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4 **Review of low-temperature vapour power cycle engines with quasi-**
5 **isothermal expansion**
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14 **Abstract**

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17 External combustion heat cycle engines convert thermal energy into useful work. Thermal energy
18 resources include solar, geothermal, bioenergy, and waste heat. To harness these and maximize work
19 output, there has been a renaissance of interest in the investigation of vapour power cycles for quasi-
20 isothermal (near constant temperature) instead of adiabatic expansion. Quasi-isothermal expansion
21 has the advantage of bringing the cycle efficiency closer to the ideal Carnot efficiency, but it requires
22 heat to be transferred to the working fluid as it expands. This paper reviews various low-temperature
23 vapour power cycle heat engines with quasi-isothermal expansion, including the methods employed to
24 realize the heat transfer. The heat engines take the form of the Rankine cycle with continuous heat
25 addition during the expansion process, or the Stirling cycle with a condensable vapour as working
26 fluid. Compared to more standard Stirling engines using gas, the specific work output is higher.
27 Cryogenic heat engines based on the Rankine cycle have also been enhanced with quasi-isothermal
28 expansion. Liquid flooded expansion and expander surface heating are the two main heat transfer
29 methods employed. Liquid flooded expansion has been applied mainly in rotary expanders, including
30 scroll turbines; whereas surface heating has been applied mainly in reciprocating expanders.
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35 **Keywords:**

36 Vapour power cycle
37 Quasi-isothermal expansion
38 Renewable energy
39 Waste heat utilisation
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1. Introduction

Owing to the global energy challenges associated with fossil fuel – rising cost, energy security and climate change – there has been growing interest into sustainable alternatives or renewable energy sources such as: wind, solar, geothermal, biomass and waste heat. Presently, renewable energy sources account for less than 15% of the global energy supply [1], of which biomass is a major contributor. However, solar has recorded the fastest growth, and renewables have been projected to become the world's second largest source of power generation by 2015 [2]. Studies have already shown that the renewable heat sources have the potential of meeting the global energy demand several times over [3]. As a means of encouraging the exploitation of the renewable heat sources, 'heat policies' (including incentives) have been introduced in some countries [4]. Globally, solar, biomass and waste heat are readily available in distributed form as low-grade (<250°C) heat, and are well suited for decentralized small-scale (<100 kW) applications. Thus there has been a renaissance of interest in small-scale external combustion heat engines (gas and vapour power cycles) to convert the thermal energy into useful work, with particular emphasis on improving performance. Isothermal expansion is one technique for achieving such improvement.

Ideally, certain gas power cycles (such as Stirling and Ericsson cycles) perform work by the isothermal (constant temperature) expansion of a compressed and heated gas working fluid (which remains gaseous throughout the entire cycle). They are noted for having the high theoretical efficiencies of the Carnot cycle – which is the maximum obtainable efficiency for given temperature limits [5]. On the other hand, for vapour power cycles (typically the Rankine cycle), the working fluid is a condensable vapour, and is intermittently vaporised and condensed; the expansion process is adiabatic (i.e. the fluid expands without experiencing heat transfer during the process) and produces less work than its isothermal counterpart [6]. Nevertheless, in comparison to the gas compression work of the gas power cycles, less input work is required to pressurize the condensed liquid of the vapour power cycles, and the total cycle pressure-volume characteristics exhibit greater work output than the gas cycles. Thus the vapour cycle engines have higher specific work output [7]. The vapour power cycles can also have advantages over gas cycle equivalents because the phase change allows smaller surface areas and temperature differences to drive the boiling/condensation required by the cycle. This inference arises from the higher heat transfer coefficients associated with phase change (by orders of magnitude) relative to that of forced convection for gas [8]. The smaller surface areas lead to compact heat exchangers and engine size [9]; this together with the higher work output gives the vapour cycle engines higher power density; and the low temperature differences aid better performance (relative to the gas cycles) in low-grade heat applications. This has been demonstrated in a study that showed the Rankine cycle to be more efficient than Stirling cycle for temperature range of 150 – 300°C [10].

In power plants operating on the Rankine cycle, reheating is a practical approach to improve the cycle efficiency and specific work output. As the number of stages of reheating increases, the expansion and reheat processes approximate an average isothermal process and the cycle efficiency increases [11]. But in the reheating process, the steam must be returned back to the boiler for each reheat, which, besides requiring many additional components, inevitably adds complexity to the plant layout and geometry, and results to heat and pressure losses [12]. Alternatively, the vapour cycle engine could be designed in such a way that (like the Stirling or Ericsson engines) heat is continuously transferred to the working fluid during the expansion process thus resulting in isothermal expansion, or more realistically, quasi-isothermal expansion – which may be somewhere between the adiabatic and ideal isothermal processes.

In this paper, relevant research works with emphasis on low temperature vapour power cycles with quasi-isothermal expansion will be presented. Various methods employed to effect quasi-isothermal operation, including concepts, studies and results, will be reviewed to provide an insight into their practicality, system performance and energy efficiency. The first part (section 2) of the paper presents

the general theoretical advantage of quasi-isothermal expansion, including the various heat transfer methods used to achieve it. The second part (section 3-5) of the work covers the power cycles to which the methods are applied. For each power cycle, the theory and principle of operation is explained, and then specific studies are reviewed in which these cycles have been implemented. Fig. 1 classifies the methods and vapour power cycles for quasi-isothermal operation according to the approach used in this review.

2. Quasi-Isothermal expansion

The paths of both the isothermal and adiabatic expansion processes can be illustrated graphically on a pressure-volume (P-v) plane as shown in Fig. 2, using the gas equation $P_1 v_1^n = P_2 v_2^n$. The expansion index n is equal to 1 and k for isothermal and adiabatic processes respectively [13], where k is the ratio of the specific heats (C_p/C_v) of the gas, and is always >1 [14]. For example, under a substantial range of operating conditions, k is about 1.4 for nitrogen gas and steam [15].

The work output is simply the integral ($\int PdV$) between the two end states (1 and 2), as is represented by the area under the path curves. Hence, from the figure it can be seen that the area under the curve (i.e. the expansion work output) for the adiabatic expansion is less than that of an isothermal expansion having the same initial operating conditions. This can also be seen numerically from the integration of both curves from state 1 (start of expansion) to state 2 (end of expansion).

The work done by isothermal expansion can be given as [16]:

$$W_{iso} = \int PdV = P_1 v_1 \ln\left(\frac{P_1}{P_2}\right) \quad (1)$$

Similarly, the work done by adiabatic expansion can be expressed as:

$$W_{ad} = \int PdV = P_1 v_1 \frac{1 - \left(\frac{P_1}{P_2}\right)^{\frac{1-n}{n}}}{n-1} \quad (2)$$

Hence, from the above equations, the relative improvement of the isothermal expansion work over the adiabatic work can be expressed in terms of the expansion index and pressure ratio $r_p = P_1/P_2$ as:

$$Relative\ improvement = \frac{W_{iso}}{W_{ad}} - 1 = \left[\frac{(n-1) \ln(r_p)}{(1-r_p)^{\frac{1-n}{n}}} \right] - 1 \quad (3)$$

For example, with $r_p = 7$ and $n = 1.4$, eq. 3 shows that the isothermal expansion gives 83% more work than the adiabatic.

The expansion process of conventional vapour power cycles is generally assumed adiabatic, and as such is subject to this reduced work output [6]. The adiabatic expansion process is also characterised by drop in temperature from T_1 to T_2 . Hence, modifying an adiabatic expansion to an isothermal one would ideally require the addition of heat to the expanding fluid to maintain its temperature constant.

In reality, when the heat absorbed by the vapour is not sufficient to maintain isothermal expansion, the result is termed quasi-isothermal expansion. In this case, the heat absorbed shifts the expansion

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4 process from adiabatic behaviour towards the ideal isothermal behaviour. Consequently, the work
5 output will be more than the adiabatic work, but less than the isothermal work available, in proportion
6 to the extent to which the expansion approaches the isothermal case. This extent has been termed
7 isothermality, γ , defined as the ratio of actual work output to the ideal isothermal work [17].
8

$$\gamma = \frac{W_{ac}}{W_{iso}} \quad (4)$$

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12 Thus it determines the work output as a fraction of the isothermal work available. On the other hand,
13 for rotary expanders some authors have described the extent of isothermal behaviour as the ratio of
14 discharge temperature to supply temperature [18].
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17 18 2.1. Methods of effecting quasi-isothermal expansion 19

20 Over the years, a number of methods have been developed, by which a vapour power cycle's working
21 fluid can continuously gain heat during the expansion process to effect quasi-isothermal expansion;
22 often times this result in variants of the traditional power cycles. The identified methods can be
23 generally grouped on the basis of the means of heat transfer as: secondary fluid heating and expander
24 surface heating. The methods and the power cycles (including the variants) to which it is applied are
25 shown in Table 1.
26

27 28 2.1.1. Expander surface heating 29

30 A simple approach to achieve heat transfer to the working fluid during the expansion process is to
31 provide a means of heating the expander sufficiently above the fluid temperature; such that during the
32 expansion process, heat could be effectively transferred from the surface of the expansion chamber to
33 the fluid, as illustrated in Fig. 3a. This is quite popular for reciprocating expanders as found in
34 conventional Stirling engines, and steam-jacketed steam engines. The extent of isothermal operation
35 achievable here will depend on the rate of heat transfer, which is a function of the overall heat transfer
36 coefficient and temperature differential between the engine wall and the fluid, and the surface area of
37 the wall exposed to the fluid [19]. As such, geometries giving high surface to volume ratios such as
38 tubes and fins are generally utilised to increase the total heat transfer area as found in conventional
39 Stirling engines [20].
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42 43 2.1.2. Secondary fluid heating 44

45 The heat transfer required to effect quasi-isothermal expansion could be provided by means of a
46 secondary fluid which co-exists with the working fluid in the expander during the expansion process
47 (Fig. 3b). In this case, the secondary fluid – which will ideally be of a high thermal content – is
48 dispersed into the working fluid such that during the expansion process, the temperature dropped by
49 the expanding working fluid is quickly recovered from the secondary fluid. The heating fluid could
50 ideally be a vapour – as with direct steam injection; or more practically, a liquid – as with liquid
51 flooded expansion.
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53 54 2.1.2.1. Direct steam injection 55

56 The concept of achieving isothermal expansion by direct steam injection entails injecting small
57 amount of relatively very high temperature steam (secondary fluid) into the expanding steam [21].
58 The secondary steam transfers heat to the working steam by virtue of its higher temperature thermal
59 content, as such requires the secondary steam to be continuously injected with appropriate amount and
60 temperature in such a way as to keep the expansion temperature constant.
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2.1.2.2. Liquid flooding

The liquid flooding process involves literally flooding a screw or scroll machine with a large quantity of liquid simultaneously as the working fluid passes through the device, such that the liquid provides a medium of heat exchange with the working fluid whilst in transit through the device. Unlike with steam injection, the secondary fluid is normally different from the working fluid, and is immiscible with it. This concept can ideally be applied to compression and expansion processes (its application to expansion processes will be covered in section 3.2.1). Over the last two decades, there have been a significant number of studies on the application of liquid flooding to compressors. Researchers have studied oil-flooding in screw compressors [22] and scroll compressors [23] primarily to improve sealing and lubrication, but without much emphasis on heat transfer [24]. In recent years, conventional screw [25] and scroll [26] compressors have been effectively used in reverse as expanders (with minor modifications) , thus widening the scope for liquid-flooded expansion. The combinations of the different working fluids and flooding liquid considered in the literature are shown in Table 2.

The concept of flooded expansion (and compression) was studied by Hugenroth [27] in a liquid flooded Ericson cycle cooler, which used liquid flooding of both the compressor and the expander (to achieve nearly isothermal compression and expansion) to overcome the practical difficulties of achieving isothermal conditions in the basic reverse Ericson cycle. In a later experimental work [28], off-the-shelf automotive scrolls were used as the compressor and expander, nitrogen as the working fluid and alkyl-benzene as the flooding liquid. The performance of the off-the-shelf scroll machine was not sufficient to achieve high cycle efficiency. For increasing operating pressure ratios, the expander adiabatic efficiency was seen first to increase and then to decrease. This effect was partly attributed to the limitation of the expander not being designed for liquid flooded operation

To optimize the design of the compressor and the expander, Bell et al. [29] developed comprehensive models of both machines. Validation of the models and optimization of the design were also carried out [30]. The model developed was an extension of earlier models that were developed by Halm [31], and Chen et al [32] for scroll compressors without liquid flooding. The important contribution of the work was said to be the treatment of a mixture of gas and large fraction of oil. Also, Lemort et al. [33] further studied the performance of liquid flooded expansion using scroll expander and developed a detailed model of the flooded scroll expander, to facilitate predictions of the performance over a wide range of operating conditions and design changes. The model was able to predict the shaft power to about 6.7% maximum deviation from measured experimental value.

2.2. Summary

In summary, quasi-isothermal expansion has been identified as a realistic alternative to adiabatic expansion to improve the work output of vapour power cycle engines. This can be achieved by further heat addition to the working fluid during the expansion process. The heat can be transferred by means of heating the expander external surface, or by means of a secondary heating (flooding) fluid. The expander surface heating is found to be more popular with reciprocating engines, whereas the secondary fluid heating is more popular with rotary engines.

3. Quasi-isothermal Rankine cycle engines

3.1. Theory and principle of operation

The quasi-isothermal Rankine cycle is simply a Rankine cycle whose working fluid gains significant amount of heat during the expansion process of the cycle, such that it is somewhere between adiabatic and isothermal, but its reference limit is ideally isothermal, as depicted on the temperature entropy (T-s) diagrams in Fig. 4. Fig 4a shows a case where the expansion starts from a super-heated state [34]; while in Fig 4b, the expansion starts from a saturated state [35]. As a result of the heat addition during the expansion process, the spent vapour becomes significantly superheated at the end of expansion, thus necessitating regeneration (utilising the heat available at the end of expansion to preheat the feed working fluid) to improve the thermal efficiency. Studies have shown that the efficiency of the ideal cycle (with isothermal expansion and regeneration) can be up to 93% of the efficiency of a Carnot cycle operating with the same temperatures limits [21]. Where isothermal expansion is not fully achieved, the resulting quasi-isothermal cycle's performance will depend on the quantity of heat successfully absorbed during expansion, which of course is dependent on the heat transfer technique employed.

3.2. Studies and performance

Using the thermodynamic cycles of Fig 4, researchers have proposed and studied different versions of the quasi-isothermal Rankine cycle using different modes of heat transfer. Thus, both liquid flooded and external heated surface machines have been reported. These implementations will now be reviewed.

3.2.1. Liquid-flooded Rankine cycle

The idea of liquid flooded expansion can be applied to Rankine cycle, as patented by Woodland [36]. A schematic of the system is depicted in Fig. 5. The working fluid and the flooding liquid are both pressurised and heated to the required high side pressure and temperature (via separate pumps and heat exchangers). The fluids are then mixed and fed to the expander where they flow together to do work. During the expansion process, temperature drop of the working fluid (vapour) is inhibited by heat gain from the liquid (because the liquid has a relatively higher heat capacity), thus resulting in a near isothermal expansion. At the end of expansion, the superheated working fluid is then separated from the liquid and passed through a regenerator (before being condensed) to preheat the condensed fluid pumped for the next cycle, as the flooding liquid is simultaneously re-pressurized and heated back to the high side conditions.

Woodland [37] also carried out theoretical study of the application of liquid flooding to organic Rankine cycle (ORC) with regeneration, for different working fluids (ammonia, carbon dioxide, R410a and dry fluids such as iso-butane, n-pentane and R245fa). The analysis showed that, working fluids ammonia and R410a exhibited higher performance improvement due to the flooded expansion. For ammonia, the addition of the liquid flooding offered about 20% more improvement in thermal efficiency. A later study [38] that featured water as a working fluid in the liquid flooded ORC, showed a relative improvement of 10% due to the flooded expansion; the improvement increased with the source temperature. In contrast, the improvement for the dry fluids was significantly less (only about 5%), and approaches zero at higher (>250°C) operating temperatures. Higher work output was expected from the more isothermal flooded expansion than from ordinary expansion process. However, for these dry fluids, the improvement in work output is not high enough to significantly outweigh the additional energy inputs (pump work and heat input) required for the flooding process.

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4 Lemort et al. [39] developed a prototype of a flooded Rankine cycle engine with a hermetic scroll
5 expander and R245fa working fluid. The study was focused on investigating the impact of oil quantity
6 on the expander performance. For operating pressure ratio of 4.2 bar, supply temperature of 92°C and
7 oil mass fraction of 0.023 – 0.1, the results showed that the expander overall isentropic effectiveness
8 (ratio of the measured power output to the ideal expander power) decreased with increasing oil
9 quantity. Further investigation was recommended to ascertain with certainty the underlying reason;
10 nevertheless, increase of supply pressure drops (at the expander inlet) and viscous losses were
11 mentioned as likely reasons for the decrease in performance. This is in agreement with the results of a
12 previous study on the performance of liquid flooded expansion using scroll expander [33]. For a given
13 pressure level, in the experiment, the measured power output reportedly decreased with the oil flow
14 rate as a result of increasing pressure drops due of the oil suction process at the expander inlet. The
15 study also analysed the variation of exhaust temperature with oil fraction for different operating
16 speeds. As would be expected, the result further showed that the expansion tends to approach
17 isothermal behaviour for higher oil fractions. The range of isothermal expansion (in this case defined
18 as the ratio of discharge temperature to supply temperature) achieved was about 0.93 to 0.99 for oil
19 fractions of 0.2 to 0.8 respectively. This shows that, although the liquid flooding facilitated sufficient
20 heat transfer, such that isothermal behaviour is approached, there are practical challenges in
21 translating it to net performance improvement. Another practical issue worth noting is that the
22 separation of the refrigerant from the oil in the oil separator is not generally perfect, as such some
23 amount of refrigerant usually remain entrained in the oil [28]. This entrainment may pose a durability
24 issue in the long run, as higher oil flow rate will result to larger amount of refrigerant entrained, thus
25 it can result in the need for frequent servicing, as has been observed with oil flooded compressor [40].
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28 For the purpose of increasing the efficiency of a trans-critical CO₂ Rankine cycle thermo-electric
29 energy storage (TEES) system, Kim et al. [41] proposed the application of a variant of the liquid
30 flooded concept to achieve isothermal expansion (and compression) for the discharging (and
31 charging) process of the TEES system. The discharging process is basically the retrieval of
32 mechanical-electrical energy from the stored thermal energy by means of a heat engine (Rankine
33 cycle, in this case). Fig. 6 depicts the discharging process of the proposed isothermal TEES system.
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35 The system is somewhat like a double cylinder engine. On operation, pressurised CO₂ is heated in the
36 evaporator and fed via valve 'A' into the first cylinder which is initially filled with hot liquid. The
37 vapour then exerts pressure and expands against the hot liquid (serving as a liquid piston) which flows
38 through the 4-way valve and the hydraulic motor (wherein the flow and pressure of the liquid is
39 converted into rotary work). During the expansion, the circulation pump continually sprays a portion
40 of the hot liquid unto the expanding vapour, thus providing a means of heating the vapour to effect
41 isothermal expansion. The expended liquid continuous in flow, through the heat exchanger in the hot
42 storage tank and back through the 4-way valve into the second cylinder, thus exhausting the hot
43 expanded vapour in the second cylinder via valve 'D' and the regenerator to the condenser. As the
44 stroke ends, the 4-way valve switches to reverse the flow (between the two cylinders), without
45 changing the hydraulic pump's direction of rotation. An analysis of the system performance for the
46 operating conditions of 160 bar and 122°C showed that the isothermal expansion can result in a 46%
47 increase in work output.
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50 51 3.2.2. Expander surface heated engines

52 53 3.2.2.1. Steam jacketed reciprocating steam engine

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55 The steam engine with steam jacket is a classic approach to quasi-isothermal expansion. Nevertheless,
56 certain features and observations are interesting in the modern context where steam or other (organic)
57 working fluids may be used.
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59 In steam engines, there tends to be heat transfer between the steam and the cylinder wall, in such a
60 way that heat is rejected by the steam to the cylinder during the admission and early expansion
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4 process, while heat is transferred from the cylinder to the steam in the later part of the expansion and
5 exhaust. This phenomenon is most pronounced for dry steam (relative to superheated steam) as the
6 heat rejection and gain respectively leads to steam condensation on the cylinder wall and re-
7 evaporation of some of the condensate during the rest of the expansion process thus leaving behind
8 some amount of condensate-water in the cylinder. The condensation of steam in the cylinder results in
9 a very rapid drop in maximum pressure and thus decrease in work output, which implies an increase
10 in steam consumption (quantity of steam) required to achieve a given power output. This
11 consequently results to reduced efficiency, since not all the admitted steam is available to produce
12 work for a given amount of heat energy input to generate the steam [42].
13

14 Besides the use of sufficiently superheated steam, or protecting the cylinder with lagging (insulation),
15 steam jacketing the cylinder can be effectively utilised to mitigate the heat loss from the steam.
16 Various Experiments carried out by a number of researchers, as recorded by Clark [43] in the 1800s,
17 have showed that the alternate condensation and re-evaporation in steam jacketed cylinders are much
18 less than that in unprotected cylinder. The steam jacketed cylinders results to economy in the steam
19 consumption and displayed a greater degree of efficiency than the cylinder with superheated steam,
20 whilst both of them are clearly superior to an unprotected cylinder with saturated steam. The steam
21 jackets have reportedly resulted to economy of 14 - 25% in steam consumption rate per power output,
22 net specific work output increase of 42% (from 224 to 318 kJ/kg) and efficiency (in terms of the total
23 heat passed into the cylinder and the work output) increase of 28% (from 8.65 to 11.05%). Further
24 results showed that better performance was recorded for higher working pressure – this could be
25 explained by the fact that heat transfer is facilitated by higher pressure. It was also demonstrated that
26 by the utilisation of the steam jacket with high temperature, heat can be supplied (from the cylinder to
27 the working steam) in quantity sufficient to prevent (or mitigate) the initial condensation in the
28 cylinder and to re-evaporate the whole of such that may have been condensed.
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32 3.2.2.2. Surface heated boiler-less Rankine engine

34 The speed of heat transfer is a limiting factor in the steam jacket design, but for certain applications
35 speed is not considered critical. Igobo and Davies [44] proposed to use a slow-moving machine to
36 drive a high pressure reverse osmosis process for desalination that works on a cycle time of the order
37 of minutes. In this case, it was proposed to eliminate the traditional boiler (evaporator) of the steam
38 engine and rely on the jacket (which may be thermal oil fed) alone for heat transfer to vaporise the
39 working fluid and to maintain quasi-isothermal expansion. Fig. 7 shows a schematic layout for the
40 cycle, its corresponding temperature-entropy (T - s) is similar to that depicted in Fig 4b; on operation,
41 water injected into the heated cylinder vaporises on contact with the hot walls, and exerts pressure on
42 the piston to perform work while expanding. Given the relatively higher temperature of the cylinder
43 wall, further heat is transferred to the steam during the expansion process. At the end of expansion,
44 the superheated exhaust steam could be passed through a heat exchanger – prior to been condenser, to
45 preheat the condensed fluid pumped for the next cycle.
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49 Parametric analysis of the engine showed that, the heat transfer rate and thus speed of operation will
50 increase with increasing wall temperature and with decreasing cylinder size. Preliminary experiment
51 carried out on a 100 mm bore cylinder at 250°C wall temperature, showed that engine performance
52 increased with the volume of water injected (0.8 – 1.6 ml). A maximum pressure of about 18 bar and
53 336 KJ/kg of specific work output was achieved for 1.6 ml of injected water. The cycle efficiency also
54 increased with the injected water volume, as efficiency range of 14–16% was achieved, which is
55 about a half of the ideal cycle efficiency. The less-than-ideal performance was attributed mainly to
56 non-isothermal operation as a result of insufficient surface area (of the expansion space) for heat
57 transfer. This assertion is expected, as it has been noted in literature that: in reality, isothermal
58 operation cannot be carried out in reciprocating engine, due to limited heat transfer area [45].
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3.2.2.3. Surface heated Rankine cycle scroll engine

The scroll expander is a compact device with few moving parts compared to the reciprocating engine. Scroll expanders and compressors are widely used in refrigeration cycles and have become popular for use in small scale ORC heat engines [46]. Among these, engines using isothermal expansion are an interesting option.

Kim et.al. [47] proposed a scroll expander with external heating structure which included external fins attached on the scroll casing and a heating jacket (as depicted in Fig. 8); such that heat could be effectively transferred from an external source, through the scroll casing into the scroll interior. In the expansion process of the system, the transfer of heat from the scroll interior to the working fluid will reduce the temperature drop that would have otherwise resulted, thus effecting a quasi-isothermal expansion, and consequently contributing to improvement in specific work and thermal efficiency. For air as the working fluid, the isothermal process can result in a potential 34% increase in the expansion work. The system was suggested to be applicable to Ericsson cycle, refrigeration cycle and Rankine cycle.

For use in Rankine cycle, they also highlighted the possibility of the system acting as an expander and partially as a boiler, such that a very wet vapour could be employed as the working fluid at the point of entry into the expander, since the scroll machines are noted for tolerating substantial quantities of liquid fraction. In that case, given that sufficient heat is available from the scroll, the liquid fraction will vaporise during the expansion process, thus tending to reduce the rate of fall in pressure that would have otherwise resulted, and permitting higher volumetric expansion ratio and thereby enhancing the extraction of more work.

3.3. Summary

To summarise with regard to the Rankine cycle engine and its implementation with quasi-isothermal expansion, the expander surface heating can achieve significant improvement in performance even though the expansion chamber surface area available for heat transfer may not be sufficient to approach the level of isothermal behaviour reported with the liquid flooding system. On the other hand, the liquid flooding may experience deteriorating performance in reality, mainly because, unlike the expander surface heating, the liquid flooding incurs additional pumping energy input (for the liquid loop) and increased suction pressure drop, which (together with other associated losses) can eventually outweigh the expected performance improvements. From the perspective of technology availability, liquid flooding can be easily implemented, since its main components (scroll compressor, pump and heat exchanger) are readily commercially available. Nevertheless, it is a relatively new technology (that is yet to be fully developed), in comparison to steam jacketing, which can be regarded as a mature technology that has been proven effective and operational. However, for practical consideration for both technologies, proper insulation is recommended, to ensure that the heat loss (from the engine and piping) to the ambient is greatly minimised, so as not to result to a detrimental effect on the overall performance. In addition, further research work should be carried out on modelling of complex, unsteady multi-phase heat transfer with liquid flooding devices; and development of efficient separation mechanism for the flooding liquid separator.

4. Cryogenic heat engine

4.1. Theory and principle of operation

Cryogenic engines are another example where quasi-isothermal expansion is used. It is interesting to review the works in this area for possible application of similar features to heat powered engines working at higher temperatures.

Cryogenic heat engines utilize the thermodynamic potential between the ambient atmosphere and a cryogenic fluid, which is generally regarded as energy storage medium. The basic concept of the cryogenic heat engine is to utilize ambient heat from the atmosphere as heat source to heat a pressurised cryogenic fluid which can be used to drive a prime mover. This is in contrast with typical heat engines which utilize an energy source at temperature significantly above ambient and use the atmosphere as a heat sink [48]. As with conventional heat engines, the performance of the cryogenic engine is strongly dependent on the cryogenic working fluid employed. A study pointed out the benefits of using low-mass gases (like H₂, He, Ne, N₂, and air) in two-phase system, as having large maximum specific work values [49], with H₂ having the largest value. Other common cryogenics are hydrocarbons, including liquefied natural gas (LNG), of which methane (CH₄) is noted for having high specific work output potential [50]. Nevertheless, liquid nitrogen and liquid air are considered most attractive because they are essentially inexhaustible resource (that can be effectively produced from air) with considerable safety and environmental benefits.

Standard thermodynamic power cycles can be employed to produce useful work from the cryogenic fluid. For instance, cryogenic gas Stirling cycle could utilise seawater (ambient temperature) as the heat source to heat nitrogen gas in the expander, while liquefied natural gas (LNG) serves as the heat sink to cool the gas during compression [51]. Similarly, ambient evaporation of a cryogenic fluid and condensation by means of LNG as heat sink, can be employed for cryogenic Rankine cycle (Fig. 9a); and multiple cryogenic cycles can be cascaded to yield better cold energy recovery (Fig. 9b and c) [52]. For these closed cycles, propane (C₃H₈) and ethane (C₂H₆) are commonly considered as the working fluids; nevertheless, other low boiling point substances can be employed. The cryogenic power cycle can also be used as the bottom cycle in combined (or hybrid) cycles with other relatively higher temperature power cycles [53]. However, the simplest and most applicable power cycle is the open system (direct expansion) Rankine cycle [54], where the spent exhaust gas is released into the atmosphere. In this case the principle of operation is similar to that of a typical open cycle steam engine.

A schematic of a typical cryogenic heat engine is depicted in Fig. 10. The cryogenic liquid stored in a tank (which may be vacuum jacketed) is pumped to the required working pressure; the pressurised liquid is then vaporised and heated in an appropriate ambient heat exchanger system, and then fed to an expander, where it expands to do work. Since the rapid expansion process of the cryogenic fluid results in the temperature of the fluid always being less than ambient, the expander will be at a relatively higher temperature than the expanding fluid, thus during the expansion process, further heat may be transferred from the expander to the fluid, resulting to a possible quasi-isothermal expansion process [48]. The T-s diagram of the ideal cycle at critical pressure operation is shown in Fig. 10b. Process 1-2 indicates the pumping process, process 2-3 is the heating process in the heat exchanger, and process 3-0 is the isothermal expansion. Process 0-4-1 is the condensation stage (for closed loop system), or the liquefaction process which takes place remotely in an air processing plant [55] (for open system).

4.2. Studies and performance

Over the years, there have been investigations on the application of cryogenic heat engine for power generation, and also as an automotive propulsion for non-polluting zero emission vehicles; concept and technical feasibility have been evaluated [56], flow simulations in the engine have been carried out [57], and demonstration models have been built to test its practicality [58]. Key for practical realisation of the engine is the heat exchanger. Considering the low temperature of the cryogenic fluid, it will be essential for the liquid to be vaporized without the accumulation of frost, so as to avoid deteriorating performance. William et al., [59] developed a frost free heat exchanger for using atmospheric air to vaporize and superheat relatively large quantities of liquid nitrogen without the adverse building up of frost. Amrit et al. [60] also developed a cryogenic heat exchanger and presented analytical model for turbulent flows.

Research work carried out at the University of Washington highlighted substantial benefits in the overall energy efficiency for isothermal expander over an adiabatic one in liquid nitrogen cryogenic engines [61]. The study investigated the specific work output as a function of peak cycle pressure for adiabatic and isothermal expansions and showed that the isothermal work increases monotonically with increasing pressure, while that for the adiabatic process is found to be only weakly dependent on peak cycle pressure above 4 MPa. For pressure range of 10 to 300 bar at 300 K, the net specific work is 190 to 420 kJ/kg and 140 to 190 kJ/kg for isothermal and adiabatic conditions respectively.

Knowlen [62] studied the performance of two other cryogenes (namely CH_4 and C_2H_6) alongside N_2 for both isothermal and adiabatic expansion, and also showed that for all the working fluids, at a given injection pressure, the specific work obtainable from isothermal expansion exceeded that of the adiabatic expansion, with the difference greater as pressure is increased. The study also examined the use of N_2 as a heat sink for different closed loop CH_4 and C_2H_6 topping cycles, and found that for binary (N_2 - CH_4) and ternary (N_2 - CH_4 - C_2H_6) cascaded cycles, specific energies in the range of 200-380 kJ/kg and 300-450 kJ/kg can be realized respectively, depending on the extent of isothermal operation achievable. Yuanwei et al. [63] proposed a Temperature-Energy level-Energy (T- Ω -H) diagram method for analysing the performance of two different configurations of three-loop cascaded cycles with seawater and LNG respectively as the heat source and heat sink. They claimed that the proposed method facilitates quick optimisation process on a base case design. A number of authors have also explored different closed cycles that use seawater and LNG respectively as the heat source and heat sink. Choi et al. [64] compared the performance of different configurations of two and three loop cascaded cycles and combined (closed-open) cycles in comparison with the conventional single closed or open cycles. The study showed that the cascaded cycles exhibited better performance than the conventional single closed or open cycles; it also showed that, C_3H_8 - C_2H_6 cascaded cycle exhibited 51%, 49% and 89% more work output than C_2H_6 - C_3H_8 cascade, C_3H_8 and C_2H_6 cycles respectively; while the C_3H_8 cycle gave 27% more work than C_2H_6 . Liu and Guo [65] studied a variant of the cascaded cycle combined with vapour absorption process, the cycle employed a binary mixture of Tetrafluoromethane (CF_4) and C_3H_8 as the working fluid. The study showed that, the proposed cycle can achieve 206 kJ/kg specific work output, which is 63% higher than that of a C_3H_8 cycle (124 kJ/kg). In a study by Li et al. [54], an open cycle with two-stage expansion was shown to exhibit 326 kJ/kg work output. This compares reasonably with the performance reported for other two-loop cascaded cycles. Hence, although cascading closed cycles can significantly improve performance, it is also possible to achieve reasonable performance improvement with the relative simpler open system, with the aid of multiple expansion stages.

In a bid to avoid drop in expander wall temperature, which could result to deteriorating performance, Knowlen [48] suggested the use of “warmant” anti-freeze liquid (as a heat transfer fluid) to be pumped through the wall, so as to maintain it at near ambient temperature. Also, a parametric analysis on engine (reciprocating expander) geometry showed that long strokes, small bore and low RPM enhances heat transfer during the expansion process. Nevertheless, the transferable heat will be limited by the expander’s surface area exposed to the fluid, which will limit the degree of isothermal operation achieved. For standard engine (without modifications to cylinder piston geometry),

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4 isothermality is typically about 0.75 and can be improved further by enhancing heat transfer during
5 expansion. Further analysis showed that finned piston and cylinder head geometries (Fig. 11) having
6 high surface-to-volume ratios can be used to facilitate further heat transfer during the expansion,
7 resulting in potential net work output of 0.85 of the ideal isothermal work.
8

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10 Liquid air has similar properties to those of liquid nitrogen since air is composed of 78% nitrogen.
11 Chen et al. [17] studied the performance of a liquid air engine for a range of working conditions and
12 reported that, for a properly designed and manufactured engine with operating conditions of 100 bar
13 and 300 K, the practical (taking into account the losses associated with conventional engines) net
14 work outputs of the liquid air engine for isothermality of $\gamma = 0.90$ and 0.75 were respectively 200
15 kJ/kg and 150 kJ/kg, i.e. respectively about 122 and 66% higher than that for an adiabatic engine
16 (about 90 kJ/kg). Given that the energy consumption for liquid air production is about 1080 kJ/kg
17 [55], the efficiency of the cryogenic engine (in terms of energy in and energy out) for the above stated
18 isothermality will be about 18.5% and 13.9%, while that for the adiabatic condition will be 8.3%.
19 However, Ameer et al. [66] indicated that the efficiency of the isothermal cycle can be improved by
20 about 17%, if the liquefaction process is combined with the heat engine.
21

22 Dearman [67] developed a variant of the cryogenic engine, whereby the cryogenic liquid is directly
23 injected into a heat exchange liquid (water) in a reciprocating expander, thus the heat exchange takes
24 place inside the engine, consequently eliminating the need for the relatively complicated, heavier and
25 expensive heat exchanger as required previously. The principle of operation is such that, when the
26 piston is at the top of the cylinder, water is admitted into the cylinder dead space, and then a little
27 amount of the cryogen is injected into the water. Since the water temperature (ambient) is
28 substantially higher than that of the cryogen, the cryogen rapidly vaporises, builds up pressure,
29 becomes superheated and pushes the piston as it expands to do work. At the return stroke, the spent
30 gaseous cryogen and the water are exhaust out. The water can be recovered, reheated and pumped
31 back to the cylinder for another cycle [68].
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33 Wen et al [69] studied the heat transfer behaviour between liquid nitrogen and water (as the heat
34 transfer fluid) in Dearman's engine, and reported a much stronger heat transfer than that obtained
35 from boiling on smooth surfaces and flow boiling through pipes, but comparable to that of rough
36 surfaces and pipes with porous inserts. The pressure was seen to develop very rapidly (up to 500
37 kPa/s) and increased approximately linearly with the injection pressure; thus indicating that high
38 pressure could be effectively developed to run the engine. Morse and Kytömaa [70] also carried out
39 experimental study of the vaporisation of liquid nitrogen and LNG in water, and found that, the
40 evaporation rate is significantly dependent on both the turbulence intensity of the water surface, and
41 the thickness of the cryogenic liquid layer. However, vaporising LNG in water may require safety
42 precautions against possible ignition of the vapour, as has been reported with incidents of LNG spills
43 on sea [71].
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47 4.3. Summary

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49 In summary, the cryogenic engine provides an inherent means of effecting quasi-isothermal expansion
50 with ambient temperature. The potential isothermal performance increases with increasing pressure
51 and could be as much as twice that of the adiabatic case. Cascading multiple cycles would give better
52 energy recovery than single closed or open cycles; however, the open cycle is the most applicable. For
53 an operating pressure of 10 bar, the potential performance of the liquid nitrogen open cycle cryogenic
54 engine can have an ideal efficiency of 19% and specific work of 200 kJ/kg; but this performance is
55 quite low in comparison to the 27% ideal efficiency predicted for a surface heated engine operating
56 on steam with similar pressure [44], and the reported 318 kJ/kg specific work achieved for a real surface
57 heated (steam jacketed) engine operated at 5 bar [43]. Furthermore, unlike the surface heated engine,
58 although the cryogenic engine has the advantage of not losing heat to the ambient (since it can be at
59 the same or even lower temperature potential with the ambient), it could suffer evaporative losses and
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4 safety (explosion) risks at the storage tank; as it slowly absorbs heat from the ambient, which could
5 result to excessive pressure rise [72].
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8 9 10 **5. Vapour Stirling cycle engine**

11 5.1 Theory and principle of operation

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14 The ideal Stirling cycle is a classical implementation of isothermal expansion. Though ideally
15 efficient, it suffers from low specific power output at moderate temperatures and pressures [73]. As a
16 means of increasing the specific power output, the use of condensable working fluid has been
17 investigated in prior arts – the vaporisation of liquid at the hot side of the Stirling engine followed by
18 condensation at the cold side has been identified as a viable solution [74], the use of refrigerants as
19 working fluid has also been considered [75]. Prior arts (including a number of patents) have
20 investigated various means of employing vapour as the working fluid in the Stirling cycle engine
21 (including liquid-piston variants).
22

23
24 The concept of liquid-piston Stirling (fluidyne) engine is to replace the conventional solid-pistons of
25 Stirling engine with columns of liquid (typically water) in U-tubed cylinder. Unless the liquid in the
26 expansion cylinder has a low vapour pressure at the operating temperature or is separated from the hot
27 gas by some kind of insulating float (generally referred to as dry fluidyne), ample evaporation will
28 take place from the liquid surface and wetted cylinder walls to effect a mixture of gas and vapour
29 working fluid [76]. As such the fluidyne engine can provide both gas and vapour power cycle. One
30 critical design parameter in the fluidyne engine is the frictional losses in the oscillating liquid columns
31 [77]. Studies have shown large dry fluidynes to be quite successful, but on the other hand, small dry
32 fluidynes (which generally suffer from the large transient heat-transfer and flow losses associated with
33 small-diameter tubes) have been reported to be impractical in the absence of evaporation [76]. The
34 evaporation tends to raise the pressure during the expansion phase and thus increases the indicated
35 power in the fluidyne engine. Owing to the fact that the power output is available in the form of
36 pulsating pressure/movement of liquid in a tube, the most obvious application was as a pumping
37 engine [78]. However, a rotating shaft power output option have also been identified, via the use of
38 hydraulic motor [79] or solid pistons [80]; with the former, as shown if Fig. 12, the solid piston
39 converts the pressure in the liquid piston into a force which can then be applied to a shaft, like
40 conventional engines.
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43 Since liquids can conform to irregular shapes, unlike solid-piston, liquid pistons have the advantage of
44 possibly allowing the adoption of working chambers with very large surface area to volume ratios
45 such as wire matrix, tube bundle, metal foam, etc. (Fig. 12), to substantially improve heat transfer to
46 the working fluid and consequently bring the working fluid behaviour into the nearly isothermal
47 regime (which will result to improved power output and efficiency). However, the high area to
48 volume ratio will result to smaller size of flow passages, increased flow restrictions and thus,
49 increased viscous losses. As such the heat transfer area and the viscous frictional losses must be
50 adjusted to maximize the efficiency of the liquid piston engine [81]. Besides the increased viscous
51 losses, the liquid piston also suffers operating stroke and frequency limitations imposed by gravity-
52 controlled oscillation and by surface instability at high frequency; and the need to keep a more or less
53 constant orientation of the engine [80].
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56 Various concepts involving the conventional solid-piston Stirling engines variants with modifications
57 on operational configurations have also been recorded. Redderson [82] patented a vapour Stirling
58 machine based on the alpha Stirling configuration. It featured heating and cooling chambers on the
59 hot and cold cylinder tops respectively, and with a regenerator interconnecting the two chambers (Fig.
60 13). But in contrast, the working fluid in the cooling chamber is substantially in the liquid phase as
61 such resulting to a significantly larger swept volume ratio than a conventional Stirling engine. On
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4 operation, the upward motion of the cold cylinder piston pumps the fluid through the regenerator into
5 the hot chamber where it gets completely vaporised and superheated and then expands to perform
6 work against the hot piston while gaining further heat from the hot chamber, thus tending to approach
7 isothermal expansion. At the end of expansion, the upward motion of the hot piston pushes the spent
8 vapour through the regenerator and into the condenser where it condenses back to water. As a means
9 of providing output control, a control cylinder is included at the cold section to vary the effective
10 mass of the working fluid within the engine.
11

12 Davoud and Burke [83] patented a condensing vapour Stirling engine, in which at the end of
13 expansion, a portion of the spent vapour is expelled (via a receiver cylinder) and condensed, while the
14 remaining portion is compressed in the power cylinder, during which the weight equivalent of the
15 condensed portion is pump and injected back into the cylinder as a fine spray of water. This was said
16 to lower the entropy and enthalpy of the steam in the cylinder, and thus lower the compression work
17 that would have been required. The compressed steam gets superheated in the heater tubes
18 arrangement at the top dead centre of the cylinder, and then expands against the piston to do work.
19 They later went further to patent a simpler version (with only one cylinder), in which bulk of the spent
20 steam is expelled directly to the condenser. The condensed water is then pumped and injected into the
21 cylinder top dead volume containing the heater tubes where it gets vaporised and superheated [84].
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25 5.2. Studies and performance

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27 West [74] developed a two-phase, two component working fluid system for an alpha Stirling engine
28 configuration (Fig. 14), in which, the working fluid consists of both a condensable vapour (steam) and
29 permanent gas (air), such that the air is contained in the cold section, and prevented from passing into
30 the hot section by means of controlled evaporation (i.e. steam pressure) in the hot section. Water
31 injected into the evaporator vaporises into the hot cylinder where it expands to do work. The
32 expended vapour then passes into the cold end where it condenses and is subsequently removed.
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34 The analysis showed that under moderate operating conditions the engine can achieve a cyclic power
35 output at least five times greater than a conventional Stirling-cycle machine of similar dimensions, but
36 at the expense of significantly lower ideal cycle efficiency. Nevertheless, by controlling the rate at
37 which the liquid is evaporated into the expansion cylinder an indicated efficiency in the range of 3 to
38 9% at low temperatures (110°C to 130°C) may be achievable even without regeneration.
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41 Isshiki et.al. [85], developed a steam Stirling engine which operates as a hybrid of Stirling and
42 Rankine systems, such that the engine featured a power cylinder (with heating tube at the cylinder
43 top), displacer cylinder and a regenerator in between, as with Stirling; but also has injection/exhaust
44 port, thus spent steam could be ejected, condensed, pump and re-vaporised externally just like
45 Rankine. On operation, when the power piston comes near its top dead centre, saturated steam from
46 the external boiler injected into the displacer cylinder, passes through the regenerator and heater, and
47 then expands into power cylinder at near constant high temperature. On the return stroke, the spent
48 steam passes through the regenerator and is exhausted to a condenser where it gets condensed and
49 then pumped back to the boiler. Experiment carried out on a mini scale prototype operated at 0.2 Mpa
50 (gauge) and 250°C showed that output power of about 12 watt was achieved at 400 rpm. This is
51 significantly higher (approximately five times) than the reported 2.6 watt achieved for a conventional
52 gas Stirling engine operated at 320°C [86].
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54 5.3. Summary

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56 In summary, the use of vapour as the working fluid in Stirling engines can result in power outputs
57 about five times larger compared to conventional non-condensable gas working fluid. To facilitate
58 more heat transfer to the fluid to approach a more isothermal behaviour, liquid pistons could be
59 employed to allow the expansion space to be enhanced with high surface area geometries like wire
60 matrix. However, it introduces practical issues that will need to be further investigated. As such it is
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4 recommended that further research be carried out on: modelling the behaviour of the oscillating liquid
5 in liquid piston devices with particular attention to viscous forces and inertia effect of the liquid
6 oscillation. Since the various technologies presented are still in the concept or early development
7 stage, further experimental studies should be carried to give a better insight on their practical
8 realisations; and optimization of the various full engine dynamics to maximize efficiency and power
9 density for specific applications.

10 11 12 **6. Conclusion**

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15 To convert low-grade thermal energy into useful work, external combustion engines using vapour
16 cycles (though relatively less efficient) have been preferred over those using gas powered cycles due
17 to the former's higher specific work output and smaller engine size. Relative to the traditional ideal
18 adiabatic expansion process in the vapour power cycle engines, quasi-isothermal expansion has been
19 found to improve the specific work output and cycle efficiency of the engines.

20
21 Two main methods of effecting the quasi-isothermal expansion have been identified – liquid flooding
22 and expander surface heating. The expander surface heating has been studied for both reciprocating
23 and rotary expanders; however there are more references in the literature for its use with reciprocating
24 expanders. Liquid flooding is referenced more for use with rotary expanders.

25
26 In practical performance of the quasi-isothermal expansion, studies have showed that liquid flooded
27 expansion approaches isothermal behaviour with increasing oil fraction; but at the expense of
28 deteriorating overall performance, that was partly attributed to the resulting increased suction pressure
29 drop and viscous losses. On the other hand, the expander surface heating has been shown to achieve
30 significant improvement in performance (over 40% and 20% increase in specific work output and
31 efficiency respectively). Here, a relatively slower operating speed is required to enable significant
32 heat transfer during the expansion process as the cylinder wall surface area available for heat transfer
33 limits the isothermal operation. However expander geometries with high surface-to-volume ratios
34 (such as fins) could be employed to facilitate heat transfer and further improve performance, as has
35 been demonstrated with cryogenic engine. Furthermore, much higher surface area to volume ratios
36 (such as wire matrix) could be easily realized with the adoption of liquid pistons.

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39 With regards technology availability, it can be seen that the expander surface heating has been ready
40 for many decades in the form of steam jacketing, whereas liquid flooding is a relatively new
41 technology that is yet to be fully developed. Nevertheless, it can be easily implemented with
42 commercially available parts.

43
44 This paper concludes that, while quasi-isothermal vapour power cycle engines have the potential to
45 significantly improve the performance in a number of applications (e.g. desalination, transport and
46 heat recovery), there are research areas to be further examined. As such, it is recommended that
47 further research be carried out on: modelling of complex, unsteady multi-phase heat transfer with
48 liquid flooding devices to predict performance and tailor to applications; modelling the behaviour of
49 the oscillating liquid in liquid piston devices with particular attention to inertia and viscous losses; and
50 the investigation (selection) of other appropriate liquids and working fluids for a range of low
51 temperature operations. Further experimental studies are also recommended to give better insights on
52 the practical realisations and optimisations of the technologies presented as concepts or early
53 developmental stages.

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Review of low-temperature vapour power cycle engines with quasi-isothermal expansion

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Abstract

External combustion heat cycle engines convert thermal energy into useful work. Thermal energy resources include solar, geothermal, bioenergy, and waste heat. To harness these and maximize work output, there has been a renaissance of interest in the investigation of vapour power cycles for quasi-isothermal (near constant temperature) instead of adiabatic expansion. Quasi-isothermal expansion has the advantage of bringing the cycle efficiency closer to the ideal Carnot efficiency, but it requires heat to be transferred to the working fluid as it expands. This paper reviews various low-temperature vapour power cycle heat engines with quasi-isothermal expansion, including the methods employed to realize the heat transfer. The heat engines take the form of the Rankine cycle with continuous heat addition during the expansion process, or the Stirling cycle with a condensable vapour as working fluid. Compared to more standard Stirling engines using gas, the specific work output is higher. Cryogenic heat engines based on the ~~open~~ Rankine cycle have also been enhanced with quasi-isothermal expansion. Liquid flooded expansion and expander surface heating are the two main heat transfer methods employed. Liquid flooded expansion has been applied mainly in rotary expanders, including scroll turbines; whereas surface heating has been applied mainly in reciprocating expanders.

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Keywords:

Vapour power cycle
Quasi-isothermal expansion
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Waste heat utilisation

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1. Introduction

Owing to the global energy challenges associated with fossil fuel – rising cost, energy security and climate change – there has been growing interest into sustainable alternatives or renewable energy sources such as: wind, solar, geothermal, biomass and waste heat. Presently, renewable energy sources account for less than 15% of the global energy supply [1], of which biomass is a major contributor, while, However, solar has recorded the fastest growth. The IEA has projected the, and renewables have been projected to become the world's second largest source of power generation by 2015 [1, 2][2]. Studies have already shown that the renewable heat sources have the potential of meeting the global energy demand several times over [3, 4][3]. As a means of encouraging the exploitation of the renewable heat sources, 'heat policies' (including incentives) have been introduced in some countries [5, 6][4]. Globally, solar, biomass and waste heat are readily available in distributed form as low-grade (<250°C) heat, and are well suited for decentralized small-scale (<100 kW) applications. Thus there has been a renaissance of interest in small-scale external combustion heat engines (gas and vapour power cycles) to convert the thermal energy into useful work, with particular emphasis on improving performance. Isothermal expansion is one technique for achieving such improvement.

Ideally, certain gas power cycles (such as Stirling and Ericsson cycles) perform work by the isothermal (constant temperature) expansion of a compressed and heated gas working fluid (which remains gaseous throughout the entire cycle). They are noted for having the high theoretical efficiencies of the Carnot cycle – which is the maximum obtainable efficiency for given temperature limits [7]. On the other hand, for vapour power cycles, [5]. On the other hand, for vapour power cycles (typically the Rankine cycle), the working fluid is a condensable vapour, and is intermittently vaporised and condensed; the expansion process is adiabatic (i.e. the fluid expands without experiencing heat transfer during the process) and produces less work than its isothermal counterpart [8][6]. Nevertheless, in comparison to the gas compression work of the gas power cycles, less input work is required to pressurize the condensed liquid of the vapour power cycles, and the total cycle pressure-volume characteristics exhibit greater work output than the gas cycles. Thus the vapour cycle engines have higher specific work output [9][7]. The vapour power cycles can also have advantages over gas cycle equivalents because the phase change allows smaller surface areas and temperature differences to drive the heat supply/removal/boiling/condensation required by the cycle. This inference arises from the higher heat transfer coefficients associated with phase change (by orders of magnitude) relative to that of forced convection between a gas and solid surface for gas [8]. The smaller surface areas lead to compact heat exchangers and engine size [10][9]; this together with the higher work output gives the vapour cycle engines higher power density; and the low temperature differences aid better performance (relative to the gas cycles) in low-grade heat applications. This has been demonstrated in a study that showed the Rankine cycle to be more efficient than Stirling cycle for temperature range of 150 – 300°C [10].

In power plants operating on vapour cycles (typically the Rankine cycle), reheating is a practical approach to improve the cycle efficiency and specific work output. As the number of stages of reheating increases, the expansion and reheat processes approximate an average isothermal process and the cycle efficiency increases [11]. But in the reheating process, the steam must be returned back to the boiler for each reheat, which, besides requiring many additional components, inevitably adds complexity to the plant layout and geometry, and results to heat and pressure losses [11, 12][12]. Alternatively, the vapour cycle engine could be designed in such a way that (like the Stirling or Ericsson engines) heat is continuously transferred to the working fluid during the expansion process thus resulting in isothermal expansion, or more realistically, quasi-isothermal expansion – which may be somewhere between the adiabatic and ideal isothermal processes.

In this paper, relevant research works with emphasis on low temperature vapour power cycles with quasi-isothermal expansion will be presented. Various methods employed to effect quasi-isothermal

operation, including concepts, studies and results, will be reviewed to provide an insight into their practicality, system performance and energy efficiency. The first part (section 2) of the paper presents the general theoretical advantage of quasi-isothermal expansion, including the various heat transfer methods used to achieve it. The second part (section 3-5) of the work covers the power cycles to which the methods are applied. For each power cycle, the theory and principle of operation is explained, and then specific studies are reviewed in which these cycles have been implemented. Fig. 1 classifies the methods and vapour power cycles for quasi-isothermal operation according to the approach used in this review.

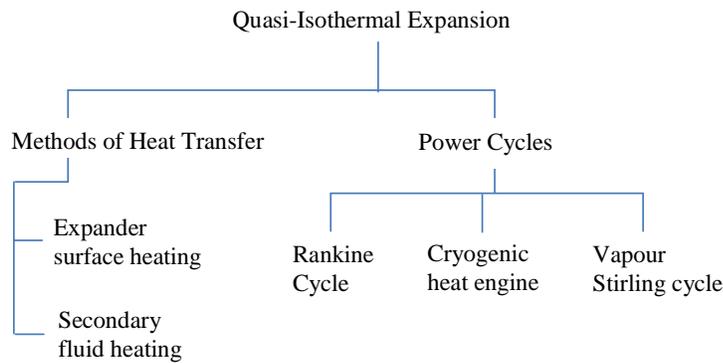


Fig. 1. Overview of the review approach

2. Quasi-Isothermal expansion

The paths of both the isothermal and adiabatic expansion processes can be illustrated graphically on a pressure-volume (P-v) plane as shown in Fig. 2, using the gas equation $P_1 v_1^n = P_2 v_2^n$. The expansion index n is equal to 1 and k for isothermal and adiabatic processes respectively [13, 14][13], where k is the ratio of the specific heats (C_p/C_v) of the gas, and is always >1 [14]. For example, under a substantial range of operating conditions, k is about 1.4 for nitrogen gas and steam [15].

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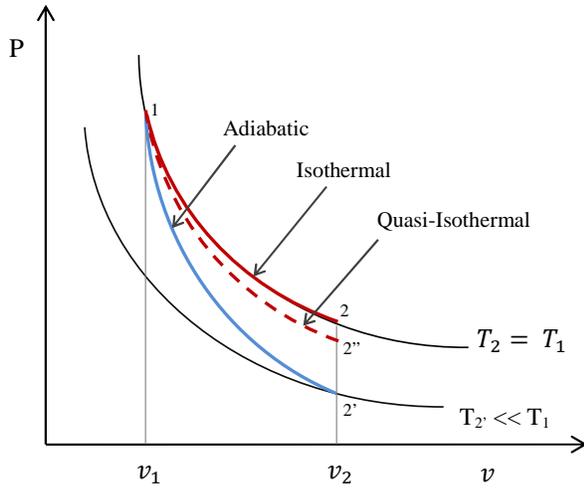


Fig. 2. Graphical representation of isothermal and adiabatic expansion processes

The work output is simply the integral ($\int PdV$) between the two end states (1 and 2), as is represented by the area under the path curves. Hence, from the figure it can be seen that the area under the curve (i.e. the expansion work output) for the adiabatic expansion is less than that of an isothermal expansion having the same initial operating conditions. This can also be seen numerically from the integration of both curves from state 1 (start of expansion) to state 2 (end of expansion).

~~The work done by isothermal expansion can be given as [16]:~~
~~The work done by isothermal expansion can be given as [16]:~~

$$W_{iso} = \int PdV = P_1 v_1 \ln \left(\frac{P_1}{P_2} \right) \quad (1)$$

Similarly, the work done by adiabatic expansion can be expressed as:

$$W_{ad} = \int PdV = P_1 v_1 \frac{1 - \left(\frac{P_1}{P_2} \right)^{\frac{1-n}{n}}}{n-1} \quad (2)$$

Hence, from the above equations, the relative improvement of the isothermal expansion work over the adiabatic work can be expressed in terms of the expansion index and pressure ratio $r_p = P_1/P_2$ as:

$$Relative\ improvement = \frac{W_{iso}}{W_{ad}} - 1 = \left[\frac{(n-1) \ln(r_p)}{\left(1 - r_p \right)^{\frac{1-n}{n}}} \right] - 1 \quad (3)$$

For example, with $r_p = 7$ and $n = 1.4$, eq. 3 shows that the isothermal expansion gives 83% more work than the adiabatic.

The expansion process of conventional vapour power cycles is generally assumed adiabatic, and as such is subject to this reduced work output [8, 17]-[6]. The adiabatic expansion process is also

characterised by drop in temperature from T_1 to T_2' . Hence, modifying an adiabatic expansion to an isothermal one would ideally require the addition of heat to the expanding fluid to maintain its temperature constant.

In reality, when the heat absorbed by the vapour is not sufficient to maintain isothermal expansion, the result is termed quasi-isothermal expansion. In this case, the heat absorbed shifts the expansion process from adiabatic behaviour towards the ideal isothermal behaviour. Consequently, the work output will be more than the adiabatic work, but less than the isothermal work available, in proportion to the extent to which the expansion approaches the isothermal case. This extent has been termed isothermality, γ , defined as the ratio of actual work output to the ideal isothermal work [18],[17].

$$\gamma = \frac{W_{ac}}{W_{iso}} \quad (4)$$

Thus it determines the work output as a fraction of the isothermal work available. On the other hand, for rotary expanders some authors have described the extent of isothermal behaviour as the ratio of discharge temperature to supply temperature [19,20],[18].

2.1. Methods of effecting quasi-isothermal expansion

Over the years, a number of methods have been developed, by which a vapour power cycle's working fluid can continuously gain heat during the expansion process to effect quasi-isothermal expansion; often times this result in variants of the traditional power cycles. The identified methods can be generally grouped on the basis of the means of heat transfer as: secondary fluid heating and expander surface heating. The methods and the power cycles (including the variants) to which it is applied are shown in ~~table~~Table 1.

Table 1. Heating methods and the applicable power cycles for quasi-isothermal operation, with relevant examples from the literature

Methods Applications	Secondary fluid heating	Expander surface heating
Rankine cycle engine (section 3)	Theoretical study of liquid flooded scroll turbine, using various fluids [21],[19]	Theoretical study of surface heated scroll turbine [12]
	Experimental study of the effect of flooding liquid quantity in scroll turbine [22]	Experimental study of surface heated reciprocating cylinder [23] Theoretical study of surface heated scroll turbine [21]
		Experimental study of surface heated reciprocating cylinder [22]

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Cryogenic engine (section 4)	<u>Experimental study of evaporating cryogenic liquid in water [24, 25]</u> <u>Experimental studies of evaporating cryogenic liquid in water [23, 24]</u>	<u>Theoretical study of surface heated reciprocating cylinder [24, 26]</u> <u>Theoretical studies of surface heated reciprocating cylinder [23, 25]</u>
Stirling cycle engine (section 5)		<u>Theoretical study of controlled evaporation in Stirling engine [27, 28]</u> <u>Experimental study of vapour Stirling engine [28]</u> <u>Theoretical studies of controlled evaporation in Stirling engine [26, 27]</u> <u>Experimental study of vapour Stirling engine [27]</u>

2.1.1. Expander surface heating

A simple approach to achieve heat transfer to the working fluid during the expansion process is to provide a means of heating the expander sufficiently above the fluid temperature; such that during the expansion process, heat could be effectively transferred from the surface of the expansion chamber to the fluid, as illustrated in ~~fig~~Fig. 3a. This is quite popular for reciprocating expanders as found in conventional Stirling engines, and steam-jacketed steam engines. The extent of isothermal operation achievable here will depend on the rate of heat transfer, which is a function of the overall heat transfer coefficient and temperature differential between the engine wall and the fluid, and the surface area of the wall exposed to the fluid [46],[28]. As such, geometries giving high surface to volume ratios such as tubes and fins are generally utilised to increase the total heat transfer area as found in conventional Stirling engines [29].

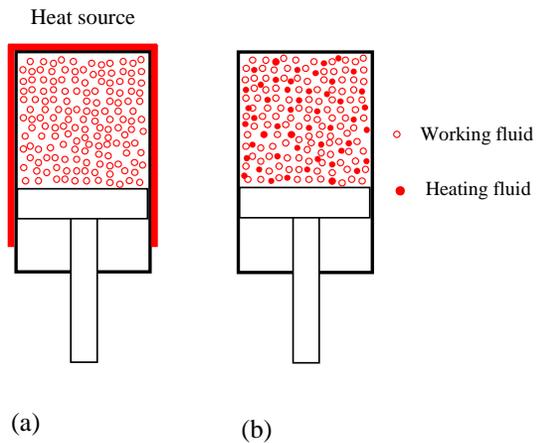


Fig. 3. The two main means of heat transfer used to achieve isothermal expansion: (a) expander surface heating; (b) secondary fluid heating system

2.1.2. Secondary fluid heating

The heat transfer required to effect quasi-isothermal expansion could be provided by means of a secondary fluid which co-exists with the working fluid in the expander during the expansion process (Fig. 3b). In this case, the secondary fluid – which will ideally be of a high thermal content – is dispersed into the working fluid such that during the expansion process, the temperature dropped by the expanding working fluid is quickly recovered from the secondary fluid. The heating fluid could ideally be a vapour – as with direct steam injection; or more practically, a liquid – as with liquid flooded expansion.

2.1.2.1. Direct steam injection

The concept of achieving isothermal expansion by direct steam injection entails injecting small amount of relatively very high temperature steam (secondary fluid) into the expanding steam [30]. The secondary steam transfers heat to the working steam by virtue of its higher temperature thermal content, as such requires the secondary steam to be continuously injected with appropriate amount and temperature in such a way as to keep the expansion temperature constant.

2.1.2.2. Liquid flooding

The liquid flooding process involves literally flooding a screw or scroll machine with a large quantity of liquid simultaneously as the working fluid passes through the device, such that the liquid provides a medium of heat exchange with the working fluid whilst in transit through the device. Unlike with steam injection, the secondary fluid is normally different from the working fluid, and is immiscible with it. This concept can ideally be applied to compression and expansion processes (its application to expansion processes will be covered in section 3.2.1). Over the last two decades, there have been a significant number of studies on the application of liquid flooding to compressors. Researchers have studied oil-flooding in screw compressors [31] and scroll compressors [32] primarily to improve sealing and lubrication, but without much emphasis on heat transfer [33]. ~~In recent years,~~

~~conventional screw and scroll compressors have been effectively used in reverse as expanders (with minor modifications)~~In recent years, conventional screw [34] and scroll [34, 35], [35] compressors have been effectively used in reverse as expanders (with minor modifications), thus widening the scope for liquid-flooded expansion. The combinations of the different working fluids and flooding liquid considered in the literature are shown in ~~table~~Table 2.

Table 2. Combinations of different working fluids and flooding liquid

Working fluid	Flooding liquid	Expansion device	Ref.	Study type
Ammonia (R717) Carbon dioxide (R744) R410A R600a n-pentane R245fa	Water Zerol 60	Scroll	[21] [19]	T
R245fa	Compressor oil	Scroll	[22] [20]	Ex
Liquid air	Water	Reciprocating cylinder	[24, 25] [23, 24]	Ex

T. Theoretical

Ex. Experimental

The concept of flooded expansion (and compression) was studied by Hugenholtz [36] in a liquid flooded Ericson cycle cooler, which used liquid flooding of both the compressor and the expander (to achieve nearly isothermal compression and expansion) to overcome the practical difficulties of achieving isothermal conditions in the basic reverse Ericson cycle. In a later experimental work [37], off-the-shelf automotive scrolls were used as the compressor and expander, nitrogen as the working fluid and alkyl-benzene as the flooding liquid. The performance of the off-the-shelf scroll machine was not sufficient to achieve high cycle efficiency. For increasing operating pressure ratios, the expander adiabatic efficiency was seen first to increase and then to decrease. This effect was partly attributed to the limitation of the expander not being designed for liquid flooded operation

~~To optimize the design of the compressor and the expander, Bell et al. [38] developed comprehensive models of both machines. Validation of the models and analysis of the machines were carried out. The model developed was an extension of earlier models that were developed by Halm [39] and Chen [40, 41] for scroll compressors without liquid flooding. The important contribution of the work was said to be the treatment of a mixture of gas and large fraction of oil. Also, Lemort et al. [19] further studied the performance of liquid flooded expansion using scroll expander and developed a detailed model of the flooded scroll expander, to facilitate predictions of the performance over a wide range of operating conditions and design changes.~~[38] developed comprehensive models of both machines. Validation of the models and optimization of the design were also carried out [39]. The model developed was an extension of earlier models that were developed by Halm [40], and Chen et al [41] for scroll compressors without liquid flooding. The important contribution of the work was said to be the treatment of a mixture of gas and large fraction of oil. Also, Lemort et al. [42] further studied the performance of liquid flooded expansion using scroll expander and developed a detailed model of the flooded scroll expander, to facilitate predictions of the performance over a wide range of operating conditions and design changes. The model was able to predict the shaft power to about 6.7% maximum deviation from measured experimental value.

2.2. Summary

In summary, quasi-isothermal expansion has been identified as a realistic alternative to adiabatic expansion to improve the work output of vapour power cycle engines. This can be achieved by further heat addition to the working fluid during the expansion process. The heat can be transferred by means of heating the expander external surface, or by means of a secondary heating (flooding) fluid. The expander surface heating is found to be more popular with reciprocating engines, whereas the secondary fluid heating is more popular with rotary engines.

3. Quasi-isothermal Rankine cycle engines

3.1. Theory and principle of operation

The quasi-isothermal Rankine cycle is simply a Rankine cycle whose working fluid gains significant amount of heat during the expansion process of the cycle, such that it is somewhere between adiabatic and isothermal, but its reference limit is ideally isothermal, as depicted on the temperature entropy (T-s) diagrams in Fig. 4. Fig 4a shows a case where the expansion starts from a super-heated state [42]; while in Fig 4b, the expansion starts from a saturated state [43],[44]. As a result of the heat addition during the expansion process, the spent vapour becomes significantly superheated at the end of expansion, thus necessitating regeneration (utilising the heat available at the end of expansion to preheat the feed working fluid) to improve the thermal efficiency. Studies have shown that the efficiency of the ideal cycle (with isothermal expansion and regeneration) can be up to 93% of the efficiency of a Carnot cycle operating with the same temperatures limits [23, 30],[30]. Where isothermal expansion is not fully achieved, the resulting quasi-isothermal cycle's performance will depend on the quantity of heat successfully absorbed during expansion, which of course is dependent on the heat transfer technique employed.

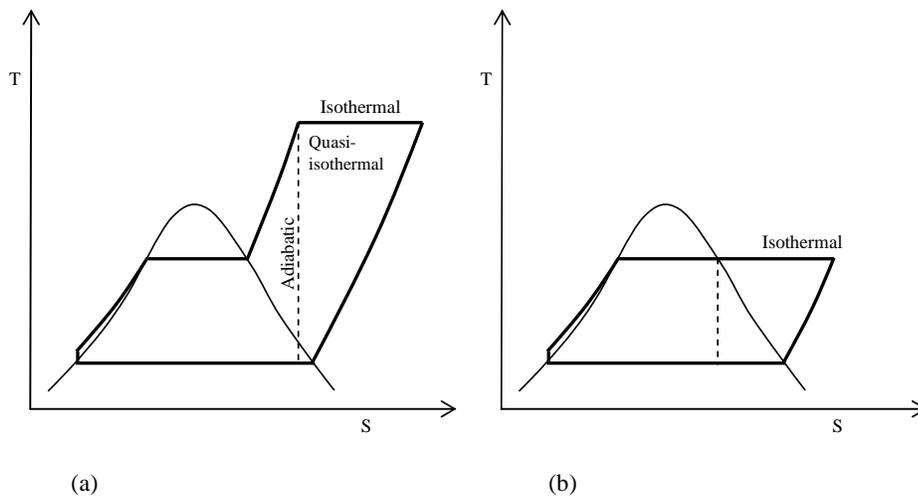


Fig. 4. T-s diagrams of Rankine cycle with isothermal expansion [42, 43], (a) starting from superheated state; (b) starting from saturated state. T-s diagrams of Rankine cycle with isothermal expansion, (a) starting from superheated state [30]; (b) starting from saturated state [44].

3.2. Studies and performance

Using the thermodynamic cycles of Fig 4, researchers have proposed and studied different versions of the quasi-isothermal Rankine cycle using different modes of heat transfer. Thus, both liquid flooded and external heated surface machines have been reported. These implementations will now be reviewed.

3.2.1. Liquid-flooded Rankine cycle

The idea of liquid flooded expansion can be applied to Rankine cycle, as patented by Woodland [44]. A schematic of the system is depicted in fig-[45]. A schematic of the system is depicted in Fig. 5. The working fluid and the flooding liquid are both pressurised and heated to the required high side pressure and temperature (via separate pumps and heat exchangers). The fluids are then mixed and fed to the expander where they flow together to do work. During the expansion process, temperature drop of the working fluid (vapour) is inhibited by heat gain from the liquid (because the liquid has a relatively higher heat capacity), thus resulting in a near isothermal expansion. At the end of expansion, the superheated working fluid is then separated from the liquid and passed through a regenerator (before being condensed) to preheat the condensed fluid pumped for the next cycle, as the flooding liquid is simultaneously re-pressurized and heated back to the high side conditions.

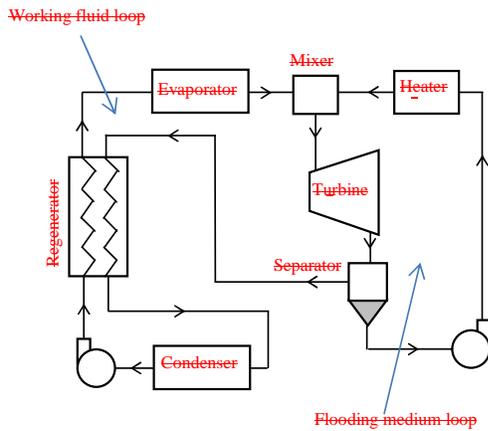


Fig. 5. Schematic of the liquid flooded ORC [21]

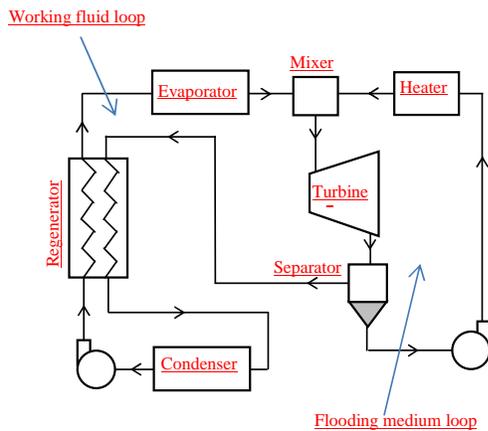


Fig. 5. Schematic of the liquid flooded ORC [19]

Woodland [24][19] also carried out theoretical study of the application of liquid flooding to organic Rankine cycle (ORC) with regeneration, for different working fluids (ammonia, carbon dioxide, R410a and dry fluids such as iso-butane, n-pentane and R245fa). The analysis showed that, working fluids ammonia and R410a exhibited higher performance improvement due to the flooded expansion. For ammonia, the addition of the liquid flooding offered about 20% more improvement in thermal efficiency. A later study [45]A later study [46] that featured water as a working fluid in the liquid flooded ORC, showed a relative improvement of 10% due to the flooded expansion; the improvement increased with the source temperature. In contrast, the improvement for the dry fluids was significantly less (only about 5%), and approaches zero at higher (>250°C) operating temperatures. Higher work output was expected from the more isothermal flooded expansion than from ordinary expansion process. However, for these dry fluids, the improvement in work output is not high enough to significantly outweigh the additional energy inputs (pump work and heat input) required for the flooding process.

Lemort et al. [22][20] developed a prototype of a flooded Rankine cycle engine with a hermetic scroll expander and R245fa working fluid. The study was focused on investigating the impact of oil quantity on the expander performance. For operating pressure ratio of 4.2 bar, supply temperature of 92°C and oil mass fraction of 0.023 – 0.1, the results showed that the expander overall isentropic effectiveness (ratio of the measured power output to the ideal expander power) decreased with increasing oil quantity. Further investigation was recommended to ascertain with certainty the underlying reason; nevertheless, increase of supply pressure drops (at the expander inlet) and viscous losses were mentioned as likely reasons for the decrease in performance. This is in agreement with the results of a previous study [19] on the performance of liquid flooded expansion using scroll expander. This is in agreement with the results of a previous study on the performance of liquid flooded expansion using scroll expander [42]. For a given pressure level, in the experiment, the measured power output reportedly decreased with the oil flow rate as a result of increasing pressure drops due of the oil suction process at the expander inlet. The study also analysed the variation of exhaust temperature with oil fraction for different operating speeds. As would be expected, the result further showed that the expansion tends to approach isothermal behaviour for higher oil fractions. The range of isothermal expansion (in this case defined as the ratio of discharge temperature to supply temperature) achieved was about 0.93 to 0.99 for oil fractions of 0.2 to 0.8 respectively. This shows that, although the liquid flooding facilitated sufficient heat transfer, such that isothermal behaviour is approached, there are practical challenges in translating it to net performance improvement. Another practical issue worth noting is that the separation of the refrigerant from the oil in the oil separator is not generally perfect, as such some amount of refrigerant usually remain entrained in the oil [37]. This entrainment may pose a durability issue in the long run, as higher oil flow rate will result to larger amount of refrigerant entrained, thus it can result in the need for frequent servicing, as has been observed with oil flooded compressor [46][47].

For the purpose of increasing the efficiency of a trans-critical CO₂ Rankine cycle thermo-electric energy storage (TEES) system, Kim et al. [48] proposed the application of a variant of the liquid flooded concept to achieve isothermal expansion (and compression) for the discharging (and charging) process of the TEES system. The discharging process is basically the retrieval of mechanical-electrical energy from the stored thermal energy by means of a heat engine (Rankine cycle, in this case). Fig. 6 depicts the discharging process of the proposed isothermal TEES system.

The system is somewhat like a double cylinder engine. On operation, pressurised CO₂ is heated in the evaporator and fed via valve 'A' into the first cylinder which is initially filled with hot liquid. The vapour then exerts pressure and expands against the hot liquid (serving as a liquid piston) which flows through the 4-way valve and the hydraulic motor (wherein the flow and pressure of the liquid is converted into rotary work). During the expansion, the circulation pump continually sprays a portion

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of the hot liquid unto the expanding vapour, thus providing a means of heating the vapour to effect isothermal expansion. The expended liquid continuous in flow, through the heat exchanger in the hot storage tank and back through the 4-way valve into the second cylinder, thus exhausting the hot expanded vapour in the second cylinder via valve 'D' and the regenerator to the condenser. As the stroke ends, the 4-way valve switches to reverse the flow (between the two cylinders), without changing the hydraulic pump's direction of rotation. An analysis of the system performance for the operating conditions of 160 bar and 122°C showed that the isothermal expansion can result in a 46% increase in work output.

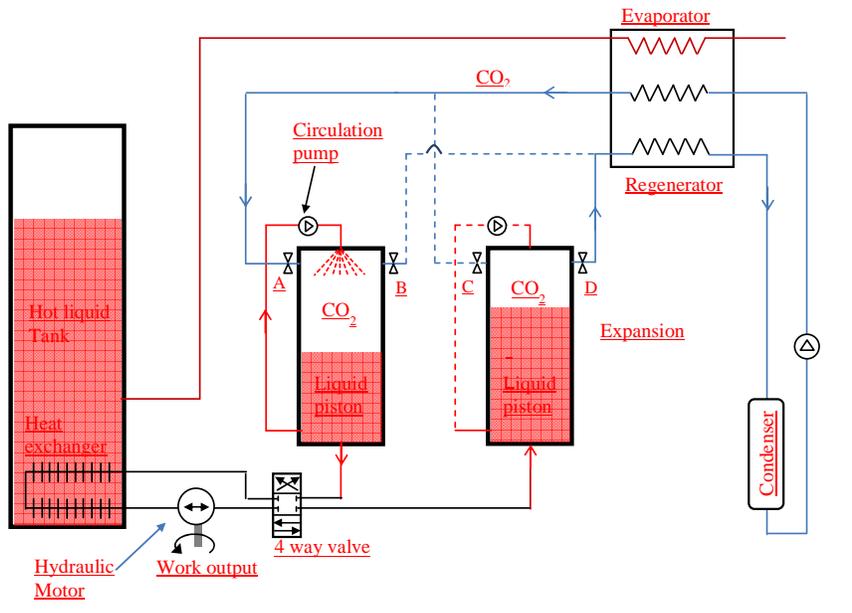


Fig. 6. Isothermal TEES system [48]

3.2.2. Expander surface heated engines

3.2.2.1. Steam jacketed reciprocating steam engine

The steam engine with steam jacket is a classic approach to quasi-isothermal expansion. Nevertheless, certain features and observations are interesting in the modern context where steam or other (organic) working fluids may be used.

In steam engines, there tends to be heat transfer between the steam and the cylinder wall, in such a way that heat is rejected by the steam to the cylinder during the admission and early expansion process, while heat is transferred from the cylinder to the steam in the later part of the expansion and exhaust. This phenomenon is most pronounced for dry steam (relative to superheated steam) as the heat rejection and gain respectively leads to steam condensation on the cylinder wall and re-evaporation of some of the condensate during the rest of the expansion process thus leaving behind some amount of condensate-water in the cylinder. The condensation of steam in the cylinder results in a very rapid drop in maximum pressure and thus decrease in work output, which implies an increase in steam consumption (quantity of steam) required to achieve a given power output. This consequently results to reduced efficiency, since not all the admitted steam is available to produce work for a given amount of heat energy input to generate the steam [16, 4749].

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Besides the use of sufficiently superheated steam, or protecting the cylinder with lagging (insulation), steam jacketing the cylinder can be effectively utilised to mitigate the heat loss from the steam. Various Experiments carried out by a number of researchers, as recorded by Clark ~~[47]~~[50] in the 1800s, have showed that the alternate condensation and re-evaporation in steam jacketed cylinders are much less than that in unprotected cylinder. The steam jacketed cylinders results to economy in the steam consumption and displayed a greater degree of efficiency than the cylinder with superheated steam, whilst both of them are clearly superior to an unprotected cylinder with saturated steam. The steam jackets have reportedly resulted to economy of 14 - 25% in steam consumption rate per power output, net specific work output increase of 42% (from 224 to 318 kJ/kg) and efficiency (in terms of the total heat passed into the cylinder and the work output) increase of 28% (from 8.65 to 11.05%). Further results showed that better performance was recorded for higher working pressure – this could be explained by the fact that heat transfer is facilitated by higher pressure. It was also demonstrated that by the utilisation of the steam jacket with high temperature, heat can be supplied (from the cylinder to the working steam) in quantity sufficient to prevent (or mitigate) the initial condensation in the cylinder and to re-evaporate the whole of such that may have been condensed.

3.2.2.2. Surface heated boiler-less Rankine engine

The speed of heat transfer is a limiting factor in the steam jacket design, but for certain applications speed is not considered critical. ~~Igobo and Davies [23]~~Igobo and Davies [22] proposed to use a slow-moving machine to drive a high pressure reverse osmosis process for desalination that works on a cycle time of the order of minutes. In this case, it was proposed to eliminate the traditional boiler (evaporator) of the steam engine and rely on the jacket (which may be thermal oil fed) alone for heat transfer to vaporise the working fluid and to maintain quasi-isothermal expansion. Fig. ~~67~~ shows a schematic layout for the cycle, its corresponding temperature-entropy (T - s) is similar to that depicted in ~~Fig~~Fig 4b; on operation, water injected into the heated cylinder vaporises on contact with the hot walls, and exerts pressure on the piston to perform work while expanding. Given the relatively higher temperature of the cylinder wall, further heat is transferred to the steam during the expansion process. At the end of expansion, the superheated exhaust steam could be passed through a heat exchanger – prior to been condenser, to preheat the condensed fluid pumped for the next cycle.

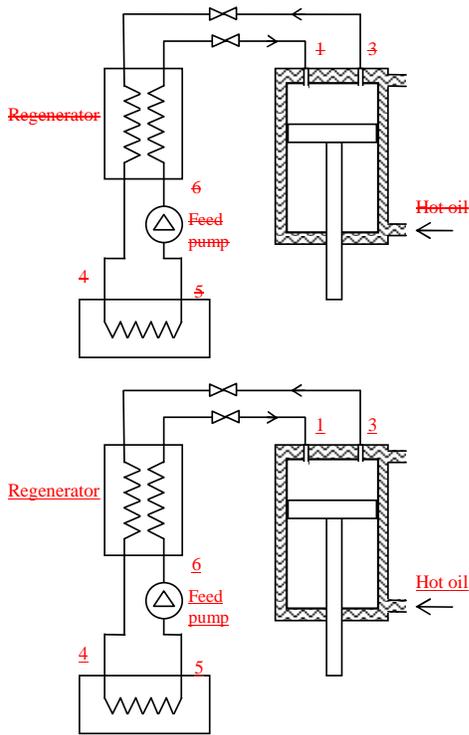


Fig. 67. Schematic of the boiler-less engine [2322]

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Parametric analysis of the engine showed that, the heat transfer rate and thus speed of operation will increase with increasing wall temperature and with decreasing cylinder size. Preliminary experiment carried out on a 100 mm bore cylinder at 250°C wall temperature, showed that engine performance increased with the volume of water injected (0.8 – 1.6 ml). A maximum pressure of about 18 bar and 336 KJ/kg of specific work output was achieved for 1.6 ml of injected water. The cycle efficiency also increased with the injected water volume, as efficiency range of 14–16% was achieved, which is about a half of the ideal cycle efficiency. The less-than-ideal performance was attributed mainly to non-isothermal operation as a result of insufficient surface area (of the expansion space) for heat transfer. This assertion is expected, as it has been noted in literature that: in reality, isothermal operation cannot be carried out in reciprocating engine, due to limited heat transfer area [4851].

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3.2.2.3. Surface heated Rankine cycle scroll engine

The scroll expander is a compact device with few moving parts compared to the reciprocating engine. Scroll expanders and compressors are widely used in refrigeration cycles and have become popular for use in small scale ORC heat engines [49], [52]. Among these, engines using isothermal expansion are an interesting option.

Kim et.al. [12], [21] proposed a scroll expander with external heating structure which included external fins attached on the scroll casing and a heating jacket (as depicted in fig-7 Fig. 8); such that heat could be effectively transferred from an external source, through the scroll casing into the scroll interior. In the expansion process of the system, the transfer of heat from the scroll interior to the working fluid will reduce the temperature drop that would have otherwise resulted, thus effecting a quasi-isothermal

expansion, and consequently contributing to improvement in specific work and thermal efficiency. For air as the working fluid, the isothermal process can result in a potential 34% increase in the expansion work. The system was suggested to be applicable to Ericsson cycle, refrigeration cycle and Rankine cycle.

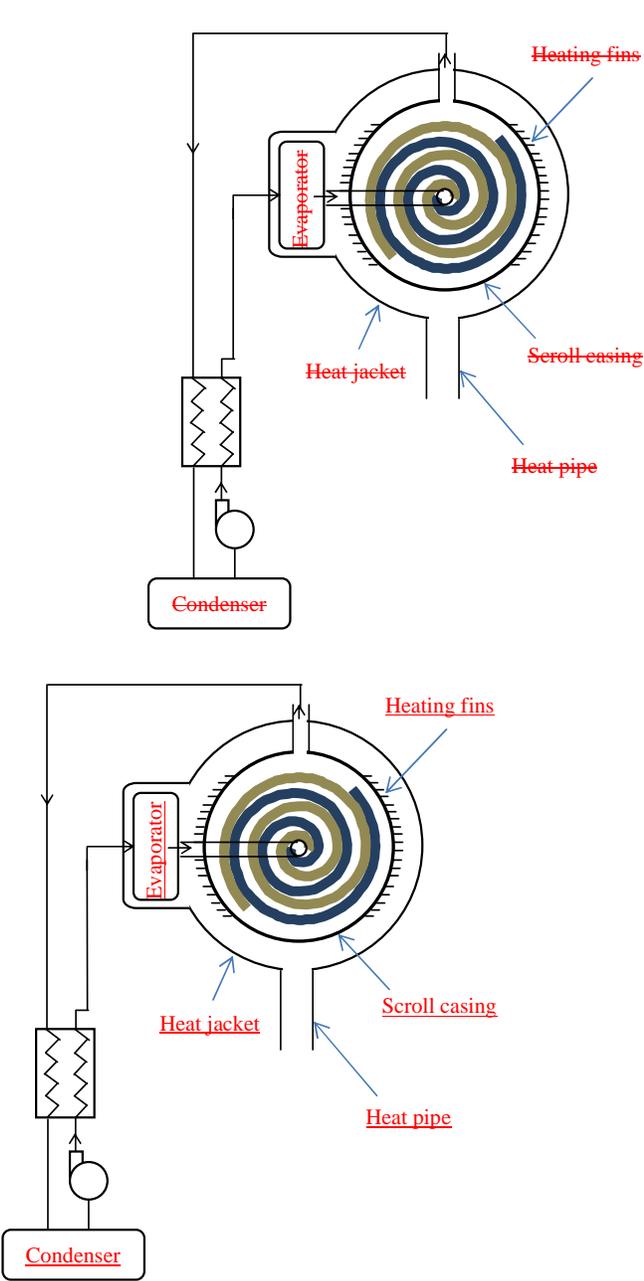


Fig. 7. Schematic of the Rankine cycle with a heated scroll expander [12]
 Fig. 8. Schematic of the Rankine cycle with a heated scroll expander [21]

For use in Rankine cycle, they also highlighted the possibility of the system acting as an expander and partially as a boiler, such that a very wet vapour could be employed as the working fluid at the point of entry into the expander, since the scroll machines are noted for tolerating substantial quantities of liquid fraction. In that case, given that sufficient heat is available from the scroll, the liquid fraction will vaporise during the expansion process, thus tending to reduce the rate of fall in pressure that would have otherwise resulted, and permitting higher volumetric expansion ratio and thereby enhancing the extraction of more work.

3.3. Summary

To summarise with regard to the Rankine cycle engine and its implementation with quasi-isothermal expansion, the expander surface heating can achieve significant improvement in performance even though the expansion chamber surface area available for heat transfer may not be sufficient to approach the level of isothermal behaviour reported with the liquid flooding system. On the other hand, the liquid flooding may experience deteriorating performance in reality, mainly because, unlike the expander surface heating, the liquid flooding incurs additional pumping energy input (for the liquid loop) and increased suction pressure drop, which (together with other associated losses) can eventually outweigh the expected performance improvements. From the perspective of technology availability, liquid flooding can be easily implemented, since its main components (scroll compressor, pump and heat exchanger) are readily commercially available. Nevertheless, it is a relatively new technology (that is yet to be fully developed), in comparison to steam jacketing, which can be regarded as a mature technology that has been proven effective and operational. However, for practical consideration for both technologies, proper insulation is recommended, to ensure that the heat loss (from the engine and piping) to the ambient is greatly minimised, so as not to result to a detrimental effect on the overall performance. In addition, further research work should be carried out on modelling of complex, unsteady multi-phase heat transfer with liquid flooding devices; and development of efficient separation mechanism for the flooding liquid separator.

4. Cryogenic heat engine

4.1. Theory and principle of operation

Cryogenic engines are another example where quasi-isothermal expansion is used. It is interesting to review the works in this area for possible application of similar features to heat powered engines working at higher temperatures.

Cryogenic heat engines utilize the thermodynamic potential between the ambient atmosphere and a cryogenic fluid, which is generally regarded as energy storage medium. The basic ~~idea~~concept of the cryogenic heat engine is to utilize ambient heat from the atmosphere as a heat source to ~~vaporize and superheat a heat a pressurised~~ cryogenic ~~liquid into pressurized gas~~fluid which can be used to drive a prime mover. This is in contrast with typical heat engines which utilize an energy source at temperature significantly above ambient and use the atmosphere as a heat sink [26, 50]-[25]. As with conventional heat engines, the performance of the cryogenic engine is strongly dependent on the cryogenic working fluid employed. A study pointed out the benefits of using low-mass gases (like H₂, He, Ne, N₂, and air) in two-phase system, as having large maximum specific work values [51], with H₂ having the largest value. Another cryogen reported elsewhere with high specific work value is CH₄ [52]-[53], with H₂ having the largest value. Other common cryogens are hydrocarbons, including liquefied natural gas (LNG), of which methane (CH₄) is noted for having high specific work output potential [54]. Nevertheless, liquid nitrogen and liquid air are considered most attractive because they are essentially inexhaustible resource (that can be effectively produced from air) with considerable safety and environmental benefits.

Standard thermodynamic power cycles can be employed to produce useful work from the cryogenic fluid, but the most extensively investigated one is the open system Rankine cycle [18]. For instance, cryogenic gas Stirling cycle could utilise seawater (ambient temperature) as the heat source to heat nitrogen gas in the expander, while liquefied natural gas (LNG) serves as the heat sink to cool the gas during compression [55]. Similarly, ambient evaporation of a cryogenic fluid and condensation by means of LNG as heat sink, can be employed for cryogenic Rankine cycle (Fig. 9a); and multiple cryogenic cycles can be cascaded to yield better cold energy recovery (Fig. 9b and c) [56]. For these closed cycles, propane (C_3H_8) and ethane (C_2H_6) are commonly considered as the working fluids; nevertheless, other low boiling point substances can be employed. The cryogenic power cycle can also be used as the bottom cycle in combined (or hybrid) cycles with other relatively higher temperature power cycles [57]. However, the simplest and most applicable power cycle is the open system (direct expansion) Rankine cycle [58], where the spent exhaust gas is released into the atmosphere. In this case the principle of operation is similar to that of a typical open cycle steam engine.

A schematic of a typical cryogenic heat engine is depicted in fig-8 Fig. 10. The cryogenic liquid stored in a tank (which may be vacuum jacketed) is pumped to the required working pressure; the pressurised liquid is then vaporised and heated in an appropriate ambient heat exchanger system, and then fed to an expander, where it expands to do work. Since the rapid expansion process of the cryogen fluid results in the temperature of the fluid always being less than ambient, the expander will be at a relatively higher temperature than the expanding fluid, thus during the expansion process, further heat may be transferred from the expander to the fluid, resulting to a possible quasi-isothermal expansion process [26]. The T-s diagram of the ideal cycle at critical pressure operation is shown in fig- 8b[25]. The T-s diagram of the ideal cycle at critical pressure operation is shown in Fig. 10b. Process 1-2 indicates the pumping process, process 2-3 is the heating process in the heat exchanger, and process 3-0 is the isothermal expansion. Process 0-4-1 is the ~~would be~~ condensation stage ~~i.e.~~ (for closed loop system), or the liquefaction process which takes place remotely in an air processing plant [53]. Nevertheless, the possibility of combining the liquefaction process with the Rankine cycle has been investigated [54],[59] (for open system).

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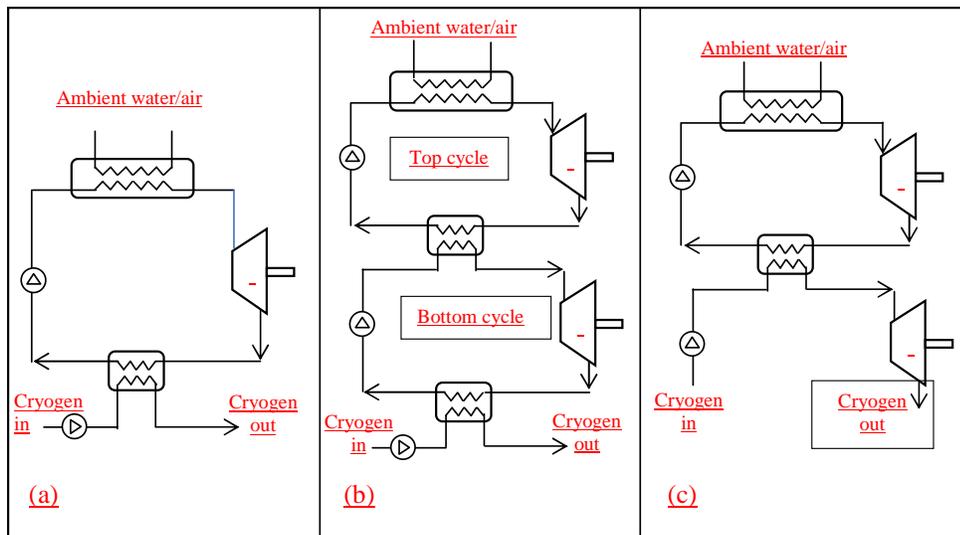


Fig. 9. Schematic configurations of cryogenic Rankine cycles [54]: (a) Rankine cycle, (b) cascaded Rankine cycle, (c) combined closed-open cycle

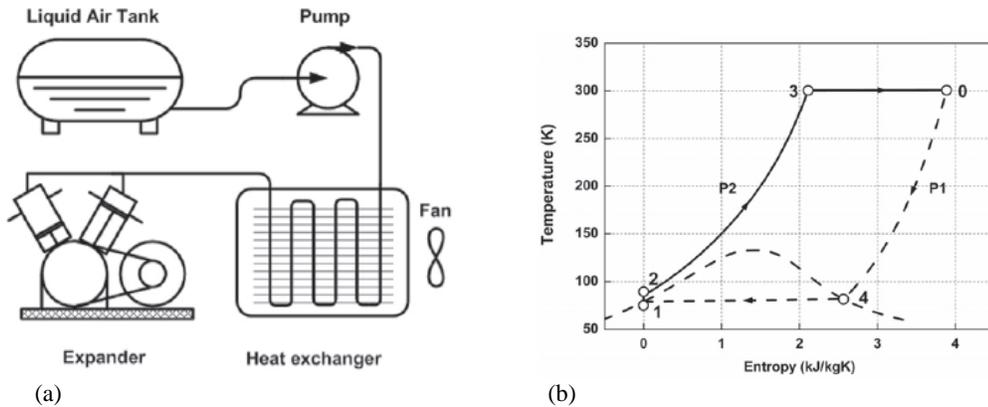


Fig. 8.10. Schematic of a direct expansion (open system) Cryogenic heat engine [48,17]

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4.2. Studies and performance

Over the years, there has been investigations on the application of cryogenic heat engine as an automotive propulsion for non-polluting zero emission vehicles, concept and technical feasibility have been evaluated [18, 55], and demonstration model cars have been built to test its practicality [56, 57]. Key for practical realisation of the engine is the heat exchanger. Considering the low temperature of the cryogenic fluid, it will be essential for the liquid to be vaporized without the accumulation of frost, so as to avoid deteriorating performance. William et al., [58] developed a frost free heat exchanger for using atmospheric air to vaporize and superheat relatively large quantities of liquid nitrogen without the adverse building up of frost.

Over the years, there have been investigations on the application of cryogenic heat engine for power generation, and also as an automotive propulsion for non-polluting zero emission vehicles: concept and technical feasibility have been evaluated [60], flow simulations in the engine have been carried out [61], and demonstration models have been built to test its practicality [62]. Key for practical realisation of the engine is the heat exchanger. Considering the low temperature of the cryogenic fluid, it will be essential for the liquid to be vaporized without the accumulation of frost, so as to avoid deteriorating performance. William et al., [63] developed a frost free heat exchanger for using atmospheric air to vaporize and superheat relatively large quantities of liquid nitrogen without the adverse building up of frost. Amrit et al. [64] also developed a cryogenic heat exchanger and presented analytical model for turbulent flows.

Research work carried out at the University of Washington highlighted substantial benefits in the overall energy efficiency for isothermal expander over an adiabatic one in eryogenic engines [47]-liquid nitrogen cryogenic engines [65]. The study investigated the specific work output as a function of peak cycle pressure for adiabatic and isothermal expansions and showed that the isothermal work increases monotonically with increasing pressure, while that for the adiabatic process is found to be only weakly dependent on peak cycle pressure above 4 MPa. For pressure range of 10 to 300 bar at 300 K, the net specific work is 190 to 420 kJ/kg and 140 to 190 kJ/kg for isothermal and adiabatic conditions respectively. Knowlen [52]

Knowlen [66] studied the performance of two other cryogens (namely CH₄ and C₂H₆) alongside N₂ for both isothermal and adiabatic expansion, and also showed that for all the working fluids, at a given injection pressure, the specific work obtainable from isothermal expansion exceeded that of the adiabatic expansion, with the difference greater as pressure is increased. And beyond 3 MPa, the adiabatic cycle exhibited relatively very little gain in specific work. The study also examined the use of N₂ as a heat sink for different closed loop CH₄ and C₂H₆ topping cycles, and found that for binary

(N₂-CH₄) and ternary (N₂-CH₄-C₂H₆) systems cascaded cycles, specific energies in the range of 200-380 kJ/kg and 300-450 kJ/kg can be realized respectively, depending on the extent of isothermal operation achievable. Yuanwei et al. [67] proposed a Temperature-Energy level-Energy (T-Q-H) diagram method for analysing the performance of two different configurations of three-loop cascaded cycles with seawater and LNG respectively as the heat source and heat sink. They claimed that the proposed method facilitates quick optimisation process on a base case design. A number of authors have also explored different closed cycles that use seawater and LNG respectively as the heat source and heat sink. Choi et al. [68] compared the performance of different configurations of two and three loop cascaded cycles and combined (closed-open) cycles in comparison with the conventional single closed or open cycles. The study showed that the cascaded cycles exhibited better performance than the conventional single closed or open cycles; it also showed that, C₃H₈-C₂H₆ cascaded cycle exhibited 51%, 49% and 89% more work output than C₂H₆-C₃H₈ cascade, C₃H₈ and C₂H₆ cycles respectively; while the C₃H₈ cycle gave 27% more work than C₂H₆. Liu and Guo [69] studied a variant of the cascaded cycle combined with vapour absorption process, the cycle employed a binary mixture of Tetrafluoromethane (CF₄) and C₃H₈ as the working fluid. The study showed that, the proposed cycle can achieve 206 kJ/kg specific work output, which is 63% higher than that of a C₃H₈ cycle (124 kJ/kg). In a study by Li et al. [58], an open cycle with two-stage expansion was shown to exhibit 326 kJ/kg work output. This compares reasonably with the performance reported for other two-loop cascaded cycles. Hence, although cascading closed cycles can significantly improve performance, it is also possible to achieve reasonable performance improvement with the relative simpler open system, with the aid of multiple expansion stages.

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~~To achieve more work output by isothermal expansion, Knowlen [26] In a bid to avoid drop in expander wall temperature, which could result to deteriorating performance, Knowlen [25] suggested the use of “warmant” anti-freeze liquid (as a heat transfer fluid) to be pumped through the wall-of the expander, so as to maintain the cylinder wall at near ambient temperature, thus enhancing heat transfer during expansion, hence effecting quasi isothermal operation.~~ Also, a parametric analysis on engine (reciprocating expander) geometry showed that long strokes, small bore and low RPM enhances heat transfer during the expansion process. Nevertheless, the transferable heat will be limited by the expander’s surface area exposed to the fluid, which will limit the degree of isothermal operation achieved. ~~For standard reciprocating engine (without modifications to cylinder piston geometry), isothermality of about 0.75 has been reported [18, 26]; and this~~ For standard engine (without modifications to cylinder piston geometry), isothermality is typically about 0.75 and can be improved further by enhancing heat transfer during expansion. Further analysis showed that finned piston and cylinder head geometries (fig-9 Fig. 11) having high surface-to-volume ratios can be used to facilitate further heat transfer during the expansion, resulting in potential net work output of 0.85 of the ideal isothermal work ~~[26].~~

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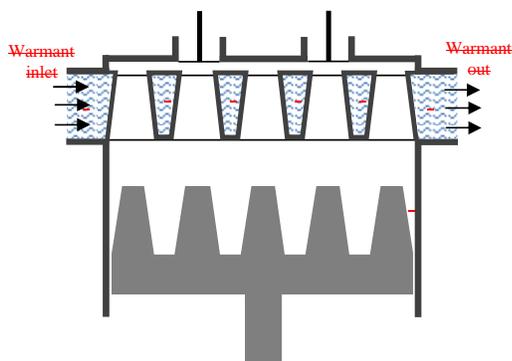


Fig. 9. Conical finned piston and heater core cylinder head [26]

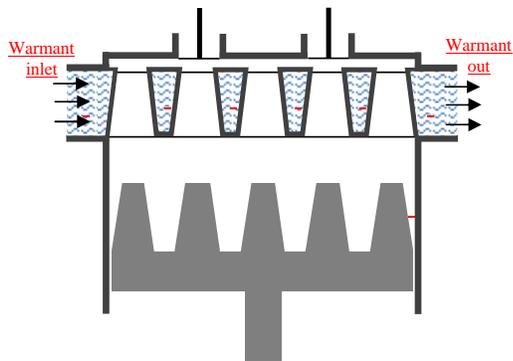


Fig. 11. Conical finned piston and heater core cylinder head [25]

Liquid air ~~is of~~has similar properties ~~with to those of~~ liquid nitrogen since air is composed of 78% nitrogen. ~~Chen et al. [18] studied the performance of a liquid air engine for a range of working pressure and temperatures and reported that over the working temperatures range studied (270–320 K), both the theoretical total and net work output for the engine increases linearly with increasing working temperature. For a working pressure range of 50 to 400 bar, the work output was also found to increase monotonically with increasing pressure and the increase tends to level off at high pressures. For~~Chen et al. [17] studied the performance of a liquid air engine for a range of working conditions and reported that, for a properly designed and manufactured engine with operating conditions of 100 bar and 300 K, the practical (taking into account the losses associated with conventional engines) net work outputs of the liquid air engine for isothermalitys of $\gamma = 0.90$ and 0.75 ~~are were~~ respectively 200 kJ/kg and 150 kJ/kg, ~~which are i.e.~~ respectively about 122 and 66% higher than that for an adiabatic engine (about 90 kJ/kg). Given that the energy consumption for liquid air production is about 1080 kJ/kg [53][59], the efficiency of the cryogenic engine (in terms of energy in and energy out) for the above stated isothermalitys will be about 18.5% and 13.9%, while that for the adiabatic condition will be 8.3%. ~~However, Ameel et al. [70] indicated that the efficiency of the isothermal cycle can be improved by about 17%, if the liquefaction process is combined with the heat engine.~~

~~Dearman [24, 59]~~Dearman [23] developed a variant of the cryogenic engine, whereby the cryogenic liquid is directly injected into a heat exchange liquid (water) in a reciprocating expander, thus the heat exchange takes place inside the engine, consequently eliminating the need for the relatively complicated, heavier and expensive heat exchanger as required previously. The principle of operation is such that, when the piston is at the top of the cylinder, water is admitted into the cylinder dead space, and then a little amount of the cryogen is injected into the water. Since the water temperature (ambient) is substantially higher than that of the cryogen, the cryogen rapidly vaporises, builds up pressure, becomes superheated and pushes the piston as it expands to do work. At the return stroke, the spent gaseous cryogen and the water are exhaust out. The water can be recovered, reheated and pumped back to the cylinder for another cycle: [71].

~~Wen et al [25] studied the heat transfer behaviour between liquid cryogen and water (as the heat transfer fluid) in Dearman's engine, and reported a much stronger heat transfer than that obtained from boiling on smooth surfaces and flow boiling through pipes, but comparable to that of rough surfaces and pipes with porous inserts. The pressure was seen to develop very rapidly (up to 500 KPa/s) and increased approximately linearly with the injection pressure; thus indicating that high pressure could be effectively developed to run the engine.~~

Wen et al [24] studied the heat transfer behaviour between liquid nitrogen and water (as the heat transfer fluid) in Dearman's engine, and reported a much stronger heat transfer than that obtained from boiling on smooth surfaces and flow boiling through pipes, but comparable to that of rough surfaces and pipes with porous inserts. The pressure was seen to develop very rapidly (up to 500 kPa/s) and increased approximately linearly with the injection pressure; thus indicating that high pressure could be effectively developed to run the engine. Morse and Kytömaa [72] also carried out experimental study of the vaporisation of liquid nitrogen and LNG in water, and found that, the evaporation rate is significantly dependent on both the turbulence intensity of the water surface, and the thickness of the cryogenic liquid layer. However, vaporising LNG in water may require safety precautions against possible ignition of the vapour, as has been reported with incidents of LNG spills on sea [73].

4.3. Summary

In summary, the cryogenic engine provides an inherent means of effecting quasi-isothermal expansion with ambient temperature. The potential isothermal performance increases with increasing pressure and could be as much as twice that of the adiabatic case. Cascading multiple cycles would give better energy recovery than single closed or open cycles; however, the open cycle is the most applicable. For an operating pressure of 10 bar, the potential performance of the liquid nitrogen open cycle cryogenic engine can have an ideal efficiency of 19% and specific work of 200 kJ/kg; but this performance is quite low in comparison to ~~that of the 27% ideal efficiency predicted for~~ a surface heated engine operating on steam with similar pressure, ~~which can ideally have 27% efficiency [23]. Also, the ideal specific work of the cryogen is rather low compared to [22], and~~ the reported 318 kJ/kg specific work achieved for a real surface heated (steam jacketed) engine operated at 5 bar ~~[47]-[50]~~. Furthermore, unlike the surface heated engine, although the cryogenic engine has the advantage of not losing heat to the ambient (since it can be at the same or even lower temperature potential with the ambient), it could suffer evaporative losses and safety (explosion) risks at the storage tank; as it slowly absorbs heat from the ambient, which could result to excessive pressure rise ~~[60]-[74]~~.

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5. Vapour Stirling cycle engine

5.1 Theory and principle of operation

The ideal Stirling cycle is a classical implementation of isothermal expansion. ~~Though ideally efficient, it suffers from low specific power output at moderate temperatures and pressures [61, 62]. As a means of increasing the specific power output, the use of condensable working fluid has been investigated in prior arts — the vaporisation of liquid at the hot side of the Stirling engine followed by condensation at the cold side has been identified as a viable solution [27, 63], the use of refrigerants as working fluid has also been considered [64]. Prior arts (including a number of patents) have investigated various means of employing vapour as the working fluid in the Stirling cycle engine (including liquid-piston variants).~~ Though ideally efficient, it suffers from low specific power output at moderate temperatures and pressures [75]. As a means of increasing the specific power output, the use of condensable working fluid has been investigated in prior arts – the vaporisation of liquid at the hot side of the Stirling engine followed by condensation at the cold side has been identified as a viable solution [26], the use of refrigerants as working fluid has also been considered [76]. Prior arts (including a number of patents) have investigated various means of employing vapour as the working fluid in the Stirling cycle engine (including liquid-piston variants).

The concept of liquid-piston Stirling (fluidyne) engine is to replace the conventional solid-pistons of Stirling engine with columns of liquid (typically water) in U-tubed cylinder. Unless the liquid in the expansion cylinder has a low vapour pressure at the operating temperature or is separated from the hot gas by some kind of insulating float (generally referred to as dry fluidyne), ample evaporation will take place from the liquid surface and wetted cylinder walls to effect a mixture of gas and vapour working fluid [65]. ~~As such the fluidyne engine can provide both gas and vapour power cycle.[77]. As such the fluidyne engine can provide both gas and vapour power cycle. One critical design parameter in the fluidyne engine is the frictional losses in the oscillating liquid columns [78].~~ Studies have shown large dry fluidynes to be quite successful, but on the other hand, small dry fluidynes (which generally suffer from the large transient heat-transfer and flow losses associated with small-diameter tubes) have been reported to be impractical in the absence of evaporation [65]-[77]. The evaporation tends to raise the pressure during the expansion phase and thus increases the indicated power in the fluidyne engine. Owing to the fact that the power output is available in the form of ~~either~~ pulsating pressure/movement of liquid in a tube, the most obvious application ~~is was~~ as a pumping engine [66]. ~~However, a rotating shaft power output option have also been identified lately[79]. However, a rotating shaft power output option have also been identified, via the use of hydraulic motor [80] or solid pistons [67]. Here, as shown if fig. 10, a[81]; with the former, as shown if Fig. 12, the solid piston converts the pressure in the liquid piston into a force which can then be applied to a shaft, like conventional engines.~~

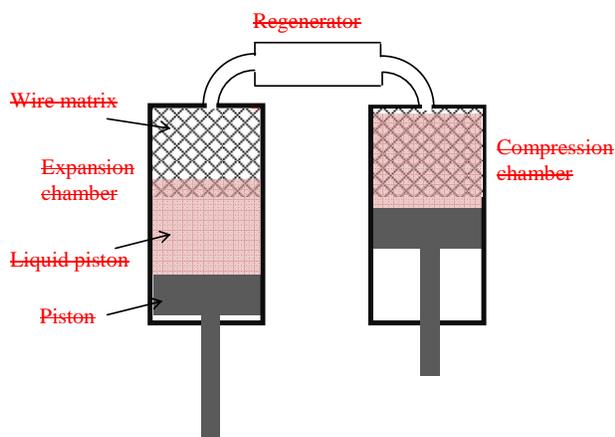


Fig. 10. Liquid-piston Stirling engine [67]

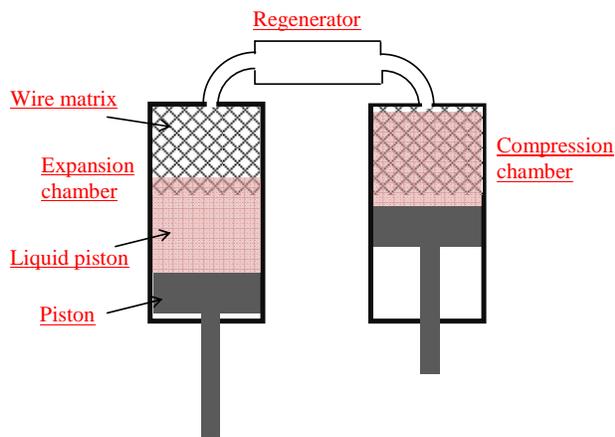


Fig. 12. Liquid piston Stirling engine [81]

Since liquids can conform to irregular shapes, unlike solid-piston, liquid pistons have the advantage of possibly allowing the adoption of working chambers with very large surface area to volume ratios such as wire matrix, tube bundle, metal foam, etc. (Fig. 12), to substantially improve heat transfer to the working fluid and consequently bring the working fluid behaviour into the nearly isothermal regime (which will result to improved power output and efficiency). However, the high area to volume ratio will result to smaller size of flow passages, increased flow restrictions and thus, increased viscous losses. As such the heat transfer area and the viscous frictional losses must be adjusted to maximize the efficiency of the liquid piston engine [65, 68][82]. Besides the increased viscous losses, the liquid piston also suffers operating stroke and frequency limitations imposed by gravity-controlled oscillation and by surface instability at high frequency; and the need to keep a more or less constant orientation of the engine [65, 67][81].

Various concepts involving the conventional solid-piston Stirling engines variants with modifications on operational configurations have also been recorded. Rederson [69][83] patented a vapour Stirling machine based on the alpha Stirling configuration. It featured heating and cooling chambers on the hot and cold cylinder tops respectively, and with a regenerator interconnecting the two chambers (Fig. 13). But in contrast, the working fluid in the cooling chamber is substantially in the liquid phase as such resulting to a significantly larger swept volume ratio than a conventional Stirling engine. On operation, the upward motion of the cold cylinder piston pumps the fluid through the regenerator into the hot chamber where it gets completely vaporised and superheated and then expands to perform work against the hot piston while gaining further heat from the hot chamber, thus tending to approach isothermal expansion. At the end of expansion, the upward motion of the hot piston pushes the spent vapour through the regenerator and into the condenser where it condenses back to water. As a means of providing output control, a control cylinder is included at the cold section to vary the effective mass of the working fluid within the engine.

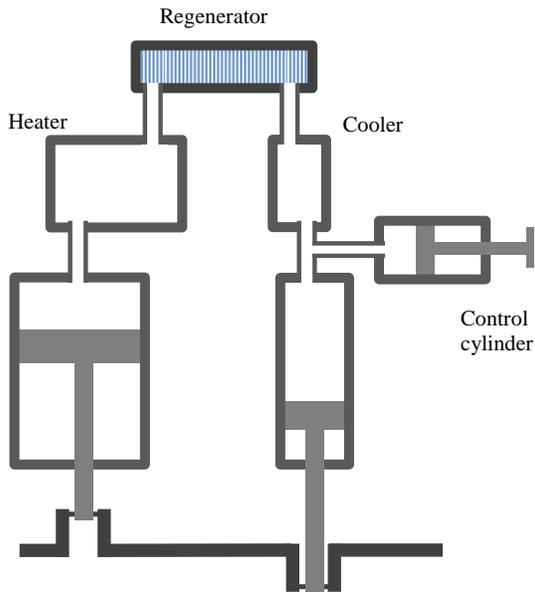


Fig. 13. Vapour Stirling engine [97]

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Davoud and Burke [70][84] patented a condensing vapour Stirling engine, in which at the end of expansion, a portion of the spent vapour is expelled (via a receiver cylinder) and condensed, while the remaining portion is compressed in the power cylinder, during which the weight equivalent of the condensed portion is pumped and injected back into the cylinder as a fine spray of water. This was said to lower the entropy and enthalpy of the steam in the cylinder, and thus lower the compression work that would have been required. The compressed steam gets superheated in the heater tubes arrangement at the top dead centre of the cylinder, and then expands against the piston to do work. They later went further to patent a simpler version (with only one cylinder), in which bulk of the spent steam is expelled directly to the condenser. The condensed water is then pumped and injected into the cylinder top dead volume containing the heater tubes where it gets vaporised and superheated [74][85].

5.2. Studies and performance

West [27][26] developed a two-phase, two component working fluid system for an alpha Stirling engine configuration (fig-12 Fig. 14), in which, the working fluid consists of both a condensable vapour (steam) and permanent gas (air), such that the air is contained in the cold section, and prevented from passing into the hot section by means of controlled evaporation (i.e. steam pressure) in the hot section. Water injected into the evaporator vaporises into the hot cylinder where it expands to do work. The expanded vapour then passes into the cold end where it condenses and is subsequently removed.

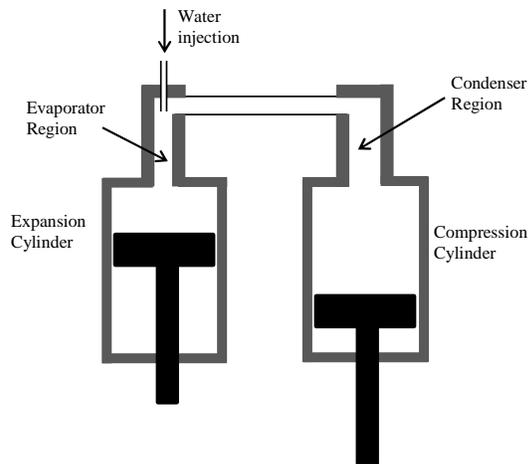


Fig. 12 Fig. 14. Basic layout of the two-phase, two-component Stirling engine [27][26]

The analysis showed that under moderate operating conditions the engine can achieve a cyclic power output at least five times greater than a conventional Stirling-cycle machine of similar dimensions, but at the expense of significantly lower ideal cycle efficiency. Nevertheless, by controlling the rate at which the liquid is evaporated into the expansion cylinder an indicated efficiency in the range of 3 to 9% at low temperatures (110°C to 130°C) may be achievable even without regeneration.

Isshiki et.al. [28][27], developed a steam Stirling engine which operates as a hybrid of Stirling and Rankine systems, such that the engine featured a power cylinder (with heating tube at the cylinder

top), displacer cylinder and a regenerator in between, as with Stirling; but also has injection/exhaust port, thus spent steam could be ejected, condensed, pump and re-vaporised externally just like Rankine. On operation, when the power piston comes near its top dead centre, saturated steam from the external boiler injected into the displacer cylinder, passes through the regenerator and heater, and then expands into power cylinder at near constant high temperature. On the return stroke, the spent steam passes through the regenerator and is exhausted to a condenser where it gets condensed and then pumped back to the boiler. Experiment carried out on a mini scale prototype operated at 0.2 Mpa (gauge) and 250°C showed that output power of about 12 watt was achieved at 400 rpm. This is significantly higher (approximately five times) than the reported 2.6 watt achieved for a conventional gas Stirling engine operated at 320°C [7286].

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5.3. Summary

In summary, the use of vapour as the working fluid in Stirling engines can result in power outputs about five times larger compared to conventional non-condensable gas working fluid. To facilitate more heat transfer to the fluid to approach a more isothermal behaviour, liquid pistons could be employed to allow the expansion space to be enhanced with high surface area geometries like wire matrix. However, it introduces practical issues that will need to be further investigated. As such it is recommended that further research be carried out on: modelling the behaviour of the oscillating liquid in liquid piston devices with particular attention to viscous forces and inertia effect of the liquid oscillation. Since the various technologies presented are still in the concept or early development stage, further experimental studies should be carried to give a better insight on their practical realisations; and optimization of the various full engine dynamics to maximize efficiency and power density for specific applications.

6. Conclusion

To convert low-grade thermal energy into useful work, external combustion engines using vapour cycles (though relatively less efficient) have been preferred over those using gas powered cycles due to the former's higher specific work output and smaller engine size. Relative to the traditional ideal adiabatic expansion process in the vapour power cycle engines, quasi-isothermal expansion has been found to improve the specific work output and cycle efficiency of the engines.

Two main methods of effecting the quasi-isothermal expansion have been identified – liquid flooding and expander surface heating. The expander surface heating has been studied for both reciprocating and rotary expanders; however there are more references in the literature for its use with reciprocating expanders. Liquid flooding is referenced more for use with rotary expanders.

In practical performance of the quasi-isothermal expansion, studies have showed that liquid flooded expansion approaches isothermal behaviour with increasing oil fraction; but at the expense of deteriorating overall performance, that was partly attributed to the resulting increased suction pressure drop and viscous losses. On the other hand, the expander surface heating has been shown to achieve significant improvement in performance (over 40% and 20% increase in efficiency and 40% increase in specific work output and efficiency respectively). Here, a relatively slower operating speed is required to enable significant heat transfer during the expansion process as the cylinder wall surface area available for heat transfer limits the isothermal operation. However expander geometries with high surface-to-volume ratios (such as fins) could be employed to facilitate heat transfer and further improve performance, as has been demonstrated with cryogenic engine. Furthermore, much higher surface area to volume ratios (such as wire matrix) could be easily realized with the adoption of liquid pistons.

With regards technology availability, it can be seen that the expander surface heating has been ready for many decades in the form of steam jacketing, whereas liquid flooding is a relatively new

technology that is yet to be fully developed. Nevertheless, it can be easily implemented with commercially available parts.

This paper concludes that, while quasi-isothermal vapour power cycle engines have the potential to significantly improve the performance in a number of applications (e.g. desalination, transport and heat recovery), there are research areas to be further examined. As such, it is recommended that further research be carried out on: modelling of complex, unsteady multi-phase heat transfer with liquid flooding devices to predict performance and tailor to applications; modelling the behaviour of the oscillating liquid in liquid piston devices with particular attention to inertia and viscous losses; and the investigation (selection) of other appropriate liquids and working fluids for a range of low temperature operations. Further experimental studies are also ~~recommended~~ recommended to give better insights on the practical realisations and optimisations of the technologies presented as concepts or early developmental stages.

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Figures

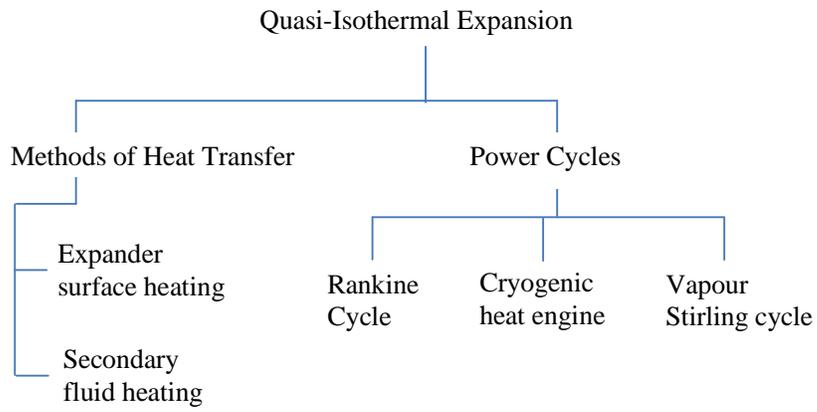


Fig. 1. Overview of the review approach

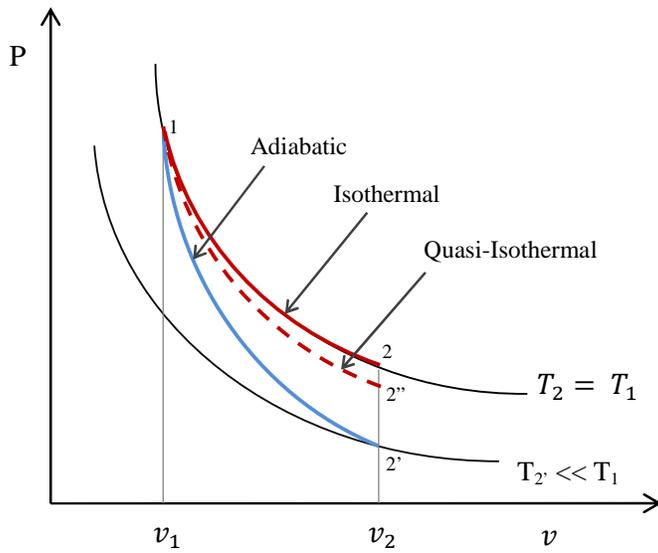


Fig. 2. Graphical representation of isothermal and adiabatic expansion processes

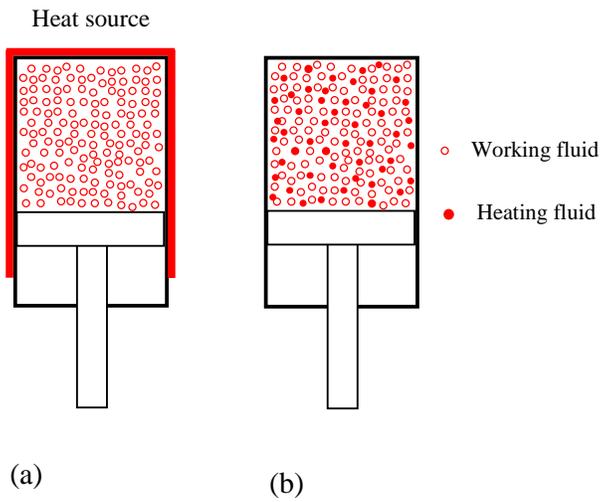


Fig. 3. The two main means of heat transfer used to achieve isothermal expansion: (a) expander surface heating; (b) secondary fluid heating system

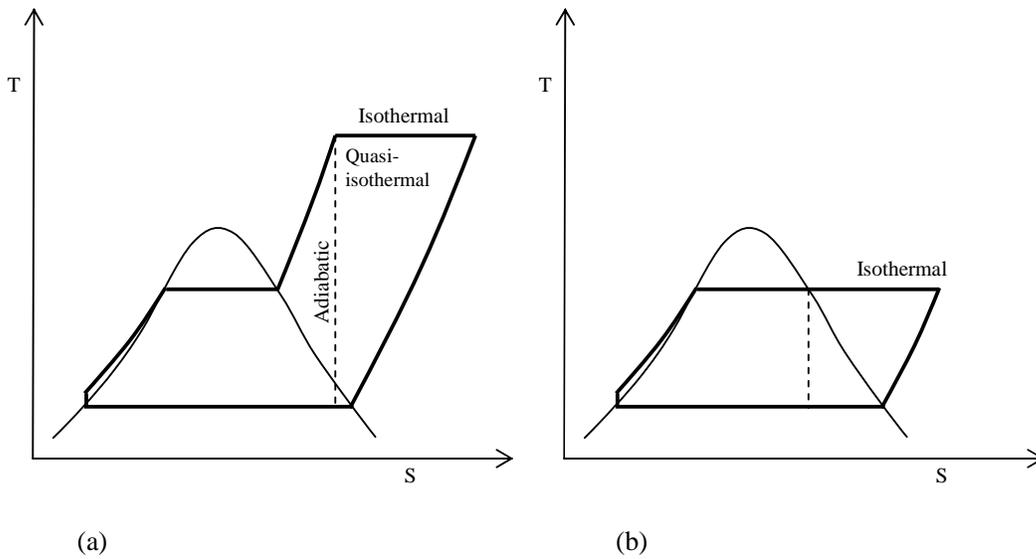


Fig. 4. T-s diagrams of Rankine cycle with isothermal expansion, (a) starting from superheated state [30]; (b) starting from saturated state [44].

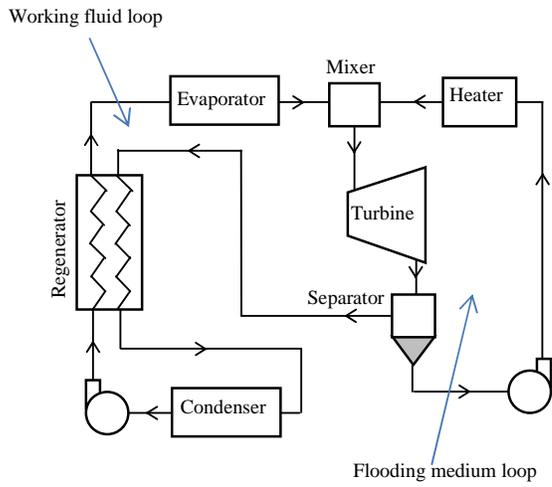


Fig. 5. Schematic of the liquid flooded ORC [19]

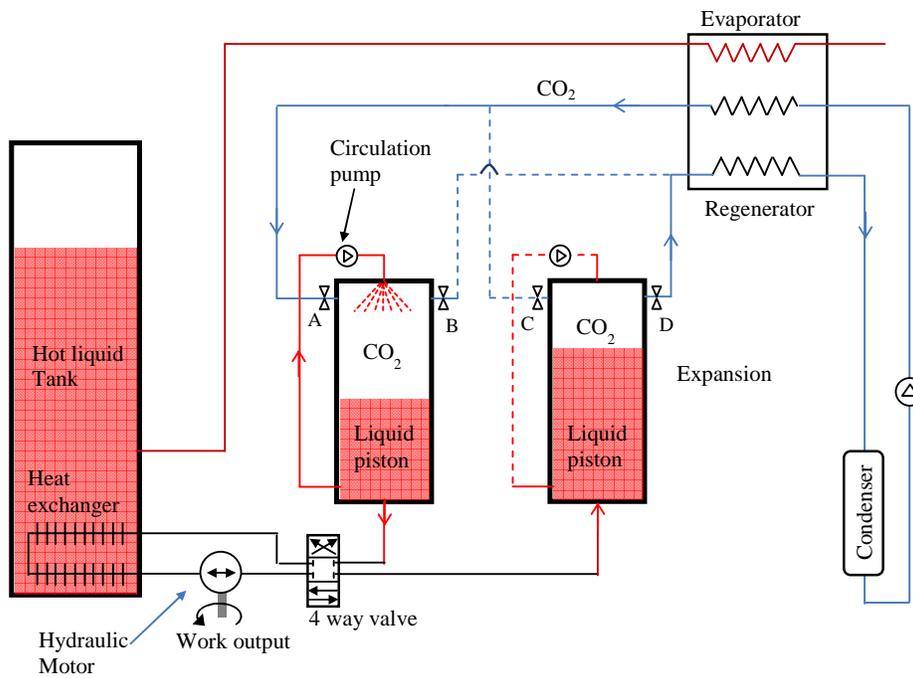


Fig. 6. Isothermal TEES system [48]

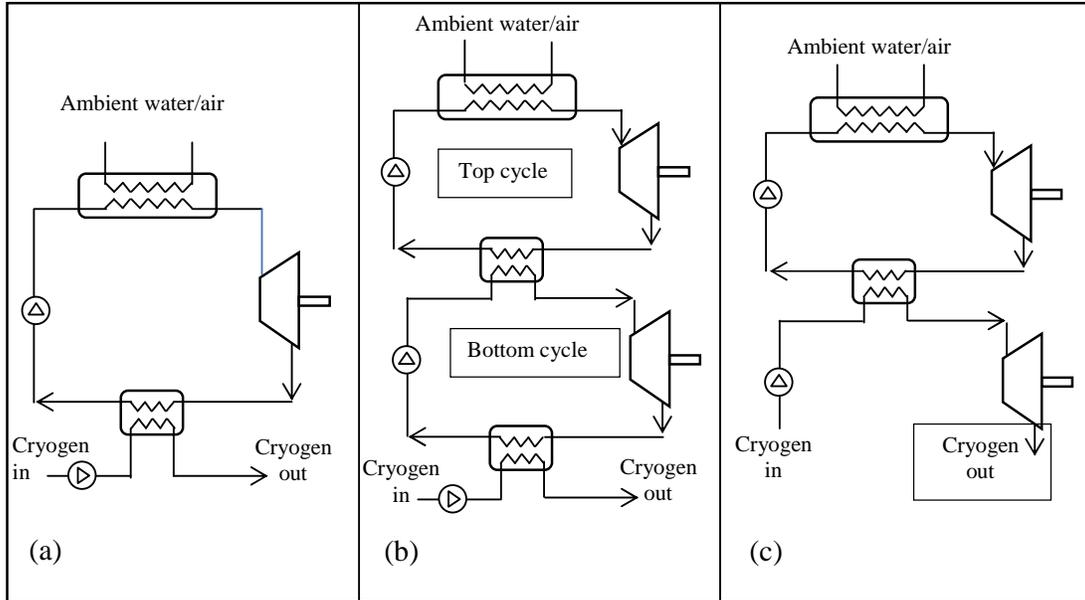
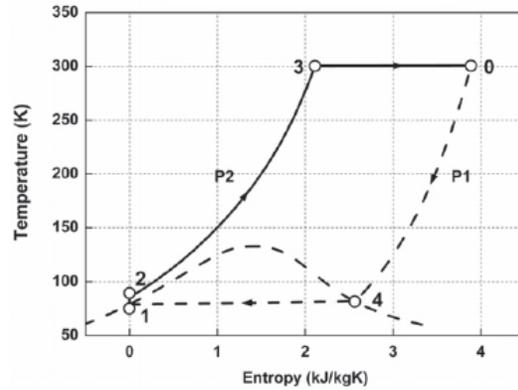
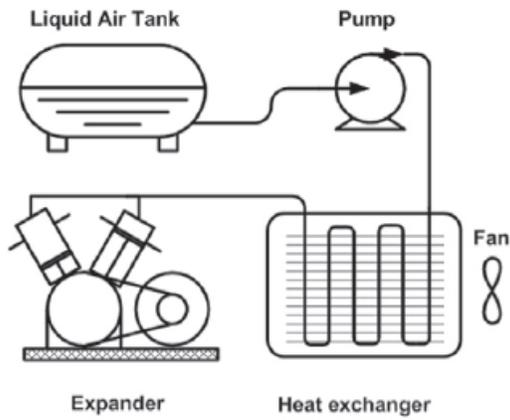


Fig. 9. Schematic configurations of cryogenic Rankine cycles [54]: (a) Rankine cycle, (b) cascaded Rankine cycle, (c) combined closed-open cycle



(a) (b)
Fig. 10. Schematic of a direct expansion (open system) Cryogenic heat engine [17]

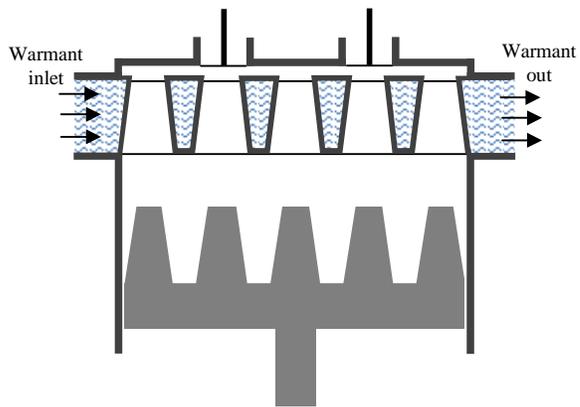


Fig. 11. Conical finned piston and heater core cylinder head [25]

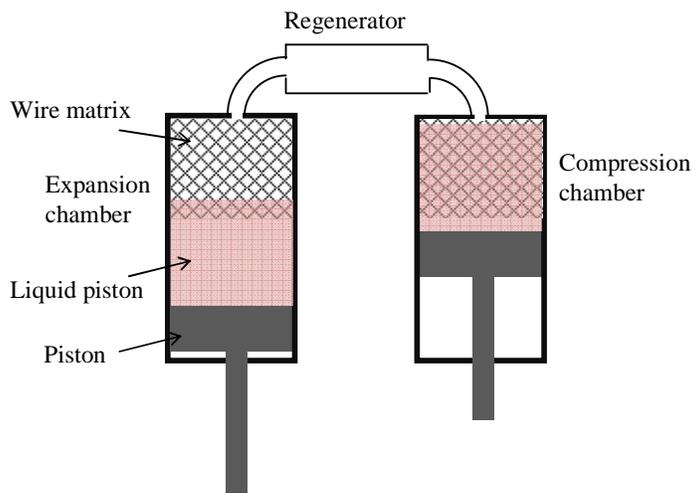


Fig. 12. Liquid piston Stirling engine [81]

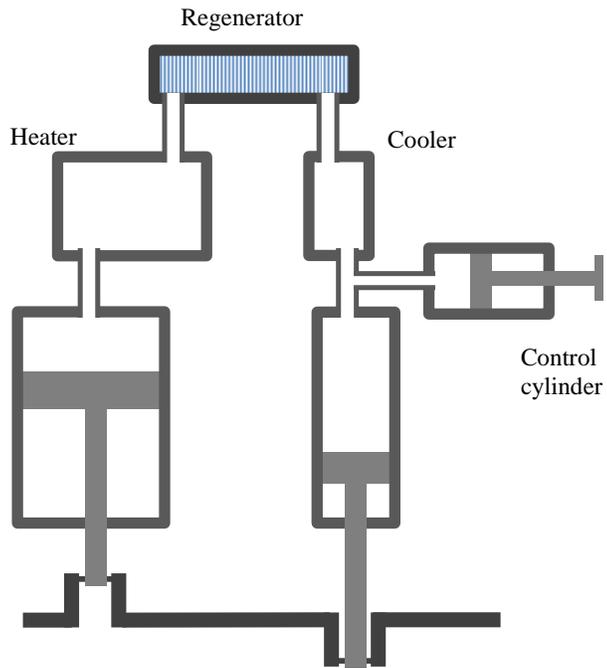


Fig. 13. Vapour Stirling engine [7]

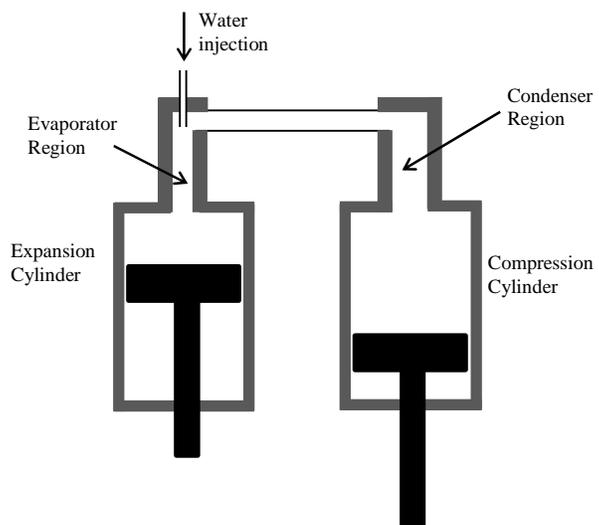


Fig. 14. Basic layout of the two-phase, two-component Stirling engine [26]

Tables

Table 1. Heating methods and the applicable power cycles for quasi-isothermal operation, with relevant examples from the literature

Methods Applications	Secondary fluid heating	Expander surface heating
Rankine cycle engine (section 3)	Theoretical study of liquid flooded scroll turbine, using various fluids [19] Experimental study of the effect of flooding liquid quantity in scroll turbine [20]	Theoretical study of surface heated scroll turbine [21] Experimental study of surface heated reciprocating cylinder [22]
Cryogenic engine (section 4)	Experimental studies of evaporating cryogenic liquid in water [23, 24]	Theoretical studies of surface heated reciprocating cylinder [23, 25]
Stirling cycle engine (section 5)		Theoretical studies of controlled evaporation in Stirling engine [26, 27] Experimental study of vapour Stirling engine [27]

Table 2. Combinations of different working fluids and flooding liquid

Working fluid	Flooding liquid	Expansion device	Ref.	Study type
Ammonia (R717) Carbon dioxide (R744) R410A R600a n-pentane R245fa	Water Zerol 60	Scroll	[19]	T
R245fa	Compressor oil	Scroll	[20]	Ex
Liquid air	Water	Reciprocating cylinder	[23, 24]	Ex

T. Theoretical
Ex. Experimental