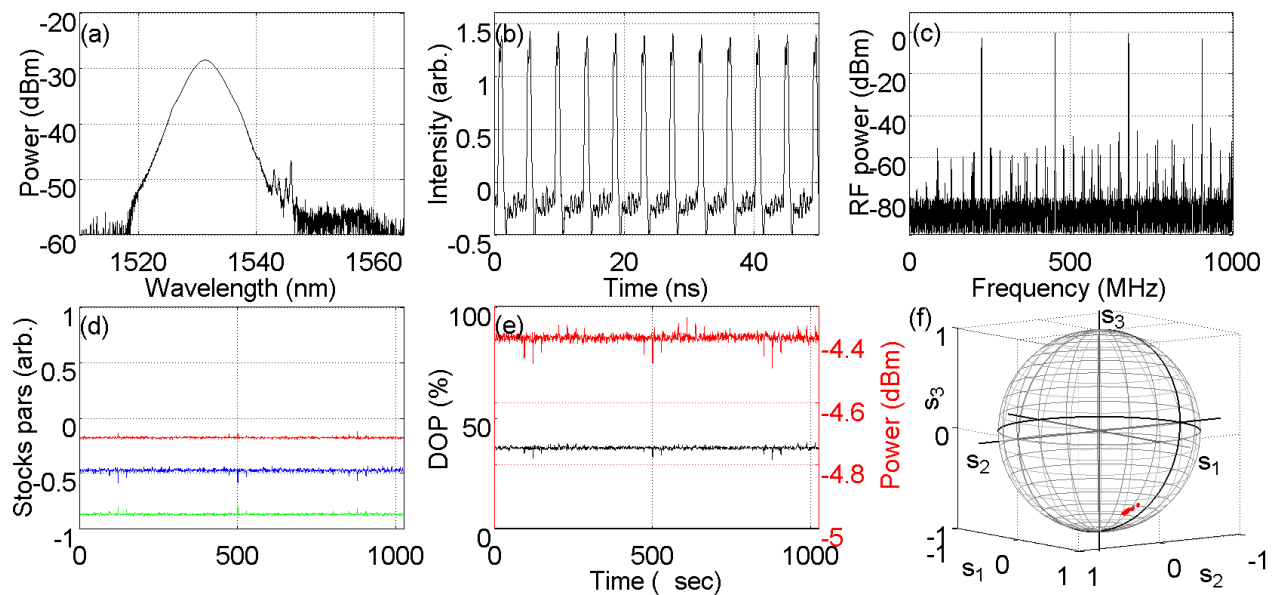


Figure 5. VDSs at the 8th harmonic with locked polarization. (a) optical spectrum, (b) pulse train, (c) electronic spectrum, (d) normalized Stokes parameters, (e) degree of polarization (black) and output power (red), (f) Poincaré sphere.

Polarization attractors measured for laser 2 are shown in Figs. 5-7. Figure 5 shows polarization-locked VDSs at 8th harmonics. Polarization-locked VDSs could be achieved for different harmonics studied and fundamental mode-locking operation as well. Figures 6 and 7 show VSs at 11th harmonic with localized (Fig. 6) and chaotic (Fig. 7) polarization. Polarization-locked VSs were also achieved at 11th harmonic. Remarkably, optical (a), RF spectra (c) and pulse trains (b) were nearly identical for all these regimes, and only polarization attractors could reveal the differences.

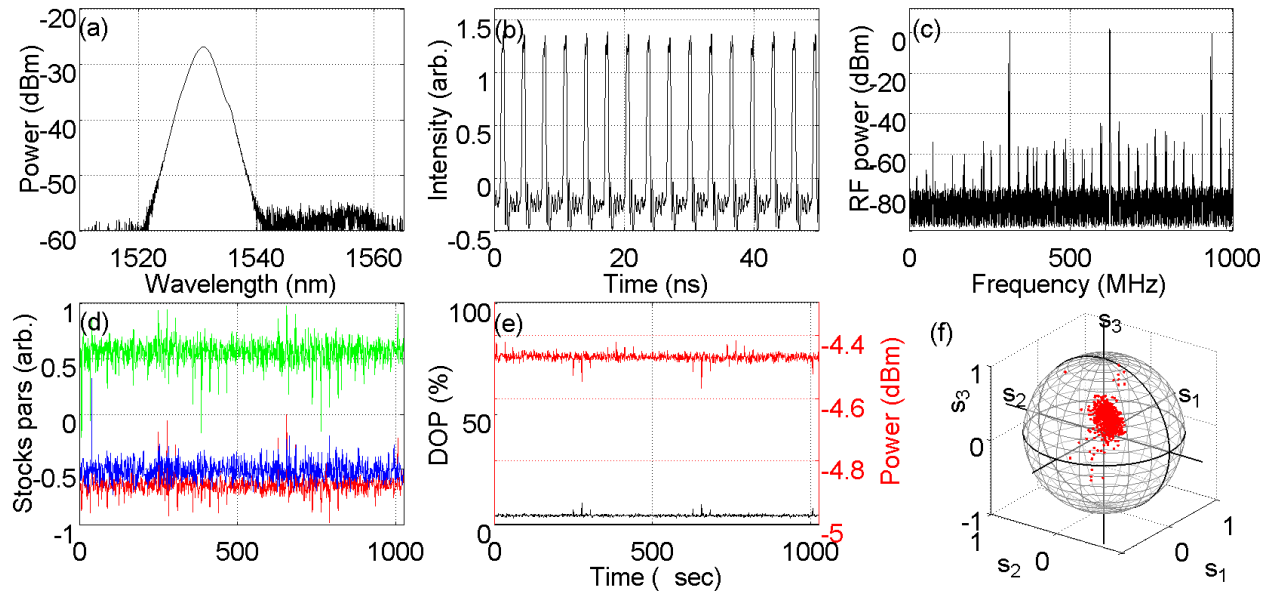


Figure 6. VDSs at the 11th harmonic with polarization localized in a disk area. (a) optical spectrum, (b) pulse train, (c) electronic spectrum, (d) normalized Stokes parameters, (e) degree of polarization (black) and output power (red), (f) Poincaré sphere.

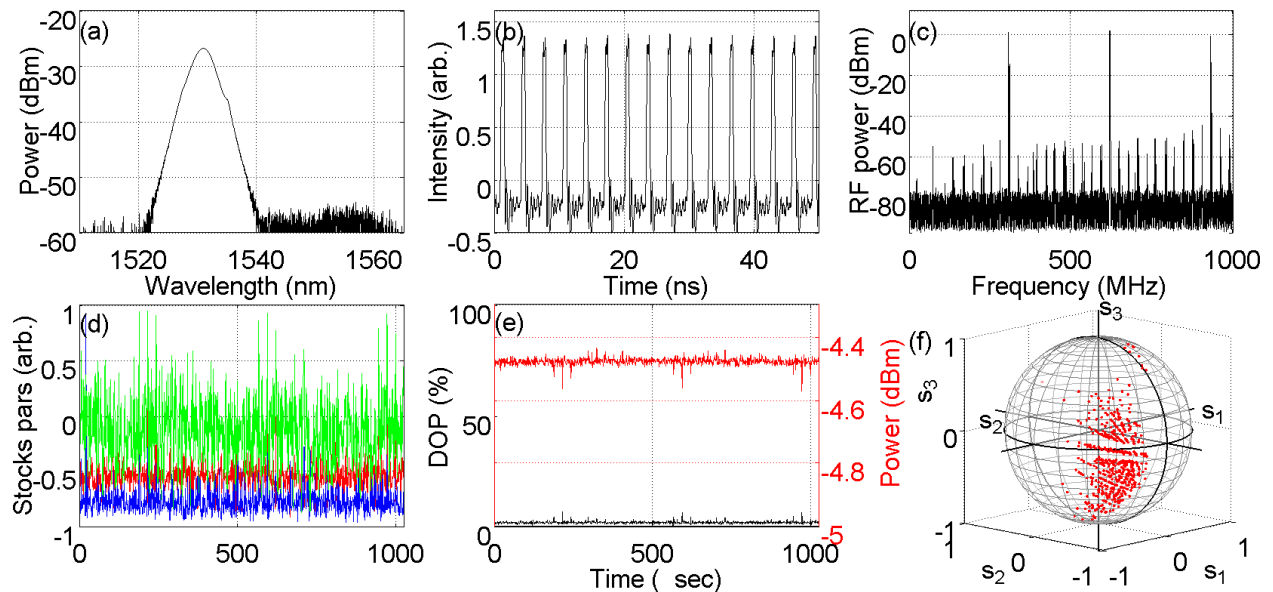


Figure 7. VDSs at the 11th harmonic with chaotic polarization. (a) optical spectrum, (b) pulse train, (c) electronic spectrum, (d) normalized Stokes parameters, (e) degree of polarization (black) and output power (red), (f) Poincaré sphere.

4. DISCUSSION

As shown by Akhmediev and Soto-Crespo²⁷ and Komarov et al²⁸, the eigenstates in a fiber in the presence of linear birefringence and circular birefringence caused by nonlinear self-phase modulation are split into two pairs:

$$S^{(1,2)} = \begin{pmatrix} S_0 \\ \pm S_0 \\ 0 \\ 0 \end{pmatrix}, \quad S^{(3,4)} = \begin{pmatrix} S_0 \\ -\alpha \\ 0 \\ \pm \sqrt{S_0^2 - \alpha^2} \end{pmatrix}. \quad (3)$$

Here $S_0 = \text{const}$ and α is determined by the ratio of linear to circular birefringence strength. In mode locked laser, in-cavity polarization controller contributes both into linear and circular birefringence, whereas anisotropy induced by pump light is suppressed due to relaxation orientation caused by excitation migration²⁹. Mode-locked operation also changes the birefringence in the cavity (both linear and circular) due to polarization hole burning and so it leads to pulse-to-pulse evolution of the SOP. If the beat length for the anisotropy caused by in-cavity polarization controller and polarization hole burning is equal to the round trip and pulse-to-pulse power is constant, then pulse SOP is not changed and so vector soliton is polarization locked¹³. In the case of round trip distance being equal to half or third of beat length, the SOP is reproduced in two or three round trips and, therefore, polarization switching takes the forms shown in Fig. 4. With increased pump power, amplitude instability emerges and leads to periodical oscillations of the output power. If the round trip is equal to the rational part of the beat length then SOP after few round trips will slightly deviate from the initial one and can only reproduce itself for the period of pulse power oscillations. Otherwise, pulse-to-pulse SOPs cannot be reproduced and so the SOPs fill densely the circle on Poincare sphere, as shown in Fig. 3 (c).

5. CONCLUSIONS

We have revealed new types of vector solitons in a carbon nanotube mode locked fiber laser with anomalous dispersion cavity. The observed evolution of the states of polarization includes periodic polarization switching between two SOPs, and circular evolution of SOP. We achieved high harmonics operation with sideband suppression ratio of over 50 dB up to 10th harmonic. Our experimental studies can help to design new types of lasers with controlled dynamical states of polarization that are of a special high interest for applications in fiber optic telecommunications²²⁻²⁵, in nano-optics (trapping and manipulation of nanoparticle and atoms¹⁹), and spintronics (vector control of magnetization²⁰).

6. ACKNOWLEDGMENTS

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