

AN OPERATIONAL APPROACH

TO

MULTIVARIATE CLASSIFICATION

with Reference to Agriculture

by

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A B S T R A C T

Social and economic classification schemes have traditionally been administrator constructed, are essentially univariate in nature and reflect the historical development of a range of structures in society. Advances in multivariate statistical analysis over the last fifty years, together with modern computing power, have made possible the classification of companies, farms, people, families, commodities or any other entities using data based polythetic methods.

The feasibility of designing an efficient and understandable operational approach to this type of multivariate classification is investigated with reference to agriculture and the results compared with a proposed *a priori* Farm Typology.

The requirement to reduce the size of the variable set employed in an optimisation-partition method of cluster analysis suggested the value of principal components or factor analysis as a means of identifying major 'source' dimensions against which to measure farm differences and similarities. Such source dimensions were found to be not unduly sensitive to changes in the sets of either observations or original variables. The need to standardise variables prior to the extraction of factors was, however, confirmed.

The euclidean cluster analysis incorporating the reduced dimensions quickly converged to a stable solution and was little influenced by the initial number or nature of 'seeding' partitions of the data. The most distinctive cluster classes were equally identified in three experimental samples of 500 observations, while the slightly poorer resolution of general mixed farm groups was hopefully eliminated by final classification based on a ten per cent sample of some 2200 observations.

Although size standardisation of most Farm Structure Survey variables has occurred, *Classification I* using unstandardised component scores still had an important holding size element. Upon standardisation the first two size/technology components have their weight in classification reduced so that an alternative *Classification II* was produced.

The assignment of non-sampled observations from the population to the classes of *Classifications I* and *II* was completed using classification functions, stepwise multivariate analysis of variance having indicated the number of useful discriminating variables to be some two-thirds of the total originally included in analysis.

The final schemes were found to be both interpretable and meaningful agriculturally and superior in their explanatory power in comparison with the Farm Typology.

KEYWORDS CLASSIFICATION, MULTIVARIATE, CLUSTER, AGRICULTURE, ASSIGNMENT.



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CHAPTER I

AN INTRODUCTION TO CLASSIFICATION

1.1 The Origin of Classification

One of the basic methodologies of science, in reducing the complexities of nature to a manageable form, is to classify. Classifying things is perhaps the most fundamental and characteristic activity of the human mind and underlies all forms of scientific endeavour. Man as a problem solver has developed from primitive roots essentially by feats of classification.

Durkheim and Mauss (1903) maintain that the first logical categories were social categories, the first classes of things were classes of men. They claim to show how the notion of a system of classification was born and they conclude by identifying the forces which induced men to divide things as they did between classes. The argument is based upon the fact that our ancestors were already social animals at the point in time when they became human. Effective social group organisation would depend on the ability to recognise, classify and react appropriately to a large number of other individuals and events. In particular, this would be based on communication through language, the essential elements in which are nouns and verbs implying the classification of things and of actions or events.

The development of the concept of numbers, of counting and of measurement is clearly of fundamental importance to the development of science. However, neither counting nor measuring can be considered the most fundamental process in studying man and his environment. Before you can do either to any purpose there must first be a selection of what it is proposed to count or measure, which presupposes a classification.



## 1.2 A Historical Perspective

In all branches of science classification, whether it is of stellar spectra, of igneous rocks, of pressure distributions, of algae, of industry, of social class, or of books, has always occupied a central position comparable with that of mathematics and logic. Formal classification in botany and zoology predates other applications. Aristotle (384-322 BC) gave to the animal kingdom the first written formalisations of categories and referred to such major groups as birds, fishes, whales and insects. Currently accepted families of plants were recognised at the same time by Theophrastus (380-320 BC). Greek and Roman physicians also developed several typologies based on variations in physical characteristics thought to result from a mixture of the four humours (eg Galen AD 129-199).

No further developments in formal classification construction are identifiable until the Renaissance, when Gesner (1516-1609), Willughby (1635-1673) and Ray (1628-1705) initiated classification nomenclature used by Linnaeus in his *Genera Plantarum* (1737) and *Critica Botanica* (1737). To Linnaeus is owed the system running from phylum and class down to genus and species, a system well known and almost universally adopted in the animal kingdom.

The range<sup>(1)</sup> and extent of classifications in the life sciences at the present time is bewildering. The observations classified include not only plants, animals and insects, but cells, micro-organisms, communities of interdependent members, fossil records, diseases, symptoms of disease and drugs.

The spread of classification activities outside the life sciences, in the past 150 years, is equally impressive. In the earth and engineering sciences, taxonomies of land and rock formations, soil, river systems,

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(1) A list of papers on classification applications is provided in the Bibliography.



cities, counties, regions of the world, land use patterns, weather conditions, finger prints, regional accents, wave forms, radar signals and circuit design illustrate the diversity of applications. Although in the social sciences one can trace administratively based classifications back to the Domesday Book, classifications of occupation and industry to the Craft Guilds, and commodity classifications to Customs and Excise records, the enthusiasm of the social scientist for formal classification is most evident in the 20th century. Among the many objects of their analysis are found families, neighbourhoods, clubs and other social organisations, criminals and crime, cultures, teaching methods, languages, archaeological findings and sites, political regions, legislators, political issues, consumers, trade cycles, markets, investments and credit risks, as well as the well-known industry, product and social class (socio-economic group) classifications. It is this realm of study which has provided the most innovative examples of classification methodology in the past two decades.

### 1.3 Terminology

A classification may be defined as a means by which entities or observations are usefully divided into meaningful subgroups (classes) such that entities within a subgroup are as similar as possible while differences between subgroups of entities are as great as possible. Clearly a classification is only meaningful in relationship to its end use and will be valuable only insofar that the number of classes is considerably smaller than the number of observations to be classified.

While there is a widespread agreement on the nature and broad objective of a classification, there is less agreement on the terminology to be used. The words classification, systematics, typology and taxonomy are commonly treated as synonyms. Crowson (1970) suggests that "originally



and properly, classification would have denoted the activity of placing things in classificatory groups", whereas *systematics* would be the body of general theory leading to the formation of classificatory groups and underlying the classification activity. Dagnelie (1966), on the other hand, claims that the process of choosing which of a number of defined classes a new entity should be allotted, is better described as *identification* or *assignment*. Kendall (1966) adds further to the discussion by distinguishing between classification and *dissection* on the basis of the presence or absence of the requirement that entities in one class should be distant from entities in another class. He argues that "all collections of entities can be dissected; not all can be classified". The terms *typology* and *taxonomy* have come into common use only recently and appear to be more related to Crowson's systematics than to Dagnelie's assignment. Specific uses of *numerical taxonomy* usually refer to computer-based methods of *cluster* analysis which forms the main basis of classification to be considered in this thesis. It is finally necessary to distinguish between classifying things and naming them. *Nomenclature* is concerned with the naming of groups of entities which comprise the elements of the classification under consideration. Nomenclature does not imply names in the strict grammatical sense of the word. The Dewey library classification system is based on numbers, and other schemes on combinations of numbers and letters as in market research social class groupings.

No resolution to this problem of semantics is offered here. The use of each word will, hopefully, be intuitively obvious in the context in which it is employed.

#### 1.4 Classification Methodology

There are two quite distinct methods employed in classification construction. These are the *a priori* and the *data based* approaches. The former is typified by the subjective, administrator-constructed, *standard* classifications of industry, agriculture, trade, occupations, social class, commodities and products. These are in day-to-day use in most countries' statistical offices or bureaux for the collection, analysis and presentation of the data used to monitor the social and economic health of the country. Such classifications are frequently the evolutionary product of historical forces and political factors and are usually univariate in structure.

It is certainly true that the UK Standard Industrial Classification has changed in detail over the past thirty years to allow, for example, the separate specification of electronics and plastics industries. It is equally clear, however, that the basic criterion of classification for companies is univariate, being determined by the company's declared principal activity, and is a historical development from the way in which pre-industrial revolution industry was organised. As such the classification may mask important differences in companies which are more crucial than their end product to the diagnosis of industrial and economic well being. Types and sources of materials, patterns of energy use, range of skill - grades of labour, geographical location, methods of distribution used, sophistication of technology, finance, size, ownership and control are among the many factors which may be as important or more important than end product. Government policy may need to be directed towards changing any combination of these elements and yet has to be based on evidence compiled in relationship to only one.



Data based approaches to classification are, in contrast, multivariate, and seek to group together into classes observations which are similar to each other with respect to a range of measurable characteristics or variables. Inevitably, there are non-numerical constraints in a real-world classification scheme which such methods cannot incorporate. In classifying agricultural holdings on a European basis there may be political considerations which need to be allowed for in the sense that one country, more dependent than others on a particular crop type or more sensitive to the interests of a particular type of holder, will require these elements to be separately depicted in the classification scheme. While such external factors cannot be explicitly taken into account, other than through the selection of classification variables, they should be considered in the practical interpretation of data based methods.

Clifford and Stephenson (1975) divide data based methods into *monothetic* and *polythetic* types. The first involves the subdivision of the observations to be classified by one variable after another in sequence. Thus one first seeks that variable from those available for classification which most distinguishes one group of observations from other groups. Given the classes so formed, a search is made among the remaining variables to find the best one for further class breakdown. The principle is continued until an acceptable classification has been developed. When used with dichotomous qualitative variables, indicating the possession or non-possession of a defined attribute, this is the classic data based hierarchical method of the biologist.

Polythetic approaches involve the formation of classes on the basis of the overall similarity or dissimilarity of individual observations with respect to all the classification variables simultaneously. Because of the problems inherent in manually handling large quantities

of data on numerous qualitative or quantitative variables, the polythetic methods find their main applications through the medium of fast digital computer systems and have developed rapidly in the last twenty years.

Cormack (1971) subdivides polythetic approaches into three:

"(i) *hierarchical classification*, in which the classes are themselves classified into groups, the process being repeated at different levels to form a tree (or dendogram);

(ii) *partitioning*, in which classes are mutually exclusive, thus forming a partition of the set of entities;

(iii) *clumping*, in which classes or clumps can overlap, and a clump and its complement are treated as different types of class."

The advantages of both the *a priori* and the monothetic data based methods are that group definitions are simple and unambiguous. This leads to understandability and the specification of simple rules for the assignment of new observations to classes.

The monothetic approach has an important advantage over polythetic methods in that computation is relatively fast and the addition of new observations to the data set usually leaves the majority of groups unaltered. Offsetting these advantages is the proneness of monothetic methods to generate mis-classifications. Suppose that two groups are distinguishable by a binary attribute. An observation which on the whole resembles members of the first group happens to possess the state of the attribute corresponding to the second group. It will thus be misclassified from the polythetic viewpoint of the classification users who are concerned with overall resemblance.

This is also the essential weakness of the *a priori* univariate approach. For example, a privately owned, small, labour intensive company manufacturing on a multi-product basis, may be classified as



belonging to Order IV (Chemicals and Allied Industries) of the UK S.I.C. because its principal product is paraffin wax. Its resemblance to other members of that order such as the publicly-quoted, large, capital intensive oil refiners (eg Esso, Shell, BP and ICI) is minimal. Its affinity to other small companies in a variety of other industries is much greater in relationship to the ownership, management, finance and technology employed.

The simultaneous strength and weakness of the polythetic approach is that all relevant variables contribute to the determination of classes. This might appear to lead to impossibly large quantities of computation. Fortunately, strategies have been developed to overcome this difficulty, albeit that some are sub-optimal in a mathematical sense.

Also, the problem of weighting of classifying variables is seen by many antagonists of the polythetic approach as a major weakness. The choice and weighting of variables is, however, no more and no less of a problem in relationship to this method compared with any other. As Yeomans and Golder (1975) point out in a similar problem area, "When as is common in the social sciences there are many potentially dependent variables in an enquiry with little or no qualitative knowledge of the relation between these and the stratifying factors, there will be almost no way of weighting these factors' relative importance *vis-a-vis* the aims of the whole research project. With developments like the multi-purpose questionnaire of S.S.R.C. or the socio-economic area classification suggested by OPCS (Craig, 1975), one would additionally need to weight the relative importance of different research projects or even potential research projects as well as for the multiplicity of dependent variables." Thus the purpose(s) of the classification dominate the discussion and will determine the selection of variables and any

arbitrary weighting of these. As Muir *et al* (1970) succinctly put it "the arguments about the ethics of weighting become irrelevant when it is realised that infinitely more weight is given to an observed variable compared with an unobserved one." As long as the basis of any weighting is made clear to the user of a classification obtained in this way, then he may decide for himself as to its merits.

### 1.5 Purposes and Properties of Classification

That there is no single purpose in classification is shown by the increasing bibliography of classification classifications (Good, 1965; Ball, 1971). In addition to the obvious attempts to find true typologies which provide a standard of reference, various authors stress the usefulness of classification construction in data exploration, data reduction, hypothesis generation and testing and prediction. While it is true to say that any one of these objectives may be more central to a particular study, it is equally true that all are inherent in the rationale of classification construction. Without an initial hypothesis of a categorical structure within a set of entities, there is no *a priori* justification for the formation of a classification. The existence of classes of similar entities means that we may compare the characteristics of  $m$  classes rather than  $n$  individuals ( $m \ll n$ ). Through such data reduction, simplification with minimal loss of information is sought leading to a more concise and understandable account of the observations under consideration.

In developing a classification scheme, unsuspected clusterings of entities may appear, which highlights the value of the data exploration objective and may throw up further testable hypotheses which enhance the efficacy of the final operational classification.



Williams and Lance (1965) suggest that "a classification is predictive with precise purpose unknown at the time of classifying." While this may be true in certain circumstances, it is this writer's view that predictive purposes should be explicit wherever possible. Yates (1978) classified households, and particularly household shopping agents, on 16 variables ranging from social class and household composition to mobility constraints, with the specific purpose of predicting likely food shopping patterns (frequency, timing, location, expenditure). This ability to classify on one set of factors and thus successfully predict differences in other variables is clearly of the essence of classification. Without this property a classification is of limited value. Williams (1971) has attempted a formalisation of this concept of predictability by distinguishing between *extrinsic* and *intrinsic* classification. In the former, the classification of intrinsic data is arranged to predict as closely as possible the extrinsic situation. Intrinsic classifications are used to derive groups solely from known group characteristics. As in Yates' (1978) research, the groups may then be examined to determine if they reflect extrinsic discontinuities. The value of the explicit extrinsic approach was illustrated by Macnoughton-Smith (1965) in sociological analyses where it was found that "irrelevant" resemblances masked investigations of extrinsic basic causality. However, the power of the intrinsic method, which must rest on the existence of correlations between predictor (classifying) and predicted variables, is that measurements need only be made on easily observed characteristics of individuals.

The properties of a classification scheme are suggested in part from the consideration of their purpose(s). In relationship to biological classification Silvestri and Hill (1964) have stated *objectivity, stability and predictivity* to be among the more important



features of a classification. By objectivity they imply that independent workers should reach similar conclusions on class structure, which in principle rules out *a priori* methods. A classification may be said to be stable if it is little influenced by new data or if several samples from the same data material lead to the same class configuration. As such, stability should also imply robustness against errors in the data. If a classification is to remain essentially unaltered when additional individuals are observed or when extra variables are measured on the same entities, it must clearly be able in some sense to predict unobserved variables, and the variate values of new individuals.

Borko (1965) and Forgy (1965) also include *practicability* and *interpretability* as criteria for assessing the quality of a classification. It is claimed by them that a classification should be practical in that the classes isolated empirically from samples of data should reflect the structure of the whole. By this it is suggested that if an accepted standard classification exists for the mass it should be determined whether its most important classes are identified by the new classification procedure. Cormack (1971) takes exception to this view in stating that "the current swell of classificatory publications is mainly devoted to "testing" published techniques on data for which "standard" classifications exist. When the technique fails the author's response is to modify the technique instead of thinking about the "standard" classification or questioning the value of the whole process."

Perhaps interpretability, which indicates understandability and acceptability, is the most important criterion by which to judge a classification scheme. The orientation of modern classification procedures towards mathematically optimum efficiency may lead to a



classification which is meaningless when interpreted by practitioners of the discipline concerned. Additionally, the difficulty of prescribing relatively simple and intuitively plausible rules for the assignment of new individuals to classes may reduce the acceptability of a scheme to the relatively naïve user.

#### 1.6 Summary

It will be clear that there is an impressive and growing body of literature on classification methodology. That there are conflicts and areas poorly resolved is equally clear from perusal of this literature. To shed light on these issues Cormack (1971) suggests that "Two types of study seem likely to be highly informative but have been surprisingly little carried out. Firstly: studies of real data if either the variables or the entities are divided into subsets, either randomly or to a chosen pattern, and clustering performed independently on each subset. .... Secondly: studies of concocted data of known structure." Kendall (1971) reinforces the point when stating that "none of these methods is very reliable unless the situation is reproducible .... it seems to me to be desirable to split the observations into two or more groups and do any exercise on each of them and see if you get similar results from the subgroups .... This is a technique which ought to be much more employed than it has been."

It is the purpose of this thesis to attempt a partial remedy of these criticisms. To this end an examination of the performance of a polythetic classification of European Agricultural Holdings will be undertaken and compared with a proposed *a priori* typology.

In the next chapter the methods of multivariate analysis employed in such polythetic approaches are reviewed, while the specific techniques and algorithms of this study are discussed in Chapter III.

CHAPTER II

MULTIVARIATE METHODS IN CLASSIFICATION

2.1 The Origin and Development of Multivariate Analysis

Statistical multivariate analysis is at best just over 100 years old. It traces its origin to Francis Galton's work on correlation in *Heritory Genius* (1869). Galton, who in 1883 wrote that "the object of statistical science is to discover methods of condensing large groups of allied facts into brief and compendious expressions suitable for discussion", defined many of the eventual problems of multivariate statistics and outlined solutions which were later provided in detail by Pearson and Yule (multiple regression), Pearson, Edgeworth and Hotelling (principal component analysis) and Spearman, Burt and Thurstone (factor analysis). The upsurge of interest in the 1920's and 1930's in multivariate methods associated with psychological measurement was the setting for the pioneering work on discriminant analysis (Fisher, 1936; Welch, 1939), and canonical correlation (Hotelling, 1935 and 1936). Both of these were extended and generalised in the post-second world war period (Rao, 1948; Horst, 1961), while from the late 1950's the first of a growing volume of papers on clustering methods appeared.

2.2 The Data in Multivariate Analysis

The raw data used in multivariate analysis comprises  $p$  variables measured on  $n$  observations and may be represented as a matrix

$$X^* = \begin{bmatrix} X_{11} & X_{12} & \cdots & X_{1p} \\ X_{21} & X_{22} & \cdots & X_{2p} \\ \vdots & \vdots & \ddots & \vdots \\ X_{n1} & X_{n2} & \cdots & X_{np} \end{bmatrix} = \begin{bmatrix} X_{ij} \end{bmatrix}$$



The type of variable available has important consequences for many types of analysis.

Although in general one may distinguish any number of states of a qualitative or *nominal scale* variable, only the dichotomous distinction - "possession/non-possession" of an attribute - represented by a *binary* variable - is admissible in multivariate techniques. The restriction exists because there is no measure of order, spacing or distance in a manifold classificatory variable; yet many statistical methods assume and require such measurement concepts.

Fortunately, a multi-state qualitative variable can be reduced to a series of binary variables. For example, the sex of the farm-holder as reported in recent farm structure surveys is either

(a) Male

or (b) Female

or (c) Not applicable because of joint or corporate ownership.

While it would be unacceptable to represent the three states of this variable by 0 = Male, 1 = Female and 2 = N.a. or 1 = Male, 2 = Female and 3 = N.a., it is possible to construct two binary variables which are encoded as follows:

	<u>X<sub>1</sub></u>	<u>X<sub>2</sub></u>
Male Holder	1	0
Female Holder	0	1
Joint/Corporate Holder	0	0

Alternatively, some qualitative variables may have their states collapsed to form the required dichotomy. A question asking about other gainful work undertaken by the holder outside agriculture has three possible answers, i.e. Yes, No, Not Applicable. By merging the latter two categories one produces the following situation:

X

- 1 Individual Holder with other gainful work
- 0 All other cases.

This, of course, leads to a loss of information as does the reduction of a quantitative variable to a binary form. The conversion of data on the number of milking machines owned by a farm to a binary variable which indicates whether or not one or more milking machines are owned illustrates this.

Although used only once in this investigation, *ordinal* scale measurement may be incorporated into multivariate analysis, particularly when the *ranking* of a quantitative variable has taken place. Once again, a loss of information occurs but this may be justified by the consequential transformation of a non-linear monotonic to a simple monotonically increasing (decreasing) variable. Thus the number of years' agricultural education received by a farm manager may be represented by an ordinal variable taking the values 1 = None, 2 = Primary, 3 = Secondary and 4 = Higher.

Metric characteristics measured on a *ratio* scale have the highest information content because a measurement of distance and hence a standard unit of measurement is definable for them. As it is rare for such quantitative variables to have identical units of measurement, it is common to use dimensionless *standardised* or *normalised* values for analysis. Standardisation of a variable involves the subtraction of the mean and division by the standard deviation which gives a variate with zero mean and unit variance (thus a total sum of squared deviation round the mean of  $n$ ). Normalisation further transforms a variable such that the total sum of squares equals unity and is achieved by dividing the values of a standardised variable by  $\sqrt{n}$ . Such linear transformations



do not entail a loss of statistical information but can considerably and validly influence the results of techniques such as principal component analysis and cluster analysis.

It should be noticed at this point that variances and covariances of variables may be found by expressing the original variables as deviations round their means giving the matrix  $X$

$$X = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1p} \\ x_{21} & x_{22} & \dots & x_{2p} \\ \vdots & \vdots & \dots & \vdots \\ x_{n1} & x_{n2} & \dots & x_{np} \end{bmatrix} \quad \text{where } x_{ij} = X_{ij} - \bar{X}_j$$

and computing

$$V = \frac{1}{n} X'X = \begin{bmatrix} \text{Var}(X_1) & \text{Cov}(X_1 X_2) & \dots & \text{Cov}(X_1 X_p) \\ \text{Cov}(X_2 X_1) & \text{Var}(X_2) & \dots & \text{Cov}(X_2 X_p) \\ \vdots & \vdots & \dots & \vdots \\ \text{Cov}(X_p X_1) & \text{Cov}(X_p X_2) & \dots & \text{Var}(X_p) \end{bmatrix}$$

When standardised variates are used this *variance-covariance* matrix is the *correlation matrix*,  $R$ , showing the linear associations between variables, ie if

$$Z = \begin{bmatrix} z_{11} & z_{12} & \dots & z_{1p} \\ z_{21} & z_{22} & \dots & z_{2p} \\ \vdots & \vdots & \dots & \vdots \\ z_{n1} & z_{n2} & \dots & z_{np} \end{bmatrix} \quad \text{where } z_{ij} = \frac{x_{ij}}{s_j}$$

Then

$$R = \frac{1}{n} Z'Z = \begin{bmatrix} 1 & r_{12} & \dots & r_{1p} \\ r_{21} & 1 & \dots & r_{2p} \\ \vdots & \vdots & \dots & \vdots \\ r_{p1} & r_{p2} & \dots & 1 \end{bmatrix}$$

For normalised variates the simple cross-product matrix defines the correlation matrix, i.e.

$$R = Z^{*t} Z^* \text{ where } Z^* = \left[ \frac{z_{ij}}{\sqrt{n}} \right]$$

The geometric interpretation of the raw data matrix varies according to the data types employed in analysis. Every observation may be seen as a point in p-dimensional space,  $E_p$ , on whose co-ordinate axes, situated at right angles to each other, are plotted the values of the p characteristics. If all p characteristics are binary and can take only the values 0 and 1, then the space  $E_p$  is made up of the cornerpoints of a p dimensional cube with side-length 1. There are, therefore, a maximum of  $2^p$  points in the space. If all p-characteristics are ordinal or discrete quantitative, the space embraces a mass of grid points considerably in excess of  $2^p$ . Finally, if all p variables are continuous, the space may be fully occupied within the delimiting range of the variables in question.

### 2.3 Geometrical Representation of Multivariate Data

Clearly, with  $p = 2$  or  $p = 3$ , two or three dimensional representations of the data can be constructed and evaluations made by eye of the presence of correlations between variables and clusters of observation points. Once we move to 4 or more variates this invaluable standard graphical basis for the assessment of structure within the data can no longer be applied. Admittedly, the common practice of viewing the variates in subgroups of two or three is still possible but this can be misleading as Cattell and Coulter (1966) have demonstrated. What is needed is a method of obtaining a visual representation of multivariate data which may give qualitative insight into their 'structure' and indicate the most appropriate models to use for more detailed analyses.



*Ordination* techniques involve the representation of the  $n$ ,  $p$ -dimension vectors of observations in a lower space  $p^* = 2$  or  $3$ . Sammon (1969) has suggested a method which involves the minimisation of a function of differences in the distances  $d_{ij}$ , between the points in the original  $p$ -space and those in the reduced space  $p^*$ , denoted  $d^*_{ij}$ . The function

$$E = \frac{1}{\sum_{i < j} d_{ij}} \sum_{i < j} \frac{(d_{ij} - d^*_{ij})^2}{d_{ij}}$$

is minimised by the adjustment of points using a steepest descent procedure. A simpler method described by Gower (1966) is based upon an  $n \times n$  matrix of distances between the observations with respect to the variables. As with the standard principal component approach (discussed below) this procedure rests upon an extraction of latent roots and vectors. The first two or three of the principal co-ordinates may give a reasonable representation of the original distances between points so that a plot can be made and a visual search for 'structure' undertaken.

Andrews (1972) has described an alternative approach based on plotting a sin-cosin function for each  $p$ -dimension point defined as

$$f_x(t) = X_1 / \sqrt{2} + X_2 \sin(t) + X_3 \cos(t) + X_4 \sin 2(t) + X_5 \cos 2(t) + \dots$$

over a range of  $t$  from  $-\pi$  to  $+\pi$ . Because distances between points are preserved, close points will appear as curves which remain close together while distant points will be represented by curves distant from each other over at least some range of  $t$ . Examination of the plotted functions may thus show evidence of 'clusters', 'outliers' and other features of the data.

Chernoff (1973) proposes a third radically different solution to the problem based on the production of cartoon faces, one for each observation, in which the individual facial features vary with values taken by particular variables. The author argues that people are accustomed to studying and classifying facial types so that other observations expressed in terms of facial appearance should be equally classifiable.

Stress has so far been placed on the conventional representation of observation points in variable space. An alternative and complementary picture of the data is given by imagining variables plotted in observation space. Given an  $n \times p$  matrix such as  $X$  above, it is perfectly possible to focus on the columns rather than the rows of the matrix thus depicting the observation scores on each variable rather than the variable values of each observation. A *vector* constructed by joining the variable point to the origin of this  $n$ -space is a geometrical representation of the variable. The angle between two such vectors measures the correlation between the variables while the vector lengths are proportionate to the variable standard deviations. As  $p$  is usually much smaller than  $n$  it should be noticed that  $p$  variable vectors may be represented in a maximum of  $p$ -dimensions rather than the  $n$ -dimensions we start with. For example, with

$n = 3$  and  $p = 2$   
Observation  
1

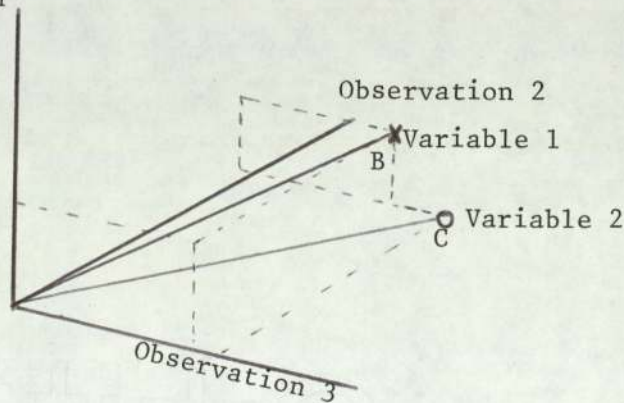
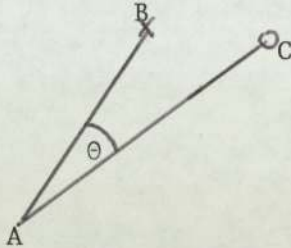


Figure 2A Vector Diagram A



Points A, B and C define a flat 2-dimensional plane so that vectors AB and AC may be shown without axes as

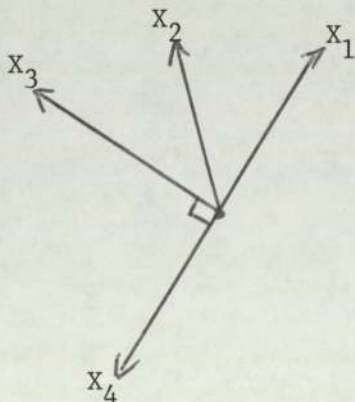


$$\text{Where } \cos(\theta) = r_{12}$$

$$\text{and } \frac{AB}{AC} = \frac{S_1}{S_2}$$

Figure 2B Vector Diagram B

Vectors close together ( $\theta \rightarrow 0^\circ$ ) show high positive correlations, those at rightangles ( $\theta = 90^\circ$ ) are *orthogonal* and have zero correlations, while obtuse angles ( $90^\circ < \theta < 180^\circ$ ) between variable vectors indicate inverse associations. (Figure 2C).



Correlation Matrix

$$R = \begin{bmatrix} 1 & 0.5 & 0 & -1 \\ 0.5 & 1 & 0.5 & -0.5 \\ 0 & 0.5 & 1 & 0 \\ -1 & -0.5 & 0 & 1 \end{bmatrix}$$

Figure 2C Vector Representation of Correlations between Variables

Vectors of standardised or normalised variables will have equal lengths and possess the additional property that projections from one to another will also define correlations, ie Fig. 2D

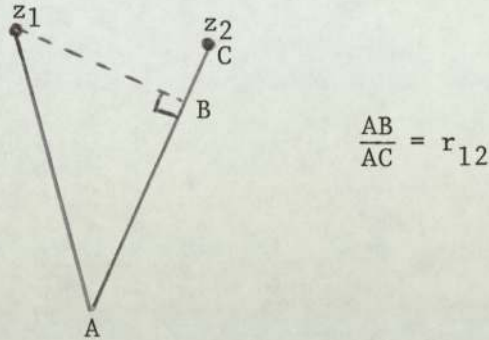


Figure 2D Vector Diagram C

It is evident that such representations of variables in vector diagram form most clearly portray the pattern of variable relationships in the data.

#### 2.4 Principal Components

It is frequently the case that  $p$ , the number of variables in a multivariate problem, is large, and in addition, that there are significant inter-correlations between the variables, so that some are substantially linear combinations of others. In this event, there will be fewer significant dimensions of difference between observation and observation than the number of variables. Therefore, to determine, for instance, a clustering of observations based on the  $p$  variates rather than  $p^* < p$  dimensions, would be both inefficient computationally and based on non-significant differences between unit and unit. Principal component analysis (PCA) has as its most distinctive characteristic the data reduction capability implied above. Given a matrix of



covariances or correlation co-efficients between a set of variables, PCA enables us to see whether some underlying pattern of relationships exists such that the data may be "re-arranged" or reduced to a smaller set of components which may be taken as source variables accounting for the observed inter-relations in the data.

The components are defined as exact mathematical transformations of the original data and are extracted in such a way that each component is independent from the others; that is, components are orthogonal. No particular assumption about the underlying structure of the variables is required, other than the exclusion of multi-state nominal scale measurement. It is only necessary to find the best linear combination of original variables - best in the sense that the specified combination would account for more of the variance in the data as a whole than any other linear combination of variables. The first (principal) component may therefore be viewed as the single best summary of linear relationships exhibited in the data. The second component, also expressed as a linear combination of variables, must be orthogonal to the first and should account for as much of the residual variance as possible after the effect of the first component is removed from the data. Subsequent components are similarly defined until all the variance in the data has been exhausted. Thus, unless there is perfect multi-collinearity in the data, the principal component solution requires as many components as there are original variables.

The transformation can be explained geometrically in two ways. The first assumes that the dispersion of observed values in the space  $E_p$  is approximately described by an ellipsoid. Representation of the data can be considerably simplified if new co-ordinate axes are determined which coincide with the principal axes of the ellipsoid. Thus in a  $p = 2$  example, two new axes are defined and may be seen as a rotation from the

original variate to principal co-ordinate axes.

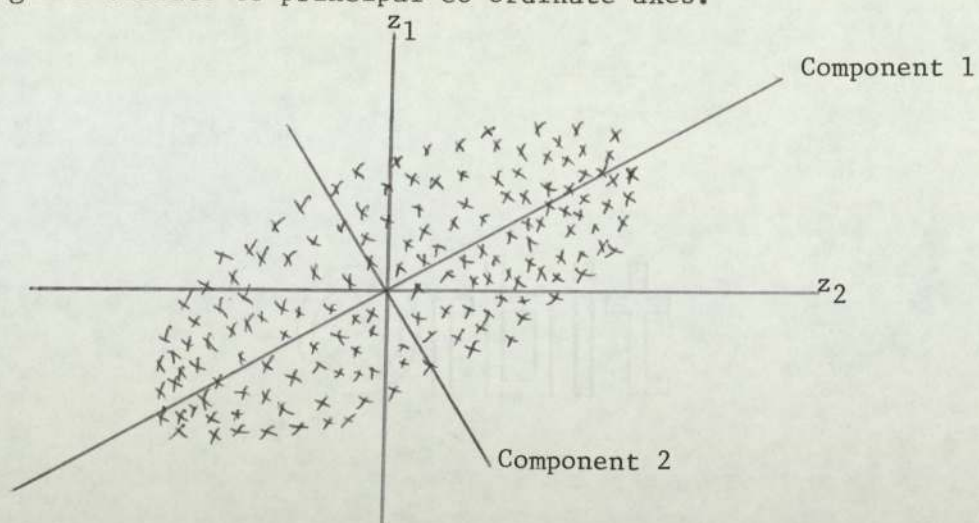


Figure 2E The geometry of principal component analysis

Alternatively, in vector form the first component is seen as a new vector having the highest possible correlation with the observed variables, while the second component is orthogonal to the first. (Figure 2F)

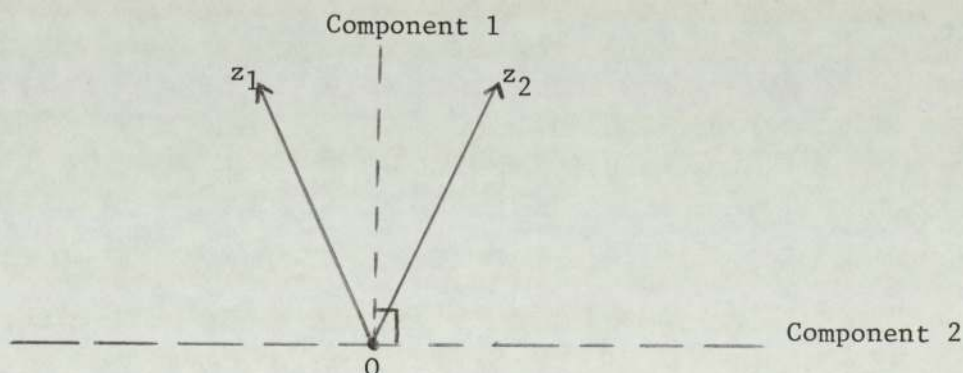


Figure 2F A vector representation of PCA

In general, the direction of the first component may be thought of as the path which would be taken by a stationary object initially at the origin in Fig. 2F, which is simultaneously pulled with equal force in the directions of each variable vector.



Thus mathematically PCA is designed to transform the matrix of observations on  $p$  observed variables in deviation or standardised form ( $X$  or  $Z$ ) into a matrix of  $p$  uncorrelated hypothetical variables,  $C$ , which decrease in variance from the first to the last. This may be achieved by post-multiplying  $X$  or  $Z$  by an orthogonal matrix of weights,  $F$  or  $G$ , columns of which are the normalised latent vectors (eigenvectors) of the  $p \times p$  variance-covariance matrix,  $V$ , or the correlation matrix,  $R$ . The  $F$  or  $G$  matrix is suitably arranged so that the first eigenvector corresponds to the largest latent root (eigenvalue) of  $V$  or  $R$ , the second vector to the second largest latent root and so on. Thus

$$C = X F \quad \text{or} \quad C = Z G$$

The latent roots of  $V$  or  $R$  may be found by solving for  $\lambda_j$  in the determinant

$$\text{or} \quad |V - \lambda_j I| = 0$$

$$|V - \lambda_j I| = 0$$

as appropriate, which in turn involves finding the roots of a polynomial of order  $p$ . Only if the  $V$  or  $R$  matrix is singular will one or more of the roots be zero. In general, there will be as many non-zero latent roots as the rank of the variance-covariance or correlation matrix.

The normalised latent vector,  $\underline{f}$ , which corresponds to one of the eigenvalues,  $\lambda$ , is used to produce a vector of component scores,  $\underline{c}$ , from

$$\underline{c} = X \underline{f}$$

$$\text{Now } \underline{c}'\underline{c} = (X \underline{f})' X \underline{f} = \underline{f}' X' X \underline{f}$$

from which 
$$\text{Var}(\underline{c}) = \frac{1}{n} \underline{c}'\underline{c} = \underline{f}'\frac{1}{n}(X'X)\underline{f} = \underline{f}'V\underline{f}$$

Denoting the Var ( $\underline{c}$ ) by  $\lambda$ , we obtain

$$\lambda = \underline{f}'V\underline{f}$$

Now the normalisation and orthogonality of

$$F \text{ in } C = XF \text{ means that } F'F = FF' = I$$

so that 
$$\underline{f}'\underline{f} = \underline{f}\underline{f}' = 1$$

Thus 
$$\lambda \underline{f}'\underline{f} = \underline{f}'V\underline{f}$$

and on the premultiplication of both sides by  $\underline{f}$  we obtain

$$\lambda \underline{f}\underline{f}'\underline{f} = \underline{f}\underline{f}'V\underline{f}$$

$$\lambda \underline{f} = V\underline{f}$$

Re-arrangement gives 
$$V\underline{f} - \lambda \underline{f} = 0$$

or 
$$(V - \lambda I)\underline{f} = 0$$

Substituting each latent root in turn into this last expression leaves us with  $p$  homogeneous equations in the  $p$  unknown elements of the  $\underline{f}$  vectors, which may be solved to give  $\underline{f}'\underline{f} = 1$  (normalisation). Such solutions will give component score vectors having variances equal to the eigenvalues corresponding to the solution.



In principle, identical steps lead from the initial use of standardised variables to

$$(R - \lambda I)g = 0$$

It should be noticed, however, that latent roots and latent vectors are not invariant under changes of scale such as that inherent in moving from variables measured in deviations round means to standardised variables. In general, different results are obtained from the use of the  $V$  and  $R$  matrices. As the fortuitous differences in the scale and thus variances of observed variates are not usually considered germane to the problem "it seems reasonable to regard the standardised variables as a better basis for judgement" (Kendall and Stuart, 1970). Nevertheless, the ultimate decision about the nature of the data to use is a non-statistical one; from the statistical viewpoint standardisation is a nuisance in that it complicates the sampling and distributional theory involved in inferences about 'significant' components.

Whether or not standardised variables are employed, it is important to realise that no information is lost in a full principal component transformation. Since  $F F' = I$ , it follows that

$$C C' = X F F' X' = X X'$$

indicating that the sum of squares for an individual is unchanged under this transformation. This is confirmed when one accepts that

$$C = X F \text{ and } X = C F'$$

While it may appear that in defining components as linear combinations of variables and variables as linear combinations of components, there is a circularity in the reasoning. This is true in the sense that the score of an observation on the full set of

components contains exactly the same information about an observation as that contained in the original variables. However, some views of the same scene are more illuminating than others and transformation of a set of data variables into components may well reveal important relationships which are difficult to discern among the variables in their original form.

One way of facilitating this understanding when dealing with standardised variables is to scale the normalised latent vectors,  $\underline{g}$ , so that the sum of squares of each is equal to the corresponding latent root,  $\lambda$ , i.e.

$$\underline{h} = \sqrt{\lambda} \cdot \underline{g}$$

The elements of the vector,  $\underline{h}$ , may be interpreted as the correlations of the observed variates with a particular component which enables the underlying dimension of this component to be better understood. These so called *factor loadings*, when squared, indicate the proportion of the total variance of an observed variable accounted for by a particular component. Contrast this with the square of an element in  $\underline{g}$  which shows the proportion of the components variance which is accounted for by a given variable. Both are clearly revealing, although examination of factor loadings enables the distinction of the factor analyst, between *common* and *unique* factors (components), to be made. When a component contains two or more variables with significant<sup>1</sup> loadings, it is described as a common factor, meaning that the component summarises and explains the information contained by such variables. A component with only one significant loading is described as unique in the sense that it is close to one variable but essentially orthogonal to all

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1 The concept of the statistical significance of eigenvalues and vectors is discussed below.



others. It is clear that such a variable contains information not reflected in remaining variables so that it will be largely uncorrelated with these. The latent root of such a unique factor can be expected to be close to unity.

Although mathematically PCA has many desirable features, in summarising data optimally, there are certain circumstances in which the substantive interpretability of results may be improved by further axis rotation, even though this will alter the relative sums of squares explained by the new factors. *Orthogonal* or *oblique* rotations may be justified in the circumstances depicted in Fig. 2G. Clockwise orthogonal rotation of axes  $C_1$  and  $C_2$  to  $A_1$  and  $A_2$  would clearly increase to near unity the loading of variables  $X_3$ ,  $X_4$  and  $X_5$  on factor  $A_1$ , while reducing the loadings of variables  $X_1$  and  $X_2$ . Similarly, the second new factor,  $A_2$ , would load highly on  $X_1$  and  $X_2$  and have low loadings on  $X_3$ ,  $X_4$  and  $X_5$ . The *varimax* method of axis rotation described by Kaiser (1958) seeks this type of clarification of the structure of variables in

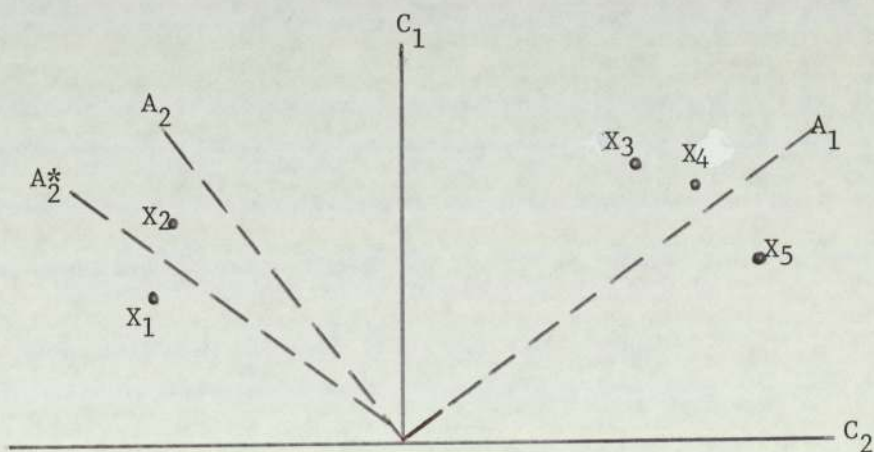


Figure 2G Possible Axis Rotation

attempting to polarise loadings between zero and unity. *Promax* rotation offers one example of a non-orthogonal or oblique approach to rotation. A rotation to  $A_1$  and  $A^*_2$  in Fig. 2G, will polarise loadings on variables even more than the varimax method, and would be justified if *a priori* grounds exist for a hypothesis of correlated source dimensions in the investigation to hand.

The problem of defining the significance of components or factor loadings has engaged writers for the past forty years.

Essentially, there are three approaches available for the investigation of the number of components which should be employed. Only common variance is required in most studies and the methods used rest on assumptions as to when this has been achieved. *Kaiser's criterion* (1961) is the simplest to define and use, which accounts for its popularity. Only components based on standardised variates and having latent roots greater than unity are considered to be of value as common factors since such components will explain more of the total variance in the data than an original observed variate. Admittedly, this is a rough-and-ready procedure for which it is difficult to advance a convincing theoretical argument. Slightly more sophisticated is Cattell's (1966) *scree test* which shows a plot of eigenvalues against component numbers. At the point where the rate of decline in the eigenvalues assumes a near linear form, one is deemed to have distinguished the *rock face* of common components from the *scree* of unique components. Craddock and Flintoff (1970) and Farmer (1971) show that the cut-off point is more clearly distinguishable if the logarithms of eigenvalues are plotted but in either case the approach often indicates a very different number of "significant" components compared with Kaiser's criterion.



Unfortunately, some of the more rigorously based methods are not particularly helpful. While it is possible to test the overall equality of the eigenvalues using the correlation determinant, the more useful specific tests for a significant cut-off number of eigenvalues are much less certain.

It may be shown that

$$-n \left\{ 1 - \frac{2p + 11}{6n} \right\} \log |R|$$

is distributed as  $\chi^2$  with  $\frac{1}{2}p(p - 1)$  degrees of freedom. A non-significant result from this test indicates that transformation to principal component scores is no better than representation of the data by the original variables; the original variables are in fact uncorrelated in the population from which the data is drawn. However, it should be pointed out that it is exceedingly rare for this test to produce non-significant results.

Kendall (1975) and Kendall and Stuart (1970) quote a number of asymptotic results concerning latent roots and vectors which were first obtained by Girshick (1939) and Anderson (1963), who proved the asymptotic normality of the distribution of these statistics. While the asymptotic standard error of the latent roots obtained from the variance-covariance matrix is relatively simple, being

$$SE(\lambda_1) = \lambda_i \left( \frac{2}{n} \right)^{\frac{1}{2}}$$

the results for a correlation matrix are much more complicated -

$$SE(\lambda_i) = \left[ \left( \frac{2}{n} \right) \lambda_i^2 + \sum_{\alpha, \beta=1}^p g_{\alpha i}^2 g_{\beta i}^2 r_{\alpha\beta}^2 - 2\lambda_i \sum g_{\alpha i}^4 \right]^{\frac{1}{2}}$$

and little used.

Bartlett (1951, 1954) has suggested alternative and somewhat heuristic tests of the distinguishability of principal components using eigenvalues. The hypothesis tested is whether the last  $p-k$  latent roots differ significantly among themselves. If the test statistic  $L$  is computed as

$$L = \frac{\left( \frac{\sum_{i=k+1}^p \lambda_i}{p-k} \right)^{p-k}}{\prod_{i=k+1}^p \lambda_i}$$

it may then be shown that

$$(n-k-1/2) \log_e L = B$$

is distributed as a  $\chi^2$  distribution with  $1/2(p-k-1)(p-k-2)$  degrees of freedom<sup>1</sup>. Once an initial test based on the correlation determinant has proved conclusive, it will be inferred that at least the first eigenvalue must differ from the rest. Then with  $k = 1$ , Bartlett's test evaluates the second eigenvalue, with  $k = 2$  the third, and so on, until no further significant result is obtained. Unfortunately, in circumstances of large  $n$  and very small final eigenvalues,

$\prod_{i=k+1}^p \lambda_i$  will be exceedingly small so that all but one or two roots

will be shown to be significant, even though close to zero. It appears that the essential difficulty in testing eigenvalues is that any non-zero value "however small is significant in the sense that it could not have arisen from a population in which the corresponding parent value is zero" (Kendall, 1975).

The asymptotic variance of the co-efficients of a latent vector, also derived by Girshick (*op cit*), is

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<sup>1</sup> Modifications to improve the  $\chi^2$  approximation are given in Lawley and Maxwell (1963).



$$\text{Var } (g_{jk}) = \frac{1}{n} \sum_{s \neq k=1}^p \frac{\lambda_k \lambda_s g_{js}^2}{(\lambda_k - \lambda_s)^2}$$

but once again this result is rarely used because of its complexity. Burt and Banks (1947) have produced the most frequently employed approach to the determination of the significance of factor loadings as opposed to normalised latent vector elements. They point out that statistically significant loadings should vary with the number of variables in the analysis and should increase the higher the component number being considered to allow for the gradual intrusion of specific and error sources of unique variance. The Burt-Banks formula is

$$h_{\alpha} = r_{\alpha} \left( \sqrt{\frac{p}{p+1-j}} \right)$$

where  $h_{\alpha}$  is a significant loading at an  $\alpha$  significance level,  $r_{\alpha}$  is the  $\alpha$  significant value of a Pearson product-moment correlation co-efficient,  $p$  is as usual the number of variables, and  $j$  is the component number. It thus has the merit of allowing not only for the sample size but also for the number of variables correlated and the number of components extracted up to the one under examination.

Finally, it should be noticed that principal component analysis, together with other multivariate techniques, is particularly sensitive to 'outliers' in the data. For example, in Fig. 2H the presence of the outlier at A would cause the principal axis of the transformation to be at or near AB, whereas for the dense ellipse of points it would be at XY

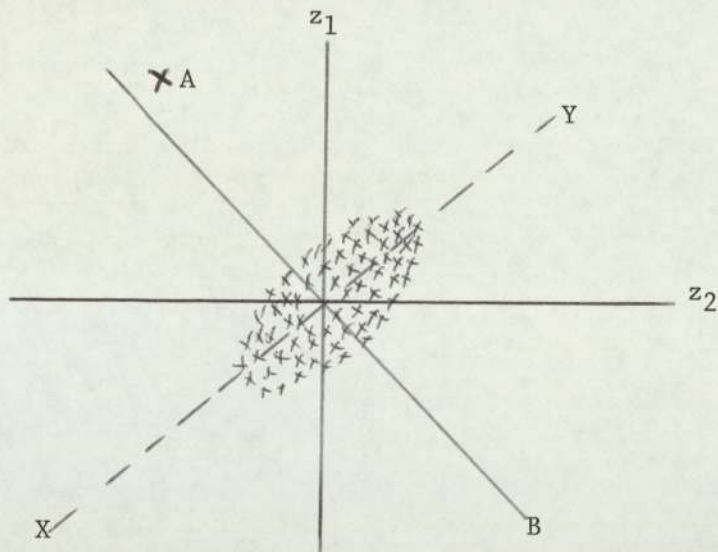


Figure 2H The Effect of Outliers

Gnanadesikin and Wilk (1969) gave an example of this problem while Anscombe (1960) and Bliss *et al* (1956) provide methods for the detection and removal of outliers in multivariate normal distributions.

## 2.5 Cluster Analysis

Principal component analysis and the related methods of factor analysis are concerned with the detection of structure within the *p-variables* of multivariate data sets. Cluster analysis methods focus on structuring the *n-observations* into *m* groups using an objective rule. This structuring should produce observation clusters in the space  $E_p$ , such that each cluster is seen as a continuous region in the space containing a relatively high density of points and separated from other dense regions by subspaces which are sparsely populated.

In the absence of prior knowledge about either the number of groups involved or their composition, the appealing solution is to enumerate all the possible arrangements of observations and choose the best one in 'some sense'. Unfortunately, this approach requires



$$\sum_{m=1}^n \left[ \frac{1}{m!} \sum_{k=0}^m (-1)^{m-k} \binom{m}{k}^n \right]$$

partitions of the data to be made. Such a sum of *Stirling* numbers of the second kind leads to over  $4 \times 10^8$  partitions with only 25 observations and is clearly impractical even with modern computing power.

Thus over the past 20 years much attention has been given to the development of cluster analysis algorithms which seek an acceptable solution to the partitioning problem while considering only a small number of the full set of alternatives. The basis and properties of the extensive range of these algorithms are reviewed in detail by Sokal and Sneath (1963), Ball (1965), Cormack (1971) and Everitt (1974), and will only be examined in outline here.

Hierarchical clustering methods require a measure of the *similarity*, *association*, or *distance* between the observations to be grouped, and are based upon matrices of such measures.

For binary variables Sokal and Sneath (1963) suggest one of a number of *similarity* or *association* co-efficients such as the *simple matching co-efficient*

$$M_{k\bar{l}} = a_{k\bar{l}} / p$$

where  $a_{k\bar{l}}$  represents the number of attributes in which the observations  $k$  and  $\bar{l}$  correspond or match. The number of similarity co-efficients discussed in the literature is large because of uncertainty over how to incorporate negative matches and whether or not matched pairs should be differently weighted compared with unmatched pairs. Sokal and Sneath conclude that no hard and fast rules exist for a decision here.

An alternative and sometimes equivalent approach is to compute association measures between observations. The chi-square statistic and

measures derived from it and correlation co-efficients of various types are examples of the more popular measures used in determining the degree of correspondence between observations.

The common use of the Pearson product moment correlation does, however, pose certain problems. In contrast to the standard (R-technique) approach which determines the strength of a correlative connection between two variables, the dual (Q-technique) involved here is based on the calculation of a correlation co-efficient between each pair of observations. This necessitates the standardisation of variable values first, since different variables measured on an observation will normally have different units of measurement. The product-moment correlation calculated on the basis of  $p$  variables for the  $k$ th and  $l$ th observations is then proportional to

$$Q_{kl} = \frac{1}{p} \sum_{j=1}^p z_{kj} z_{lj} = \frac{z_k}{z_k'} \frac{z_l}{z_l'}$$

Kendall (1966) suggested the use of rank correlation co-efficients of the original variables instead of the product-moment method based on standardised characteristics, because the former are independent of monotonic transformations. Other authors also object to the product moment approach including Fleiss and Zubin (1969), Eades (1965) and Ihm (1964), who concludes that the measure does not provide a sensible classification where the distance as well as the correlation between observations is relevant. Two observations may have parallel variable profiles, giving a high correlation, but nevertheless be very distant from one another. A further problem is that the concept of the arithmetic average, implicit in the product moment formula, has little or no meaning when calculated over the disparate variable values of a single observation.



Instead of a similarity or association measure, classification may also be based on a measure of dissimilarity of observations. The unweighted Euclidean distance, or more precisely the square of this distance, is the most widely known of a range of *metrics*, and is defined for standardised variates as

$$D_{kl}^2 = \sum_{j=1}^p (z_{kj} - z_{lj})^2 = (\underline{z}_k - \underline{z}_l)(\underline{z}_k - \underline{z}_l)'$$

for the  $k$ th and  $l$ th observations. The measure corresponds geometrically to the quadratic distance between points  $\underline{x}_k$  and  $\underline{x}_l$  in the  $p$ -dimensional Euclidean space,  $E_p$ . The Euclidean metric has a long history and was suggested by Pearson (1925) in his *co-efficient of racial likeness* which is proportional to  $D_{kl}^2$ .

It should be noticed that the similarity measures  $M_{kl}$  and  $Q_{kl}$  may be converted to Euclidean distances using the following relationships due to Gower (1966)

$$D_{kl}^2 = Q_{kk} + Q_{ll} - 2Q_{kl}$$

$$D_{kl}^2 = p(1 - M_{kl})$$

which confirms the validity of incorporating binary and ordinal variables in Euclidean-type clustering procedures.

The Euclidean distance has the great advantage of being easy to calculate. However, as early as 1936, R A Fisher pointed out that the measure has one main disadvantage. It reflects strongly correlated variables with the same weight as variables having weak correlations, so that the strongly correlated characteristics indirectly receive too great a weight. This disadvantage is avoided if the *generalised* distance suggested by Mahalanobis (1936) is applied instead, where

$$D_{k\ell}^{*2} = (\underline{z}_k - \underline{z}_\ell)' R^{-1} (\underline{z}_k - \underline{z}_\ell)$$

and  $R^{-1}$  is the inverse of the correlation matrix. If all observed variables are uncorrelated by pairs, the generalised distance becomes the unweighted Euclidean distance since  $R$  and  $R^{-1}$  will be unit or identity matrices. Otherwise, the values of individual variables are inversely weighted according to their correlations with other variables.

A direct application of the generalised distance for clustering is not practical since this requires a great deal of computation. However, it is possible to bring the theoretical advantages of this measure in line with the simple calculability of the Euclidean distance by virtue of a principal component transformation of the original data. The variable values for the  $i$ th observation are first converted to component scores

$$\underline{c}_i = \underline{z}_i G$$

and the results standardised. This involves dividing each variable element in  $\underline{c}_i$  by the square root of the eigenvalue appropriate to that variable, ie

$$\underline{b}_i = \underline{c}_i \underline{\Lambda}^{-\frac{1}{2}} = \underline{z}_i G \underline{\Lambda}^{-\frac{1}{2}} \quad \text{where} \quad \underline{\Lambda}^{-\frac{1}{2}} = \begin{bmatrix} \frac{1}{\sqrt{\lambda_1}} & 0 & \dots & 0 \\ 0 & \frac{1}{\sqrt{\lambda_2}} & \dots & 0 \\ 0 & 0 & \dots & \frac{1}{\sqrt{\lambda_p}} \end{bmatrix}$$

Now the Euclidean distance for the  $k$ th and  $\ell$ th observation with respect to the standardised component scores,  $\underline{b}_i$ , is



$$\begin{aligned}
 & (\underline{b}_k - \underline{b}_l)(\underline{b}_k - \underline{b}_l)' \\
 = & (\underline{z}_k \underline{G} \underline{\Lambda}^{-\frac{1}{2}} - \underline{z}_l \underline{G} \underline{\Lambda}^{-\frac{1}{2}})(\underline{z}_k \underline{G} \underline{\Lambda}^{-\frac{1}{2}} - \underline{z}_l \underline{G} \underline{\Lambda}^{-\frac{1}{2}})' \\
 = & (\underline{z}_k - \underline{z}_l) \underline{G} \underline{\Lambda}^{-\frac{1}{2}} (\underline{z}_k - \underline{z}_l) \underline{G} \underline{\Lambda}^{-\frac{1}{2}}' \\
 = & (\underline{z}_k - \underline{z}_l) \underline{G} \underline{\Lambda}^{-\frac{1}{2}} \underline{\Lambda}^{-\frac{1}{2}} \underline{G}' (\underline{z}_k - \underline{z}_l)'
 \end{aligned}$$

Remembering that

$$(\underline{R} - \lambda \underline{I}) \underline{g} = 0 \quad \text{or} \quad \underline{R} \underline{g} = \lambda \underline{g}$$

and the generalisation

$$\underline{R} \underline{G} = \underline{G} \underline{\Lambda}$$

we may obtain, on premultiplication of both sides by  $\underline{G}'$  and inversion

$$(\underline{G}' \underline{R} \underline{G})^{-1} = \underline{\Lambda}^{-1} \quad \text{since} \quad \underline{G}' \underline{G} = \underline{I}$$

Thus  $\underline{G}' \underline{R}^{-1} \underline{G} = \underline{\Lambda}^{-1}$

and  $\underline{R}^{-1} = \underline{G} \underline{\Lambda}^{-1} \underline{G}'$  on premultiplication

by  $\underline{G}$  and postmultiplication by  $\underline{G}'$

Now  $\underline{G} \underline{\Lambda}^{-\frac{1}{2}} \underline{\Lambda}^{-\frac{1}{2}} \underline{G}' = \underline{G} \underline{\Lambda}^{-1} \underline{G}' = \underline{R}^{-1}$

Therefore the Euclidean distance between observations  $k$  and  $l$  for standardised component scores, equals

$$(\underline{z}_k - \underline{z}_l) \underline{R}^{-1} (\underline{z}_k - \underline{z}_l)'$$

which is the generalised distance between the observations on the original variables.

Whichever measures of similarity, association or distance are employed in practice, the hierarchical approach to clustering is essentially the same. With *agglomerative* methods there are initially  $n$  clusters with one observation in each. A search of the similarity matrix is made for the most similar part of clusters, which are merged. The similarity matrix is updated and reduced in size by one row and one column. The procedure is repeated  $n-1$  times until there is one cluster of  $n$  observations. Different agglomerative procedures, such as *nearest neighbour* (single linkage), *furthest neighbour* (complete linkage), and *group average method*, are employed by varying the approach used for defining the most similar pairs and for updating the revised similarity matrix. Ward's (1963) proposal is worthy of note in that his merger rule is based on the total sum of squared deviations of every point in a cluster from the *centroid* of the cluster. At each step in the analysis the union of every possible pairs of clusters is considered and the two clusters whose fusion results in the minimum increase in the sum of within cluster sums of squares are combined.

Polythetic divisive methods of hierarchical clustering are less numerous and in some cases quite impractical for even moderately sized data sets (Edwards and Cavalli-Sforza, 1965). McNaughton-Smith's (1964) *splinter* group method offers one possibility. A splinter group is formed by sequential additions of the observation whose total dissimilarity with the remainder less its total dissimilarity with the splinter group is at a maximum. Once the splinter group is complete the procedure is repeated on the two clusters and so on, until the data are divided into  $n$  clusters of one. A second approach is based on discriminant analysis (discussed below). The essential idea is to begin with an initial partition, compute a linear discriminant function,



and then iteratively re-assign points, recomputing discriminant functions at each round so as to find the most strongly separable groups. Cassetti (1964) and Hung and Dubes (1970) both provide programmes for this method.

*Optimisation-partition* methods offer the main alternative to hierarchical clustering. All require the optimisation of a cluster criterion, based on the generalised analysis of variance, through an iterative procedure which allows the re-allocation of observations. Thus poor initial partitions may be corrected at a later stage, a feature which none of the hierarchical methods possess.

In the univariate case ( $p = 1$ ) it may be shown that

$$\sum_{k=1}^m \sum_{i=1}^n (X_{ik} - \bar{X})^2 = \sum_{k=1}^m n_k (\bar{X}_k - \bar{X})^2 + \sum_{k=1}^m \sum_{i=1}^k (X_{ik} - \bar{X}_k)^2$$

$$\text{or } T = B + W$$

where there are  $m$  groups of observations of size  $n_k$  ( $k=1, m$ ). The mean of the  $k$ th group is  $\bar{X}_k$  and the overall mean is  $\bar{X} = \frac{\sum n_k \bar{X}_k}{n}$

since  $\sum_{k=1}^m n_k = n$ . Thus the total sum of squares ( $T$ ) may be decomposed into between group ( $B$ ) and within group ( $W$ ) components. The generalisation of this result to  $p > 1$  variables is much more succinctly portrayed in matrix form as

$$T = W + B$$

$$\text{where } T = \sum_{i=1}^n (X_i - \bar{X})(X_i - \bar{X})'$$

$$B = \sum_{j=1}^m n_k (\bar{X}_k - \bar{X})(\bar{X}_k - \bar{X})'$$

$$W = \sum_{k=1}^m \sum_{i=1}^{n_k} (X_i - \bar{X}_k)(X_i - \bar{X}_k)'$$

where  $\tilde{X}_i$  is a row vector of  $p$ - variable values for the  $i$ th observation

$\tilde{X}$  is a row vector of overall means of the  $p$  variables

$\tilde{X}_k$  is a row vector of means of the  $p$  variables in the  $k$ th group.

With  $p = 1$  a cluster criterion might be the minimisation of  $W$  or the maximisation of  $T/W$ . With  $p > 1$  such criteria can no longer be quoted directly since  $T$  and  $B$  are matrices, while a scalar is needed as a measure of the quality of a given partitioning. Several possibilities for the reduction of a matrix to a scalar have been suggested. One may seek to minimise the trace of  $W$  (the trace is the sum of the diagonal elements of  $W$ ). It is easy to calculate  $\text{tr}(W)$  but the measure does have the disadvantages of depending on the scale of the variables and disregarding the correlations between them.

These disadvantages can be avoided if the relationship of the determinants

$$\frac{|T|}{|W|} = |\mathbf{I} - W^{-1} B| = \prod_{j=1}^p (1 - \lambda_j)$$

$$\text{or } \text{tr}(W^{-1} B) = \sum_{j=1}^p \lambda_j \quad \text{where } \lambda_j \text{ is the eigenvalue of the appropriate matrix}$$

is used instead. Both require a greater amount of calculation. They are, however, invariant under non-singular linear transformation of the original values and as such are independent of the scale of the variables and take into consideration inter-correlations.

A measure known as Wilks lambda

$$\lambda = |W|/|T| = \prod_{j=1}^p \frac{1}{1 + \lambda_j}$$

has also been employed as a cluster criterion. It was originally developed by Wilks (1932) for testing the hypothesis that  $m$  normally



distributed groups with equal variance-covariance matrices have equal mean vectors. Used as a clustering criterion, it does depend on the fulfilment of the distribution requirements and suffers, as do all these measures, from the deficiency that their values are not directly comparable for different numbers of classes. While  $|T|$  is constant  $|W|$  and  $|B|$  change with the number of partitions of the data.

Whichever clustering criterion is employed, there are three outstanding issues to be resolved before clustering commences

- (a) How are clusters initiated?
- (b) How should observations be allocated to initiated clusters?
- (c) How many clusters should there be?

Most techniques begin by finding  $m$  points in the  $p$ -dimensional space which act as initial estimates of cluster centres. These are termed *crystallising kernels*. These  $m$  points are chosen as the first  $m$  in the data set (MacQueen, 1967), regularly spaced (Beale, 1969), mutually furthest apart (Thorndike, 1953; Kennard and Stone, 1969), suitably chosen after inspection of the data (Ball and Hall, 1967; Nagy, 1969), or determined *a priori* (Jancey, 1966). Whichever method is used, the remaining observations are allocated to the cluster to which they are nearest (usually in a Euclidean sense), with updates of the cluster centroids after each point has been allocated (eg MacQueen, 1967) or only after all points have been allocated (Ball and Hall, 1967).

Golder and Yeomans (1973) combined steps (a) and (b) by ordering the first component scores for the observations and dividing these into  $m$  equal groups.

Once an initial classification has been determined, an iterative search is made for observations which should be further allocated to other groups in order to optimise the cluster criterion employed. MacQueen (1967) and Ball and Hall (1967), by slightly different mechanisms, allow  $m$  to change by enforcing the splitting of a cluster with large within cluster sums of squares or by fusing two clusters with small between cluster sums of squares according to two parameters of coarsening or refinement set by the user.

Beale (1969) also suggests starting with a larger value of  $m$  than the user anticipates being appropriate. After the optimisation of the cluster criterion with  $m$  clusters has been achieved,  $m-1$  clusters are constructed by merging two of the  $m$  clusters already formed which, when combined, produce the least increase in the pooled within group variance. The iterative re-allocation of observations is then repeated on the  $m-1$  clusters. Clearly, this cycle may be repeated  $m-1$  times until only one cluster remains.

Beale (1969) has suggested a test which is analogous with, but not equivalent to, an analysis of variance for determining the "best" group of clusters so formed.

It involves the computation of an F ratio

$$F(m_1 m_2) = \frac{R_{m_1} - R_{m_2}}{R_{m_2}} / \left\{ \frac{n - m_1}{n - m_2} \left( \frac{m_2}{m_1} \right)^{2/p} - 1 \right\}$$

with  $p(m_2 - m_1)$  and  $p(n - m_2)$  degrees of freedom.

$R_m$  is the pooled within group sum of squares obtained when a group of  $m$  clusters has been formed (ie  $\text{tr}|W|$ ). If the test is significant for any  $m_2$ , then representation of the data in terms of  $m_1$  clusters ( $m_1 < m_2$ ) is not entirely adequate. Beale suggests computing the statistic for



all  $m_1 < m_2 < m_{\max}$ , but admits that in practice the significance level does not usually depend much on  $m_2$  for  $m_2 > (m_1 + 2)$ . It should be stressed that this is a highly heuristic criterion and should not be applied mechanically. It does, however, give a guideline on when to stop the clustering process.

Beale's test shows strong similarities with a procedure for determining an adequate number of clusters suggested by Thorndike (1953). In a manner not unlike Cattell's scree test, Thorndike proposed that a plot of  $\text{tr}|W|$  against the number of clusters, should reveal a point at which further increase in the number of clusters brings no further significant reduction in dispersion. Alternatives to this are given by Friedman and Rubin (1967), and Ihm (1965), who implies that the number of classes must equate with the number,  $p^*$ , of significant latent roots of the overall correlation matrix, since with only  $p^*$  significant dimensions of difference between observation, there can only be  $p^*$  classes within the data.

All of the methods of clustering are open to criticism. For instance, hierarchical approaches have as their most serious limitation the inability to re-allocate observations which may have been poorly classified at an earlier stage in the analysis. The major problem of optimisation techniques is that sub-optimal solutions are sometimes found because there may be numerous local optima present as well as the true global optimum. Additionally, if the cluster criterion is of a Euclidean type, the clusters are assumed to be either spherical, or if not spherical of the same shape. Thus the choice of optimisation criterion can be problematic in the absence of *a priori* knowledge of the anticipated cluster configuration. Finally, optimisation of a cluster criterion tends to require large amounts of computer time which prohibits their use with very large data sets.

Ultimately, the applied numerical taxonomist, when faced with the very large number of approaches available to him, both in principle<sup>1</sup> and detail, will be forced to take a relatively arbitrary decision about the "tool" to use. Certainly the main assumptions of the different methods should be examined and matched to the problem in hand. Equally, once clusters have been formed, the intuitive reasonableness of these should be critically examined.

Kendall (1971) comes down very firmly in favour of the simplest optimisation technique, rather than hierarchical methods or methods which seek maximisation of  $|T|/|W|$  or  $\text{tr}|W^{-1}B|$ . "But when we come to cluster a large number of individuals, the number of pairs of distances between them goes up rapidly as the square of the number of individuals and in that context I would like to put in a strong plea for the use of the ordinary Euclidean metric, for two reasons. First of all, the Euclidean distance is invariant under orthogonal rotation of axes. Hence you can proceed to principal components and reduce the effective dimension number very substantially if you are prepared to sacrifice the lower eigenvalues of the matrix. .... the second advantage is that the average of the squared distance among a set of  $n$  points is simply equal to the average squared distance from the centre of gravity, so that instead of having computations of the order of  $\frac{1}{2}n(n - 1)$  you have two computations of the order  $n$ . Taking these two things into consideration you can, on occasion, reduce the computation involved by something of the order of 100. I should want a lot of persuasion, I think, to

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<sup>1</sup> Clumping and density-seeking techniques are discussed in Everitt (1974) but were not considered relevant to this research as the overlapping clusters of the former were not admissible and the assumption of multi-variate normality in the latter was considered suspect.



use other methods. There is an additional advantage that you get rid of collinearities among the variables. There are strong arguments for computational simplicity in practical work ... a number of methods proposed are quite hopeless to apply to more than a comparatively small number of observations."

## 2.6 Discriminant Analysis

Given the high computer time requirement for most polythetic data based classification procedures, it is inevitable that, when faced with large national or international data sets, with observations running into hundreds of thousands or even millions, the cluster analysis will have to be based on samples of this data. In order to classify the remainder of the population or to classify new observations (eg new companies, new families, new farms), classification or assignment rules must be determined. As has been suggested above, these rules will not be simple ones in the case of polythetic methods but may be built up employing various methods of discriminant analysis.

The broad methodology of assignment may be illustrated with reference to two groups. Let the two groups be designated  $G_1$  or  $G_2$ . An observation has measurements on  $p$  discriminating variables,  $X_1, X_2 \dots X_p$  and is to be assigned to  $G_1$  or  $G_2$  using this information. From *Bayes Law* it may be shown

$$P(G_1/\tilde{X}) = \frac{P(\tilde{X}/G_1) \times P(G_1)}{P(\tilde{X}/G_1) \times P(G_1) + P(\tilde{X}/G_2) \times P(G_2)}$$

where  $P(G_1/\tilde{X})$  is the probability that an observation with a variable vector  $\tilde{X}^1$  is a member of Group 1. This *posterior* probability is

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1 For consistency with earlier data representation  $\tilde{X}$  is a row vector.

computed from the *likelihoods*,  $P(\underline{X}/G_1)$  and  $P(\underline{X}/G_2)$  and the *prior* probabilities  $P(G_1)$  and  $P(G_2)$ . The likelihoods show the probability of an observation with the set of variable values in question arising from a particular group while the priors represent facts known about the groups outside the measured variables, which permits the formulation of hypothesised probabilities of group membership for a random observation.

An assignment rule may now be developed. If  $P(G_1/\underline{X})$  is greater than  $P(G_2/\underline{X})$  assign the observation with the vector of variable values,  $\underline{X}$ , to Group 1, and conversely to Group 2 if  $P(G_2/\underline{X}) > P(G_1/\underline{X})$ .

In this two group case the rule could be stated as, "Assign to Group 1 if  $P(G_1/\underline{X}) > \frac{1}{2}$ " since  $P(G_1/\underline{X}) + P(G_2/\underline{X}) = 1$ . An observation must be assigned to one of the two groups even though  $P(\underline{X}/G_1)$  or  $P(\underline{X}/G_2)$  or both may be very small, indicating that the observation bears little resemblance to these two populations and may be a member of a third which has not been explicitly considered.

A second alternative rule is to assign the observation to Group 1 if

$$\frac{P(G_1/\underline{X})}{P(G_2/\underline{X})} > 1$$

otherwise to Group 2.

From Bayes Law

$$\frac{P(G_1/\underline{X})}{P(G_2/\underline{X})} = \frac{P(\underline{X}/G_1) \times P(G_1)}{P(\underline{X}/G_2) \times P(G_2)}$$

when the common denominators of the two basic probability equations are cancelled.



Given the assumption that the variables in the two groups have multivariate normal distributions then  $P(\underline{X}/G_1)$  is proportionate to the density at the points,  $\underline{X}$ , given by

$$\frac{1}{(2\pi)^{p/2} |\Sigma_1|^{-1/2}} e^{-\frac{1}{2}(\underline{X}-\eta_1)\Sigma_1^{-1}(\underline{X}-\eta_1)'}$$

therefore

$$\frac{P(G_1/\underline{X})}{P(G_2/\underline{X})} = \left( \frac{|\Sigma_1|}{|\Sigma_2|} \right)^{-1/2} \cdot \frac{e^{-\frac{1}{2}(\underline{X}-\eta_1)\Sigma_1^{-1}(\underline{X}-\eta_1)'}}{e^{-\frac{1}{2}(\underline{X}-\eta_2)\Sigma_2^{-1}(\underline{X}-\eta_2)'}} \cdot \frac{P(G_1)}{P(G_2)}$$

after the cancellation of  $\frac{1}{(2\pi)^{p/2}}$ , where  $\Sigma_1$ ,  $\Sigma_2$ ,  $\eta_1$  and  $\eta_2$  are

population variance-covariance matrices and vectors of means for the two groups.

Now the assignment rule

$$\frac{P(G_1/\underline{X})}{P(G_2/\underline{X})} > 1 \text{ is equivalent to } \log_e \left[ \frac{P(G_1/\underline{X})}{P(G_2/\underline{X})} \right] > 0$$

since  $\log_e(1) = 0$ , so that taking natural logarithms, cancelling and rearranging gives

$$\log_e \left[ \frac{P(G_1/\underline{X})}{P(G_2/\underline{X})} \right] = -\frac{1}{2} \left[ (\underline{X}-\eta_1)\Sigma_1^{-1}(\underline{X}-\eta_1)' - (\underline{X}-\eta_2)\Sigma_2^{-1}(\underline{X}-\eta_2)' \right] - \frac{1}{2} \log_e \left[ \frac{|\Sigma_1|}{|\Sigma_2|} \right] + \log_e \left[ \frac{P(G_1)}{P(G_2)} \right]$$

In practice the population variance/covariance matrices and the vectors of true means will be unknown so that the sample estimators,  $V^*$  and  $\bar{X}_j$  are used instead, where

$$V^* = W/n-m \quad (n = \text{total observations} \\ m = \text{number of groups})$$

If, as is common, equal group dispersion matrices are assumed, considerable simplification results. Now

$$\log_e \left[ \frac{P(G_1/\bar{X})}{P(G_2/\bar{X})} \right] = \bar{X} \Sigma^{-1} (\eta_1 - \eta_2)' - \frac{1}{2} (\eta_1 + \eta_2) \Sigma^{-1} (\eta_1 - \eta_2)' + \log_e \left[ \frac{P(G_1)}{P(G_2)} \right]$$

$$\begin{aligned} \text{since } (\bar{X}_{\eta_1}) \Sigma^{-1} (\bar{X}_{\eta_1})' &= (\bar{X}_{\eta_2}) \Sigma^{-1} (\bar{X}_{\eta_2})' \\ &= \bar{X} \Sigma^{-1} (\bar{X}_{\eta_1})' - \eta_1 \Sigma^{-1} (\bar{X}_{\eta_1})' - \bar{X} \Sigma^{-1} (\bar{X}_{\eta_2})' + \eta_2 \Sigma^{-1} (\bar{X}_{\eta_2})' \\ &= \bar{X} \Sigma^{-1} \bar{X}' - \bar{X} \Sigma^{-1} \eta_1' - \eta_1 \Sigma^{-1} \bar{X}' + \eta_2 \Sigma^{-1} \eta_1' \\ &\quad - \bar{X} \Sigma^{-1} \bar{X}' + \bar{X} \Sigma \eta_2' + \eta_2 \Sigma^{-1} \bar{X}' + \eta_2 \Sigma^{-1} \eta_2' \end{aligned}$$

Eliminating the first and fifth terms and noting that

$$\eta_1 \Sigma^{-1} \bar{X}' = \bar{X} \Sigma^{-1} \eta_1' \quad \text{this reduced to}$$

$$-2 \bar{X} \Sigma^{-1} (\eta_1 - \eta_2)' + \eta_1 \Sigma^{-1} \eta_1' - \eta_2 \Sigma^{-1} \eta_2'$$

If  $\eta_2$  is added to the last two terms and  $\eta_2'$  subtracted, we obtain

$$-2 \bar{X} \Sigma^{-1} (\eta_1 - \eta_2)' + (\eta_1 + \eta_2) \Sigma^{-1} (\eta_1 - \eta_2)'$$

Finally multiplication by  $-\frac{1}{2}$  gives the main part of the result above.



As an alternative to asking whether the natural logarithm of the probability ratio, given by its right hand side, is greater than zero, we may test whether

$$\bar{X}_{\Sigma}^{-1} (\eta_1 - \eta_2)' + \log_e \left[ \frac{P(G_1)}{P(G_2)} \right] > \frac{1}{2} (\eta_1 + \eta_2) \Sigma^{-1} (\eta_1 - \eta_2)'$$

where  $\Sigma^{-1} (\eta_1 - \eta_2)'$  is the co-efficient vector for the two group discriminant function defined by Fisher (1936) in his pioneering work in this field.

The final alternative, which has been generalised to the multi-group situation by Fisher (1938), Rao (1948) and Rao and Slater (1949), is to determine whether

$$\bar{X}_{\Sigma}^{-1} \eta_1' - \frac{1}{2} \eta_1 \Sigma^{-1} \eta_1' + \log_e P(G_1) >$$

$$\bar{X}_{\Sigma}^{-1} \eta_2' - \frac{1}{2} \eta_2 \Sigma^{-1} \eta_2' + \log_e P(G_2)$$

in which case the observation is assigned to Group 1.

In general, one has as many *classification functions* of the form

$$s_g = \bar{X} \bar{w}_g - c_g$$

$$\text{where } \bar{w}_g = \Sigma^{-1} \eta_g'$$

$$\text{and } c_g = \frac{1}{2} \eta_g \Sigma^{-1} \eta_g' + \log_e P(G_g)$$

as there are groups. The value of  $s_g$  is computed for each function and the group producing the highest score is the one to which the observation is assigned. The probability of group membership may then be obtained from

$$P(G_g / \underline{X}) = \frac{e^{-\frac{1}{2}(\underline{X} - \eta_g) \Sigma^{-1} (\underline{X} - \eta_g)} \times P(G_g)}{\sum_{j=1}^m e^{-\frac{1}{2}(\underline{X} - \eta_j) \Sigma^{-1} (\underline{X} - \eta_j)} \times P(G_j)} \quad j=1, 2 \dots g \dots m$$

from which  $P(\underline{X}/G_g)$  for the maximum  $P(G_g/\underline{X})$  may be extracted.

A number of issues are raised by the assignment rules defined above. Although the use of unequal prior probabilities appears justified when, for instance, it is known that the sizes of the group populations are very different, it may sometimes be undesirable to follow this course. Suppose that the information contained in the likelihood is very limited; that is to say, the vector of variable values has little predictive power in terms of indicating group membership. A set of powerful prior probabilities in these circumstances can lead to apparently successful classification of observations (on posterior probabilistic grounds) and the illusion of predictive validity. Thus, when the object of research is to display the predictive validity of the measurement system, prior probabilities may be misleading.

At a more pragmatic level, the computation of probabilities or classification scores when a large number of variables, groups and observations are involved, will involve a considerable drain on the most robust research budgets. Although one can do little about the number of groups or the number of observations to be assigned to these groups, there are two strategies which may be employed, singly or in combination, to significantly reduce the variable space dimensions of the data.

Not all hypothesised discriminating variables will possess the discriminating power originally envisaged. As a first step, one-way analysis of variance tests will show whether variables individually



have significantly different values between the groups. Inevitably, such tests are of limited value in that they cannot reveal interaction effects between apparently non-significant variables and will not indicate when two or more individually highly significant variables contain exactly the same discriminating information in relationship to group membership. A step-wise multivariate analysis of variance (MANOVA) is clearly the answer to such problems, although like its univariate counterpart it is subject to the restrictive assumptions of normality in the distributions, homoscedastic dispersion matrices and random sampling from the populations under study. Nevertheless, in providing guidelines about the most useful variables for successful discrimination between groups, stepwise MANOVA can frequently reduce the original variable set by up to fifty per cent.

The process begins by choosing that variable which singly has the highest value of the multivariate F ratio in tests of the differences among group centroids. This initial variable is then paired with each of the other potential discriminating variables one at a time and the multivariate F ratios are computed. The new variable, which in conjunction with the initial variable produces the best F value, is chosen as the second best discriminator. The procedure is then repeated until all variables are selected or no new variable produces a partial multivariate F ratio which is significant at a user specified level. It should be pointed out that not all possible variable subsets are considered using this stepwise procedure, so that the results are not fully optimal. Nevertheless, it is an efficient way of approximately locating the best set of discriminating variables.

Of even more importance from a theoretical standpoint is the possibility of reducing the p-variable test space to a  $m - 1$  discriminant

function space ( $p \gg m - 1$ ). Discriminant functions, like the classification functions, are weighted linear combinations of the  $p$ -discriminating variables but constructed so that the groups are forced to be as statistically distinct as possible with observations in groups occupying different positions on the orthogonal dimension(s) defined by the linear equation(s) formed.

The maximum number of functions which may be derived is either one less than the number of groups or equal to the number of discriminating variables, if there are more groups than variables. It should be stressed that where there are more than two groups it may be possible to obtain satisfactory discrimination with fewer than the maximum number of functions. While as a general rule in geometry we may say that  $k$  points define  $(k-1)$  dimensions, there are the degenerate cases of, for example, three points lying on the same line. The last point is situated such that it does not add a new dimension and merely falls into a space defined by the other points. The identical principle applies to discriminant analysis where the centroids (when  $X_{i1} = \bar{X}_1$ ,  $X_{i2} = \bar{X}_2$ ,  $X_{i3} = \bar{X}_3$ , etc) of the groups are treated as points and each discriminant function is a unique (orthogonal) dimension describing the location of that group relative to the others. Thus three groups may be quite adequately described by one function if the centroids of those groups lie in the main along the same dimensions,  $D_1$  (See Figure 2.I). Admittedly this one function would not pick up all of the information in the discriminating variables. However, the second potential function  $D_2$  would probably be deemed to be non-statistically significant. It would be ignored on the grounds that its presence merely resulted from sampling and measurement error and that it did not actually exist as a separate dimension in the population.



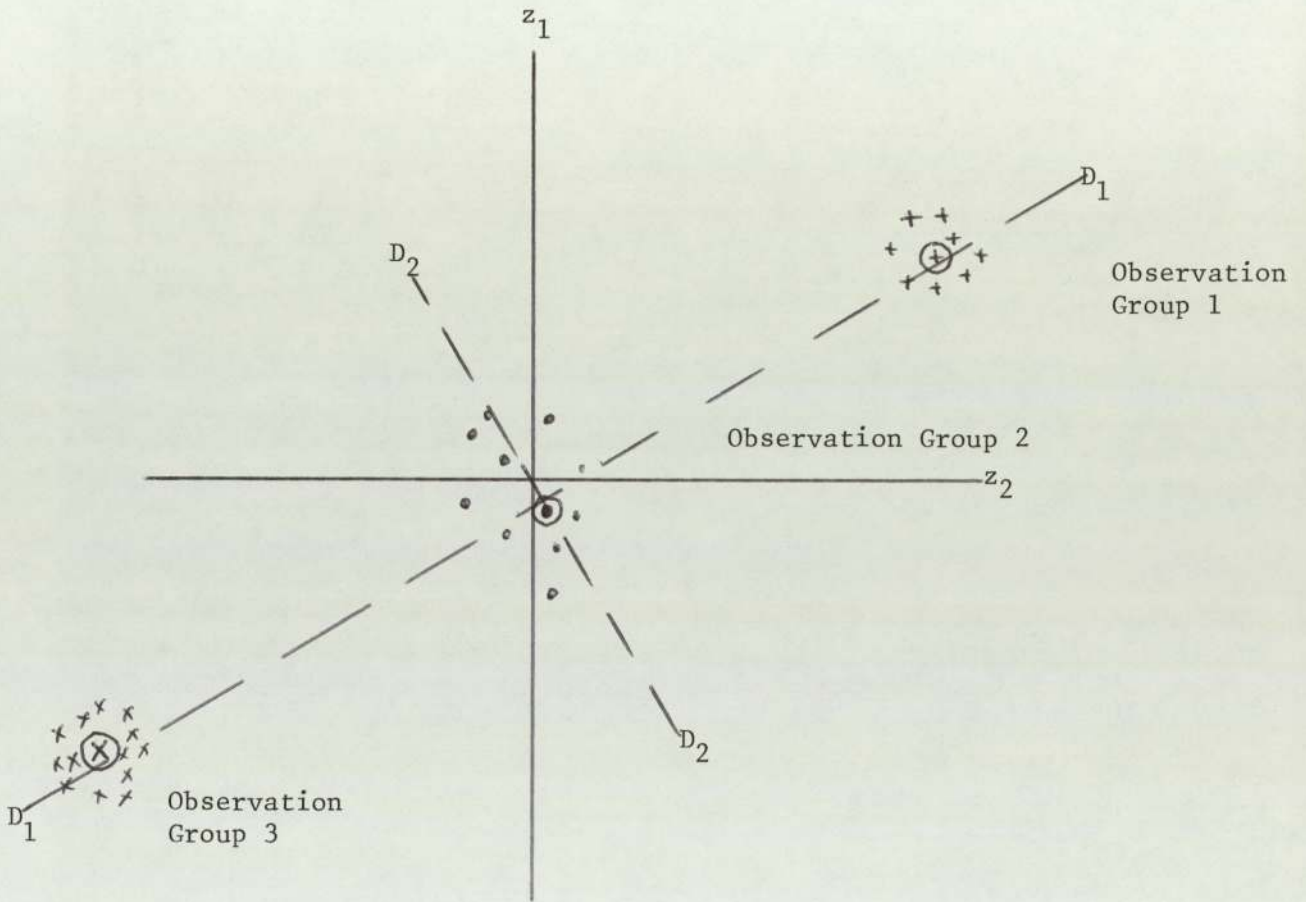


Figure 2 I

*The Principle of Discriminant Analysis*

A discriminant function is of the form

$$D_{gi} = v_{g1}x_{i1} + v_{g2}x_{i2} + v_{g3}x_{i3} + \dots + v_{gp}x_{ip}$$

where  $D_g$  is the discriminant function score for the  $i$ th observation on the  $g$ th function,  $v_{g1} \dots v_{gp}$  are weights and  $x_{ij}$  is as usual the deviation of the  $i$ th individual's value round the mean of the  $j$ th variable.

In matrix terms the scores for all individuals are given by the vector  $\underline{d}$

$$\underline{d} = X\underline{v}$$

where  $X$  is an  $n \times p$  matrix of variate values and  $\underline{v}$  is a column vector of weights. Consider  $n$  observations divided among  $m$  groups. With respect to the original variables the pooled within group deviation cross product matrix and between group deviation cross product matrix are as usual designated  $W$  and  $B$ . The sum of squares between and within groups for the discriminant score vector,  $\underline{d}$ , are respectively

$$\underline{v}' B \underline{v} \text{ and } \underline{v}' W \underline{v}$$

Now

$$\lambda = \underline{v}' B \underline{v} / \underline{v}' W \underline{v}$$

if multiplied by  $(n-m)/(m-1)$  is an  $F$  ratio for a one-way analysis of variance for the discriminant scores,  $\underline{d}$ , in the  $m$  groups. Thus if  $\underline{v}$  is such that  $\lambda$  is at a maximum, then the differences between the group means, with respect of the discriminant score variable will be maximised.



To maximise  $\lambda$  the partial derivative

$$\frac{\delta \lambda}{\delta \underline{v}'} = 0$$

which gives  $B \underline{v} = \lambda W \underline{v}$

$$\text{or } [B - \lambda W] \underline{v} = 0$$

$$\text{or } [W^{-1}B - \lambda I] \underline{v} = 0$$

It is clear that  $\lambda$  is a latent root of  $W^{-1}B$  and  $\underline{v}$  is the corresponding latent vector.

As long as the variates are linearly independent and  $(n - m) > p$ , the matrix  $W$  will be of full rank,  $p$ , and will be non-singular. The matrix  $B$  of order  $p$  has a rank of  $p$  or  $(m - 1)$  whichever is smaller since there are only  $m - 1$  independent comparisons between group means. Hence the rank of  $W^{-1}B$  is also the smaller of  $p$  or  $(m - 1)$  which confirms the observation made above concerning the number of discriminant functions which may be extracted. Additionally the latent roots of  $W^{-1}B$  provide a means of testing for significant discriminant dimensions using tests by Bartlett (1941), Wilks (1932) and Rao (1952).

Wilks lambda criterion is computed as a function of the eigenvalues of  $W^{-1}B$  as follows

$$\Lambda = \prod_{j=1}^{m-1} \frac{1}{1 + \lambda_j}$$

Bartlett's  $\chi^2$  test for the significance of discrimination afforded by the remaining  $m - 1 - k$  functions after the acceptance of the first  $k$ , is then calculated as

$$\chi^2 = - (n - 1 - \frac{p+m-1}{2}) \log_e \Lambda'$$

where  $\Lambda' = \prod_{j=k+1}^{m-1} \frac{1}{1+\lambda_j}$

with  $(p - k)(m - k - 1)$  degrees of freedom.

The proportion of the total discriminating power of the variable set contained in the  $j$ th discriminant function may be taken to be

$$\frac{\lambda_j}{m-1} \frac{1}{\sum_{j=1}^m \lambda_j}$$

while  $\sqrt{\frac{\lambda_j}{1-\lambda_j}}$  may be seen as a canonical correlation co-efficient

between the discriminant function and a set of binary variables coded to distinguish the groups. Multiple discriminant analysis is in fact a special case of canonical correlation and was discussed by Bartlett (1938) from this standpoint.

The apparent computational efficiency of employing  $m - 1$  (or fewer) discriminant score variables in the assignment rules described earlier, rather than the  $p$  original variables, is illusionary when it is remembered that the total computation has involved the transformation from measured variables to functions and back to function scores prior to assignment. The main justifications for the use of discriminant function scores are that the underlying differences between the groups may be better understood through interpretation of the function co-efficient vectors and that, while original variables may not possess multivariate normality, discriminant functions, being linear combinations of these, are much more likely to conform to this distributional requirement. The further argument that random noise in the system is eliminated by the use of only the more important functions is perhaps less telling when



discrimination has been preceded by a stepwise MANOVA phase to eliminate poor discriminating variables. The validity of employing discriminant function scores is indicated by the fact that an observation's position in the original variable space is identical to its position in the full discriminant space as long as the group dispersion matrices are equal.<sup>1</sup> It has been shown that linear discriminant functions only arise from the use of the  $W$  matrix of pooled within group deviation cross products which implies such homoscedasticity. Thus only if we assume near homogeneous group variance-covariance matrices is the movement to discriminant space justified. It is evident that the whole procedure through MANOVA, discriminant analysis and the use of discriminant scores in assignment rules, is wedded to the concept of equal group dispersion which accounts for the previously mentioned adherence to this assumption. If one departs from it, either the assignment must be based on original variates or we move into the realms of quadratic discriminant functions (Smith, 1946; Lubin, 1950; Maxwell, 1977) with their added computational complexities. In either case, multivariate normality can no longer be automatically claimed.

As a complete alternative to the methods of discrimination and assignment discussed above, Kendall (1966) and Richards (1972) describe a distribution free discriminant analysis which is essentially monothetic. In it there is no misclassification; rather it ends with some observations unclassified. Others have described attempts at non-parametric discrimination to overcome the restrictive assumptions of the classical model, including Leaverton (1971) and Zimmerman and Brown (1972), who find their method to perform reasonably well on non-normal data.

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1 Lohnes (1961) has conducted a Monte Carlo study of this question and suggests that moderate departures from homogeneity of dispersion do not affect the results greatly.

CHAPTER III

APPROACHES TO THE CLASSIFICATION OF AGRICULTURE

3.1 Developments in Agricultural Classification

Although statistical information on agriculture has been collected by many countries and international organisations for numerous years, it is only in the past decade that interest has been shown in the construction of an agricultural classification comparable with the classifications of industry which are widely available. Reports of agricultural censuses and surveys have been and still are largely presented in terms of simple one and two-way tabulations of investigated variables. Thus, while important global information is readily available on such aspects of agriculture as area cultivated by crop, crop output per acre (hectare) and labour and capital inputs, there is little or no data relating to distinctive groupings of agricultural holdings, representable by a classification, and based on their total production systems. Yet the need for such information is clear. If the structure of the agricultural industry is to be fully understood and a sounder forecasting basis for policy formulation and decision taking obtained, there must be a more systematic approach to the collection and dissemination of agricultural data.

In a European context the Common Agricultural Policy has highlighted the need for appropriate means of presenting the information collected in the very large-scale 1966/7 and 1976/7 E.E.C. Farm Structure Surveys. Over a period of ten years there has emerged from the officers of the European Commission a proposal for an *a priori* classification of agricultural holdings which has a principal activity basis. The "Group



of Experts Farm Typology" (1977) is shown in detail in Appendix A and provides a breakdown of holdings according to their output value. In all, the Farm Typology produces 51 detailed classes (Steps 2 and 3 combined) which are merged into either 30 (Step 2) or finally 10 (Step 1) broader groupings as follows:

1. Field Crops ( $>2/3$ )
2. Horticulture ( $>2/3$ )
3. Permanent Crops (exc. Vineyards) ( $>2/3$ )
4. Vineyards ( $>2/3$ )
5. Grazing Livestock (exc. Dairy Cows) ( $>2/3$ )
6. Dairy Cows ( $>2/3$ )
7. Pigs and Poultry ( $>2/3$ )
8. Field Crops and Grazing Livestock (both between  $1/3$  and  $2/3$ )
9. Grazing Livestock II (between  $1/3$  and  $2/3$ ) and others ( $\leq 1/3$ )
10. Others.

While there exists clear evidence that in some cases these 'classes' will represent distinctive production types with holdings having similar technologies and character (eg horticulture), there will be others where farm to farm differences with respect to a range of variables are much more noticeable than the common denominator of principal activity. For instance, the members of Class 6 will vary from highly efficient, fully automated and large dairy herd operations, to tiny peasant holdings with one hand-milked cow, a small subsistence plot and a holder whose main employment may not be in agriculture at all. Additionally, the *a priori* basis of the classification inevitably means that some of the groups will be very large in size with others having a very small and potentially insignificant membership. There may also be the difficulty that the creation of classes for political reasons will not have produced technol-



ogically distinctive groups of holdings. The separation of Vineyards from other Permanent Crops is a case in point.

Although subject to these criticisms, it seems likely that the Farm Typology will be adopted by the Statistical Office of the European Communities<sup>1</sup>, if for no other reason, because of the simple 2/3 and 1/3 "threshold" rules for assigning holdings to classes. Nevertheless, concurrently with the discussions leading to this *a priori* scheme, there have been several attempts to examine a data based polythetic approach to the problem. Shaffer (1972) discusses a classification of 100 Belgian agricultural holdings using a clustering method proposed by MacQueen (1967) and refined and programmed by Kammerer (1969). Among Shaffer's conclusions are, that the clustering produced is strongly influenced by the choice of variables, and particularly by the inclusion of binary variables, that 7-8 "genuine" (large in size) and numerous "non-genuine" (small in size) classes were formed, and that much larger samples are needed to assist in the determination of the number of genuine classes. Lenco (1974) reports a much more extensive investigation based on 6000 French agricultural holdings which was later applied to a larger sample of 20,000 holdings. Although not clear from the report of this research, it appears that the classification was mainly based on an examination of the eigenvalues, eigenvectors, and principal component scores of the correlation matrix, from which decisions were taken about the variables most distinguishing farm from farm and the methods of partitioning these to form initial classes. Ultimately, two alternative schemes are presented, one based on the types and amount of labour used by holdings and the other on the principal crops and livestock produced. Although the principle of iterative reallocation of observations to class centres is mentioned, the detailed clustering procedure, if used, is not discussed; nor is the claim for stability justified when the analysis was extended to 20,000 holdings.

<sup>1</sup> The final version of the Farm Typology and a simple Holding Size Classification were ratified by the Commission on 7 April 1978, (Official Journal of the E.E.C., Vol. 21, No. L148, 5 June 1978).



The only Europe-wide study of the problem of agricultural classification (Rainelli and Kerbaol, 1975) is based not on farm units but administrative regions in the six founder-member nations of the E.E.C. Both agricultural and economic variables relating to these regions were used in a series of orthogonal factor analyses which were subjectively interpreted to form regional classes. However, these effectively distinguish only Italy from France, from the Benelux countries and Germany, which confirms broad but fairly predictable differences in prevailing agricultural, climatic, economic and social conditions.

It is clear that none of these studies is geographically general enough nor sufficiently established or tested to provide a serious alternative to the Farm Typology. None have been tested for reproducibility and stability and nowhere have rules for the allocation of non-sampled holdings been defined. Equally, no comparisons of the data based with the *a priori* method have been undertaken, in order to examine the relative efficiency of the two approaches. That there is scope for further investigation into the viability of a data based polythetic classification is apparent. The basis for such an investigation is outlined below and developed in the following chapters.

### 3.2 The Research Design for Classifying Agricultural Holdings

The development of the final proposed classification of European agricultural holdings involved three distinct phases. Experimentally, three multivariate procedures were applied to a small sample of 500 holdings drawn systematically from the 1966/7 E.E.C. Farm Structure Survey. These were aimed at investigating and reducing the dimensionality of a data matrix having over fifty holding characteristics, exploring various numerical taxonomies of observations on the basis of

the reduced dimensions and finally determining assignment rules for observations not previously classified and based on the original variable set.

Once acceptable results had been obtained, in statistical, agricultural and comparative terms, the same methods were applied to two further independent samples of the same size to test the reproducibility and predictability of the results. Specifically, the classes to which observations in the second and third samples would be assigned, based upon the assignment rules developed from the first sample, were compared with the independently-determined and cluster analysis based class memberships of these observations. Having evaluated this inter-sample predictability and thus ascertained the stability of the classification, the final scheme was obtained from a fourth independent sample of some 2000 holdings.

Throughout, comparisons have been made between the proposed multivariate classification and a standard principal activity classification based on the Farm Typology. To this end, the proportion of the variance in the data explained by the classification has been calculated in each case. (i.e.  $\text{trace}(B)$  as a percentage of  $\text{trace}(T)$ ).

### 3.3 Data and Sample Designs

The data base (population) for this study was provided by the Statistical Office of the European Communities and consisted of information on 132 variables for 22026 farm holdings in Belgium, France, Germany, Holland, Italy and Luxembourg. The magnetic data tape had been compiled by S.O.E.C. from the returns of these countries to the 1966 E.E.C. Farm Structure Survey originally for the purpose of testing the programming of proposed survey tabulations. Because some countries had provided full census information while others only samples of various



sizes, and in order to have a reasonably sized sample of holdings from each member nation, the data tape was constructed by systematically sampling national returns using the following sample fractions:

<u>Country</u>	<u>Sampling Fraction</u>	<u>Sample Size</u>
Belgium	1/10	3355
France	1/100	4277
Germany	1/100	4482
Holland	1/10	2705
Italy	1/100	5225
Luxembourg	1/1	1982
		<hr/>
		22026

For each holding, the information available comprised binary, manifold classificatory, ranked and quantitative variables on holding location, the holder and manager, land uses, livestock, machinery employed, labour by type, quantity and age, the size of the holding, and other general holding and management characteristics. It was decided at the outset to reduce and redefine the number of variables to be included in subsequent analyses. There were three reasons for the decision. Firstly, information on geographical location (country, region and district) was omitted because it was felt that any classification scheme devised should be based on agricultural, holding and holder practices rather than be influenced or even dominated by the historical accident of political boundaries. Secondly, by combining certain available variables into relevant "activity" group characteristics, there would be significant reductions in computer time requirements. Thirdly, a high proportion of available variables were correlates of the size of the holding so that it was deemed appropriate to 'standardise' these by a measure of size, such as total holding area or the area of used agricultural land. Size

measures could then be separately represented and thus appropriately weighted in the classification. The resultant holding characteristics are shown below (Table 3.1) and are defined in detail in Appendix B which also lists the original variables available in the 1966/67 Farm Structure Survey.

It should be stressed that the rationale for the formation of this set of 53 operational variables was that a reasonable balance between main variable groupings should be produced and one which reflected the range and proportion of information originally collected. Equally, these variables were constructed as far as possible to conform to definitions proposed for the Farm Typology and were agreed to be appropriate after discussions with staff of the Agricultural Division of S.O.E.C.

Inevitably, the classification scheme produced, using the final variable set, assumes that the correct weighting of holding characteristics has been used. The ultimate test of the validity of this assumption must rest upon the user who will know the purposes of the classification and therefore the appropriate balance of weights.

On quite arbitrary, but pragmatic, grounds, it was decided that three samples of approximately 500 holdings should be drawn from the population for experimental purposes. It was felt that this sample size was such that representative cross-sections of European holdings would be obtained and that the burden of computer analysis would not be unreasonable. Inspection of the population data tape showed holdings to be in Country, Region, District and Size order. Consequently, two of the samples were selected systematically from a random start, sampling each 44th holding. Given the structure of the sampling frame, this quasi-random sampling scheme would achieve the effect of a standard stratification by holding location and size. In the event, random



Table 3.1

*Operational Variables*

S01	Total Holding Area (in ares)	
S02	Area of Used Agricultural Land (in ares)	
S03	Total "Standard" Livestock <sup>1</sup> (number)	
S04	Total Labour Input (Annual Work Units <sup>2</sup> )	
S05	Total Number of Machinery Accesses <sup>3</sup>	
L01	Cereal	} Land used for these purposes as % of S02
L02	Rootcrops	
L03	Industrial Plants	
L04	Horticulture	
L05	Other Arable	
L06	Fallow	
L07	Subsistence	
L08	Pasture	
L09	Vineyards	
L10	Other Permanent Crops	
L11	Unused Agricultural Land as % of S02 + Unused Agricultural Land	
L12	Woodland and Other land as % of S01	
L13	Whether Successive and Intermediate Crops Grown (1=Yes, 0=No)	
L14	Whether Permanent and Associated Crops Grown (1=Yes, 0=No)	

1 See Appendix B for conversion codes from head of livestock to 'standard' animals.

2 See Appendix B for the calculation of Annual Work Units.

3 From ownership, sharing or hiring.

A01	Horses	}	"Standard" livestock as % of S03
A02	Dairy Cows		
A03	Other Cattle		
A04	Sheep and Goats		
A05	Pigs		
A06	Poultry		
A07	"Standard" livestock per hectare of S01		
W01	Annual Work Units per 10 hectares of S01		
W02	Family A.W.U.'s as % of S04		
W03	Regular Workers under 25 years old	}	As % of total number of regular (non-casual) workers
W04	Regular Workers between 25 and 35 years old		
W05	Regular Workers between 35 and 45 years old		
W06	Regular Workers between 45 and 65 years old		
W07	Regular Workers 65 years old and over.		
M01	Whether 1 or more tractors owned	}	(1=Yes, 0=No)
M02	Whether 1 or more cultivators owned		
M03	Whether 1 or more harvesters owned		
M04	Whether 1 or more machines shared or hired		
M05	Whether 1 or more milking machines owned		
M06	Area of Greenhouses as % of S02		
M07	Whether draft animals used (1=Yes, 0=No)		
M08	Machines Access (S05) per 10 hectares of S01.		



H01	Whether the holding has a holder-manager (1=Yes, 0=No)	
H02	Manager's Education (1=None, 2=Primary, 3=Secondary, 4=Higher)	
H03	Whether Owner Male (1=Yes, 0=No)	
H04	Whether Owner Female (1=Yes, 0=No)	
H05	Holder's Age (in years) <sup>1</sup>	
H06	Whether holder has other non-agricultural gainful employment (1=Yes, 0=No)	
G01	Owned Agricultural Land	} As % of S02
G02	Rented Agricultural Land	
G03	Share Cropped Agricultural Land	
G04	Whether Accounts Kept (1=Yes, 0=No)	
G05	Co-operative Memberships (Number)	
G06	Contracted Crops (Number)	

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<sup>1</sup> Where there is corporate ownership or joint ownership, a default value of 52 years has been used.

starts from the 6th and 30th holdings were made which produced samples of 501 and 500 holdings respectively.

The third experimental sample was drawn using simple random sampling without replacement to provide a truly independent replicate of the first two. In addition, it was intended as a check of the superiority (or otherwise) of the implicit stratification in the first two samples.

A 10% sample of holdings was employed in the final classification analyses, and for this, systematic selection was again used from the 4th holding, giving a fourth sample of 2202 holdings in all.

From initial analyses of the data obtained from these samples, it became clear that there were holdings with either no recorded land of any kind, no used agricultural land or no labour inputs. While it may be that these were very small<sup>1</sup>, it was decided to eliminate them from the analyses on the grounds that either measurement errors existed or that they were no longer agricultural holdings in any meaningful sense. Their inclusion would have clearly created difficulties over size standardisation of variables, and in any event, would probably have been reflected in the formation of at least one separate class.

Early experimental principal component and cluster analyses highlighted the further problem of 'outliers' in each of the samples. Such outliers were found to be extreme observations with respect to one or more of the operational variables and as such were so 'distant' from other holdings that they consistently formed cluster analysis-based classes of 1, or at most 2, holdings. Their removal frequently reduced variances by fifty percent or more and was justified in terms of their uniqueness as farm types. While such holdings could be classified,

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1 Areas of under 50 square metres are for most purposes declared as zero.



albeit poorly, when the classification scheme has been developed, it was felt inappropriate to allow them to influence and maybe distort the scheme itself.

After the exclusion of spurious and extreme outlier observations, the following usable samples of data were obtained for analysis. Partial comparison with the population shows no major discrepancies.

	Original Size	Spurious Observations		Outlier Observations		Final Size	
	Number	Number	%	Number	%	Number	% of Original Size
Systematic Sample A	501	13	2.6	1	0.2	487	97.2
Systematic Sample B	500	7	1.4	7	1.4	486	97.2
Random Sample C	500	8	1.6	2	0.4	490	98.0
Systematic Sample D	2,202	31	1.4	10	0.5	2,161	98.1
Population	22,026	283	1.3	Not tested		21,743	98.7

In Table 3.2, the means, standard deviations, minimum and maximum values of the 53 operational variables are shown. The effect of outlier exclusions in bringing the four samples into startling similarity is apparent. In no cases are there statistically significant differences in means, and only rarely in variances.

#### 3.4 Methodology and Algorithms

Computer analysis in the research was undertaken both at the University of Aston on an I.C.L. 1904S computer, and at the University of Manchester on their CDC 7600 machine. While the majority of the programs were specifically written and developed in *Fortran* for the research project, use was also made of the I.C.L. Statistical Package (1971) for principal component transformation of the data, and of the Statistical Package for Social Sciences (SPSS) for linear discriminant analysis (Nie *et al*, 1975).

The selection of samples, elimination of spurious observations and transformation of the original data to operational variables was completed simultaneously using the programs, SYSTSAM and RANSAM, which are produced with the other programs in Appendix C. These also assigned to observations classification codes for an *a priori* classification scheme based upon, but not identical to, the Farm Typology. As holding output-value data was unavailable, the *a priori* classification employed for comparative purposes in the research rested on relative land uses and the proportion of standard livestock reared during the survey year.

Seventeen classes were distinguished (Table 3.3), many of which are analogous to those found in Steps 1 and 2 of the Farm Typology. The principle for classifying a holding was that the first of the set of criteria to be satisfied, moving from low to high numbered classes, determined class membership.

Having created EDS files holding the sample data, these were eventually edited to remove outliers and summary characteristics, including a country of origin distribution, were computed for each class of holdings using program STANMEAN. This program also computed the 'explanatory power' of the *a priori* classification as the percentage ratio of between total sum of squares of standardised variables, namely

$$\frac{\sum_{k=1}^m n_k \sum_{j=1}^p z_{jk}^2}{\sum_{j=1}^p \sum_{i=1}^n z_{ij}^2} \quad \text{where } m = \text{no. of classes}$$

$$n = \sum n_k$$

Although not strictly comparable with the samples, a standard classification summary was also obtained for the total population using POPPROG.

The Aston macro UASTATSXDS3 enabled a full set of eigenvalues, latent vectors and principal component scores to be obtained before or



Table 3.3

*A Priori Land Use (%) and Standard Livestock (%) Classes*

<u>Class</u>	<u>Description</u>
I	Cereal > 66.7% of Used Agricultural Land (UAL)
II	Cereal and Root Crops both > 33.3% of UAL
III	Field Crops > 66.7% of UAL (but excluding Class I and II)
IV	Horticulture > 66.7% of UAL
V	Vineyards > 66.7% of UAL
VI	Permanent Crops > 66.7% of UAL (but excluding Class V)
VII	Permanent Pasture > 66.7% of UAL and Dairy Cows > 66.7% of Total Standard Livestock (TSL)
VIII	Permanent Pasture > 66.7% of UAL and Grazing Livestock > 66.7% of TSL (but excluding Class VII)
IX	Pigs and Poultry > 66.7% of TSL
X	Field Crops and Permanent Pasture > 33.3% of UAL and Grazing Livestock > 33.3% of TSL
XI	Permanent Pasture > 33.3% of UAL and Pigs and Poultry and Grazing Livestock > 33.3% of TSL
XII	Field Crops > 33.3% of UAL and Pigs and Poultry > 33.3% of TSL (but excluding Classes I, II, III and IX)
XIII	Field Crops and Permanent Crops > 33.3% of UAL (but excluding Classes I, II, III and VIII)
XIV	Field Crops and Horticulture > 33.3% of UAL
XV	Field Crops > 33.3% of UAL
XVI	Grazing Livestock > 33.3% of TSL
XVII	Others

after variable standardisation. The output from such runs was held on EDS files and edited using the I.C.L. MOP facilities together with program PRINSORT to produce principal component score input data for program CLUSTPROG. The original form of this cluster analysis algorithm was written by P. A. Golder at the University of Aston in 1971/2 to handle small amounts of data before principal component transformation. It was modified and developed to the present form in consultation with the author to enable the various proposed experiments to be undertaken starting from principal component scores.

Essentially, the method is based on the procedure suggested by Beale (1969) and is an optimisation technique using the ordinary Euclidean metric which seeks to minimise  $\text{tr}(W)$ . The cluster seeding is implemented by a subdivision of observations into a user determined number of groups based on ranked first component scores. Thereafter, the rule for forming clusters is based on the local minimisation of within cluster variances and the maximisation of between cluster variances. At each round in the analysis each observation,  $i$ , is examined in turn and is allocated to that cluster  $k$  for which

$$\sum_{j=1}^P (X_{ij} - \bar{X}_{jk})^2$$

is a minimum. Here  $X_{ij}$  is the  $j$ th variable for the  $i$ th observation and  $\bar{X}_{jk}$  is the mean of the  $j$ th variable in the  $k$ th cluster after the inclusion of the  $i$ th observation. The procedure continues until no observation is moved to a new cluster in a round or until a user pre-set maximum number of iterations has been reached. Having formed  $k$  clusters, the rule for determining  $k-1$  clusters involves finding two (of the  $k$ ) clusters already formed which, when combined, produce the least increase in the pooled within group variance. The merging of these is followed by a repetition



of the iterative reallocation of observations based on the cluster criterion. Because of expected initial instability, the seeding starts at a number of clusters higher than the expected optimum, and the number of iterations allowed is doubled at the  $k_{\max}$  and  $k_{\max-1}$  steps compared with later stages in the analysis.

Several other variants on the basic method are possible with the algorithm in its current form; the results of some of these are reported in the next chapter. As an alternative to the subdivision of principal component scores, the initial cluster configuration may be provided by the user as an input list showing the cluster membership code of each observation. Thus the clustering might be started using the *a priori* class codes or might be based on the results from a simpler monothetic hierarchical method of clustering.

Unstandardised, standardised, or user weighted principal component scores may be employed in the analysis by the setting of an input parameter. In the last case, weights are required as an input list and the data is transformed using these. One important form of weighting, which is facilitated in a different manner, is the exclusion of higher numbered components scores from the procedure.

Finally, the range of  $k$ , the number of clusters, for which detailed output is to be produced, may be set by the user. The detailed output gives information on each cluster membership, the distance of each observation from its cluster centre, a summary of cluster mean values with respect to the variables employed in the analysis, and an ANOVA-type table of trace  $(W)$ , trace  $(B)$  and trace  $(T)$  in absolute and percentage terms. Outside the range of  $k$ , for which such detailed output is requested, only the ANOVA table is given, together with information on the number of iterations employed at that stage in the analysis.



Whichever set of options is selected, the results of the test by Beale discussed in Chapter II are produced on the termination of the clustering (i.e. when a single cluster of all observations has been formed).

In order to obtain information on the cluster characteristics in relation to operational variables, rather than their principal component transforms, program CLUSMEAN was written. It takes output produced by CLUSTPROG on cluster membership at each stage in the agglomeration from  $k_{\max}$  to 1 cluster, and uses this to produce results identical in principal to those from STANMEAN. Thus decisions may be taken on the 'best' group of clusters from which to form the classification using both a statistical criterion based on the Beale test and substantive agricultural evidence about cluster characteristics.

CLUSMEAN also creates a new data file for each sample which shows in addition to the operational variables and the *a priori* classification code, the cluster group membership of each observation at each stage in cluster analysis. From this, SPSS analyses may be set up to examine the nature of the merging of clusters and to produce discriminant analysis assignment rules for new observations. SPSS was chosen for this second purpose because it has considerable flexibility in allowing a step-wise build-up of discriminating variables and the fixing of the maximum percentage trace of  $W^{-1} B$ . In addition, observations do not have to be in group (class) order and prior probabilities of group membership may be set. Lastly, the SPSS Version 6 available at Manchester, allows observations which are not used in forming the discriminant rules to be assigned automatically. In consequence, the best group of clusters in terms of internal (within sample) and external (between sample) assignment success may be found and discriminant rules of increasing complexity evaluated.



As an alternative to classical linear discriminant analysis, program KENDIS was written to the author's specification by Mrs V Perks of the University of Aston. KENDIS is a multi-group generalisation of the procedure suggested by Kendall (1966) and allows for binary and categorical data as well as quantitative variables. In its most restricted form, this distribution-free method performed very poorly on the peculiarly heterogeneous agricultural data to hand. Although not completed at this time, less restrictive re-specification of the Kendall procedure has taken place and looks more encouraging.

The final program written for the research was BARTTEST. This was employed in initial tests of the eigenvalues of the correlation matrix derived from operational variables. As it consistently showed significant components through to the penultimate one or two, it was deemed to be of little help in decisions about the dimensionality of the data.

Table 3.2 Summary Statistics-Operational Variables

MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Statistic	Systematic A	Systematic B	Random C	Systematic D	Population				
S01	Total Holding Area (in Ares)	$\bar{X}$	1,753	1,754	2,117	1,852	2,266	2,051	1,795	1,757	2,015
		S	2,581	2,583	5,137	2,586	5,773	3,119	2,699	2,398	7,427
		Min	5	5	7	7	4	4	5	7	2
		Max	23,300	23,300	85,700	30,520	110,000	24,920	51,800	27,500	751,300
S02	Used Agricultural Land (in Ares)	$\bar{X}$	1,550	1,551	1,910	1,666	1,918	1,756	1,580	1,552	1,695
		S	2,356	2,358	4,872	2,399	4,511	2,642	2,253	2,074	4,397
		Min	1	1	1	1	2	2	3	3	1
		Max	23,260	23,260	85,700	28,370	83,000	23,800	31,700	19,710	413,100
S03	Total "Standard" Livestock (number)	$\bar{X}$	15.8	14.8	20.9	16.9	15.8	15.9	17.1	15.8	18.9
		S	32.4	23.0	59.9	24.4	24.7	24.8	50.9	23.4	96.6
		Min	0	0	0	0	0	0	0	0	0
		Max	518.6	256.9	898.7	323.1	261.0	261.0	2,054.0	341.0	10,960.0
S04	Total Labour Input (A.W.U.'s)	$\bar{X}$	1.83	1.83	2.09	1.92	1.96	1.96	1.92	1.91	1.96
		S	1.24	1.24	4.13	1.53	1.86	1.86	1.59	1.49	2.16
		Min	0.07	0.07	0.02	0.04	0.07	0.07	0.07	0.07	0.07
		Max	9.73	9.73	87.23	18.27	20.3	20.3	23.55	21.00	134.6
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743



MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Statistic	Systematic A	Systematic B	Systematic C	Systematic D	Population				
S05	No. of Total Machine Accesses (through ownership, sharing or from agencies)	$\bar{X}$	2.43	2.44	2.56	2.54	1.96	2.60	2.55	2.55	2.58
		S	1.86	1.87	2.18	1.93	1.86	2.02	1.98	1.96	2.07
		Min	0	0	0	0	0.07	0	0	0	0
		Max	10.0	10.0	25.0	10.0	46.0	13.00	15.0	15.0	54.0
L01	Cereal area as % of SO2	$\bar{X}$	26.1	26.1	24.6	24.9	26.0	26.1	25.1	25.2	25.6
		S	23.3	23.3	22.7	22.7	23.9	23.9	23.1	23.1	23.6
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	
L02	Root Crops area as % of SO2	$\bar{X}$	7.8	7.8	7.1	7.2	6.9	6.9	7.5	7.5	7.3
		S	12.2	12.2	10.4	10.5	11.2	11.2	11.1	11.1	11.2
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	69.2	69.2	80.8	80.8	98.8	98.8	100
L03	Industrial Plants area as % of SO2	$\bar{X}$	0.4	0.4	0.5	0.6	0.6	0.6	0.8	0.8	0.6
		S	2.4	2.4	2.8	2.8	3.0	2.98	5.2	5.2	3.5
		Min	0	0	0	0	0	0	0	0	0
		Max	28.7	28.7	37.5	37.5	36.8	36.8	91.3	91.3	100
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743

MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Stat- istic	Systematic A	Systematic B	Random C	Systematic D	Population				
L04	Horticulture area as % of SO2	$\bar{X}$	2.5	2.5	2.5	2.5	3.1	3.0	3.3		
		S	13.3	13.3	13.3	13.3	15.5	15.2	15.7		
		Min	0	0	0	0	0	0	0		
		Max	100	100	100	100	100	100			
L05	Other Arable Crops as % of SO2	$\bar{X}$	9.3	9.4	10.3	10.3	10.4	10.5	10.2	10.2	
		S	15.9	15.9	16.7	16.7	17.0	17.0	17.0	16.2	
		Min	0	0	0	0	0	0	0	0	
		Max	100	100	100	100	100	100	100		
L06	Fallow Land area as % of SO2	$\bar{X}$	1.1	1.1	1.7	1.5	1.4	1.4	1.3	1.3	
		S	5.4	5.4	9.0	8.2	7.7	7.8	6.8	6.8	6.1
		Min	0	0	0	0	0	0	0	0	0
		Max	58.2	58.2	100	100	85.9	85.9	96.0	96.0	100
L07	Subsistence Crops area as % of SO2	$\bar{X}$	1.3	1.3	1.7	1.3	1.5	1.5	1.3	1.2	1.5
		S	6.8	6.8	9.6	7.3	8.1	8.1	6.9	6.9	8.2
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743



MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Stat- istic	Systematic A		Systematic B		Random C		Systematic D		Population
L08	Pasture Land area as % of SO2	$\bar{X}$	39.5	39.4	41.4	41.7	37.5	37.5	39.9	39.9	40.1
		S	34.3	34.2	35.6	35.4	35.3	35.2	35.2	35.1	34.8
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
L09	Vineyards area as % of SO2	$\bar{X}$	3.8	3.8	4.6	4.5	4.7	4.7	4.0	4.0	4.5
		S	15.0	15.0	16.8	16.5	16.7	16.7	14.9	14.9	16.0
		Min	0	0	0	0	0	0	0	0	0
		Max	99.1	99.1	100	100	100	100	100	100	100
L10	Other Permanent Crops area as % of SO2	$\bar{X}$	8.2	8.3	5.5	5.4	6.9	6.8	6.9	6.9	6.2
		S	23.7	23.7	17.9	17.8	22.0	22.0	21.5	21.5	19.8
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	
L11	Unused Agricultural Land as % of SO2 + Unused Agricultural Land (Marginal Land)	$\bar{X}$	1.7	1.7	2.1	1.9	2.0	2.0	1.9	1.9	2.0
		S	7.4	7.5	9.3	8.7	8.5	8.5	9.1	9.0	9.0
		Min	0	0	0	0	0	0	0	0	0
		Max	80.0	80.0	79.9	79.9	83.9	83.9	93.6	93.6	99.6
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743

MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Statistic	Systematic A	Systematic B	Random C	Systematic D	Population				
L12	Woodland and Other Land as % of SO1	$\bar{X}$	9.7	9.6	9.7	9.5	10.1	10.0	8.9	8.9	9.5
		S	14.4	14.3	14.8	14.3	16.8	16.8	13.7	13.7	14.6
		Min	0	0	0	0	0	0	0	0	0
		Max	86.7	86.7	96.8	96.8	96.9	96.9	95.5	95.5	99.7
L13	Whether Successive and Intermediate Crops grown (1=Yes, 0=No)	$\bar{X}$	11.1	11.1	12.0	11.9	11.6	11.6	11.5	11.4	11.1
		S	31.4	31.4	32.5	32.4	32.0	32.1	31.9	31.8	31.4
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
L14	Whether Permanent and Associated Crops grown (1=Yes, 0=No)	$\bar{X}$	20.7	20.7	24.1	23.4	21.5	21.6	23.0	23.0	22.8
		S	40.5	40.5	42.8	42.9	41.1	41.2	42.1	42.1	41.9
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
AO1	Standard Horses as % of SO3	$\bar{X}$	3.6	3.7	4.7	4.7	5.5	5.5	4.2	4.2	4.4
		S	13.3	13.3	16.6	16.7	18.8	18.9	15.4	15.5	15.8
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
	SAMPLE SIZE		488	487	493	486	492	496	2,171	2,161	21,743



MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Statistic	Systematic A	Systematic B	Random C	Systematic D	Population					
A02	Standard Dairy Cows as % of S03	$\bar{X}$	29.9	29.9	31.5	31.8	28.6	28.7	30.7	30.8	30.8	
		S	29.5	29.5	29.4	29.4	29.6	29.6	29.6	29.7	29.7	29.7
		Min	0	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100	
A03	Standard Other Cattle as % of S03	$\bar{X}$	25.2	25.2	26.4	26.5	24.6	24.7	24.2	24.3	24.6	
		S	26.9	26.9	26.7	26.6	26.9	26.9	26.9	25.9	25.9	26.3
		Min	0	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100	
A04	Standard Sheep and Goats as % of S03	$\bar{X}$	2.8	2.8	2.6	2.6	3.6	3.6	3.1	3.0	31.9	
		S	14.3	14.3	12.5	12.6	15.8	15.8	14.5	14.5	14.5	
		Min	0	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100	
A05	Standard Pigs as % of S03	$\bar{X}$	14.1	13.9	14.4	14.2	13.2	13.3	14.0	13.9	14.1	
		S	24.1	23.9	23.1	22.7	24.0	24.1	23.7	23.5	23.7	
		Min	0	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100	
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743	

MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Statistic	Systematic A	Systematic B	Random C	Systematic D	Population				
AO6	Standard Poultry as % of SO3	$\bar{X}$	3.8	3.7	4.5	4.3	5.3	5.3	4.3	4.2	4.6
		S	14.2	14.2	15.4	14.9	18.0	18.1	15.1	14.2	15.8
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
AO7	Standard Animals per hectare of SO1	$\bar{X}$	1.37	1.30	2.26	1.40	1.38	1.39	1.76	1.51	1.96
		S	3.63	3.28	12.34	2.68	3.66	3.66	7.59	4.57	13.51
		Min	0	0	0	0	0	0	0	0	0
		Max	50.57	50.57	246.3	31.1	42.0	42.0	209.3	108.3	964.3
WO1	Annual work units per 10 hectares of SO1	$\bar{X}$	3.42	3.42	3.92	3.42	4.22	4.22	3.53	3.33	3.76
		S	7.19	7.19	10.37	7.90	10.27	10.29	10.02	6.91	10.56
		Min	0.11	0.11	0	0.04	0	0.03	0.04	0.04	0.04
		Max	105.30	105.3	113.2	87.6	117.2	117.2	333.3	121.0	604.2
WO2	Family AMU as % of SO4	$\bar{X}$	85.0	85.2	83.4	83.8	82.9	83.0	84.7	84.9	84.3
		S	28.8	28.6	30.9	30.5	30.8	30.6	28.6	28.4	29.2
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743



MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Stat- istic	Systematic A	Systematic B	Random C	Systematic D	Population	
W03	% of Regular Labour < 25 years old	$\bar{X}$	8.2	8.2	8.9	8.7	8.3	8.5
		S	17.3	17.3	19.0	18.6	17.5	17.7
		Min	0	0	0	0	0	0
		Max	100	100	100	100	100	100
W04	% of Regular Labour 25 < 35 years old	$\bar{X}$	13.8	13.8	13.2	13.2	13.8	14.0
		S	25.7	25.7	24.9	25.0	25.7	26.1
		Min	0	0	0	0	0	0
		Max	100	100	100	100	100	
W05	% of Regular Labour 35 < 45 years old	$\bar{X}$	21.8	21.8	20.4	20.2	22.1	21.9
		S	33.8	33.8	31.5	31.4	32.5	33.4
		Min	0	0	0	0	0	0
		Max	100	100	100	100	100	
W06	% of Regular Labour 45 < 65 years old	$\bar{X}$	41.2	41.0	42.6	42.9	40.8	41.1
		S	39.1	39.1	38.9	38.8	38.9	38.9
		Min	0	0	0	0	0	0
		Max	100	100	100	100	100	
	SAMPLE SIZE		488	487	493	486	492	490
							2,171	2,161
								21,743

MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Statistic	Systematic	Systematic A	Systematic B	Random C	Systematic D	Population			
W07	% of Regular Labour ≥ 65 years old	$\bar{X}$	13.7	13.7	14.0	14.2	15.7	15.8	13.2		
		S	28.0	28.0	27.4	27.5	30.2	30.2	27.9		
		Min	0	0	0	0	0	0	0		
		Max	100	100	100	100	100	100	100		
M01	Whether 1 or more tractors owned (1=Yes, 0=No)	$\bar{X}$	46.5	46.6	49.7	50.2	46.8	46.9	48.4		
		S	49.9	49.9	50.0	50.0	49.9	49.9	50.0		
		Min	0	0	0	0	0	0	0		
		Max	100	100	100	100	100	100	100		
M02	Whether 1 or more cultivators owned (1=Yes, 0=No)	$\bar{X}$	12.7	12.5	14.4	14.2	14.2	14.1	13.9		
		S	33.3	33.1	35.1	34.9	34.9	34.8	34.6		
		Min	0	0	0	0	0	0	0		
		Max	100	100	100	100	100	100	100		
M03	Whether 1 or more harvesters owned (1=Yes, 0=No)	$\bar{X}$	14.6	14.6	18.1	18.1	17.3	17.4	17.8		
		S	35.3	35.3	38.5	38.5	37.8	37.9	38.2		
		Min	0	0	0	0	0	0	0		
		Max	100	100	100	100	100	100	100		
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743



MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Statistic	Systematic A	Systematic B	Random C	Systematic D	Population					
M04	Whether 1 or more machines shared or hired from agency (1=Yes, 0=No)	$\bar{X}$	68.6	68.8	65.5	66.3	70.9	71.0	68.4	68.7	68.7	68.7
		S	46.4	46.3	47.5	47.3	45.4	45.4	46.5	46.4	46.4	46.4
		Min	0	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100	100
M05	Milking machines owned (1= Yes, 0=No)	$\bar{X}$	25.8	25.9	29.0	29.2	27.0	27.1	27.6	27.7	28.2	28.2
		S	43.8	43.8	45.4	45.5	44.4	44.5	44.7	44.8	45.0	45.0
		Min	0	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100	100
M06	Area of Greenhouses as % of SO2	$\bar{X}$	0.55	0.55	0.93	0.92	1.22	1.22	0.96	0.90	1.05	1.05
		S	5.36	5.36	7.87	7.92	9.61	9.63	7.23	6.87	8.11	8.11
		Min	0	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100	100
M07	Whether draft animals used (1= Yes, 0=No)	$\bar{X}$	5.9	5.0	4.9	4.7	7.1	7.1	5.1	5.1	4.8	4.8
		S	23.6	23.7	21.5	21.2	25.7	25.8	22.0	22.1	21.4	21.4
		Min	0	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100	100
	SAMPLE USED		488	487	493	486	492	490	2,171	2,161	21,743	21,743

MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Stat- istic	Systematic A	Systematic B	Random C	Systematic D	Population			
M08	Machines Accessed (S05) per 10 hectares of S01	$\bar{X}$	3.66	3.78	3.60	4.90	4.34*	3.81	3.82	3.98
		S	5.29	7.48	5.94	14.74	7.54*	6.37	6.34	9.16
		Min	0	0	0	0	0	0	0	0
		Max	47.6	105.30	51.28	285.7	71.43	71.43	71.43	500.0
H01	Whether holder-manager (1=Yes, 0=No)	$\bar{X}$	94.9	93.5	93.6	94.3	94.5	95.4	95.5	94.8
		S	22.1	24.6	24.4	23.2	22.8	21.0	20.8	22.2
		Min	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	
H02	Manager's Education (1=Non, 2=Primary, 3=Secondary, 4=Higher)	$\bar{X}$	1.28	1.32	1.32	1.26	1.26	1.29	1.28	1.29
		S	0.58	0.62	0.62	0.56	0.56	0.59	0.59	0.59
		Min	1	1	1	1	1	1	1	1
		Max	4	4	4	4	4	4	4	
H03	Whether holder male (1=Yes, 0=No)	$\bar{X}$	87.3	88.0	88.3	87.0	87.1	86.9	87.0	87.2
		S	33.3	32.5	32.2	33.6	33.5	33.7	33.7	33.4
		Min	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	
	SAMPLE SIZE		488	493	486	492	490	2,171	2,161	21,743



MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Statistic	Systematic A	Systematic B	Random C	Systematic D	Population				
H04	Whether holder female (1=Yes, 0=No)	$\bar{X}$	7.6	7.6	5.5	5.4	7.3	7.3	8.5	8.5	7.6
		S	26.5	26.5	22.8	22.5	26.0	26.1	27.8	27.9	26.4
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
H05	Age of Holder (in years) (Where joint or coroporate holder = 52)	$\bar{X}$	52.5	52.5	52.1	52.1	52.4	52.4	52.1	52.1	51.9
		S	12.1	12.2	12.3	12.3	13.0	13.1	12.3	12.3	12.5
		Min	21	21	21	21	15	15	18	18	15
		Max	84	84	91	91	88	88	87	87	94
H06	Whether holder has non-agricultural gainful work (1=Yes, 0=No)	$\bar{X}$	24.0	24.0	21.5	21.2	21.5	21.6	23.2	23.2	21.6
		S	42.7	42.7	41.1	40.9	41.1	41.2	42.2	42.2	41.1
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
G01	Owned agricultural land as % of SO1	$\bar{X}$	61.1	61.0	64.3	64.1	60.9	60.9	61.2	61.2	61.1
		S	41.1	41.1	41.1	41.1	41.5	41.5	41.3	41.3	41.6
		Min	0	0	0	0	0	0	0	0	0
		Max	100	100	100	100	100	100	100	100	100
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743

MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Stat- istic	Systematic	A	B	Random	C	D	Population		
G02	Rented Agricultural Land as % of SO2	$\bar{X}$	34.6	34.7	32.2	32.5	34.0	33.9	34.7	34.8	34.2
		S	39.8	39.8	39.9	40.0	40.1	40.0	40.2	40.3	40.3
		Min Max	0 100	0 100	0 100	0 100	0 100	0 100	0 100	0 100	0 100
G03	Share Cropped Agricultural Land as % of SO2	$\bar{X}$	4.3	4.3	3.4	34.7	5.1	6.2	4.0	4.0	4.7
		S	20.0	20.0	17.3	17.4	21.2	21.3	18.5	18.4	20.2
		Min Max	0 100	0 100	0 100	0 100	0 100	0 100	0 100	0 100	0 100
G04	Whether Accounts kept (1 = Yes, 0 = No)	$\bar{X}$	22.1	22.2	22.9	22.4	21.3	21.4	22.2	22.1	22.0
		S	41.5	41.5	42.0	41.7	41.0	41.0	41.5	41.5	41.4
		Min Max	0 100	0 100	0 100	0 100	0 100	0 100	0 100	0 100	0 100
G05	No. of Co-operative Memberships	$\bar{X}$	1.49	1.49	1.49	1.50	1.42	1.42	1.53	1.54	1.52
		S	1.54	1.54	1.49	1.49	1.52	1.52	1.52	1.52	1.51
		Min Max	0 4	0 4	0 4	0 4	0 4	0 4	0 4	0 4	0 4
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743



MEANS, STANDARD DEVIATIONS, MINIMUM AND MAXIMUM VALUES OF VARIABLES USED IN ANALYSIS

(Second set of figures show effect of outlier removal)

Label	Variable	Stat- istic	Systematic A		Systematic B		Random C		Systematic D		Population
G06	No. of Contracted Crops	$\bar{X}$	0.074	0.074	0.101	0.099	0.079	0.080	0.083	0.082	0.089
		S	0.269	0.269	0.346	0.337	0.285	0.285	0.302	0.299	0.318
		Min	0	0	0	0	0	0	0	0	0
		Max	2	2	2	2	2	2	3	3	5
	SAMPLE SIZE		488	487	493	486	492	490	2,171	2,161	21,743

CHAPTER IV

EXPERIMENTAL CLASSIFICATION SCHEMES

4.1 The Nature of Experiments Undertaken

The experiments described in the following paragraphs had the clear purpose of finding a meaningful, but efficient and parsimonious classification of agricultural holdings. By their nature they are testing much more generally the characteristics of a broad methodology which might be applied equally to any other classification problem.

There are essentially eleven areas in which experimentation, leading to potentially different classifications, might be undertaken.

These are:

1. Selection of variables for principal component analysis.
2. Use of standardised or non-standardised variables in principal component transformation.
3. Number of iterations used in cluster analysis.
4. Number of principal component variables in cluster analysis.
5. Use of standardised or non-standardised component variables in cluster analysis.
6. Number of clusters to "seed" analysis.
7. Effect of subjective initial seeding of cluster analysis.
8. Different classification schemes, particularly number of classes, in discriminant analysis.
9. Different significance levels in decisions about the best discriminating variables or discriminant functions.
10. Effect of prior probability specification in discriminant analysis.
11. Use of distribution free discriminant analysis.



When it is remembered that for some of these there are many different values of experimental parameters possible, it is clear that only a restricted subset of all combinations of experimental factors can be considered.

In Table 4.1 are listed the experimental analyses undertaken. It will be seen that Analysis I is the standard of reference (control) against which all others are compared. This particular experiment was based on the full set of 53 operational variables defined earlier. The component analysis was run on standardised values of these and the clustering on the unstandardised scores of the first 10 component variables. A group of 30 clusters initiated the cluster analysis from a partitioning of ranked first component scores. After the first two steps (30 and 29 clusters), only two iterations were allowed in the reallocation of observations between clusters. Discriminant analysis was based on a group of 10 cluster classes with termination of the MANOVA based step-wise variable selection procedure at the point where the 25 most significant discriminating variables had been selected. Although on usual partial-F statistic criteria a further 25 variables were significant ( $\alpha = 0.05$ ) after this stage in the analysis, it was felt necessary to take a peculiarly severe line as the clustering basis of group membership

is the antithesis of randomness assumed in MANOVA. The partial-F statistic at the point of cut-off was in fact more than double the value normally required for tests of group separation at a 0.1% significance level.

For assignment or identification purposes, classification functions were computed, although formal classification of observations to groups was based on discriminant function scores. The number of discriminant functions used for this purpose was determined by the first of the following criteria to be satisfied.

- (a) No further function is significantly contributing to the discrimination at a 5% level.
- (b) At least 95% of the trace of  $W^{-1}B$  is contained within the first  $g$  discriminant functions ( $g \leq m - 1$ ).
- (c) All 9 discriminant functions are included.

In the event, criterion (a) never operated as all functions were significant at all reasonable levels, and (c) was inoperable since fewer than 9 functions accounted for 95% of the trace of the  $W^{-1}B$  matrix. In the assignment phase prior probabilities proportionate to class size were employed while equal class variance-covariance matrices were assumed.

The decision to use this particular set of classification parameters was based partly on *a priori* reasoning, partly on early empirical invest-



Experimental Analysis	I	II	III	IV	V	VI	VII	VIII	IX	X	XI	XII	XIII	XIV	XV	XVI	XVII	XVIII	XIX	XX	XXI	XXII	XXIII	XXIV	XXV	XXVI	XXVII
Experimental Factor	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A	A
Variable Selection	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S	S
Variable Treatment for PCA	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U	U
Component Variable Treatment for Clustering	2	4	6	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
No. of iterations in Clustering	30	30	30	25	20	30	30	30	30	30	30	17*30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30
No. of Component Variables used in Clustering	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10
No. of Classes in Discriminant Analysis	10																										
% Trace of $W^{-1}B$ to determine number of functions	95																										
Prior Probability specification	Si																										
No. of Discriminating Variables	25																										
Distribution free discrimination																											

Abreviation	Meaning	Abreviation	Meaning
A	All variables	*	<i>A priori</i> class seeding
O	Odd Numbered Variables (1st, 3rd ... 53rd)	Si	Priors proportionate to size of class
E	Even Numbered Variables (2nd, 4th ... 52nd)	Eq	Priors equal
S	Standardised to zero mean and unit variance	√	Non-parametric discrimination
U	Unstandardised		

Table 4.1 Experimental Analyses

igation and was partly arbitrary. In the event, the decision appears not unreasonable.

As will be seen from Table 4.1, not all experimental analyses were conducted over the full range of experimental factors. Particular stress was placed on the principal component and cluster analysis phases as these were deemed the most uncertain and least investigated by other researchers. The separate experiments are listed in Table 4.2.

#### 4.2 Principal Component Interpretation

The four sets of PCA results for Sample A, which are used in the various experimental analyses, are summarised in Table 4.3, Figures 4A and 4B, and Tables 4.4 and 4.5.

The problem of working with unstandardised variables, possessing enormous scale variations, is highlighted in this case. Because of the large variances of the two main farm size measures (S01 and S02), these completely dominate the first two components derived from the variance-covariance matrix. The normalised eigenvector elements associated with total holding area and the area of used agricultural land are many times bigger than the weights attached to any other variable. The consequence is that the first two components account for 99.8 per cent of the total variance in the data. The use in clustering of unstandardised component scores which have been obtained from such an analysis will inevitably mean that holding size will be the main classification variable. Nevertheless, the effect of classifying holdings almost exclusively on a size criterion was thought to be of potential interest and Experimental Analysis IX was completed. Of course, a totally different picture may be expected if these component variables are standardised by the square roots of their very different eigenvalues prior to clustering. In such circumstances size would have an equal weighting with other dimensions



Table 4.2 Experiments Conducted

Experiment	Description	Experimental Analyses
A	Evaluation of changing the number of iterations in clustering	I, II, III
B	Evaluation of changing the 'seeding' number of clusters	I, IV, V
C	Evaluation of changing the number of component variables in clustering	I, VI, VII
D	Effect of standardisation v. unstandardisation of variables	I, VIII, IX, X
E	Effect of using <i>a priori</i> classification codes to seed analysis	I, XI
F	Effect of using variable sub-sets	I, XII, XIII, XIV, XV
G	Effect of varying classical discriminant analysis parameters	I, XVI to XXVI
H	Comparison of classical with non-parametric discrimination	I, XXVII

represented by lower numbered components and cluster analyses may produce results not unlike those obtainable when the components of the correlation matrix are involved.

The investigation of dimensionality was based substantially on the latent roots of the 53 variable correlation matrix. It is evident from Table 4.3 that according to Kaiser's criterion, approximately 20 components would be seen as significant, accounting for some 70 per cent of the variance in the 53 standardised variables. However, inspection of 'scree-test' plot of the logarithms of the eigenvalues against component numbers in Figure 4A, suggests at most 10 or so significant components explaining approximately 50 per cent of data variability. For the variable subsets, the corresponding figures would be 10 and 5 components. Although there is some uncertainty over this issue, the author tends to favour scree-test findings, based on a spirit of caution in defining dimensionality. If there is unique variance in later components, this is likely to be sample specific, thus reducing classification stability between different data sets. This point notwithstanding, the effect of using 5, 10, 15 and 20 component variables in clustering is investigated below.

The significant factor loadings shown in Tables 4.4 and 4.5, are derived from eigenvector elements and indicate the simple correlations between operational variables and components. Only loadings found to be significant using the Burt-Banks formula have been tabulated. In the first component, loadings of 0.14 or higher were defined as significant at better than a 0.1 per cent level, by the conventional t-test criterion (485 degrees of freedom).

On grounds of space economy, only the loadings of the first 10 components are shown for the main analysis, and the first 5 in other cases. These should suffice to illustrate the interpretability of the



Table 4.3 Sample A Principal Component Analysis - Eigenvalues

Component	All Variables Correlation Matrix		All Variables Covariance		Odd Variables Correlation Matrix		Even Variables Correlation Matrix	
Number	Latent Root ( $\lambda$ )	Cum % of Variance	Latent Root ( $\lambda$ )	Cum % of Variance	Latent Root ( $\lambda$ )	Cum % of Variance	Latent Root ( $\lambda$ )	Cum % of Variance
1	6.034	11.4	755.9x10 <sup>4</sup>	85.6	3.289	12.2	3.536	13.6
2	3.269	17.6	126.0x10 <sup>4</sup>	99.8	2.260	20.6	2.500	23.2
3	2.442	22.2	3662.1	99.9	1.689	26.8	1.841	30.3
4	2.207	26.3	2070.9	99.9	1.510	32.4	1.527	36.2
5	2.022	30.1	1194.3	99.9	1.410	37.6	1.483	41.9
6	1.902	33.7	987.8	99.9	1.316	42.5	1.376	47.2
7	1.807	37.1	834.1	99.9	1.225	47.0	1.108	51.4
8	1.757	40.5	758.2	99.9	1.209	51.5	1.080	55.6
9	1.649	43.6	740.2	100.0	1.070	55.5	1.056	59.7
10	1.553	46.5	652.6	100.0	1.047	59.4	0.965	63.4
11	1.449	49.2	564.0	100.0	1.034	63.2	0.910	66.9
12	1.363	51.8	451.1	100.0	0.946	66.7	0.891	70.3
13	1.260	54.2	414.2	100.0	0.905	70.0	0.851	73.6
14	1.234	56.5	362.4	100.0	0.844	73.2	0.764	76.5
15	1.173	58.7	270.4	100.0	0.786	76.1	0.729	79.3
16	1.131	60.9	241.0	100.0	0.781	79.0	0.684	81.9
17	1.092	62.9	228.2	100.0	0.759	81.8	0.634	84.4
18	1.076	65.0	204.1	100.0	0.727	84.5	0.622	86.8
19	1.057	66.9	182.0	100.0	0.633	86.8	0.572	89.0
20	1.013	68.9	175.3	100.0	0.607	89.1	0.515	90.9
21	0.977	70.7	151.6	100.0	0.566	91.2	0.481	92.8
22	0.984	72.5	136.9	100.0	0.507	93.0	0.461	94.6
23	0.894	74.2	100.0	100.0	0.482	94.8	0.440	96.3
24	0.860	75.8	84.3	100.0	0.444	96.5	0.401	97.8
25	0.857	77.4	64.9	100.0	0.405	98.0	0.352	99.2
$\sum_{j=1}^p \lambda_j$	53		8833872		27		26	

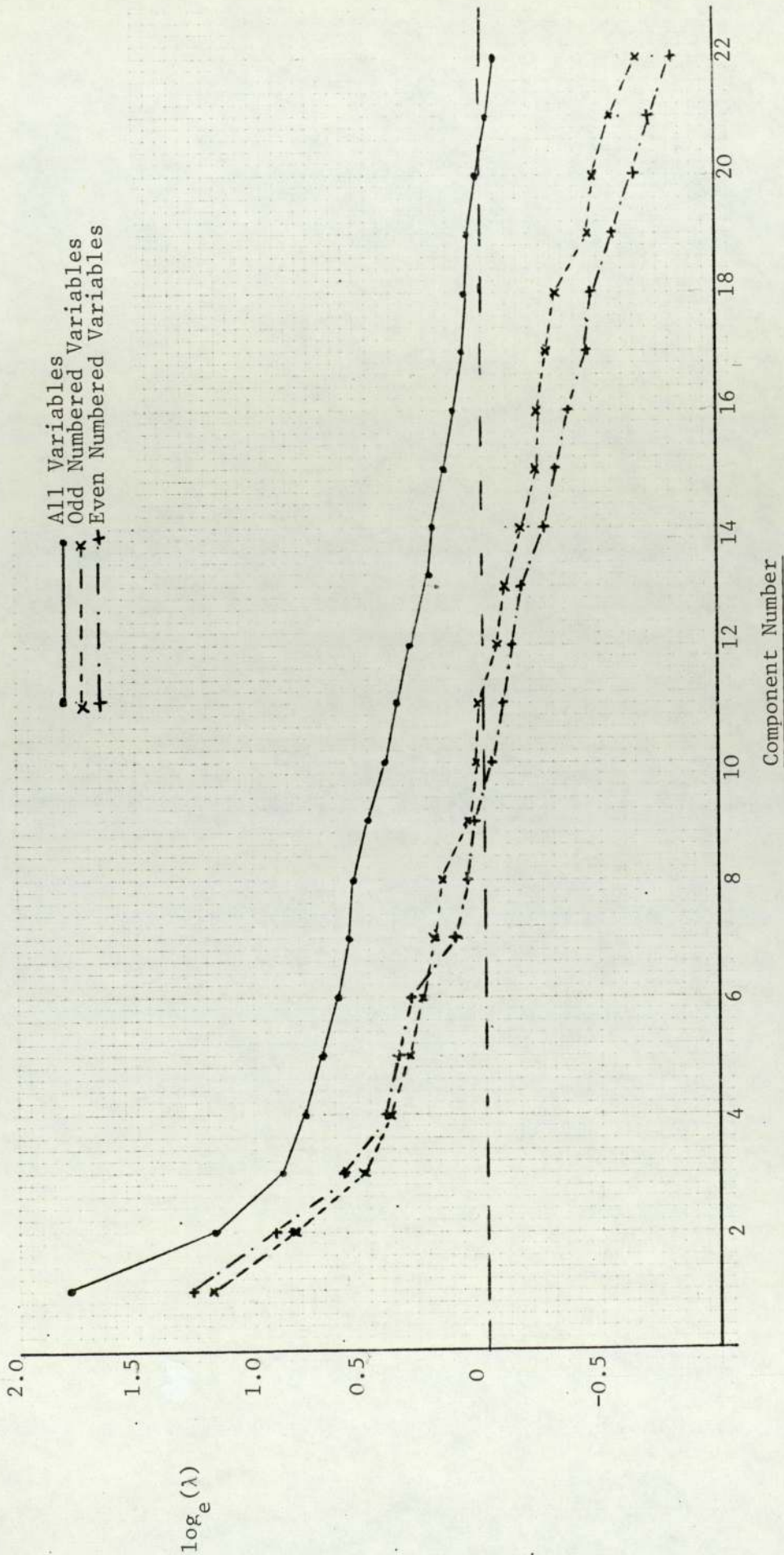


Figure 4.A Scree Test Plot of Eigenvalues of the Correlation Matrix - Sample A.



dimensions or source variables derived and for comparison between the different approaches.

From the first section of Table 4.4, it is evident that Components 1 and 2 are both size/holding technology measures but distinguished by differences in land use, livestock, land tenure, management and labour/capital inputs. Figure 4B shows in vector diagram form the relationship of operational variables to these first two components. Although certain variable numbers are omitted in order to avoid over-printing the general size-related features of Component 1 are clearly shown. In addition to the variables measuring total holding land area, total livestock and total capital and labour inputs, it can be seen that tractor, harvester and other capital goods ownership and the number of co-operative memberships are all positive correlates of component (factor) number one. The inverse relationships of labour inputs per hectare and the proportion of holders with non-holding employment to this component confirms the size syndrome interpretation. That component number two is more related to management practices and control within a size context is revealed by the weighting of H01, H03, and W02, compared with other variables. By and large, the corporately-owned holdings are larger than holder-managed farms and, having no specific holder, show a low proportion of male holders and a low percentage of labour provided by the holder's family.

Component 3 represents a continuum from highly intensive 'horticultural-type' holdings to mixed farms with an emphasis towards dairy herds and cattle rearing. The characteristics of component 4 are shown by the high negative weighting of S03, L07, L08, A05, A07 and H06, and the positive weighting of S04, L01, L05, L13, M02, M04, M07 and G03. The first group suggests small pig farms relying on subsistence plots and a holder with other non-holding employment, while the second



Table 4.4 Eigenvectors of 53 Variable Matrices - Sample A

Variable	53 Variables-Correlation Matrix-Significant Factor Loadings										53 Variables-Covariance Matrix Normalised Eigenvectors					53 Variables-Covariance Matrix Significant Factor Loadings				
	Compo- nent 1	Compo- nent 2	Compo- nent 3	Compo- nent 4	Compo- nent 5	Compo- nent 6	Compo- nent 7	Compo- nent 8	Compo- nent 9	Compo- nent 10	Compo- nent 1	Compo- nent 2	Compo- nent 3	Compo- nent 4	Compo- nent 5	Compo- nent 1	Compo- nent 2	Compo- nent 3	Compo- nent 4	Compo- nent 5
S01	0.68	0.41	-	-	-	-	-	-	-	-	0.56	0.83	0.00	0.00	0.00	0.60	0.34	-	-	-
S02	0.59	0.45	-	-	-	-	-	0.16	-	-	0.53	-0.56	-0.00	-0.00	-0.00	0.96	-0.26	-	-	-
S03	0.54	-	-	-0.42	-	0.26	-0.19	-	0.19	-0.19	0.00	0.00	-0.05	0.00	-0.02	0.42	0.21	-	-	-
S04	0.58	0.57	-0.18	0.27	-	0.15	-	-	-	-	0.00	0.00	-0.00	-0.00	0.00	0.58	-	-	-	-
S05	0.83	-	-0.22	-	-	-	-	-0.16	-	-	0.00	0.00	-0.01	-0.00	-0.00	0.53	0.16	-0.16	-0.30	-
L01	0.20	-	0.19	0.22	-	-	-	-	-0.17	-	0.00	0.00	-0.00	-0.00	-0.00	-	-	-	-	-
L02	0.19	-0.22	-0.33	-	-	-	-	-	-0.40	-	-0.00	0.00	-0.04	-0.00	0.06	-	-	-0.21	-	0.16
L03	0.18	-	-	-	-	-	-	0.16	-0.24	-	0.00	-0.00	-0.00	-0.00	0.00	0.18	-	-	-	-
L04	-0.14	-	-0.66	-	-	-	-	-	0.36	-	-0.00	-0.00	-0.02	-0.02	0.03	-	-	-	-	-
L05	-	-	-	0.39	-	-	-0.47	-	-	-	0.00	0.00	0.00	-0.02	0.02	-	-	-	-	-
L06	-	0.14	-	-	-	-	-	-	0.28	-	0.00	-0.00	0.01	-0.00	0.00	-	-	0.14	-	-
L07	-0.22	-	-	-0.24	-	0.31	-	-	-	-	-0.00	-0.00	0.01	-0.01	0.00	-	-	-	-	-
L08	-	-	0.20	-0.32	-	-0.21	0.27	0.33	0.21	-	-0.00	0.00	-0.02	-0.01	-0.05	-	-	-	-	-
L09	-0.28	-	-	-	-	0.28	-	-0.21	-	-0.21	-0.00	-0.00	0.05	0.00	0.02	-	-	0.20	-	-
L10	-0.41	0.30	-	-	0.20	-	-	-	-	-	-0.00	-0.00	0.14	0.05	0.19	-	-	0.35	-	0.27
L11	-0.20	0.14	-	-	-	0.23	-	-	-	-	-0.00	-0.00	0.02	-0.00	0.01	-	-	0.16	-	-
L12	-0.15	0.26	-	-	-	0.30	-	-	0.32	-	-0.00	0.00	0.06	0.02	0.00	-	0.17	0.25	-	-
L13	-0.23	0.16	-	0.36	0.23	0.15	-0.27	-	0.26	-0.21	-0.00	0.00	0.00	-0.00	0.00	-	-	-	-	-
L14	0.18	-0.21	-	-	-	-0.17	-0.28	-	-	-0.26	-0.00	0.00	-0.00	-0.00	-0.00	-	-	-0.18	-	-
A01	-	-	-	0.15	-	-	0.16	-	-	-0.49	-0.00	-0.00	-0.00	0.00	0.02	-	-	-	-	-
A02	0.41	-0.22	0.32	-	-0.27	-0.16	-	0.15	0.24	-	0.00	0.00	-0.16	-0.09	-0.32	0.14	-	-0.32	-	-0.38
A03	0.40	-0.20	0.33	0.19	-	-	-	-	-	-	0.00	0.00	-0.12	0.02	-0.11	0.18	-	-0.27	-	-
A04	-	-	-	-	0.15	-	-	0.17	-	0.32	0.00	-0.00	0.03	0.01	0.03	-	-	0.14	-	-
A05	-	-	-0.22	-0.17	-	0.25	-0.30	-0.37	-	-0.19	-0.00	0.00	0.02	0.04	0.08	-	-	-	-	-
A06	-	0.14	-	-	-	-	-	0.15	-0.20	-	-0.00	-0.00	0.03	-0.02	0.02	-	-	-	-	-
A07	-	-	-	-0.59	-0.20	0.19	-0.35	-	-	-0.31	-0.00	0.00	-0.00	-0.00	0.00	-	-	-	-	-
W01	-0.23	-0.15	-0.35	-	-	-	-	-	0.20	-	-0.00	-0.00	-0.00	-0.01	0.01	-0.15	-	-	-	-
W02	-	-0.16	0.22	-	-	-	-	-	-	-	-0.00	0.00	-0.15	-0.01	-0.23	-0.30	-	-0.31	-	-0.27
W03	0.23	-	-	-	-	-	0.16	0.24	0.17	-	0.00	0.00	-0.03	-0.05	-0.04	0.16	-	-	-	-
W04	0.30	-	-	-0.22	0.17	-	-	-	0.16	-	0.00	0.00	-0.07	0.10	-0.31	0.15	-	-0.17	0.18	-0.41
W05	-	-	-	-0.15	0.60	-0.25	-	0.33	-	-	0.00	-0.00	-0.12	0.50	0.59	-	-	-0.21	0.68	0.60
W06	-0.18	-	-	-	-0.37	0.24	-0.30	0.55	-0.27	-	-0.00	-0.00	0.15	-0.80	0.24	-	-	0.24	-0.92	0.21
W07	-0.24	-	-	-	-0.34	-	0.45	-0.45	-	-	-0.00	-0.00	0.04	0.22	-0.50	-0.17	-	-	0.36	-0.62
M01	0.71	0.21	-	-	-	-	-	-	-	-	0.00	0.00	-0.00	0.00	0.00	0.45	0.17	-0.15	-	-
M02	-0.14	-	-0.50	0.28	-	0.19	-	-	-	0.22	-0.00	-0.00	0.00	-0.00	0.00	-	-	-	-	-
M03	0.53	0.15	-	-	-	0.22	0.16	-0.23	-	-	0.00	0.00	-0.00	0.00	-0.00	0.36	0.15	-	-	-
M04	0.39	-0.26	-	0.18	-	-0.17	-0.22	-0.19	-0.27	-	0.00	0.00	-0.00	-0.00	-0.00	-	-	0.25	-	-
M05	0.61	-	0.15	-	-0.17	-	0.16	-	0.18	-	0.00	0.00	-0.00	0.00	-0.00	0.30	0.22	-0.23	-	-0.16
M06	-0.14	-	0.36	-	-	-	-	-	0.41	0.32	-0.00	-0.00	0.00	0.01	0.01	-	-	-	-	-
M07	-0.33	0.23	-	0.20	-	-	0.33	-0.18	-	-0.47	-0.00	0.00	0.00	0.00	0.00	-	-	0.18	-	-
M08	-0.24	-0.30	-	-	-	-	-	-0.24	-0.16	0.18	-0.00	-0.00	-0.00	-0.00	0.01	-0.33	-	-	-	-
H01	-	-0.65	-	-	-	0.28	-	-	-	-	-0.00	0.00	-0.00	-0.00	-0.00	-0.16	-	-0.22	-	-
H02	0.32	0.15	-0.42	-	-	-	0.31	-	-	-0.16	0.00	0.00	-0.00	0.00	0.00	0.21	-	-	-	-
H03	0.18	-0.59	-	0.16	0.23	0.54	0.29	-	-	-	-0.00	0.00	-0.00	-0.00	-0.00	-	-	-0.26	-	-
H04	0.17	0.21	-	-	-0.37	-0.51	-0.26	-0.24	-	-	-0.00	-0.00	0.00	0.00	-0.00	-	-	-0.15	-	-
H05	-0.31	-	-	0.32	-0.14	-	0.22	-	-	-	-0.00	-0.00	0.06	-0.00	-0.13	-0.15	-	0.30	-0.21	-0.36
H06	-0.34	-0.23	-	-0.32	0.34	0.22	-	-	-	-	-0.00	-0.00	0.00	0.00	0.00	-0.27	-	-	-	0.18
G01	-0.46	0.42	-	-0.17	-0.17	0.19	-	-	-0.22	0.21	-0.00	-0.00	0.73	0.13	-0.03	-	-	0.99	-	-
G02	0.39	-0.49	-	-	-	-0.32	-	0.23	-	-	0.00	0.00	-0.57	-0.12	0.11	-	-	-0.86	-	-
G03	-0.15	-	-	0.34	0.24	-	-	-	0.33	-0.33	-0.00	0.00	-0.01	0.02	0.01	-	-	-	-	-
G04	0.23	-	-0.44	-0.15	-0.18	-	0.19	0.24	-	-0.26	0.00	-0.00	-0.00	-0.00	0.00	-	-	-	-	-
G05	0.52	-	-0.18	-	-0.12	-	-	-0.25	-	-	0.00	0.00	-0.00	0.00	-0.00	0.24	-	-0.15	-	-
G06	0.20	-	-0.26	-	-	-	-	-	-	-	0.00	0.00	-0.00	0.00	0.00	0.20	-	-	-	-



Table 4.5 Eigenvectors of Variable Subsets - Sample A

Variable	Odd-Numbered Variables Correlation Matrix Significant Factor Loadings					Even-Numbered Variables Correlation Matrix Significant Factor Loadings				
	Component 1	Component 2	Component 3	Component 4	Component 5	Component 1	Component 2	Component 3	Component 4	Component 5
S01	0.64	0.21	0.45	-	0.16	-	-	-	-	-
S02	-	-	-	-	-	0.56	0.46	-	0.16	-
S03	0.55	0.18	0.30	-	-	-	-	-	-	-
S04	-	-	-	-	-	0.58	0.36	0.19	0.17	-
S05	0.76	-0.26	-	0.18	0.21	-	-	-	-	-
L01	-	-	-	-	-	0.22	-	0.20	-	0.23
L02	0.24	-0.39	-0.25	0.36	-	-	-	-	-	-
L03	-	-	-	-	-	0.18	-	-	0.18	-
L04	-0.20	-0.68	0.22	-0.32	-	-	-	-	-	-
L05	-	-	-	-	-	-	-	0.36	-0.19	0.20
L06	-0.18	-	-	0.27	-	-	-	-	-	-
L07	-	-	-	-	-	-0.24	-	-0.26	-	-
L08	-	0.27	-	-0.36	0.54	-	-	-	-	-
L09	-	-	-	-	-	-0.30	-	-	0.19	-0.44
L10	-0.47	-	0.20	0.22	-	-	-	-	-	-
L11	-	-	-	-	-	-0.22	-	-	-	-
L12	-0.20	-	0.48	-	-	-	-	-	-	-
L13	-	-	-	-	-	-0.26	0.17	0.43	-0.30	-
L14	0.31	-0.15	-0.23	-	-	-	-	-	-	-
A01	-	-	-	-	-	-	-	0.22	-	-0.50
A02	0.47	0.23	-0.19	-0.44	-	-	-	-	-	-
A03	-	-	-	-	-	0.43	-0.21	0.30	-	0.28
A04	-0.18	-	0.21	0.26	-	-	-	-	-	-
A05	-	-	-	-	-	-	-	-0.61	-	-0.27
A06	-	-	-	-	-	-	-	-	-	-
A07	-	-	-	-	-	-	-0.16	-0.55	-0.19	-
W01	-0.26	-0.40	-	-0.33	-0.15	-	-	-	-	-
W02	-	-	-	-	-	-	-0.87	-	-	-
W03	0.28	-	0.20	-0.16	0.15	-	-	-	-	-
W04	-	-	-	-	-	0.41	-	-0.15	-0.47	-0.20
W05	-	-	-	0.42	-0.31	-	-	-	-	-
W06	-	-	-	-	-	-0.26	-	-	0.49	0.29
W07	-0.23	-	-0.22	-0.27	0.20	-	-	-	-	-
M01	-	-	-	-	-	0.74	0.19	-	-	-
M02	-0.21	-0.50	0.18	-	0.30	-	-	-	-	-
M03	-	-	-	-	-	0.61	-	-	0.20	-0.24
M04	0.49	-0.21	-0.39	-	0.18	-	-	-	-	-
M05	-	-	-	-	-	0.61	-	-	-	-
M06	-0.23	-0.34	0.39	-0.17	-	-	-	-	-	-
M07	-	-	-	-	-	-0.36	0.23	0.21	0.18	-0.61
M08	-0.26	-0.64	-0.28	-	0.15	-	-	-	-	-
H01	-	-	-	-	-	-	-0.80	0.22	0.21	-0.15
H02	0.33	-0.32	0.35	-	-0.27	-	-	-	-	-
H03	-	-	-	-	-	0.19	-0.66	0.27	-	-
H04	-0.14	-	-	-0.24	0.36	-	-	-	-	-
H05	-	-	-	-	-	-0.34	-	-	0.59	-
H06	-0.38	-	-	0.36	-0.47	-	-	-	-	-
G01	-	-	-	-	-	-0.43	0.24	-0.27	0.23	-
G02	0.42	-0.23	-0.35	-	-0.32	-	-	-	-	-
G03	-	-	-	-	-	-0.15	-	0.50	-0.37	-0.27
G04	0.32	-0.38	0.26	-0.16	-0.35	-	-	-	-	-
G05	-	-	-	-	-	0.53	-	-	0.20	-0.24
G06	0.25	-0.21	0.15	0.21	-	-	-	-	-	-





tends towards share cropping production of arable and successive and intermediate crops with cultivators and draft animals, rather than tractors or harvesters and a limited amount of non-intensive cattle rearing. Component 5 appears to separate older holder-owners concerned with dairy herd operations on a fairly traditional basis, from sheep and goat rearing sharecropping operations run by younger holders many of whom also have outside work. Components 6 to 10 emphasise variously subsistence holdings with higher proportions of unused agricultural land and other land combined with the cultivation of vines, several combinations of livestock rearing, and age differences in the holder and the regular farm labour used on the land.

Comparison of factor loadings between the analysis on all variables with the two analyses using alternate variable sub-sets, reveals remarkable similarity, not only in the pattern of loadings but also their magnitude. This in itself suggests stability in the underlying dimensions of farm-to-farm resemblances/differences present in the data which are reflected in a variety of measurable characteristics. Although not as noticeable in detail, the set of five factor loadings obtained from the component analysis of unstandardised operational variables also highlight the main size, tenure, land use, and age distribution dimensions, which confirms the earlier observation that upon standardisation the analysis of components of the covariance matrix may produce not radically different clustering results.

#### 4.3 Experimental Analysis I - Clustering Results

The clustering results for Analysis I are summarised in Tables 4.6 to 4.9, while an example of the typical output from CLUSTPROG is given in Appendix D. From Table 4.6 it may be observed that with the seeding number of 30 clusters, the within class sum of squares represents 30.6 per cent of

the total variance contained in the first 10 components, so that the classification into 30 groups *explains* 69.4% of these components' variability. At 20 and 10 clusters, the corresponding figures are 65.0 per cent and 51.9 per cent respectively, showing that the explanatory power falls much more slowly than the number of classes.

When it is remembered that the first 10 components of the correlation matrix themselves account only for 50 per cent of the variances of the standardised operational variables, the meaning of the figures in the third column of Table 4.6 become more apparent. They show the explanatory power of the cluster configurations determined from the 10 component variables but with respect to the full set of 53 operational variables. Although only between approximately a third and a quarter of the total sample variance is explained by the classification of farms into 20 to 10 groups, these figures should be compared with the *a priori* scheme described in Chapter III. For this sample, the explanatory power of the 17 class, *a priori* method was only a little over 20%. With the same number of classes the cluster classification gives an explanatory power of nearly 34 per cent which represents a two-thirds improvement over the *a priori* approach. It seems that the data based method performs significantly better than the much debated system suggested by the "Group of Experts Farm Typology". That the two are quite fundamentally different in allocating holdings to classes, is illustrated in Table 4.7, which cross-tabulates 20 cluster classes against the 17 *a priori* classes. Only in the case of Horticulture (Cluster Class 7 and A Priori Class IV) do the classifications approximately correspond.

The Beale F-tests reported in Table 4.6 would indicate that from a statistical viewpoint 16 clusters of holdings are better than 15, 11 are better than 10, and 9 are better than 8. Remembering, however that the test is not rigorously based, it is preferable to rely more on the trends



Table 4.6 Summary of Cluster Analysis Results - Analysis I

No. of Clusters (Classes)	Within Group Sum of Squares	Beales F Test	Explanatory Power of Classification (%)
30	3633	-	
29	3635	1.79	
28	3695	1.51	
27	3748	1.39	
26	3799	1.57	
25	3859	1.92	
24	3936	1.44	
23	3997	0.74	
22	4030	2.03	
21	4124	1.36	
20	4191	1.40	35.5
19	4264	1.62	35.1
18	4354	1.95	34.3
17	4470	1.93	33.6
16	4594	2.44*	32.6
15	4764	2.29	31.5
14	4939	1.80	31.1
13	5091	1.92	30.3
12	5270	2.04	29.4
11	5482	2.40*	27.9
10	5763	2.25	26.5
9	6067	2.33*	
8	6434	2.25	
7	6856	1.77	
6	7261	1.62	
Total Sum of Squares	11980	*Significant at 1% level	

*A Priori Classification - Class Number*

	I	II	III	IV	V	VI	VII	VIII	IX	X	XI	XII	XIII	XIV	XV	XVII	Total
1	1	1	6				1	1	1	11		3					24
2	1		13			2	4			16	1	1				1	39
3		2	7		1									4	1		15
4	1		5		6		2	3							2	5	24
5	5	1	4		3		5	3	3	3	1	1	2		4	1	33
6	4		13				3		3				1		2	2	28
7				8		1										1	10
8					6	5		1					2		1	2	17
9	3		1			3	5		4	2	2					5	25
10	1		8		1				1				2				13
11			2		1								2			2	7
12	1		10			5	11		16	1	1	3			1		48
13						10	4				1						15
14		5	5														10
15	1	1	14			2	5	1	15			3			3		45
16			8			1	6		16	1						4	36
17	1	2	5		4	3	8	1	4			1			2	2	33
18			1		3	8	2	3	1			1	4			7	30
19	1		4		4	6	3	3	4				1		1	2	29
20					1			5									6
Total	20	12	106	8	10	34	32	59	21	94	7	15	14	4	17	34	487

Experimental Analysis I - Class Number

Table 4.7 Comparison of Cluster and A Priori Schemes





Table 4.8 The Nature of Cluster Fusions\*

No. of Clusters	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
20	24	39	15	24	33	28	10	17	25	13	7	48	15	10	45	36	33	30	29	6
19	24	42	15	24	53	28	10	17	26	13	7	51	15	10	45	33	39	29	6	
18	24	43	16	24	52	29	10	15	26	10	55	15	10	45	36	42	29	6		
17	54	16	24	52	29	10	15	26	10	63	15	12	47	37	41	29	7			
16	51	17	24	60	29	10	30	10	65	15	12	48	37	43	29	7				
15	48	61	24	28	10	33	10	72	16	13	48	41	47	29	7					
14	57	57	25	28	10	36	10	72	13	53	43	47	29	7						
13	58	60	25	31	10	37	10	71	23	74	52	29	7							
12	76	105	24	34	10	34	10	28	80	48	29	7								
11	91	98	27	36	10	34	29	77	51	27	7									
10	107	108	27	37	12	34	76	52	27	7										

\* Only the strongest links between clusters are shown in this simplified diagram.





73 per cent are in the 45-65 age group, which reflects the age of holders at 57 years. Again the holdings are exclusively holder-managed by male holders, 26 per cent of whom have other gainful work. There is an almost even split between owned and rented agricultural land and none is held as a sharecropper. At first sight, capital intensitivity appears quite low with only 21 per cent owning a tractor, 13 per cent with cultivators and none with owned harvesters or milking machines. However, 89 per cent make use of shared or rented equipment, and for their size machine accesses per 10 hectares are high at 7.4. 67 per cent of the holdings in the class are in the Benelux countries.

Class 3    Large, Corporately Owned, Unintensive Farms  
(24 holdings)

The conspicuous features of these large holdings (54 hectares) are that they are mainly corporately owned (83%), they have a higher proportion of other land (18%) and appear unintensively worked with only 17.5 standard head of livestock and an average of 2.4 machine accesses per holding. With the biggest single land use being pasture (40%), the absence of intensive husbandry appears evident. Of course, the quality of the pasture determines the density of livestock and from the relative importance of sheep and goats (11.6% of total standard livestock), it might be inferred that rougher grazing figures significantly in their pasture area. The two other largest land uses on these holdings are for permanent crops (27%) and cereal production (17%). Although large, only 70% of these holdings own a tractor, 17% a cultivator and 8% any type of harvester. While 54 per cent use shared or agency machinery, 12.5 per cent still employ draft animals in working the land. All in all, a picture of rather unsophisticated farming emerges. The holdings which are almost exclusively owned by the corporate holders are mainly found in Italy (46%).



Class 4 Medium Cereal/Arable Farms - Sharecropping  
(28 holdings)

All of these medium sized holdings (14 hectares) are in Italy. Livestock rearing is insignificant with only 13 per cent of agricultural land being permanent pasture. Like Class 3 holdings, they have a relatively high proportion of marginal land (4%) and other land (19%). Cereal production is the single major activity (40% of land) with other arable production taking up a further 36 per cent and vineyards and other permanent crops 8.5% together. A notable feature of the class is that 82% of holdings grow successive and intermediate crops, and 43% permanent and associate crops. Dairy cows and other cattle rearing represent 76% of their limited livestock. Once again, capital intensity is low on all counts, with the exception of cultivator ownership at 29 per cent of holdings. The exclusively male, agriculturally uneducated, holder-managers own 54% of their land and share-crop a further 39%. Only 7% keep accounts, 18% have other employment, and very little commercial activity exists in terms of contracted crops or co-operative membership.

Class 5 Very Small Horticultural Holdings  
(10 holdings)

Horticultural activities completely separate this class of market-gardening operations (1.2 hectares) from other holdings. 78 per cent of land is used for horticulture while a further 12 per cent is under permanent crops. With the exception of a small amount of "other arable crops", none of the traditional farm crops (eg cereal, roots) are grown. The total production system with high labour inputs in total (2.5 A.W.U.'s) and per 10 hectares (30 A.W.U.'s), high capital inputs (12.7 machine accesses per 10 hectares), 24 per cent of used agricultural land under glass and 80 per cent of holdings owning cultivators, is consistent with this type of agricultural activity. As would be expected, all the

holdings in this horticulture class are holder-managed, by above averagely-educated managers, 60 per cent of whom keep accounts. The holdings are evenly distributed among the six EEC countries in 1966.

Class 6 Small Mixed Arable/Cattle/Permanent Crops - Elderly Holders  
(33 holdings)

The outstanding characteristics of this class are the high proportion of vineyards (26% of land) and the fact that almost all the labour is provided by older (69 years) owner-holder-managers. In practice, these are small, mixed farms (3.3 hectares) with on average 39 per cent permanent pasture, 40 per cent arable land and 12 per cent of other permanent crops in addition to the vineyard area. Within this summary picture there are many variations in land use. However, there does appear to be generally a low level of capital inputs with only 12 per cent owning tractors, 27 per cent cultivators, 3 per cent harvesters and milking machines, and 27 per cent relying on draft animals. Completing the impression of tired and old-fashioned land husbandry is the fact that only 18 per cent keep accounts, there is no contracted production, and the agricultural education of the holders is typically low or non-existent. Holdings of this type are found in all countries and are representative of the low productivity units with older holders reported in Britain by the Agricultural EDC (1973).

Class 7 Small Permanent Crop Farms - Unintensive Sharecropping  
(10 holdings)

70 per cent of the agricultural land of these farms is held as a sharecropper and only 20 per cent is owned. All show a startling absence of any owned capital equipment. 90 per cent use draft animals and indeed horses represent 40 per cent of the total standard livestock. The predominant land use is the growing of vines and permanent crops (together 52%). Cereal production represents a further 28% of land use,



while 9 per cent of total agricultural land is unused and 16 per cent of the total holding area is woodland and other land. None of the managers has any relevant education, only 10 per cent keep accounts, and there is no co-operative membership or contracting of crops at all. 30 per cent of holders have work in addition to the holding. Italy is again the main location of such holdings.

Class 8 Medium Dairy/Cattle/Cereal Farms  
(72 holdings)

This large class of typical medium sized mixed arable/dairy holdings has 20 hectares of land on average. Nearly half the land is under grass, 30 per cent produces various cereals, and a further 20 per cent is used for other arable crops. Of the livestock, 47 per cent are dairy cows, 35 per cent other cattle, and 13 per cent pigs. 60 per cent of the labour is in the 45-65 age group, as are the majority of holders. Capital equipment ownership, sharing and renting is moderately high, and land tenure a mixture of ownership and renting. In general, a group of "average" holdings found in most countries of the EEC.

Class 9 Medium Dairy/Cattle Farms  
(16 holdings)

Of a similar size to Class 8, these holdings have 19 hectares of land, 99.1 per cent of which is under permanent pasture. Consistent with this land use situation is the fact that 71 per cent of livestock is dairy cows and a further 18 per cent other cattle. Because of the cattle rearing nature of these farms, there is little ownership of tractors, cultivators and harvesters. 56 per cent of holdings do own milking machines and 63 per cent make use of shared or rented machinery. Land is mainly rented (83%) by the holder-managers of these farm units, who have a higher-than-average educational level. Accounts are kept in 75 per cent of cases, and only 6 per cent of holders have off-farm employment. 11 of these 16 holdings are in Holland.

Class 10 Large Arable Farms  
(13 holdings)

With over 60 hectares of land this class of holdings is made up of the biggest farms and the most committed to arable crop production. (Cereal 44%, Root Crops 34%, Other Arable 6.4%, and Industrial Plants 4.2%). Of the 3.9 annual work units' labour input, only 40 per cent is family labour on exclusively holder-managed farms. As might be expected, capital equipment levels are high with 92% of farms owning tractors, 62% harvesters, and 100% making use of shared and rented appliances. The low emphasis on dairy cattle (13%) is reflected in a low ownership of milking machines (7.7% of holdings). Most managers have at least secondary level education and are younger than the sample average at 48 years. 85 per cent keep accounts for their mainly rented farms (67% rented), and make considerable use of co-operatives (3 on average) and contracting arrangements for produce (62%). Again, a high proportion (69%) are in Holland.

Class 11 Medium Dairy/Cereal Farms - Young Holders  
(48 holdings)

The youth of the holders (37 years) characterises these mixed cattle/cereal producing farms of medium size (21 hectares). Cereal production (34%) and permanent pasture (43%) are the main land uses. Of the 24 head of standard livestock, 80 per cent are dairy cows and other cattle, and 17 per cent pigs. Reflecting the holders' age, the regular labour is mainly under 45 years of age. More of the land is rented (70%) than owned (29%). Educational levels of holders are not especially high nor are the number of holdings keeping accounts (23%). Tractor ownership is high at 83 per cent and 50 per cent own milking machines, although in other respects there is obvious heavy reliance on sharing and renting capital equipment (94% doing this). With the exception of Italy, the geographical distribution of these holdings is even and widespread.



Class 12 Small/Medium Mixed - Young Holders  
(41 holdings)

In many respects this class is similar to Class 11 in being mixed arable/pasture with young holders. The major differences are the holding size (6 hectares) and the consequential lower level of machine ownership and access, a much higher proportion of outside work by the holders (68%) and a lower level of holdings with accounts (7%). The land holding is more evenly distributed between ownership and tenancy than in Class 11, although the holdings have a similar geographical spread.

Class 13 Small/Medium Livestock/Permanent Crops/Arable  
(47 holdings)

Of not dissimilar average size to Class 11 and 12, the farms in this class have a lower emphasis on pasture (32.6%) and much more concentration on vineyards and other permanent crops (9.4% and 28% of land use respectively). Arable crops amount to only 23 per cent of used agricultural land. As is noticeable in certain other classes with a high Italian representation (59% in this case), cattle rearing is relatively less important than sheep and goats (at 14% the highest of all groups) and in this case poultry (also 14%). The land is mainly owned (93%) and the male holder-managers are older than in the previous two classes at 55 years. Again, a high proportion of holders work in addition to running the holding (62%), which is perhaps associated with the 6 per cent keeping holding accounts. Both membership of co-operatives and the contracting of crops is low, as is somewhat unexpectedly the growing of permanent and associated crops.

Class 14 Small/Medium Cattle/Arable/Farms - Female Holders

27 of the 29 holdings in this group are held by women with no agricultural education at all. Only 3 per cent keep accounts (the lowest proportion in any class) which together with an average age of 58 suggests that a high proportion may be widows who have taken over the running of these 7 hectare farms on the death of their husbands. Representation of holdings in the class across the European countries is consistent with this interpretation as is the predominance of permanent pasture (49%) over other land uses. Although cattle rearing (48% of livestock) is important, pigs and poultry (together 16%) are also significant here. Land is 83 per cent owned by holders in this class.

Class 15 Small/Medium Pig/Subsistence Farms  
(7 holdings)

Averaging only 7.7 hectares these holdings are noteworthy in having 93 standard livestock (22.4 per hectare), 91.6 per cent of which are pigs. This suggests that the 47 per cent of permanent pasture is not intensively used for cattle rearing and that other than subsistence plots (18.1% of land) and vineyards (14.2%) cultivation is a fairly peripheral activity. This is reinforced when one observes that 71 per cent of the holder managers have employment outside the holdings. Nevertheless, 57 per cent (ie four holdings) keep accounts and two of the seven have contracted their output. In this group, characterised by the special importance of pigs, there is undoubtedly a mixture of subsistence peasant holdings and intensive pig units producing bacon and pork commercially (eg the 4 in Holland).

That the clustering has achieved a meaningful and useful partitioning of holdings is evident. Quite distinctively different production units have emerged in terms of a range of operational variables. Size land use, animal husbandry, land tenure and management types and



CLUSTER CLASSIFICATION - SAMPLE A

GROUP MEANS		VARIABLES										SIZE						
GROUP	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05								
1	0.4349E	04	0.3723E	02	0.2961E	01	0.4136E	02	0.5808E	01	0.2840E	00	0.4063F-01	0.1048E	02	48		
2	0.4091E	03	0.4422E	01	0.1313E	01	0.2737E	02	0.1563F	02	0.1106E	01	0.4710E	01	0.1058E	02	61	
3	0.5390E	04	0.4672E	04	0.1745E	02	0.2748E	01	0.2375F	01	0.1709E	02	0.4065F	01	0.5654E	00	24	
4	0.1401E	04	0.1034E	04	0.5704E	01	0.2418E	01	0.1821E	01	0.4037E	02	0.2890F	01	0.0000E	00	28	
5	0.1217E	05	0.9610E	02	0.6000E-01	0.2484F	01	0.1500F	01	0.0000E	00	0.0000E	00	0.0000E	00	0.7812F	02	10
6	0.3262E	03	0.3125E	03	0.2711E	01	0.1054E	01	0.1344F	01	0.1630E	02	0.2104F	01	0.0000E	00	33	
7	0.3890E	05	0.2736E	03	0.5400E	00	0.1113E	01	0.7000F	00	0.2743E	02	0.2798F	01	0.0000E	00	10	
8	0.1990E	04	0.1821E	04	0.2005F	02	0.2275E	01	0.3406E	01	0.3036E	02	0.7666F	01	0.2432E	00	72	
9	0.1900E	04	0.1782E	04	0.2352F	02	0.1558F	01	0.1687E	01	0.0000E	00	0.2994F	00	0.0000E	00	16	
10	0.6025E	04	0.5558E	04	0.2044E	02	0.3875E	01	0.6154E	01	0.4407E	02	0.3550F	02	0.4151E	01	13	
11	0.2052E	04	0.1970E	04	0.2422E	02	0.1843F	01	0.3708F	01	0.3410E	02	0.1068F	02	0.5725E	00	48	
12	0.5979E	05	0.4953E	03	0.5436E	01	0.1049E	01	0.1390E	01	0.2584E	02	0.9379F	01	0.0000E	00	41	
13	0.7410E	05	0.6034E	03	0.3232E	01	0.1062E	01	0.3830F	00	0.1562E	02	0.4426F	01	0.0000E	00	47	
14	0.6877E	05	0.6051E	03	0.4527E	01	0.1144E	01	0.1345E	01	0.1729E	02	0.6489E	01	0.0000E	00	29	
15	0.7687E	05	0.6747E	03	0.9310E	02	0.1246E	01	0.1000E	01	0.1841E	01	0.3850E	01	0.0000E	00	7	
TOTAL	0.1754E	04	0.1551E	04	0.1475E	02	0.1826E	01	0.2435E	01	0.2610E	02	0.7848E	01	0.3976E	00	487	

CLUSTER CLASSIFICATION - SAMPLE A

GROUP MEANS		VARIABLES										SIZE						
GROUP	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01								
1	0.4469E	00	0.4115E	02	0.0000E	00	0.2185E	00	0.1198E	02	0.0000E	00	0.1250E	00	0.3571E	00	48	
2	0.1104E	01	0.3603E	02	0.1142E	01	0.1260E	01	0.5323E	00	0.5652F	01	0.6557E-01	0.2951E	00	0.7059E	01	61
3	0.2712E	01	0.5979E	02	0.3312E	00	0.2711E	02	0.1767E	01	0.1827E	02	0.1667E	00	0.0000E	00	24	
4	0.5545E	00	0.4654E	00	0.1540E	02	0.5385E	01	0.4032E	01	0.1904E	02	0.8214E	00	0.4286E	00	28	
5	0.6210E	00	0.0000E	00	0.6271E	01	0.1156E	02	0.5966E	01	0.2065F	02	0.1000E	00	0.0000E	00	10	
6	0.8470E	00	0.1783E	01	0.3863E	02	0.1239E	02	0.6088E	00	0.6223F	01	0.9091E-01	0.6061E-01	0.6030E	00	33	
7	0.5222E	01	0.6910E	00	0.7864E	01	0.1201F	02	0.3967E	02	0.9155E	01	0.1550F	02	0.5000E	00	10	
8	0.3754E	00	0.3224E	00	0.4708E	02	0.1716E	00	0.8326E	00	0.7601E	00	0.6710F	01	0.1369E-01	0.2917E	00	72
9	0.0000E	00	0.1437E-01	0.9910E	02	0.0000E	00	0.1169E	00	0.0000E	00	0.6651E	01	0.0000E	00	0.2855E	01	16
10	0.9231E-01	0.1392E	00	0.7628E	01	0.0000E	00	0.0000E	00	0.0000E	00	0.7674E	01	0.0000E	00	0.3846E	00	13
11	0.6331E	00	0.5848E	00	0.4256E	02	0.8090E	00	0.5471E	00	0.7729E-01	0.3634F	01	0.4167E-01	0.3125E	00	48	
12	0.7090E	00	0.1501E	01	0.4948E	02	0.6827E	00	0.9406E	01	0.6629E	00	0.7439E	01	0.4878E-01	0.2439E	00	41
13	0.5549E	01	0.6716E	01	0.3259E	02	0.9415E	01	0.2756E	02	0.6584E	01	0.1645F	02	0.1277E	00	47	
14	0.4352E	00	0.6997E	00	0.4902E	02	0.1358E	01	0.1459E	02	0.1755E	01	0.5509E	01	0.6897E-01	0.3103E	00	29
15	0.0000E	00	0.1812E	02	0.4667E	02	0.1416E	02	0.0000E	00	0.4977E	01	0.1645F	02	0.1429E	00	7	
TOTAL	0.1097E	01	0.1302E	01	0.3938E	02	0.3781E	01	0.8225E	01	0.1734E	01	0.9600E	01	0.1109E	00	487	

Table 4.9 Operational Variable Means - 15 Cluster Classes - Sample A



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES															SIZE
	A02	A03	A04	A05	A06	A07	M01	M02	M03	M04	M05	M06	M07	M08		
1	0.4314E 02	0.5900E 02	0.1646E 00	0.1483E 02	0.2485E 01	0.0754E 00	0.9629E 00	0.8951E 02	0.1080E 02	0.2733E 02	0.9166E 01	0.1250E 02	0.2733E 02	0.48		
2	0.2444E 02	0.2527E 02	0.1434E 01	0.1491E 02	0.3944E 01	0.1059E 01	0.4053E 01	0.9776E 02	0.8716E 01	0.3115E 01	0.9116E 02	0.0000E 00	0.4978E 01	61		
3	0.1056E 02	0.7425E 01	0.1164E 02	0.1553F 02	0.8841E 01	0.7113E 00	0.9475F 00	0.5380E 01	0.3619E 01	0.1486E 02	0.8564E 02	0.1292E 02	0.8274E 01	24		
4	0.3240E 02	0.4375E 02	0.2085E 01	0.7093F 01	0.2080F 01	0.5486E 00	0.3602F 01	0.8564E 02	0.1292E 02	0.8274E 01	0.7687E 02	0.9166E 01	0.1250E 02	28		
5	0.0000E 00	0.0000E 00	0.1000F 02	0.1000E 02	0.0000F 02	0.3800E-01	0.3006F 02	0.7687E 02	0.9166E 01	0.1250E 02	0.9116E 02	0.0000E 00	0.4978E 01	10		
6	0.2056E 02	0.1329E 02	0.6003E-01	0.1730E 02	0.2729F 01	0.9191E 00	0.4261F 01	0.9116E 02	0.0000E 00	0.0000E 00	0.5295E 02	0.6667E 01	0.0000E 00	33		
7	0.6667E 01	0.5333E 01	0.0000E 00	0.0000F 00	0.0000E 00	0.1450E 00	0.4065E 00	0.5295E 02	0.6667E 01	0.0000E 00	0.4486E 02	0.1665E 02	0.1062E 02	10		
8	0.4735E 02	0.3472E 02	0.3262F 00	0.1319E 02	0.2127E 01	0.1239E 01	0.1521F 01	0.4486E 02	0.1665E 02	0.1062E 02	0.8762F 02	0.1042E 02	0.1458E 02	72		
9	0.7070E 02	0.1843E 02	0.6437E 00	0.6989F 01	0.3825F 00	0.2072E 01	0.2100F 01	0.8762F 02	0.1042E 02	0.1458E 02	0.4043E 02	0.5458E 01	0.3079E 02	16		
10	0.1361E 02	0.2032E 02	0.0000E 00	0.1209E 02	0.2825E 01	0.3515E 00	0.1002E 01	0.4043E 02	0.5458E 01	0.3079E 02	0.4747E 02	0.9722E 01	0.2778E 02	13		
11	0.4092E 02	0.3947E 02	0.5000E-02	0.1714F 02	0.1186E 01	0.1591E 01	0.1244E 01	0.4747E 02	0.9722E 01	0.2778E 02	0.9762E 02	0.1220E 01	0.2541E 02	48		
12	0.2812E 02	0.3158E 02	0.2746E 01	0.1461E 02	0.6165E 00	0.1203E 01	0.3964E 01	0.9762E 02	0.1220E 01	0.2541E 02	0.8356E 02	0.3191E 01	0.6206E 01	41		
13	0.7012E 01	0.5806E 01	0.1416E 02	0.6850F 01	0.1319F 02	0.5257E 00	0.4173E 01	0.8356E 02	0.3191E 01	0.6206E 01	0.8379E 01	0.4023E 01	0.5747E 01	47		
14	0.5241E 02	0.1579E 02	0.1157E 01	0.1031E 02	0.5033E 01	0.1140E 01	0.3705E 01	0.8379E 01	0.4023E 01	0.5747E 01	0.8482E 02	0.1667E 02	0.1429E 02	29		
15	0.1744E 01	0.2939E 01	0.1257E 00	0.9157E 00	0.3129E 02	0.2239E 01	0.1230F 02	0.8482E 02	0.1667E 02	0.1429E 02	0.8518E 02	0.8207E 01	0.1378E 02	7		
TOTAL	0.2994E 02	0.2523E 02	0.2840E 01	0.1392E 02	0.3671E 01	0.1501E 01	0.3423E 01	0.8518E 02	0.8207E 01	0.1378E 02	0.5529E 00	0.5529E 00	0.5955E-01	487		

CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES															SIZE
	M05	M06	M07	M01	M02	M03	M04	M05	M06	M07	M08	M09	M10	M11		
1	0.1618E 02	0.2781E 02	0.1788E 02	0.1000E 02	0.6250E-01	0.8333E 00	0.6250E 00	0.9375E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	48		
2	0.6339E 01	0.7172E 02	0.1011E 02	0.2131E 00	0.1311E 00	0.0000E 00	0.8852E 00	0.0000E 00	0.1652E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	61		
3	0.2135E 02	0.4006E 02	0.3264E 01	0.7083E 01	0.1667F 00	0.8333E-01	0.5417E 00	0.1250E 00	0.0000E 00	0.0000E 00	0.1250E 00	0.0000E 00	0.1250E 00	24		
4	0.3214E 02	0.4369E 02	0.2976E 01	0.3214E 00	0.2857F 00	0.7143E-01	0.6429F 00	0.7143E-01	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	28		
5	0.2500E 02	0.3417E 02	0.1917E 02	0.0000F 00	0.8000E 00	0.0000E 00	0.2000F 00	0.0000E 00	0.2397E 02	0.2000E 00	0.3030E-01	0.0000E 00	0.2727E 00	10		
6	0.6948E 01	0.1446E 02	0.7501E 02	0.1212E 00	0.2727E 00	0.3030E-01	0.6667F 00	0.3030E-01	0.0000E 00	0.2727E 00	0.5000F 00	0.0000E 00	0.9000F 00	33		
7	0.1000E 02	0.2533E 02	0.4000F 02	0.0000E 02	0.0000F 00	0.0000E 00	0.5000F 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	10		
8	0.7222E 01	0.5979E 02	0.5734E 01	0.7917E 01	0.8333F-01	0.1389E 00	0.889F 00	0.5278E 00	0.4861E-02	0.0000E 00	0.5625E 00	0.4137E 00	0.0000E 00	72		
9	0.1875E 02	0.4575E 02	0.1250F 02	0.2500E 00	0.6250F-01	0.0000E 00	0.6250F 00	0.5625E 00	0.4137E 00	0.0000E 00	0.7692E-01	0.0000E 00	0.7692E-01	16		
10	0.2784E 02	0.3592E 02	0.0000E 02	0.9231E 00	0.1538F 00	0.6154E 00	0.1000F 01	0.7692E-01	0.0000E 00	0.0000E 00	0.5000E 00	0.0000E 00	0.0000E 00	13		
11	0.5347E 02	0.1736E 01	0.7291E 01	0.8333E 00	0.2083F-01	0.1667E 00	0.9375F 00	0.5000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	48		
12	0.6504E 02	0.5488E 01	0.2846E 01	0.2927E 00	0.9754E-01	0.0000E 00	0.6341E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	41		
13	0.9929E 01	0.7500E 02	0.5674E 01	0.6383E-01	0.8511E-01	0.0000E 00	0.2340E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	0.6383E-01	47		
14	0.1724E 02	0.4655E 02	0.2299E 02	0.2069E 00	0.1034E 00	0.0000E 00	0.6552E 00	0.6897E-01	0.0000E 00	0.0000E 00	0.6897E-01	0.0000E 00	0.6897E-01	29		
15	0.1429E 02	0.5476E 02	0.0000E 00	0.2857E 00	0.0000E 00	0.0000E 00	0.4286E 00	0.1429E 00	0.1786E 01	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	7		
TOTAL	0.2184E 02	0.4104E 02	0.1570E 02	0.4661E 00	0.1243E 00	0.1458E 00	0.6879E 00	0.2587E 00	0.5529E 00	0.5529E 00	0.5955E-01	0.5955E-01	0.5955E-01	487		

Table 4.9 (Continued)



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES															SIZE
	A02	A03	A04	A05	A06	A07	W01	W02	W03	W04						
1	0.4314E 02	0.5900E 02	0.1846E 00	0.1483E 01	0.2485E 01	0.9754E 01	0.9629E 00	0.8951E 02	0.1080E 02	0.2733E 02	48					
2	0.2442E 02	0.2527E 02	0.1434E 01	0.1491E 01	0.3944E 01	0.1059E 01	0.4053E 01	0.9776E 02	0.8716E 01	0.3115E 01	61					
3	0.1058E 02	0.7425E 01	0.1164E 02	0.1553E 02	0.8841E 01	0.7113E 00	0.9475E 00	0.5380E 01	0.3619E 01	0.1486E 02	24					
4	0.3240E 02	0.4375E 02	0.2085E 01	0.7093E 01	0.2080E 01	0.5486E 00	0.3602E 01	0.8564E 02	0.1292E 02	0.8274E 01	28					
5	0.0000E 00	0.0000E 00	0.1000E 02	0.1000E 02	0.0000E 02	0.3800E-01	0.3006E 02	0.7687E 02	0.9166E 01	0.1250E 02	10					
6	0.2056E 02	0.1529E 02	0.6305E-01	0.1730E 02	0.2729E 01	0.9191E 00	0.4261E 01	0.9116E 02	0.0000E 00	0.4978E 01	33					
7	0.6667E 01	0.5533E 01	0.0000E 00	0.0000E 00	0.0000E 00	0.1450E 00	0.4065E 01	0.5295E 02	0.6667E 00	0.0000E 00	10					
8	0.4735E 02	0.3472E 02	0.3202E 00	0.1319E 02	0.2127E 01	0.1239E 01	0.1521E 01	0.9486E 02	0.1665E 02	0.1062E 02	72					
9	0.7070E 02	0.1843E 02	0.6437E 00	0.6989E 01	0.3825E 00	0.2072E 01	0.2100E 01	0.8762E 02	0.1042E 02	0.1458E 02	16					
10	0.1361E 02	0.2032E 02	0.0000E 00	0.1299E 02	0.2825E 01	0.3515E 00	0.1002E 01	0.4045E 02	0.5458E 01	0.3079E 02	13					
11	0.4092E 02	0.3947E 02	0.5000E-02	0.1714E 02	0.1186E 01	0.1591E 01	0.1244E 01	0.9747E 02	0.9722E 01	0.2778E 02	48					
12	0.2812E 02	0.3158E 02	0.2746E 01	0.1461E 02	0.6105E 00	0.1203E 01	0.3964E 01	0.9762E 02	0.1220E 01	0.2541E 02	41					
13	0.7012E 01	0.5806E 01	0.1416E 02	0.6850E 01	0.1319E 02	0.5257E 00	0.4173E 01	0.8356E 02	0.3191E 01	0.6206E 01	47					
14	0.3241E 02	0.1579E 02	0.1137E 01	0.1031E 02	0.5033E 01	0.1140E 01	0.3705E 01	0.8379E 02	0.4023E 01	0.5747E 01	29					
15	0.1744E 01	0.2939E 01	0.1257E 00	0.9157E 02	0.3129E 02	0.2239E 01	0.1230E 02	0.8482E 02	0.1667E 02	0.1429E 02	7					
TOTAL	0.2994E 02	0.2223E 02	0.2840E 01	0.1392E 01	0.3671E 01	0.1301E 01	0.3423E 01	0.8518E 02	0.8207E 01	0.1378E 02	487					

CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES															SIZE
	W05	W06	W07	M01	M02	M03	M04	M05	M06	M07						
1	0.1618E 02	0.2781E 02	0.1688E 02	0.1000E 02	0.6250E-01	0.8333E 00	0.6250E 00	0.9375E 00	0.0000E 00	0.0000E 00	48					
2	0.6339E 01	0.7172E 02	0.1011E 02	0.2131E 02	0.1311E 00	0.0000E 00	0.8852E 00	0.0000E 00	0.1652E 00	0.0000E 00	61					
3	0.2139E 02	0.4006E 02	0.3204E 01	0.7083E 01	0.1667E 00	0.8333E-01	0.5417E 00	0.1250E 00	0.0000E 00	0.1250E 00	24					
4	0.3214E 02	0.4569E 02	0.2976E 01	0.3214E 00	0.2857E 00	0.7143E-01	0.6429E 00	0.7143E-01	0.0000E 00	0.0000E 00	28					
5	0.2500E 02	0.5417E 02	0.1917E 02	0.0000E 00	0.8000E 00	0.0000E 00	0.2000E 00	0.0000E 00	0.2397E 02	0.2000E 00	10					
6	0.6948E 01	0.1446E 02	0.7591E 02	0.1212E 00	0.2727E 00	0.3030E-01	0.6667E 00	0.3030E-01	0.0000E 00	0.2727E 00	33					
7	0.1000E 02	0.2333E 02	0.4000E 02	0.0000E 02	0.0000E 00	0.0000E 00	0.5000E 00	0.0000E 00	0.0000E 00	0.9000E 00	10					
8	0.7222E 01	0.5979E 02	0.5734E 01	0.7917E 01	0.8333E-01	0.1389E 00	0.8889E 00	0.5278E 00	0.4861E-02	0.0000E 00	72					
9	0.1879E 02	0.4575E 02	0.1430E 02	0.2500E 02	0.6250E-01	0.0000E 00	0.6250E 00	0.5625E 00	0.4137E 00	0.0000E 00	16					
10	0.2784E 02	0.3592E 02	0.0000E 01	0.8333E 01	0.2083E-01	0.1667E 00	0.1000E 01	0.7692E-01	0.0000E 00	0.7692E-01	13					
11	0.5347E 02	0.1736E 01	0.7291E 01	0.8333E 00	0.1534E 00	0.6154E 00	0.1000E 00	0.5000E 00	0.0000E 00	0.0000E 00	48					
12	0.6504E 02	0.5468E 01	0.2846E 01	0.2927E 00	0.9754E-01	0.0000E 00	0.6341E 00	0.0000E 00	0.0000E 00	0.0000E 00	41					
13	0.9929E 01	0.7500E 02	0.5674E 01	0.6383E-01	0.8511E-01	0.0000E 00	0.2340E 00	0.0000E 00	0.0000E 00	0.6383E-01	47					
14	0.1724E 02	0.4655E 02	0.2299E 02	0.2069E 00	0.1034E 00	0.0000E 00	0.6552E 00	0.6897E-01	0.0000E 00	0.6897E-01	29					
15	0.1429E 02	0.5476E 02	0.0000E 00	0.2857E 00	0.0000E 00	0.0000E 00	0.4286E 00	0.1429E 00	0.1786E 01	0.0000E 00	7					
TOTAL	0.2184E 02	0.4104E 02	0.1370E 02	0.4661E 00	0.1243E 00	0.1458E 00	0.6879E 00	0.2587E 00	0.5529E 00	0.5955E-01	487					

Table 4.9 (Continued)



Table 4.10 Univariate F-test of Differences in  
15 Class Means - Sample A

WILKS LAMBDA (U-STATISTIC) AND UNIVARIATE F-RATIO		
VARIABLE	WILKS LAMBDA	F
S01	.6134	21,2490
S02	.6373	19,1859
S03	.5879	23,6334
S04	.6350	19,3797
S05	.4054	49,4390
L01	.7732	9,8876
L02	.7555	10,9092
L03	.9095	3,3561
L04	.3017	78,0257
L05	.8118	7,8144
L06	.9542	1,6199
L07	.8749	4,8219
L08	.7854	9,2143
L09	.7972	8,5765
L10	.8042	8,2085
L11	.9063	3,4855
L12	.8682	5,1198
L13	.6262	20,1277
L14	.8883	4,2380
A01	.8065	8,0911
A02	.7044	14,1451
A03	.7588	10,7172
A04	.8960	3,9123
A05	.8188	7,4624
A06	.9346	2,3575
A07	.3830	54,3016
w01	.6518	18,0095
w02	.4410	42,7285
w03	.9086	3,3897
w04	.8600	5,4877
w05	.6835	15,6129
w06	.5948	22,9636
w07	.5966	22,7994
M01	.5343	29,3797
M02	.8625	5,3731
M03	.4894	35,1748
M04	.7761	9,7283
M05	.4902	35,0568
M06	.5981	22,6522
M07	.5330	19,5461
M08	.7791	9,5582
H01	.2978	79,4898
H02	.7579	10,7707
H03	.2208	118,9643
H04	.3153	73,2295
H05	.5486	27,7370
H06	.7268	12,6741
G01	.6898	15,1622
G02	.6441	18,6264
G03	.5714	25,2883
G04	.8111	7,8527
G05	.7159	13,3763
G06	.8556	5,6889

WITH 14 AND 472 DEGREES OF FREEDOM

FO.01 = 2.64



practices are all contributing to the classification. That these variables in some cases appear to be correlates of the country of origin, climatic variations and consequential soil types, is not surprising even though these were never included as factors in the clustering. The preponderance of sharecropping in Italy with its associated production system is clearly due to historical, economic and legal forces peculiar to that country. Similar observations apply to Luxembourg and Germany in relation to Class 1, with its much more capital intensive farms.

The evidence overall supports the view that a 15-fold categorisation of European holdings is both statistically and agriculturally valid. This is not to say that schemes with more or less classes would be any less valid for describing the pattern of agriculture for specific purposes.<sup>1</sup> However, the *raison d'être* of this research is to demonstrate the feasibility and superiority of classification construction by an analytic procedure rather than a totally subjective approach. These early results provide at least a partial vindication of this fundamental hypothesis.

#### 4.4 Experiments A to F

Before drawing further conclusions about the classification described above, it is necessary to know how sensitive it is to variations in the clustering parameters and variable treatment employed. To this end Experiments A to F were conducted, the detailed results of which are reported in Appendix F. In each case the within class sum of squares, Beale test results and explanatory power, are shown and compared with the corresponding results from the control experiment. Additionally, the distribution of holdings between each experimental classification and the control group is shown by two sample cross-tabulations, the first for 15 classes and the second for 10. Inevitably,

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<sup>1</sup> Appendix E gives the means of variables for 20 and 10 groups.

the class numbering is arbitrary in each cluster analysis, being a function of the manner in which the algorithm has redistributed observations and fused classes. Therefore, to show more forcefully the similarities between a number of the experimental analyses, these arbitrary class numbers are sometimes rearranged to maximise the magnitude of the elements on the principal diagonal of the contingency tables.

Experiment A shows that increasing the number of iterations at each round in the clustering makes virtually no difference to the within group sum of squares, and even less to the explanatory power of the classification. With 10 classes of holdings only one observation is in a different class between the 2 iteration and the 4 and 6 iteration analyses. Admittedly the picture is somewhat less conclusive when one looks at the 15 class contingency table. Nevertheless, the volatility of a maximum of 20% of holdings in no significant way improves the classification, and indicates that in such heterogeneous data as this some holdings are likely to be very marginal to several classes and may be allocated validly to any one of these without great injustice or error arising. It may, of course, be that the increase in iterations has occasioned movement of observations from class to class because the criterion for justifying movement in the clustering program has been set too finely. Whichever explanation is correct, the criticism of this type of optimisation-partition technique as being too expensive to employ is at least partially answered by the already rapid and potentially more rapid convergence of the algorithm to a near optimal solution after two iterations.

Almost identical conclusions are reached from Experiments B and E. Whether one starts with 30, 25 or 20 initial seeding classes, based on subdivision of principal component scores, very similar results are



obtained in all criteria once a fusion to 15 or fewer clusters has taken place. It is remarkable that this observation is equally valid when the *a priori* class codes are used to seed the procedure. As was seen from Table 4.7, there is very little resemblance between the *a priori* classification and the cluster classification. Nevertheless, the algorithm quickly converges to the same solution as before, which points both to its efficiency and the class structure stability in the data.

Experiments C, D and F are all concerned with modifying the variable pattern used in clustering and it is here that the most noticeable differences in the clustering results arise. The least pronounced changes are associated with the movement from 10 to 15 and 20 component variables in clustering. When it is remembered that the computation rises exponentially with the increase in the number of variables entering the cluster analysis, the benefits of such a doubling of the number of components seems dubious. With a group of 15 clusters, the explanatory power of the classification has risen from 31.5% to only 33.3%. Inevitably, this small improvement is due in part to subdivision into separate classes of observations which are more extreme with respect to the higher numbered components. However, the earlier arguments concerning the uniqueness and specificity of the data variance measured by such components would suggest that such small classes lack generality and are not of use in a multi-purpose classification scheme. Their presence undoubtedly explains the apparent significance in the Beale-tests of higher numbers of clusters when 15 or 20 components are used.

From Experiment D one finds that standardisation of component scores to unit variance prior to clustering has not radically changed the classification efficiency. The explanatory power of both Analysis I and VIII are identical with 15 to 18 classes, and Analysis VIII results are

only slightly lower in each other case. There are more obvious differences in class composition but this is to be expected when one recalls that the weighting of the first component to the tenth has changed from a ratio of nearly 4 : 1 to 1 : 1 with standardisation of the component variables. Relatively more weight is given to the lower numbered components on the grounds of the factor analyst that these represent equally important dimensions. One has an alternative classification in this case, rather than a less efficient one, so that pen-portraits could be drawn for these and evaluated.<sup>1</sup>

The effect of using unstandardised variables in principal component analysis to provide data for clustering is much more dramatic. The total and agricultural land area-dominated unstandardised component scores produce a classification of considerable inferiority to both the principal-activity *a priori* scheme and the cluster classification. Even with 20 classes, only 6.8% of the data variance is accounted for by the farm holding groups. As anticipated, the situation is greatly improved when component standardisation is initiated, but nevertheless the explanatory power of the model is substantially lower (only 25% with 15 classes) than in Analyses I and VIII.

Experiment F, which evaluates the consequences of starting with two arbitrary variable sub-sets, is quite encouraging. Whether one starts with the 27 odd-numbered variables or the 26 even-numbered variables, the explanatory powers of the classification with respect to all 53 operational variables is only moderately reduced. With 15 classes and 10 component variables, the 27 variable analysis explains 27.3% of total sample variance and the 26 variable analysis 29.0%. The corresponding figures for 5 components are 23.2% and 27.4%. This leads to the inference that underlying dimensionality in the farm data may be revealed by various combinations of variables and that a less crude and more

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<sup>1</sup> Appendix G presents the means of variables for 20, 15 and 10 classes based on clustering of standardised component score data.



thoughtful reduction and redefinition of variables might be undertaken. Savings in computer time and cost requirements would certainly accrue from this.

#### 4.5 Experimental Analysis I - Discrimination and Assignment Results

The 10-fold clustering of agricultural holdings was taken as the discriminant analysis standard of reference for Experimental Analysis I in order to illustrate the use of this particular classification structure which the Beale Tests had indicated to be statistically valid. In addition, in the several experimental analyses to be undertaken within Experiment G, computing costs would be minimised by testing for the effect of changes in numbers of discriminating variables, discriminating functions, etc. on a 10 rather than 15 or 20 class problem. Inferences drawn from the 10 class experiments (Analyses I, XVI to XXIV) could then be applied to the finer class breakdowns of holdings for evaluation (Analyses XXV and XXVI).

Table 4.11 provides the evidence from the stepwise MANOVA concerning the relative value of discriminating variables. It should be reiterated that the F statistics tabulated there are multivariate-partial F ratios and show the extent of group or class differences with respect to the new variable, after the effect of the existing discriminating variables has been taken into account. Thus the only entry in Table 4.11 which is identical to the univariate F-test results reported in Appendix E for 10 groups, is the first where for H01 the F value is 223.7. Comparison of these two tables further confirms the danger of relying on univariate evidence in the selection of discriminating variables. For example, both H03 and H04 have very high univariate F values, yet H03 is one of the three variables completely discarded by the MANOVA procedure as possessing

Table 4.11 Stepwise MANOVA Summary  
 - Sample A - 10 Classes

SUMMARY TABLE

<u>Step Number</u>	<u>Variable</u>		<u>F to Enter or Remove</u>
	<u>Entered</u>	<u>Removed</u>	
1	H01		223.70748
2	L04		144.91954
3	H04		124.70991
4	A07		84.70395
5	S05		49.50360
6	M06		36.15727
7	H05		29.94654
8	L13		20.12186
9	W06		19.63952
10	M07		18.00195
11	G02		13.68184
12	S04		11.41612
13	M03		11.02311
14	G01		10.05497
15	W07		10.06679
16	L09		10.13267
17	L10		10.36490
18	A04		7.09436
19	M05		6.68328
20	H06		6.34003
21	S02		5.95541
22	L07		5.94250
23	A03		4.82440
24	M08		4.90360
25	A02		4.70840
26	W03		4.01706
27	W02		3.80822
28	G05		3.75773
29	M01		3.00986
30	L12		2.80723
31	S03		2.90924
32	M02		2.65389
33	L08		2.30654
34	A01		1.95503
35	M04		1.78946
36	A06		1.54982
37	M02		1.46831
38	A05		1.37829
39	L11		1.34800
40	G06		1.32747
41	W01		1.22119
42	L02		1.17498
43	W05		1.12570
44	W04		2.74501
45	S01		.84289
46	L14		.67538
47	L05		.61062
48	L06		.55096
49	L01		.53992
50	G04		.28402



no additional discriminating information once H01 and H04 have been allowed for. The reason is clear when it is remembered that  $H03 = H01 - H04$ . On these three binary variables the possible values are as follows:

	H01	H03	H04
Male Holder Manager	1	0	1
Female Holder Manager	1	1	0
Corporate Holder	0	0	0

so that no extra information about a holding is provided by the third once any two are included. On the same reasoning one of the land use variables (in this case L03) and one of the land tenure variables (G01, G02 and G03) must be discarded leaving the fifty variables listed in Table 4.11.

The actual order in which variables have been selected for their discriminating power reflects major class differences revealed from the earlier pen portraits of 15 groups of farms, and those which could be produced for 10 and 20 classes from Appendix E. One class is separated from the others by virtue of having only corporately owned holdings (H01 discriminates on this), another because of the high proportion of horticultural land (L04), and a third which has mainly female holders (H04). Thus the most distinctive class differences produced by clustering are represented by the most "significant" discriminatory variables. The more subtle class differences are revealed in a less pronounced manner by variables which have consequentially lower multivariate partial F values.

The decision to include the 25 most discriminating variables in Analysis I was based on the realisation that the data to hand was neither random nor multivariate-normal in certain planes. As the

product of clustering no group of holdings could be deemed a random sample from a defined population while binary variables by their nature cannot be distributed normally. In view of these difficulties, the MANOVA F tests had to be treated as indicative and could not be rigorously interpreted from the standpoint of statistical significance. Seen in this way the cut-off at 25 discriminatory variables must be considered to be largely arbitrary and pragmatic, although it was partly based on the desirability of having representatives of each operational variable subset. Thus, of the twenty-five variables, three are size measures (S02, S04, S05), five are parameters of land use (L04, L07, L09, L10, L13), four indicate livestock husbandry practices (A02, A03, A04, A07), two are related to labour inputs (W06, W07), five are indices of capital intensivity (M03, M05, M06, M07, M08), four pertain to the holder or manager (H01, H04, H05, H06), and two reflect general holding characteristics (G01 and G02). Ultimately, the performance of this set of variables, compared with alternative sets, in successfully assigning observations to groups, provides the acid test of acceptability of the decision.

Table 4.12 summarises the results of the discriminant analysis applied to the ten groups of farms and utilising the information on the 25 discriminating variables. It is evident that, although by the Wilks test criterion all functions are significant, only eight out of nine possible functions are needed to account for over 95 per cent of the variance of  $W^{-1}B$ . The nature of these functions is shown by the standardised function co-efficients which measure the relative importance of each operational variable to the dimensions defined. Not surprisingly, the first two functions are dominated by H01 and L04, which quite reasonably appear to be at extreme ends of a measurement



NUMBER REMOVED	EIGENVALUE	CANONICAL CORRELATION	PERCENT OF TRACE	LAMBDA	CRIM-SQUARE
0	6.54838	.93141	29.1	.00005	4667.07668
1	5.34259	.91779	23.7	.00036	3718.06092
2	3.22617	.87372	14.3	.00231	2850.75933
3	2.12249	.82447	9.4	.00975	2174.07118
4	1.87131	.80730	8.3	.03044	1639.48357
5	1.11478	.72604	5.0	.08740	1144.26993
6	.93368	.69468	4.1	.18484	792.63759
7	.80757	.66841	3.6	.35742	483.03674
8	.54783	.59492	2.4	.64607	205.10151

6 FUNCTIONS WILL BE USED IN REMAINING ANALYSES

STANDARDIZED DISCRIMINANT FUNCTION COEFFICIENTS

	1	2	3	4	5	6	7	8
S02	.28650	.04712	.12403	.06775	.21555	.32518	.18427	.16610
S04	.14274	.26164	.16203	.18643	.00001	.30205	.19045	.02383
S05	.24152	.12343	.14914	.36507	.06367	.30424	.04211	.16228
L04	.78721	1.83988	.35259	.24659	.00108	.00353	.03146	.10741
L07	.05032	.04829	.20627	.07606	.31450	.05770	.02994	.11428
L09	.00387	.00261	.26148	.28446	.20516	.37807	.06374	.19776
L10	.17987	.13600	.05838	.32025	.13203	.15144	.28905	.30123
L13	.02322	.03289	.11250	.01036	.15440	.50116	.53927	.19389
A02	.16867	.05683	.22597	.20560	.21485	.07312	.02885	.20085
A03	.15199	.06207	.22597	.15986	.07826	.33945	.14995	.22545
A04	.09387	.19658	.02766	.00192	.00192	.10573	.16954	.15489
A07	.15655	.03095	.69285	.31022	1.34161	.05542	.28926	.04094
H06	.08664	.01254	.18895	.22329	.25087	.09076	.11902	.72935
H07	.09735	.01598	.40241	.32456	.28317	.53537	.20394	.24473
M03	.09299	.09423	.26212	.21995	.09605	.38224	.10993	.32776
M05	.00323	.05167	.26260	.18326	.16656	.25972	.06994	.23918
M05	.55170	.81807	.07011	.00711	.03279	.06600	.05768	.05052
M07	.07553	.11262	.12352	.23118	.04910	.47475	.31683	.47369
M08	.07704	.19804	.00381	.04605	.18595	.06520	.21161	.30852
H01	2.11567	.99016	4.1821	1.6530	.01383	.05095	.16384	.21897
H04	.88873	.20928	1.22298	.97053	.63158	.09327	.03068	.09279
H05	.06148	.03667	.03667	.08451	.09610	.07570	.40664	.54203
H06	.02040	.00357	.11383	.21617	.16279	.10498	.35683	.10813
G01	.17000	.03859	.20296	.03154	.00675	.81602	1.01193	.09874
G02	.03088	.00406	.22409	.19980	.07467	.81299	1.37483	.02976

CENTROIDS OF GROUPS IN REDUCED SPACE

GROUP 1	.78263	.56911	1.53605	1.37015	.29940	.99773	.31511	.56565
GROUP 2	.90481	.48333	.03119	.30243	.51425	.33281	.02104	.44335
GROUP 3	.87228	.87187	2.16920	1.7806	.39296	.05674	.16717	.19317
GROUP 4	.61508	.34087	1.00760	.51390	.04425	-2.45717	.21279	.38136
GROUP 5	6.27437	8.0296	1.97150	.69821	.86754	1.2430	.07282	.08905
GROUP 6	.34145	.54520	1.61122	2.69526	.51736	2.23701	-1.37646	1.29710
GROUP 7	.97290	.78234	.49935	.39590	.36275	.36275	1.27850	1.53038
GROUP 8	.16359	.35815	.78968	2.39299	.32566	.32333	1.16956	1.29502
GROUP 9	.16667	1.34901	4.66443	2.73196	.269056	.35603	.01902	.12110
GROUP 10	.18332	.08173	7.05053	1.96393	9.41111	.22594	-1.00337	.25527

Table 4.12 Discriminant Analysis - 10 Classes

continuum. Later functions give relatively more importance to H04, A07, etc. although these are less easy to interpret and 'name' as source dimensions of class differences.

The centroids of the functions are simply the mean values of discriminant function scores for each group. Because for all observations each function's score vector is standardised to zero mean and unit variance, the group centroid values show how many standard deviations from the overall mean each group lies. The use of the eight discriminant function scores to assign to classes the farms in SAMPLE A, produced the *hits and misses* pattern of Table 4.13.

Overall, 84.4 per cent of farms are correctly assigned to their cluster classes by the assignment rules developed from discriminant function scores. On a class by class breakdown, the prediction success rate varies from 71 per cent (class 10) to 100 per cent (class 5). While examination of  $P(\underline{x}/G_i)$  for  $\max [P(G_i/\underline{x})]$  suggests that some 14% of holdings fit into this class structure rather poorly  $[P(\underline{x}/G_i) < 0.25]$  the general results are encouraging. Over 70 per cent of the 67 cases cited above were correctly predicted and nearly half the misses had as their second highest group probability the group in which they were actually located. It seemed probable that such a misallocation of observations as portrayed here would be of little significance to the explanatory power of the classification of new observations. This is substantiated by the fact that for the SAMPLE A data the explanatory power of the classification for predicted group membership is 26.7 per cent, which compares with the earlier cited figure for actual group membership of 26.5 per cent. Support is therefore provided for the argument developed from the cluster analysis results which suggest that quite a high proportion of observations might equally well be classified into any one of several classes.



Table 4.13 Experimental Analysis I  
Discriminant Analysis Hits and Misses

		PREDICTED GROUP										TOTAL	% HITS
		1	2	3	4	5	6	7	8	9	10		
ACTUAL GROUP	1	87	9					8		3		107	81
	2	8	94		1	1	2		2			108	87
	3		1	23					2	1		27	85
	4	1	4		30		1	1				37	81
	5					12						12	100
	6		3				25	1	2	3		34	74
	7	6	2		1			65	1	1		76	86
	8		6		1			1	44			52	85
	9			1						26		27	96
	10							1		1	5	7	71
											487	84	

NB 37 out of 76 misses correctly predicted by second highest probability.

The assignment rules used for Table 4.13 were based on discriminant function scores which may reasonably be expected to have approximately normal distributions. The alternative is to assign observations directly, using the classification functions presented in Table 4.14. However, these employ the operational variables, some of which are certainly non-normal. This means that the distributional theory underpinning the assignment rules is contravened, so that the probabilities of group membership cannot be calculated. Nonetheless, the position of observations in  $p$ -variate space and  $m-1$  discriminant function space is identical *vis à vis* the group centroids, so that the *nearness* of an observation to the centres of each group is invariant between these alternative data representations. If, as is the case in this research, one is primarily concerned with the efficient assignment of observations not previously classified, then the classification functions using the original variables will indicate just as well the class to which an observation is *nearest*. This is shown by the hits and misses position in Table 4.15 which is in principle<sup>1</sup> identical to corresponding results from Experimental Analysis XVI. The saving in computing cost in the production of Table 4.15 is, however, significant.

#### Experiments G and H

The reported results from the majority of the experimental analyses which constitute Experiment G are confined to hits and misses tables in each case and these are shown as Appendix H.

From Analyses XVI to XVIII it is clear that an appropriate decision was originally taken about the number of discriminant functions to employ in the assignment rules. If all nine functions are employed

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1 Two observations are assigned differently which is due solely to rounding errors.



Table 4.14 Classification Functions - 10 Groups

Variable	FUNCTION WEIGHTS*																			
	1		2		3		4		5		6		7		8		9		10	
S02	0.100	-3	-0.434	-3	0.901	-3	-0.370	-3	-0.134	-2	-0.174	-4	-0.467	-3	-0.231	-3	-0.199	-3	0.517	-3
S04	-0.117	+1	-0.128	+1	0.946	0	-0.330	0	0.622	0	-0.214	+1	-0.138	+1	-0.182	+1	-0.120	+1	-0.138	+1
S05	0.178	+1	0.119	+1	0.493	0	0.895	0	0.283	+1	0.964	0	0.145	+1	0.409	0	0.686	0	0.121	+1
L04	0.558	-1	0.545	-1	0.340	-1	0.503	-1	0.231	+1	-0.228	-1	0.289	-1	0.404	-1	-0.958	-1	0.240	0
L07	-0.406	-1	-0.616	-1	0.182	-1	-0.443	-1	0.562	-1	-0.710	-1	-0.391	-1	0.354	-1	0.560	-1	0.652	0
L09	0.485	-1	0.528	-1	0.431	-1	0.253	-1	0.947	-1	0.227	0	0.711	-1	0.115	0	0.601	-1	0.279	0
L10	-0.146	-1	-0.183	-1	0.844	-1	-0.372	-1	0.217	-1	0.205	-1	-0.212	-1	0.746	-1	-0.174	-1	0.343	-1
L13	0.212	+1	0.170	0	0.447	+1	0.113	+2	0.230	+1	0.148	+1	0.233	+1	0.922	0	0.374	0	0.597	+1
A02	0.707	-1	0.784	-1	0.122	-1	0.695	-1	0.730	-1	0.432	-1	0.791	-1	0.209	-1	0.609	-1	-0.207	-1
A03	0.637	-1	0.640	-1	0.138	-1	0.108	0	0.482	-1	0.159	-1	0.771	-1	0.166	-1	0.263	-1	-0.187	-1
A04	-0.904	-1	-0.783	-1	0.462	-1	0.622	-1	0.757	-1	-0.724	-1	-0.777	-1	0.144	-1	-0.690	-1	-0.791	-1
A07	0.355	0	0.306	0	0.477	0	0.263	0	-0.114	0	0.527	0	0.401	0	0.321	0	0.716	0	0.619	+1
W06	-0.507	-1	-0.142	-1	-0.321	-1	-0.428	-1	-0.499	-1	-0.360	-1	-0.796	-1	-0.902	-2	-0.810	-2	-0.570	-1
W07	-0.139	0	-0.108	0	-0.108	0	-0.152	0	-0.938	-1	0.151	-1	-0.132	0	-0.104	0	-0.472	-1	-0.117	0
M03	0.669	+1	0.115	+1	-0.165	0	0.122	+1	-0.476	0	0.944	0	0.131	+1	0.161	+1	-0.530	0	-0.302	-2
M05	0.393	+1	-0.131	0	0.144	0	0.684	0	-0.140	+1	0.334	0	0.576	0	0.731	0	-0.126	+1	0.737	0
M06	0.346	0	0.361	0	0.424	-1	0.331	0	0.289	+1	0.234	0	0.310	0	0.194	0	-0.296	0	0.209	0
M07	-0.495	0	-0.157	+1	0.565	+1	-0.150	+1	0.224	+1	0.102	+2	-0.818	0	-0.401	+1	-0.591	+1	-0.681	+1
M08	0.593	-1	0.171	0	0.951	-1	0.189	0	-0.448	0	0.228	0	0.140	0	-0.868	-1	0.284	0	-0.117	0
H01	0.125	+3	0.126	+3	0.768	+1	0.125	+3	0.123	+3	0.122	+3	0.126	+3	0.122	+3	0.100	+3	0.117	+3
H04	-0.219	+2	-0.211	+2	-0.225	+1	-0.236	+2	-0.339	+2	-0.170	+2	-0.203	+2	-0.208	+2	0.335	+2	0.295	+1
H05	0.746	0	0.794	0	0.668	0	0.248	0	0.771	0	0.755	0	0.608	0	0.732	0	0.713	0	0.725	0
H06	0.773	0	0.156	+1	0.141	+1	0.151	+1	0.244	+1	0.242	+1	0.366	+1	0.491	+1	0.122	+1	0.533	+1
G01	0.266	0	0.265	0	0.300	0	0.150	0	0.263	0	0.279	0	0.278	0	0.287	0	0.292	0	0.286	0
G02	0.318	0	0.335	0	0.309	0	0.173	0	0.339	0	0.312	0	0.352	0	0.325	0	0.344	0	0.325	0
Cons-	-102.7		-103.7		-37.5		-93.2		-210.8		-104.5		-95.4		-97.2		-101.4		-169.9	
stant	-1.5156		-1.5061		-2.8932		-2.5773		-3.7035		-2.6618		-1.8573		-2.2370		-2.8932		-42425	

\* Each co-efficient should be multiplied by  $10^x$  where x is shown in the column following the weight, eg.  $0.100|-2| = 0.000100$ .

Table 4.15 Hits and Misses based on the Classification Functions in Table 4.14

		PREDICTED GROUP										TOTAL	% HIT
		1	2	3	4	5	6	7	8	9	10		
ACTUAL GROUP	1	87	11					6		3		107	81
	2	6	99			1	1		1			108	92
	3			23					3	1		27	85
	4	2	4		29			2				37	78
	5					12						12	100
	6		3				26	1	2	2		34	76
	7	5	3		1			65	1	1		76	87
	8		7		1			1	43			52	83
	9							1		26		27	96
	10								1		6	7	86
											487	85	



(100% trace), the proportion of hits goes up from the 84.4 per cent in Analysis I to only 85.4 per cent in Analysis XVI. The small increase is almost exclusively due to an improvement in the prediction of Class 10 which is now perfect. In the other direction, the use of only seven functions (90% trace) reduces the proportion of hits by nearly 2 per cent to 82.5 per cent, Class 7 being the only one materially affected. Once a further drop to five functions (80% trace) occurs, a quite rapid deterioration in prediction success results, particularly in Classes 4, 6 and 7, the overall rate falling to 69.4 per cent. Evidently the sixth and seventh functions must be the important discriminator dimensions in relationship to these classes.

Analyses XIX to XXII reveal that the inclusion of all possible discriminating variables does improve the prediction power of the model. However, the level of increase at approximately five per cent (for 9, 8 and 7 functions) hardly justifies the enormous increase in computing time which is entailed by moving from a discriminant analysis of 25 to one of 50 variables.

While the specification of equal prior probabilities in Analyses XXIII and XXIV produces changes in anticipated directions, the overall effect is very marginal. Some deterioration in the correct prediction of larger groups is nearly offset (in Analysis XXIV fully offset) by the increased success in correctly identifying observations to the medium or small sized classes.

The application of strategies vindicated for 10 classes, to the 15 and 20-fold partitioning of farms, appears to give quite reasonable results with 79 and 77 per cent of hits respectively. In both cases only one class is poorly predicted. Class 13 in the 20 class breakdown is, with the exception of one farm, identical to Class 9 of the 15-fold classification. It is this group which is predictable only from the

higher numbered discriminant functions or from the inclusion of further discriminating variables. It is noticeable that after the fusion to 14 classes in the cluster analysis, the group in question disappears as a separate entity. What is more, SAMPLE C does not produce a corresponding class at all, and in SAMPLE B it has been merged with others before 15 classes are formed.

The attempt to apply a distribution-free discrimination algorithm, based on a generalisation of the Kendall (1966) method, proved conspicuously unsuccessful on the agricultural data to hand. The rule used requires that classes should possess exclusive sub-ranges of some discriminating variable values, ie sub-ranges not shared by any other group. Because of conceptual problems of incorporating the binary variables, these were omitted from the analysis run and only 6 farms were discriminated, the remainder being left unclassified. Such a result is obviously unacceptable and further work is proceeding on what is a potentially most usable methodology.

#### 4.7 Summary and Conclusions

The experiments involving clustering parameters and variable numbers and treatment have revealed a general underlying stability in the classification of agriculture holdings. Although non-substantive differences in the distribution of observations to classes do occur when more iterations, different seeding patterns and additional components are incorporated, the explanatory power of the resultant classifications is little altered. This is equally true when standardised component scores are used in clustering.

The use of the latent vectors of the covariance matrix to define the component variables for clustering is confirmed to be undesirable and unsatisfactory.



Evidence is provided that further computational efficiency is possible from a careful reduction - through elimination or redefinition - in the number of operational variables used throughout the procedure.

Stepwise multivariate analysis of variance confirms this finding in indicating the major sources of difference between the various cluster group configurations. Successful assignment may either be made from a reduced operational variable set or from discriminant functions numbering fewer than the maximum possible.

The particular specification of prior probability information does not appear to materially affect overall prediction in this case.

While the broad principles underlying the distribution-free discriminant analysis method employed are intuitively appealing, the method is too demanding of the heterogeneous data pertaining to agriculture and was at this point in time less than useful.

CHAPTER V

REPLICABILITY AND PREDICTABILITY  
OF THE CLASSIFICATION

5.1 Introduction

The univariate resemblances between the first and second systematic samples (SAMPLE A and SAMPLE B) and the simple random sample (SAMPLE C) have been demonstrated in Chapter III. The extent to which SAMPLES B and C are replicates of SAMPLE A in a covariance sense is investigated in this chapter. If evidence exists to confirm that the underlying dimensionality of farm data is equally revealed by each sample, that each produces from clustering approximately the same classification of holdings, and that class membership for one such classification is substantially predictable from knowledge of the classification structure of another, then reasonable grounds exist for the claim that the results obtained from the control experiment are stable and general rather than being sensitive to data changes and consequently sample specific. Final reservations concerning the magnitude of sampling error may be answered by basing the proposed classification scheme(s) on a significantly larger sample size (SAMPLE D) than that used for experimentation.

5.2 A Priori Classification

As a first check on the inter-sample data stability, the results of the *a priori* classification of agricultural holdings for the three experimental samples are produced in Table 5.1. While full comparability between the sample results and the population is impossible due to the presence of uneliminated outliers in the population



Table 5.1

*A Priori Classification  
Distribution of Agricultural Holdings*

CLASS	SAMPLE A	SAMPLE B	SAMPLE C	POPULATION
I	20 (4.1)	16 (3.3)	23 (4.7)	1130 (5.2)
II	12 (2.5)	8 (1.6)	7 (1.4)	399 (1.8)
III	106 (21.8)	114 (23.5)	131 (26.7)	4733 (21.8)
IV	8 (1.6)	8 (1.6)	15 (3.1)	556 (2.6)
V	10 (2.1)	14 (2.9)	13 (2.7)	523 (2.4)
VI	34 (7.0)	19 (3.9)	26 (5.3)	1068 (4.9)
VII	32 (6.6)	39 (8.0)	32 (6.5)	1466 (6.7)
VIII	59 (12.1)	63 (13.10)	57 (11.6)	2670 (12.3)
IX	21 (4.3)	19 (3.9)	21 (4.3)	1079 (5.0)
X	94 (19.3)	102 (21.0)	74 (15.1)	4058 (18.7)
XI	7 (1.4)	16 (3.3)	10 (2.0)	563 (2.6)
XII	15 (3.1)	16 (3.3)	18 (3.7)	834 (3.8)
XIII	14 (2.9)	9 (1.9)	13 (2.7)	447 (2.1)
XIV	4 (0.8)	1 (0.2)	2 (0.4)	69 (0.3)
XV	17 (3.5)	12 (2.5)	15 (3.1)	666 (3.1)
XVI	0 (0)	1 (0.2)	0 (0)	15 (0.1)
XVII	34 (7.0)	29 (6.0)	33 (6.7)	1467 (6.7)
TOTAL	487 (100.0)	486 (100.0)	490 (100.0)	21,743 (100.0)
Explan- atory Power	20.3%	20.6%	19.4%	16.3%

The percentage of observations in each class is shown in parentheses.

data set, it is nonetheless clear that the samples vary from the population only within the limits of expected sampling error. Differences in the distribution of observations between classes in the three samples are possibly most pronounced for the random sample which has a higher proportion of horticultural establishments (Class IV) and arable farms (Class III), with a lower percentage of general mixed farms (Class X). Nevertheless the overall impression of broad similarity between the samples with respect to this *a priori* classification is reinforced by the near identical explanatory power of the scheme for each.

### 5.3 Comparison of Principal Components

Comparison of Tables 5.2 and 5.3 with Tables 4.3 and 4.4 demonstrates the close correspondence between the principal components solutions obtained for the three experimental samples. The eigenvalues are of much the same size and show similar patterns of change. For example, 48.1 per cent and 48.7 per cent of data variance is accounted for by the first 10 components of SAMPLES B and C which compares with 46.5% for SAMPLE A. The equivalent figures for 20 components are 71.1, 71.2 and 68.9 per cent respectively.

Examination of the significant factor loadings confirms that the earlier interpretation of the first two component variables is equally valid for SAMPLES B and C, although small differences in the magnitudes of size-measure loadings, particularly in SAMPLE B, suggest some slight variation in the precise dimensions revealed. The third component of SAMPLE B also has a noticeably different weight or correlation with variable L04, the percentage of used agricultural land devoted to horticulture. At -0.46 it is somewhat lower in absolute terms than for SAMPLE A (-0.66) and SAMPLE C (-0.70). The correlates of horticultural



Table 5.2

*Principal Component Analysis  
Latent Roots Samples B and C*

Comp. No.	SAMPLE B		Comp. No.	SAMPLE C	
	Eigenvalues	Cumulative %		Eigenvalues	Cumulative %
1	6.50	12.3	1	6.34	12.0
2	3.15	18.2	2	3.40	18.4
3	2.51	22.9	3	2.88	23.8
4	2.23	27.2	4	2.51	28.6
5	2.16	31.2	5	2.06	32.4
6	2.00	35.0	6	1.84	35.9
7	1.93	38.6	7	1.78	39.3
8	1.81	42.1	8	1.73	42.6
9	1.65	45.2	9	1.68	45.7
10	1.58	48.1	10	1.56	48.7
11	1.52	51.0	11	1.41	51.3
12	1.44	53.7	12	1.39	53.9
13	1.35	56.3	13	1.30	56.4
14	1.31	58.8	14	1.27	58.8
15	1.22	61.0	15	1.23	61.1
16	1.16	63.2	16	1.18	63.3
17	1.11	65.3	17	1.11	65.4
18	1.07	67.4	18	1.06	67.4
19	1.01	69.3	19	1.00	69.3
20	1.00	71.1	20	0.98	71.2
21	0.93	72.9	21	0.94	72.9
22	0.92	74.6	22	0.93	74.7
23	0.89	76.3	23	0.92	76.4
24	0.85	77.9	24	0.87	78.1
25	0.80	79.4	25	0.82	77.9
$\sum_{i=1}^p \lambda_i$	53.0	100	$\sum_{i=1}^p \lambda_i$	53.00	100

Table 5.3 Significant Factor Loadings  
Samples B and C

Variable	SAMPLE B					SAMPLE C				
	COMPONENT NUMBER									
	1	2	3	4	5	1	2	3	4	5
S01	0.77	0.23	-	-	0.21	0.57	0.55	-	0.19	-
S02	0.71	0.32	-	-	0.15	0.64	0.46	-	0.17	-
S03	0.66	-	-	0.15	0.19	0.71	-	-	0.26	-
S04	0.61	0.32	-	-0.25	-	0.54	0.48	-0.18	-	-
S05	0.84	-	-0.18	-	-	0.82	-	-0.18	-	0.19
L01	0.22	-	0.16	-	-0.20	0.38	-	0.17	-0.53	0.21
L02	-	-0.16	-0.21	-	-	-	-0.20	-	-0.24	0.28
L03	0.22	0.17	-0.17	-	-	0.20	-	-	-0.20	-
L04	-0.23	-	0.46	-0.45	-	-0.20	-	-0.70	-	-
L05	-	0.28	0.16	-0.22	-0.18	0.19	0.20	-	-0.40	-
L06	-	-	-	-	-	-	0.30	-	-	-
L07	-0.23	-	-0.32	-0.32	-	-0.23	-	-	0.18	0.24
L08	-	-0.18	-	0.28	0.19	-	-0.29	0.31	0.66	-0.25
L09	-0.26	0.27	-	-	-	-0.29	-	-	-	-
L10	-0.27	0.17	-	-	-	-0.34	0.16	-	-	-
L11	-0.18	-	-	-	0.23	-	0.16	0.14	-	-
L12	-0.23	-	-0.19	-	0.27	-0.22	0.23	-	0.28	0.16
L13	-	0.19	-	-0.22	-	-	0.32	-	-0.29	-
L14	0.23	-	-	-	-0.15	0.33	-	-	-	-
A01	-0.18	0.15	0.28	-	-	-0.18	0.24	0.15	-0.38	-
A02	0.34	-0.35	0.22	-	0.15	0.49	-0.27	-	0.22	-
A03	0.37	-	0.33	-	-	0.44	-	0.23	-	-
A04	-	-	-	-	-	-0.18	-	-	0.14	-
A05	-	-0.18	-0.30	0.18	-	-	-0.17	-	-	0.28
A06	-	-	-0.32	0.24	-	-	-	-	-	0.36
A07	-	-0.30	-0.37	0.48	-	-	-0.23	-	0.26	0.22
W01	-0.55	-	-0.36	-0.22	-	-0.33	-	-0.58	-	-
W02	-0.15	-0.76	-	-0.19	0.24	-	-0.73	0.24	-	-
W03	0.28	-	-0.26	-0.19	0.15	0.16	-	-	-	-
W04	0.25	-	-	-	-0.29	0.25	-	-0.29	-	-0.21
W05	-	-	-	-	-0.41	-	-	-0.17	-	-0.41
W06	-0.18	-	-	-	0.57	-	-	0.18	-	0.42
W07	-0.20	-	0.21	-	-	-0.24	-	0.20	-	-
M01	0.71	-	-	-	-	0.72	-	-	-	-
M02	-	0.31	-	-0.47	-	-	0.25	-0.48	-	-
M03	0.60	0.17	-	-	0.17	0.55	-	-	-	0.34
M04	0.20	-0.16	-	-	-0.25	0.28	-0.15	-	-0.44	-
M05	0.61	-0.23	-	0.15	-	0.67	-	-	0.20	-
M06	-0.16	-	-0.44	-0.45	-	-	-	-0.58	-	-
M07	-0.25	0.31	0.29	-	-	-0.25	0.34	-	-0.38	-
M08	-0.33	-	-0.49	-0.35	-	-0.28	-0.18	-0.53	-0.22	-
H01	-	-0.62	-	-0.32	0.31	-	-0.62	-	-0.18	-
H02	0.44	-	-0.45	0.20	-	0.31	-	-0.41	-	-
H03	-	-0.64	0.16	-0.46	0.18	0.18	-0.52	-	-0.35	0.24
H04	-0.22	0.25	-0.15	0.30	-	-0.18	-	-	0.30	-0.19
H05	-0.26	0.18	-	-	0.47	-0.24	-	0.41	-	0.34
H06	-0.33	-0.25	-	-	-	-0.33	-0.23	-	-	-
G01	-0.42	0.33	-	-	0.42	-0.47	0.19	-	0.25	0.51
G02	0.32	-0.37	-	-	-0.40	0.47	-0.36	-	-0.14	-0.14
G03	-	0.15	-	-0.16	-0.30	-	0.30	-	-0.22	-0.17
G04	0.31	-	-0.39	0.24	-0.16	0.23	-	-0.37	-	-
G05	0.42	-	-0.25	-	-	0.44	-0.20	-0.19	-	0.19
G06	0.20	0.16	-0.21	-	-	0.26	0.16	-	-	-



activity (eg W01, M02, G04 and M08) produce consistent and parallel differences in component loadings between the samples. The explanation is that component 4 in SAMPLE B, which alone has a significant loading on L04, is evidently contributing with component 3 to the measurable continuum from more traditional mixed arable/livestock farms to the more labour and capital intensive, smaller market gardening operations. Between them the two components should provide an equivalent weighting of this type of difference in farm units to that obtained from component 3 in SAMPLES A and C.

Indeed, other observable discrepancies in loadings between the samples are found to be of less substantive importance when a number of components are viewed together. One finds that essentially the same major dimensions are revealed in slightly different ways by the three data sets.

#### 5.4 Clustering Results and Inter-Sample Predictability

The outline clustering results for SAMPLES B and C are produced in Table 5.4, while the means of the operational variables for groups of 15 and 10 clusters are shown in Appendix I. Once again the points of similarity between Table 5.4 and Table 4.6 are more marked than the small, inconsequential differences. Within group sums of squares after the various clustering stages are of the same relative orders of magnitude, as are the explanatory powers of the classifications. If anything, the second and third experimental samples of holdings are better classified by the clustering than is SAMPLE A, although all three indicate that between 10 and 16 clusters are the best basis for classification construction.

Table 5.4

Cluster Analysis Results : Samples B and C  
 (seeding at 30 clusters, 10 components, 2 iterations)

No. of Classes	SAMPLE B			SAMPLE C		
	tr [W]	Beale F-test	Explan. Power (%)	tr [W]	Beale F-test	Explan. Power %
30	3479	0.54		3761	0.41	
29	3496	1.39		3775	1.55	
28	3541	1.04		3829	1.43	
27	3576	1.63		3881	1.61	
26	3633	1.83		3942	2.27	
25	3700	1.72		4032	1.87	
24	3766	1.48		4110	1.66	
23	3826	1.74		4183	1.98	
22	3900	1.62		4275	1.63	
21	3973	1.56		4355	1.71	
20	4047	2.02	39.6	4444	1.84	37.6
19	4149	1.74	39.1	4546	1.45	36.7
18	4243	2.05	38.4	4632	1.84	36.2
17	4362	2.16	37.8	4748	1.59	35.4
16	4497	2.50*	37.4	4856	1.51	34.7
15	4667	1.99	35.8	4967	1.82	34.1
14	4816	2.37*	35.1	5112	2.44*	33.3
13	5011	2.15	32.9	5325	2.71*	32.3
12	5208	2.29	31.8	5589	2.44*	31.0
11	5443	2.66*	30.2	5857	1.68	28.4
10	5753	2.24	28.4	6067	1.92	27.9
9	6055	2.31		6340	2.24	
8	6419	1.91		6708	2.19	
7	6777	2.43*		7137	1.98	
6	7327	2.19		7610	1.97	
Total sum of squares	12380	* Sig at 1% level	25760	12610	* Sig at 1% level	25970



For both the 15-fold and the 10-fold classifications of holdings, the most distinctive classes are replicated in all of the samples. Comparison of Appendix I with Table 4.9 illustrates the marked similarities of the following groups of holdings in the fifteen class partition.

	<u>SAMPLE A</u>	<u>SAMPLE B</u>	<u>SAMPLE C</u>
Larger Capital Intensive	Class 1	Class 4	Class 5
Corporately Owned	Class 3	Class 8	Class 1
Horticulture	Class 5	Class 7	Class 12
Female Holder	Class 14	Class 6	Class 9
Pig Rearing	Class 15	Class 11	Class 14

In addition, Class 2 in SAMPLE A is largely reproduced by Class 10 in SAMPLE C, while Class 7 in SAMPLE A finds a counterpart in SAMPLE B's Class 3. In other cases it does appear that some rearrangement of class configuration occurs in the three analyses and that at least one class in each case is sample specific (eg Class 9 in SAMPLE A, Class 5 in SAMPLE B and Class 6 in SAMPLE C).

This interpretation, based on the inspection of class centroids in the three sample classification schemes produced by independent clustering, is confirmed by Tables 5.5 and 5.6. These show the results of the assignment of observations in SAMPLES B and C using the discriminant function based assignment rules developed for SAMPLE A. As in earlier cases, the ordering of the arbitrarily numbered classes has been changed to highlight the predictability of the clustering of SAMPLES B and C from a knowledge of the cluster-class structure of SAMPLE A. Both sets of assignments are based on the 25 most important discriminating variables and on the number of functions required to account for 95 per cent of trace ( $W^{-1}B$ ), ie. 8 functions in the 10 class problem and 10 functions in the 15 class situation.

Prediction of SAMPLE B Class Membership from SAMPLE A Assignment Rules

		SAMPLE A : PREDICTED CLASS															Total	% Hits
		A1	A2	A3	A4	A5	A6	A7	A8	A9	A10	A11	A12	A13	A14	A15		
SAMPLE B : ACTUAL CLASS	B4	42			2				3			2			1		50	84
	B13		17		1		1		13				2	9			40	43
	B8			28													28	100
	B2	1	2		19		1		5			2	5	1			36	53
	B7		1			7											8	88
	B15		11		1		26	1	1				5	8			53	49
	B3		2	1					8						1		13	62
	B12	4	17						36			2	3	2			64	56
	B10		11											12		1	24	0
	B1	8	1	2							9				1		21	43
	B9	4	3						20		4	17	1				49	35
	B14		1									18	23		1		43	54
	B5		4		3		8	1					3	10	1		30	33
	B6					1									18	1	20	90
B11															4	4	100	
																486	54	

		SAMPLE A : PREDICTED CLASS										Total	% Hits
		A1	A2	A3	A4	A5	A6	A7	A8	A9	A10		
SAMPLE B : ACTUAL CLASS	B4	89	7					4		1		101	88
	B9	6	56		1		2	4	9	4		82	68
	B7			28						2		30	93
	B2		17		33		9	4	16	2		81	41
	B6					9						9	100
	B3		1	1		1	12		1	1		17	71
	B10	2	1					54		1		58	93
	B5		40		1	2	13	4	14	8	2	84	17
	B1	17		2						1		20	5
	B8										4	4	100
											486	62	



Prediction of SAMPLE C Class Membership from SAMPLE A Assignment Rules

		SAMPLE A : PREDICTED CLASS															Total	% Hits
		A1	A2	A3	A4	A5	A6	A7	A8	A9	A10	A11	A12	A13	A14	A15		
SAMPLE C : ACTUAL CLASS	C5	47		1					10		3				2		63	75
	C10		21						1				1	7			30	70
	C1			20		1		2							1		24	83
	C8	1		2	14							2	1	1	2		23	61
	C12		1			16							1		1		19	84
	C7		4				29	1	5				1	3			42	67
	C2		8		4		4	12						4	1		33	36
	C3	1	12		1				34			2	3	2			55	62
	C6	4		2	1									1			8	0
	C11	10							8		7	8			1		34	21
	C13	2							3			28	17				50	56
	C4	3			1	1	9					3	16	8			41	39
	C15		13		1	1			1				2	17			35	49
	C9														24		24	100
	C14												1		1	6	8	75
																	490	59

		SAMPLE A : PREDICTED CLASS										Total	% Hits
		A1	A2	A3	A4	A5	A6	A7	A8	A9	A10		
SAMPLE C : ACTUAL CLASS	C5	90	10	1	2			2		2		107	84
	C8		46					5	4			55	84
	C1			25						2		27	93
	C2		10		21		17	1				49	43
	C9		2			16	2	1	1	1		23	70
	C6	7		1	2					3		13	0
	C3	12	11					51		3		77	66
	C4	2	18		3	2	9	9	26	1		70	37
	C7		16		1		16		8	20		61	33
	C10									1	7	8	88
												490	62

Inevitably the proportion of 'hits' in these analyses is lower than was found for the internal assignment of observations in SAMPLE A. Let us assume that assignment rules developed separately from the data of SAMPLES B and C would predict class membership at the same internal rates as SAMPLE A (approximately 80% for 15 classes and 85% for 10 classes). Of the 390 (415) or so 'hits' expected from these internally generated rules, no more than 80% (85%) are likely to be predictable from the assignment rules of SAMPLE A. Thus the theoretically anticipated upper limit for 'hits' in Tables 5.5 and 5.6 is approximately 64% (15 classes) and 72% (10 classes). Judged in this light, the findings are very encouraging. The probability of independent cluster analyses producing such levels of inter-sample predictability as observed, given no systematic classification structure, is very small.

Even the pattern of misses in Tables 5.5 and 5.6 corroborates the non-randomness of the classifications produced by the three samples. Many of the classes in the SAMPLE B and C analyses are reasonable composites of two or three classes found from SAMPLE A. For instance, of the 15 classes in each case

$$B13 = A2 + A8 + A13$$

$$B12 = A2 + A8$$

$$B10 = A2 + A13$$

$$B9 = A8 + A11$$

$$B14 = A11 + A12$$

$$C5 = A1 + A8$$

$$C10 = A2 + A13$$

$$C2 = A2 + A7$$

$$C3 = A2 + A8$$

$$C13 = A11 + A12$$

$$C15 = A2 + A13$$



SAMPLE A classes which appear in these illustrative examples are, in the main, the much more 'general' classes of mixed activity farms. These can clearly be clustered in a number of marginally different ways without greatly affecting the efficiency or explanatory power of the classification. The point is made by reference to the 10 class tabulations in Tables 5.5 and 5.6. By merging the more general classes, the following situations obtain.

*Table 5.7*  
*The Effect of Merging the 'General' Classes - SAMPLE B*

		SAMPLE A PREDICTED CLASS								
SAMPLE B ACTUAL CLASS	Class Code	A1	A2+A4+A6 + A8+A9	A3	A5	A7	A10	Total	% Hits	
	B1+B4	106	9	2		4		121	88	
	B2+B3 +B5+B9	6	240	1	3	12	2	264	91	
	B7	-	2	28	-	-	-	30	93	
	B6	-	-	-	9	-	-	9	100	
	B10	2	2			54		58	93	
	B8	-	-	-	-	-	4	4	100	
								Total	486	91

Table 5.8  
The Effect of Merging the 'General' Classes - SAMPLE C

		SAMPLE A PREDICTED CLASS								
		Class Code	A1	A2+A4+A6 +A8+A9	A3	A5	A7	A10	Total	% Hits
SAMPLE C ACTUAL CLASS		C5+C6	97	19	2		2		120	81
		C8+C2 +C4+C7	2	216		2	15		235	92
		C1		2	25				27	93
		C9		6		16	1		23	70
		C3	12	14	-		51		77	66
		C10		1				7	8	88
								Total	490	84

The correspondence between the classification schemes produced by the three samples is now much more evident. There are two large classes of holdings, which may be subdivided in a number of ways according to the vicissitudes in the data obtained from the three samples of 500 observations, and four specific classes which are equally identified by the three data sets. The differences in clustering results between the samples may be put down to the presence of sampling error, which should be halved when a sample of over 2000 observations is used for final classification. Even without this increase in sample size, it should be stressed that the marginal differences in the definitions of the several 'general' classes of holdings are of no great significance. In the fifteen class pattern, the predictions of class membership for SAMPLE B and C observations made from SAMPLE A assignment rules, explain respectively 30.4% and 29.1% of the total data variance in these samples. Although some five per cent lower than the equivalent figures in Table 5.4 for 15 classes, there are two important factors to be borne in mind. Firstly,



only 14 different classes are predicted since Class A9 finds no counterpart in SAMPLES B or C. Secondly, it should be remembered that about 40 per cent of observations in SAMPLES B and C are assigned to different classes by the original internal clustering and the predictions made from SAMPLE A. That such a small decrease in explanatory power should be associated with such large differences in class distributions can only reinforce the assertion of substantial stability in, and predictability of, the classification structure revealed by clustering.

#### 5.5 Summary

The examination of the principal components and cluster analysis results for the final two experimental samples has pinpointed certain discrepancies in comparison with SAMPLE A. Some variation in the structure of the higher numbered components was observed, particularly for SAMPLE B. Paradoxically, the random SAMPLE C, which had been felt to be potentially inferior to the systematic sampling of SAMPLES A and B, produced results more in line with SAMPLE A than did SAMPLE B.

In clustering, sample specificity in the formation of groups of farms was rare, although some blurring in the precise definition of more heterogeneous classes was noticeable. The uniform performance of each sample in identifying the more extreme and homogeneous classes was, however, encouraging.

Although the predictability of the independently determined cluster-class membership of observations in SAMPLES B and C, from assignment rules computed from SAMPLE A, was far from perfect, it was nevertheless reassuringly high. The likelihood of some 60 per cent of observations being correctly assigned in this manner, if there were no stable underlying class structure, was felt to be very small. A substantial

proportion of the 40 per cent of inter-sample prediction "misses" were evidently farms which are marginal to two or more classes since their mis-assignment reduced the explanatory power of the classification by only five per cent.

The reduction in sampling error represented by the four-fold increase in sample size discussed in Chapter VI, is expected to improve the classification stability, particularly with respect to the more heterogeneous classes.



CHAPTER VI

FINAL CLASSIFICATION SCHEMES FOR EUROPEAN AGRICULTURAL HOLDINGS

6.1 The Background to Final Classification

The cumulative evidence of the last two chapters has led to the firm conclusion that on both theoretical and practical grounds a scheme for classifying agricultural holdings may be validly developed from limited multivariate sample data. Although not entirely conclusive in every respect, the findings have supported the view that

(a) principal component transformation of the original data does enable cluster analysis to be undertaken efficiently and thus at reasonable cost using the most important dimensions underlying the observed variables;

(b) essentially the same component solutions and cluster configurations are produced by different samples of data; and

(c) a relatively simple procedure may be prescribed for the assignment of non-sampled observations to classes.

Such inconsistencies as have been observed in the various experimental analyses are taken to be a function more of sampling error than of instability in the data structure or the total algorithm. As such they should be substantially reduced by the replication of proposed procedures on the ten per cent sample of observations to be discussed in this chapter.

Examination of principal components and clustering results for SAMPLE D will hopefully confirm earlier conclusions. Ultimately, the total population should be classifiable from the assignment rules obtained from SAMPLE D data so that full comparison with the *a priori* Farm Typology can be made and the relative merits of the two systems evaluated.

## 6.2 Principal Components and Cluster Analysis - SAMPLE D

In terms of the proportion of total data variance accounted for by the components of the correlation matrix, SAMPLE D with 2161 observations produces startlingly parallel results to those reported for the 500 observation SAMPLE A in Table 4.3. Furthermore, no radical differences are found when comparison with the eigenvalue patterns of SAMPLES B and C are made (Table 5.2). From Table 6.1 it will be seen that the first ten components of the SAMPLE D data explain 46.9 per cent of the total data variance (cf. 46.5% in SAMPLE A), fifteen components 59.2 per cent (cf. 58.7%) and twenty components 69.1 per cent (cf. 68.9%). Thus the inferences made earlier concerning the number of components to employ in clustering should be equally valid for the larger sample.

The latent vector interpretation is also much the same when Table 6.2 is compared with Tables 4.4 and 5.3. The stability of the lower numbered components between the different samples is exemplified by the evidence of Table 6.3 which retabulates in sample order the most significant factor loadings for Components 1 and 2. Admittedly, there is an increasingly lower degree of correspondence when comparison is extended to the higher numbered source dimensions. SAMPLE D should, however, reflect the population better than the smaller experimental samples.

Based on the results of Chapter IV experiments, the cluster analysis for SAMPLE D was undertaken on ten component variables and allowed only two iterations in the observation reallocation phase which follows each fusion from  $k$  to  $k-1$  cluster classes. As the experimental evidence had further suggested that the algorithm converges quickly to the same solution whether seeding at 30, 25 or 20 clusters occurred, it was decided to initiate this last analysis at 25 clusters. This was



Table 6.1  
Eigenvalues - Sample D

Component Number	Eigenvalue ( $\lambda$ )	Cumulative % of Variance
1	6.07	11.5
2	3.18	17.5
3	2.73	22.6
4	2.34	27.0
5	2.09	31.0
6	1.86	34.5
7	1.85	38.0
8	1.67	41.1
9	1.56	44.1
10	1.52	46.9
11	1.48	49.7
12	1.34	52.3
13	1.26	54.6
14	1.24	57.0
15	1.15	59.2
16	1.11	61.3
17	1.11	63.3
18	1.06	65.3
19	1.01	67.2
20	1.00	69.1
21	0.96	70.9
22	0.95	72.7
23	0.92	74.5
24	0.89	76.1
25	0.87	77.8
Total	53	100

Table 6.2  
Significant Factor Loading - Sample D

Variable	Component 1	Component 2	Component 3	Component 4	Component 5	Variable	Component 1	Component 2	Component 3	Component 4	Component 5
S01	0.67	0.44	0.08	0.18	-	W01	-0.37	-	-0.65	0.18	0.09
S02	0.72	0.40	-	0.15	-	W02	-0.08	-0.73	-	-0.17	0.30
S03	0.61	-	-	0.30	0.12	W03	0.23	-	-0.14	-	0.19
S04	0.59	0.44	-0.13	-	0.11	W04	0.22	-	-0.18	0.11	-0.15
S05	0.82	0.12	-0.18	-0.15	0.09	W05	0.09	-0.15	-	-	-0.48
L01	0.38	0.15	-	-0.59	-	W06	-0.12	-	-	-	0.41
L02	0.19	-0.11	-0.22	-0.38	-	W07	-0.24	-	0.22	-	0.11
L03	-	0.14	-	-0.10	-	M01	0.70	-	-	-	0.13
L04	-0.21	-	-0.73	0.23	-	M02	-0.08	0.20	-0.35	-	0.14
L05	0.09	0.20	-	-0.31	0.13	M03	0.49	0.19	-0.08	-0.08	0.16
L06	-0.12	0.16	-	-	-	M04	0.28	-0.16	-	-0.34	-
L07	-0.22	-	-0.98	0.08	0.16	M05	0.62	-0.16	-	0.24	0.12
L08	0.12	-0.50	0.40	0.61	-	M06	-0.19	-	-0.61	0.26	-
L09	-0.27	0.22	-	-0.16	-	M07	-0.27	0.26	0.07	-0.20	-0.11
L10	-0.35	0.30	-	-	-0.11	M08	-0.27	-0.14	-0.50	-0.20	-
L11	-0.19	0.15	0.08	-	0.11	H01	-	-0.54	-0.07	-0.21	0.33
L12	-0.18	0.17	-	0.18	0.25	H02	0.35	-	-0.35	0.17	-
L13	-0.11	0.26	0.09	-0.24	-	H03	0.21	-0.45	-0.15	-0.31	0.37
L14	0.29	-0.14	-	-0.26	-	H04	-0.23	0.15	0.13	0.22	-0.20
A01	-0.15	0.12	-	-0.19	-0.12	H05	-0.23	0.17	0.24	-	0.48
A02	0.38	-0.38	0.26	0.22	-	H06	-0.33	-0.25	-	-0.10	-0.08
A03	0.38	-0.07	0.21	-0.08	0.10	G01	-0.38	0.26	0.17	0.18	0.54
A04	-	0.11	-	-	-	G02	0.39	-0.38	-0.20	-0.09	-0.50
A05	-	-0.14	-0.12	-0.14	0.15	G03	-	0.25	-	-0.20	-0.10
A06	-	-	-0.08	-	0.11	G04	0.24	-0.07	-0.36	0.28	-0.08
A07	-	-0.21	-0.11	-0.15	0.12	G05	0.43	-0.12	-0.17	0.13	0.28
						G06	0.18	0.16	-0.10	-	-

With 2160 degrees of freedom loadings of 0.065 or above are significant at the 0.1% level.



Table 6.3

Sample Comparison of the Most Significant Factor Loadings

	COMPONENT 1				COMPONENT 2				
	SAMPLE				SAMPLE				
Variable	A	B	C	D	Variable	A	B	C	D
S01	0.68	0.77	0.57	0.67	S01	0.41	0.23	0.55	0.44
S02	0.59	0.71	0.64	0.72	S02	0.45	0.32	0.46	0.40
S03	0.54	0.66	0.71	0.61	S04	0.37	0.32	0.48	0.44
S04	0.58	0.61	0.54	0.59	A02	-0.22	-0.35	-0.27	-0.38
S05	0.83	0.84	0.82	0.82	W02	-0.76	-0.76	-0.73	-0.73
M01	0.71	0.71	0.72	0.70	H01	-0.65	-0.62	-0.62	-0.54
M03	0.53	0.60	0.55	0.49	H03	-0.59	-0.64	-0.52	-0.45
M05	0.63	0.61	0.67	0.62	G02	-0.49	-0.37	-0.36	-0.38
G02	0.39	0.32	0.47	0.39					
G05	0.52	0.42	0.44	0.43					

a cautious compromise but one producing significant computer time savings for over 2000 observations. As before, the seeding clusters were obtained from an equal segmentation of observations according to their first component scores. With these parameters the analysis was completed both for unstandardised and standardised component variates on the grounds that alternative but equally acceptable classifications had been produced from the SAMPLE A experiments using such cluster-variable definitions.

The summary results from these clusterings are presented in Table 6.4. As in the cases of SAMPLES A and B, they indicate that for unstandardised components 16 clusters are significantly better than a lower number. For standardised components the first significant Beale F-test is at 11 clusters which is in line with the comparable Experimental Analysis VIII findings.

In view of the consistency in these results and because no other substantive evidence was available on the 'best' number of classes, these two patterns are used for further evaluation and for the assignment of non-sampled population members.

Table 6.4

Cluster Analysis Results : Sample D

No. of Classes	Unstandardised Components			Standardised Components		
	tr (W)	Beale F-test	Explan. Power (%)	trace (W)	Beale F-test	Explan. Power (%)
25	18560	1.99		8299	1.29	
24	18880	1.76		8402	1.00	
23	19180	1.66		8468	1.66	
22	19480	1.67		8600	1.71	
21	19800	1.77		8744	1.58	
20	20160	2.16	34.1	8886	1.73	32.9
19	20630	1.75	33.3	9052	1.26	32.3
18	21040	1.63	32.9	9181	1.26	31.7
17	21450	1.51	32.0	9319	1.89	31.3
16	21860	2.45*	31.6	9542	1.81	30.6
15	22580	1.85	30.7	9774	1.75	29.3
14	23180	1.76	30.0	10020	1.88	28.8
13	23810	1.95	29.2	10310	2.10	28.1
12	24580	2.46*	28.1	10670	1.92	27.2
11	25670	1.70	26.3	11040	2.43*	25.9
10	26530	2.32*	25.4	11570	2.62*	23.9
9	27870	2.36*		12230	2.09	
8	29470	2.01		12850	2.06	
7	31100	1.64		13580	2.08	
6	32720	1.48		14480	1.67	
Total Sum of Squares	53730	* Sig at 1% level	114533	21610	* Sig at 1% level	114533



The explanatory power of these two classifications, which will be referred to as *Classifications I* and *II*, is slightly lower than obtained for corresponding numbers of clusters in earlier analyses. This is to be expected for the larger sample which inevitably shows greater data variation. However, compared with the 17-class *a priori* classification of SAMPLE D data, which also produces a smaller explanatory power at 18.0 per cent, the 16- and 11- class polythetic systems are again far superior, explaining respectively 31.6 per cent and 25.9 per cent of standardised operational variables variances. Tables 6.5 and 6.6 confirm that the cluster analyses of standardised and unstandardised components do produce some important differences. Certain classes contain a majority of identical holdings whichever data treatment takes place. The largely unaltered classes are

<u>Classification I</u>		<u>Classification II</u>	
Unstandardised Components	Standardised Components	Standardised Components	Unstandardised Components
3	2	2	3
5	14	6	4
6	4	3	6
8	6	8	7
13	7	11	11
16	16		

For the remaining groups, where rearrangement of observation clusters is found, this is not associated with radical differences in the explanatory powers of equivalent models.

The specific nature of each class in Classifications I and II is revealed by their centroids as shown in Appendix J. Extensive replication of the pen-portraits of Chapter IV is observable in the 16-class structure, except for the emergence of a class of very large holdings. Consequently, such pen-portraits will not be repeated in detail here.

Table 6.5

Comparison of 16 Clusters of Observations  
produced using Standardised and Unstandardised Component Variables

		STANDARDISED COMPONENTS																	
UNSTANDARDISED COMPONENTS	Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total	
	1	130		19		1			7	20		1	6		5	5			194
	2			22			7												29
	3	1	156					2						2		2			163
	4	3	2	3	2				89	28		1					7		135
	5		4				2							1	126				133
	6	2	7	1	127	3		2		9	1			11					163
	7										60								60
	8				1		98		1							1			101
	9		3			1				41		1	4	114			44		208
	10	33	3		1	1		11	7			85	1		1	91			234
	11	3	4		4	68		8	24		2				1	2			116
	12	35	4			1				109		1	60	2	3	13			228
	13	2		5			3	68	2	3						1	6		90
	14	16		3		1						39	72	1					132
	15	6	2	2	2	8			2			116	3	3	1			1	146
	16					4								1				24	29
Total	231	185	55	137	88	110	91	108	234	61	246	146	135	139	170	25		2161	



Table 6.6

Comparison of 11 Clusters of Observations produced using Standardised and Unstandardised Component Variables

		STANDARDISED COMPONENTS											
UNSTANDARDISED COMPONENTS	Group	1	2	3	4	5	6	7	8	9	10	11	Total
	1	248		1		4	3	59		26	8		349
	2	19		1	24	47	10	1		2	2		106
	3		165			4		2			5		176
	4	10	4	4	1	1	126	3		1	1		151
	5		5		86						121		212
	6	2	8	199		3	1	14		3			230
	7			1					62		1		64
	8	28	3	9		6	3	311		3			363
	9	18	2	5		62	20	36		121			264
	10	7	3	3			2	7		178	10	1	211
	11											35	35
	Total	333	190	223	111	127	165	433	62	334	148	36	2161

Nevertheless the problem of nomenclature remains. Because classes are formed by clustering on the basis of overall multivariate similarities and dissimilarities between holdings, it is dangerous to employ names which reference only a few distinctive characteristics. For example, in Classification I, Class 7 is characterised by holdings with a very high proportion of horticultural land, yet at least one observation in that class has no horticultural land at all. It is of the same size and has an equivalent proportion of "other arable land" cultivated as intensively as in the horticultural holdings. The obvious solution is to talk of Classes IA, IB, IC ... or Class IIIi, IIIii, IIIiii ... . Unfortunately, this is unlikely to be acceptable to most classification users who require something more immediately 'tangible' and interpretable. Thus the following nomenclature for Classification I is only tentatively suggested. (Table 6.7). If used in official tabulations, the attention of readers must be drawn to its inherent limitations and the nature and basis of multivariate classifications.

Examination of the univariate F ratios in Appendix J reinforces the expectation that classes formed by clustering from standardised component scores have a lower emphasis on holding size factors and give relatively more weight to the variables contributing to the higher numbered components. In Table 6.8, the relative distribution of observations between the two classifications is presented. While the classes of horticultural establishments, farms operated by female holders, corporately or jointly held undertakings and the small subsistence and pigs/poultry holdings remain unaltered to any degree between the two schemes, in other cases differences are consistent with the explanation above. For instance, in Class 9 of Classification II more importance is attached to parallels in the age of the holder, land tenure and crop



Table 6.7  
 Classification I Suggested Nomenclature

Class Number	Suggested Nomenclature
1	LARGE/ARABLE-DAIRYING/CAPITAL INTENSIVE/
2	VERY LARGE /ARABLE-GRAZING LIVESTOCK/CAPITAL INTENSIVE/ GOOD MANAGEMENT PRACTICES/
3	SMALL/GENERAL MIXED/LOW CAPITAL INTENSITIVITY/OLDER HOLDERS/
4	MEDIUM/ARABLE-PERMANENT CROPS/LOW CAPITAL INTENSITIVITY/ LABOUR INTENSIVE SHARECROPPING IMPORTANT/
5	SMALL/GENERAL MIXED/LOW CAPITAL INTENSITIVITY/FEMALE HOLDER/
6	SMALL/PERMANENT CROPS-ARABLE/DRAFT ANIMALS IMPORTANT/ HOLDER PART-TIME/
7	VERY SMALL/HORTICULTURE/LABOUR AND CAPITAL INTENSIVE/GOOD MANAGEMENT PRACTICES
8	MEDIUM/ARABLE-PERMANENT CROPS/LOW CAPITAL INTENSITIVITY/ CORPORATE AND JOINT HOLDERS/
9	SMALL/DAIRYING-ARABLE/LOW CAPITAL INTENSITIVITY/HOLDER PART-TIME/
10	MEDIUM/ARABLE-DAIRY/CAPITAL INTENSIVE/SUCCESSIVE AND INTERMEDIATE CROPS/MAINLY RENTED/
11	VERY SMALL/ARABLE-PERMANENT CROPS-PIGS AND POULTRY/HOLDER PART-TIME/
12	MEDIUM/DAIRY-ARABLE/CAPITAL INTENSIVE/
13	LARGE/ARABLE/SUCCESSIVE AND INTERMEDIATE CROPS/CAPITAL INTENSIVE/GOOD MANAGEMENT PRACTICES/MAINLY RENTED/
14	LARGE/DAIRYING/CAPITAL INTENSIVE/GOOD MANAGEMENT PRACTICES/ MAINLY RENTED/
15	SMALL /GRAZING LIVESTOCK-ARABLE/LOW CAPITAL INTENSITIVITY/ YOUNG HOLDERS PART-TIME/MAINLY RENTED/
16	VERY SMALL/SUBSISTENCE-PIGS AND POULTRY/PART-TIME HOLDERS/

Table 6.8

Observation Distribution  
Classification I by Classification II

CLASSIFICATION I	CLASSIFICATION II											Total
	Class Numbers	1	2	3	4	5	6	7	8	9	10	
1	172		1			12	2		2	5		194
2	6			15	4	3	1					29
3		161			2							163
4	3	3	3		1	118	5		1	1		135
5		4								129		133
6		11	145		1		5	1				163
7								60				60
8		1	1	93						6		101
9							207		1			208
10	14	3	2		24	21	49		120	1		234
11	4	1	60		15	3	17	1	9	1	5	116
12	106	5	3			2	107		2	3		228
13				3	80	4			2	1		90
14	25						38		69			132
15	2	1	8			2	2		128	1	2	146
16											29	29
Total	332	190	223	111	127	165	433	62	334	148	36	2161



Table 6.9  
 Classification II Suggested Nomenclature

Class Number	Suggested Nomenclature
1	ARABLE-DAIRYING/CAPITAL INTENSIVE/ABOVE AVERAGE SIZE/
2	GENERAL MIXED/CAPITAL UNINTENSIVE/OLDER HOLDERS/BELOW AVERAGE SIZE/
3	PERMANENT CROPS-ARABLE/DRAFT ANIMALS IMPORTANT/HOLDER PART-TIME/BELOW AVERAGE SIZE/
4	ARABLE-PERMANENT CROPS/CAPITAL UNINTENSIVE/CORPORATE-JOINT HOLDER/ABOVE AVERAGE SIZE/
5	ARABLE/CAPITAL INTENSIVE/GOOD MANAGEMENT PRACTICES/ABOVE AVERAGE SIZE/
6	ARABLE-PERMANENT CROPS/CAPITAL UNINTENSIVE/LABOUR INTENSIVE/SHARECROPPING IMPORTANT/AVERAGE SIZE/
7	DAIRYING-ARABLE/CAPITAL UNINTENSIVE/AVERAGE SIZE/
8	HORTICULTURE/LABOUR AND CAPITAL INTENSIVE/GOOD MANAGEMENT PRACTICES/WELL BELOW AVERAGE SIZE/
9	DAIRYING-ARABLE/YOUNG HOLDERS/AVERAGE SIZE/MAINLY RENTED/
10	GENERAL MIXED/CAPITAL UNINTENSIVE/FEMALE HOLDER/BELOW AVERAGE SIZE/
11	SUBSISTENCE-PIGS AND POULTRY/VERY CAPITAL UNINTENSIVE/LABOUR INTENSIVE/HOLDER PART-TIME/WELL BELOW AVERAGE SIZE/

distribution than to holding size factors. The same is true of Class 1 in Classification II which represents a merger of two distinctively different size groups in Classification I. The similarities of these holdings in capital goods ownership and crop and livestock patterns is more important than size differences after the equalisation of the weighting of source dimensions achieved through component standardisation.

Unfortunately, the differences between the classifications are more a question of shading than black-white contrasts. Summary nomenclature cannot adequately describe such subtle variations so that the only substantial changes between Tables 6.7 and 6.9 are in terms of the order in which the wording of class titles are provided.

### 6.3 Assignment Rules

In both Chapters II and IV it was seen that the most straightforward and computationally efficient method of assigning non-sampled observations to classes involves the use of classification functions. There are as many of these linear functions of discriminating variables as there are classes. The function producing the highest score from an observation's variate vector identifies the class membership of that observation.

Experimental evidence supported the view that not all variables possess equal discriminatory power to distinguish between classes. However, the experiments of Chapter IV had examined only two possibilities, namely the best 25 and 50 variables. Prior to the classification of the entire data set, it was felt to be desirable to pursue this issue further. Therefore, the internal prediction success rates were computed from classification functions of increasing numbers of variables. The summary results are given for Classification I in Table 6.10 and for Classification



Table 6.10

*The Effect of Variations in the Number of  
Discriminating Variables - Classification I*

% HITS					
NUMBER OF VARIABLES IN CLASSIFICATION FUNCTIONS					
Class	25	29	34	39	50
1	76	79	79	79	79
2	72	72	79	83	83
3	87	87	91	90	93
4	78	78	79	82	83
5	99	99	99	99	99
6	74	79	83	83	83
7	93	93	93	93	97
8	82	82	82	82	82
9	87	91	91	91	91
10	74	81	86	88	87
11	67	69	72	71	72
12	66	70	76	81	82
13	79	82	88	86	87
14	80	81	82	83	84
15	79	80	82	84	85
16	76	76	76	76	76
Total	78.8	81.2	83.9	84.9	85.6

Table 6.11

*The Effect of Variations in the Number of  
Discriminating Variables - Classification II*

% HITS						
NUMBER OF VARIABLES IN CLASSIFICATION FUNCTIONS						
Class	22	25	29	34	39	50
1	81	83	84	83	84	85
2	87	87	87	87	88	88
3	70	69	67	71	74	76
4	86	86	86	86	86	86
5	76	75	77	77	80	80
6	69	75	77	78	80	82
7	90	91	93	95	97	96
8	89	90	90	92	94	95
9	87	87	87	91	92	93
10	99	99	99	99	99	99
11	64	64	72	78	78	78
Total	83.3	83.9	85.1	86.4	87.7	88.5



II in Table 6.11. The chosen numbers of discriminating variables for these trials appear idiosyncratic at first sight. They are, in fact, largely arbitrary, the decisions being dictated by programming considerations and the intention to increase the discriminating variable set in steps of about five.

For both classifications, functions of 34 discriminating variables were chosen. For the SAMPLE D data, on which the trials were conducted, this was the point at which every class had at least 70 per cent of its observations correctly identified. The overall proportions of 'hits' in Classifications I and II were 83.9 per cent and 86.4 per cent respectively. Even with the full set of possible discriminating variables the corresponding figures rise by only a small amount to 85.6 per cent and 88.5 per cent.

The classification functions of the 34 variables in each case are shown in Tables 6.12 and 6.13. Their use in the assignment to classes of the 21743 non-spurious agricultural holdings comprising the population of this study is discussed below.

#### 6.4 Classifying the Population

The assignment of each agricultural holding in the population was accomplished using a variant of POPPROG. Program POPCLASS<sup>1</sup> was designed to read in the classification functions and, having converted survey variables to operational variables, to compute the value of each function. Having found the highest function value for each observation and thus identified the class to which the observation should be assigned, summary class characteristics were compiled and the explanatory power of the classification eventually ascertained.

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<sup>1</sup> Produced in Appendix C.

It will have been noticed from Tables 6.12 and 6.13 that the constant term for each classification function is shown in two parts. The second is the adjustment for prior probabilities proportionate to class size. If this is ignored then prior probabilities are assumed to be equal and an alternative assignment of observations is possible. The results of assigning observations using unequal and equal priors for both Classifications I and II are shown in outline in Table 6.14. The corresponding distribution between the classes of the *a priori* scheme are also repeated in the same table for comparison purposes. Confirmation is provided from these analyses that different assumptions concerning priors little affect the distribution of observations or the explanatory power of the individual models, that SAMPLE D and the population are very similar, and that the data based polythetic classifications are 50-75 per cent better than the *a priori* approach with fewer classes. The SAMPLE D distributions, of course, relate to predicted class membership and are therefore a little different to the class sizes shown in Table 6.8. However, once again it is found that the explanatory power of these predicted class distributions is very close to actual class distributions produced by clustering and shown in Table 6.4.

To complete the picture of population classification the mean, standard deviation, minimum and maximum value of each operational variable is shown in Appendix K for each class of the *a priori* classification and Classifications I and II<sup>1</sup>. Inevitably, the centroids in Appendix J and K are very similar. The population classes do, however, exhibit greater variation in some cases. Although spurious holdings have been ignored in the three classifications, 'outliers' which were eliminated for purposes of defining classes are now classified. Consequentially, the variances of some variables in certain classes are 'stretched' by their presence.

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<sup>1</sup> Using priors proportionate to class size.



Table 6.12

Classification Functions - Classification I

POPULATION ASSIGNMENT BY CLASSIFICATION I

VARIABLE	CLASSIFICATION FUNCTION NUMBER					
	1	2	3	4	5	6
S02	0.00176410	0.00753120	0.00037826	0.00034907	0.00047963	0.00036831
S03	-0.00824400	-0.03458000	-0.05169300	-0.07251900	-0.05192600	-0.04069900
S04	2.46200000	3.35260000	1.67880000	2.60760000	2.03980000	1.86380000
S05	0.99891000	0.78268000	0.44581000	0.43824000	0.27022000	0.55786000
L01	0.22185000	0.19353000	0.20536000	0.22377000	0.20895000	0.12109000
L02	0.19093000	0.24227000	0.19399000	0.13470000	0.19090000	0.06973700
L04	0.20174000	0.17259000	0.21882000	0.20109000	0.21603000	0.13202000
L05	0.23536000	0.19366000	0.22126000	0.31239000	0.23215000	0.10829000
L07	0.30337000	0.32143000	0.23830000	0.23094000	0.23866000	0.15933000
L08	0.22804000	0.18082000	0.25196000	0.21415000	0.25868000	0.12199000
L13	5.95180000	5.64850000	5.55670000	11.10800000	5.38510000	6.29710000
L14	-0.64913000	0.46218000	-0.71942000	0.62428000	-0.18242000	-1.16010000
A01	-0.05812200	-0.04757400	-0.02951300	-0.03965700	-0.03539400	-0.05587800
A03	0.03589400	0.00981010	0.02153300	0.06839700	0.02800000	0.00481120
A05	0.03761200	0.08106200	0.05766600	0.07981000	0.06544900	0.05211900
A07	0.02686200	0.17468000	-0.00527250	0.01572700	0.18062000	-0.04881500
W02	0.18337000	0.11499000	0.17853000	0.16606000	0.16264000	0.12049000
W06	-0.03714600	-0.02100300	-0.03606200	-0.02294700	-0.01661700	-0.02143200
W07	-0.02875000	-0.03593000	0.12721000	-0.04454200	-0.00417030	-0.03476300
M01	2.59370000	0.77141000	0.40612000	1.66140000	0.92055000	0.83711000
M03	6.42600000	6.61720000	-0.14872000	0.59084000	-0.60697000	-0.49440000
M05	6.53320000	3.74760000	0.48700000	0.78597000	0.70812000	1.27710000
M06	0.21504000	0.19620000	0.21427000	0.21862000	0.10506000	0.18107000
M07	2.64800000	4.16290000	1.04440000	1.69520000	-0.89519000	13.72000000
M08	0.16330000	0.32164000	0.20073000	0.16939000	0.29925000	0.13604000
H02	9.69310000	10.71600000	8.23170000	8.08570000	8.12830000	8.04640000
H03	109.58000000	66.05700000	109.43000000	110.17000000	71.39700000	109.24000000
H04	76.89700000	55.36000000	75.54700000	75.25300000	95.77800000	72.31300000
H05	0.61477000	0.61006000	0.70829000	0.62797000	0.62045000	0.60761000
H06	4.71920000	7.14820000	4.51110000	4.19280000	4.06420000	6.90370000
G01	0.38615000	0.41944000	0.40067000	0.26492000	0.39042000	0.41763000
G02	0.36375000	0.39358000	0.38506000	0.24709000	0.39105000	0.39008000
G04	-1.56260000	0.84722000	-1.65410000	-0.38792000	-2.03120000	-1.01330000
G05	0.54748000	-0.29675000	-0.16547000	-0.46943000	0.13441000	-0.26586000
CONSTANT	-131.96000000	-136.03000000	-129.18000000	-111.62000000	-108.91000000	-109.06000000
	-2.41050000	-4.31101000	-2.58455000	-2.77307000	-2.78791000	-2.58455000

VARIABLE	CLASSIFICATION FUNCTION NUMBER					
	7	8	9	10	11	12
S02	0.00063351	0.00090495	0.00030003	0.00062854	0.00069441	0.00057780
S03	-0.03210200	-0.06062400	-0.05045900	-0.04632000	-0.04606600	-0.04255200
S04	2.21970000	1.65450000	2.00340000	2.15190000	1.91890000	2.16420000
S05	0.84152000	0.01158700	0.40211000	1.07840000	0.49932000	0.74378000
L01	0.18577000	0.15951000	0.20942000	0.23056000	0.19625000	0.22321000
L02	0.17995000	0.12201000	0.19661000	0.22258000	0.23560000	0.19683000
L04	1.64020000	0.11623000	0.20882000	0.20698000	0.25146000	0.19326000
L05	0.22114000	0.16456000	0.22835000	0.21720000	0.21325000	0.23546000
L07	0.30015000	0.14608000	0.25674000	0.24841000	0.31672000	0.27643000
L08	0.23554000	0.15772000	0.28574000	0.23102000	0.20567000	0.25816000
L13	5.06850000	5.18520000	4.95780000	5.18100000	6.25890000	5.57130000
L14	-2.00070000	0.00110240	-0.43408000	1.22740000	-1.30080000	0.11993000
A01	0.04179000	-0.02487500	-0.01976900	-0.03912100	-0.03070700	-0.03354800
A03	0.02381800	0.01653800	0.01947600	0.02758100	0.01474500	0.02775900
A05	0.08259100	0.04235700	0.05812700	0.06504600	0.15794000	0.06117300
A07	-0.06323500	0.10171000	0.04313800	0.01019500	-0.01246600	0.05037200
W02	0.18271000	0.00946390	0.17702000	0.18050000	0.17595000	0.18560000
W06	-0.02716300	-0.02713300	0.02185300	-0.03972600	-0.01616100	-0.00588630
W07	-0.02084900	-0.04379700	-0.03304300	-0.02948600	-0.03678000	-0.03149800
M01	0.41799000	0.65388000	0.07993600	2.91510000	1.37000000	3.34300000
M03	-0.45531000	0.57881000	-0.31607000	0.47744000	-0.93698000	-0.28565000
M05	0.50791000	1.63690000	0.06082900	2.40280000	0.39740000	4.18310000
M06	2.00200000	0.07809900	0.22665000	0.24375000	0.30030000	0.21654000
M07	4.53330000	7.09890000	1.85020000	2.55770000	3.94020000	2.54530000
M08	0.58243000	0.18733000	0.17528000	0.12188000	0.53798000	0.17106000
H02	10.21000000	6.94170000	8.29850000	8.39690000	8.50020000	8.80270000
H03	111.99000000	18.65300000	110.19000000	109.75000000	110.44000000	110.29000000
H04	77.32600000	24.53300000	74.81100000	75.58400000	75.17700000	76.21800000
H05	0.54390000	0.60984000	0.61554000	0.54912000	0.59588000	0.62601000
H06	6.05890000	3.09210000	6.32730000	4.72200000	8.30370000	5.15280000
G01	0.38034000	0.32811000	0.37619000	0.38217000	0.38905000	0.36722000
G02	0.37865000	0.31958000	0.37266000	0.41870000	0.36389000	0.36418000
G04	-2.82710000	-0.93125000	-1.35490000	-1.59020000	-1.42100000	-0.50054000
G05	-0.85324000	-0.03353700	-0.07804700	0.00151900	0.08308300	0.54050000
CONSTANT	-204.72000000	-44.13000000	-120.87000000	-119.32000000	-123.12000000	-125.58000000
	-3.58416000	-3.06315000	-2.34081000	-2.22303000	-2.92471000	-2.24895000



Table 6.12  
(continued)

VARIABLE	CLASSIFICATION FUNCTION NUMBER			
	13	14	15	16
S02	0.00248510	0.00138410	0.00033278	0.00069087
S03	-0.08945900	0.01275300	-0.04261100	0.15446000
S04	1.78780000	1.77110000	1.95850000	1.15840000
S05	2.31920000	0.47595000	0.47586000	0.19385000
L01	0.20604000	0.19438000	0.19771000	0.20232000
L02	0.33374000	0.18417000	0.17615000	0.23564000
L04	0.17420000	0.17677000	0.21366000	0.35880000
L05	0.20437000	0.21053000	0.21404000	0.23781000
L07	0.24374000	0.31884000	0.26954000	2.40110000
L08	0.19981000	0.27058000	0.27871000	0.22251000
L13	5.61180000	5.99620000	5.78740000	6.03480000
L14	1.20380000	-1.73870000	-1.23160000	-4.01550000
A01	-0.04548500	-0.03223500	-0.02354500	-0.02508200
A03	0.02982000	0.01675500	0.02164400	-0.02801200
A05	0.04312200	0.04048600	0.06285200	0.06730800
A07	0.09113300	-0.00240980	0.00713610	3.46600000
W02	0.11263000	0.17137000	0.17566000	0.16102000
W06	-0.02801700	-0.04117700	-0.06869400	0.01105400
W07	-0.04786800	-0.04508000	-0.06199900	-0.01929100
M01	2.92590000	4.46410000	0.30223000	3.37040000
M03	6.70080000	-0.71820000	-0.35501000	0.33614000
M05	-0.41176000	7.18770000	0.13023000	-2.76290000
M06	0.25748000	0.23647000	0.23801000	0.23744000
M07	4.15020000	3.29830000	2.32400000	3.55210000
M08	-0.00041943	0.17160000	0.16592000	0.09326000
M02	11.75400000	10.06800000	8.35500000	8.20530000
M03	108.67000000	112.11000000	111.07000000	104.41000000
M04	76.60600000	77.69000000	75.66900000	79.21900000
M05	0.60485000	0.55112000	0.53338000	0.62349000
M06	5.05490000	4.31940000	7.56410000	8.44440000
G01	0.38998000	0.37841000	0.38719000	0.37794000
G02	0.41890000	0.40717000	0.39952000	0.33712000
G04	2.16480000	1.42290000	-1.50940000	-0.37188000
G05	0.10863000	0.16275000	-0.12514000	-0.31804000
CONSTANT	-136.54000000	-128.04000000	-115.11000000	-205.04000000
	-3.17845000	-2.79557000	-2.69474000	-4.31101000



Table 6.13  
Classification Functions - Classification II

POPULATION ASSIGNMENT BY CLASSIFICATION II

VARIABLE	CLASSIFICATION FUNCTION NUMBER					
	1	2	3	4	5	6
S02	-0.00103320	-0.00096555	-0.00101050	0.00021296	-0.00047960	-0.00137090
S03	0.01691700	-0.01182700	0.00611610	-0.04732500	-0.04220500	-0.00510700
S04	1.44660000	0.96127000	1.12980000	1.55510000	0.87105000	2.39930000
S05	0.98886000	0.95479000	0.90349000	0.09523800	1.68320000	0.81564000
L01	0.22454000	0.19269000	0.17023000	0.16490000	0.21932000	0.24457000
L02	0.14625000	0.15280000	0.07025700	0.13815000	0.35555000	0.10560000
L03	0.19635000	0.21548000	0.20527000	0.20346000	0.46381000	0.20998000
L04	0.14243000	0.15525000	0.10696000	0.09249800	0.14466000	0.13960000
L05	0.18888000	0.18336000	0.11339000	0.15592000	0.17676000	0.28698000
L07	0.18064000	0.12822000	0.11998000	0.08630500	0.14474000	0.16873000
L08	0.22763000	0.23117000	0.14405000	0.15690000	0.21873000	0.21480000
L13	5.57590000	5.67460000	6.65360000	5.79480000	5.87730000	9.70590000
A02	-0.02111400	-0.03451400	-0.04468100	-0.03212400	-0.04717800	-0.02052200
A03	0.01709400	0.00928100	-0.01555700	-0.00250220	0.00385710	0.04132700
A07	-0.30684000	-0.32276000	-0.34521000	0.03490500	-0.30420000	-0.27254000
W01	0.42338000	0.40322000	0.41088000	0.09205400	0.39382000	0.39934000
W02	0.14040000	0.11994000	0.10087000	0.02420500	0.06647800	0.11642000
W04	0.22475000	0.23974000	0.24527000	0.23130000	0.23367000	0.20315000
W05	0.21735000	0.21872000	0.24827000	0.21640000	0.22382000	0.19148000
W06	0.12692000	0.12319000	0.15769000	0.15756000	0.14347000	0.12037000
W07	0.17094000	0.34286000	0.17504000	0.12700000	0.16062000	0.12838000
M02	-0.96872000	-1.82340000	-0.07740700	0.86059000	-2.18100000	1.75220000
M03	3.55670000	0.31701000	-0.50064000	0.75381000	3.74970000	0.29958000
M05	4.94270000	1.31960000	2.12370000	1.36880000	-0.43917000	1.56910000
M06	0.17406000	0.18000000	0.18468000	0.05065200	0.24540000	0.16665000
M07	10.86800000	10.24300000	18.50700000	7.14490000	11.53500000	9.92770000
H01	126.94000000	128.33000000	123.42000000	20.39600000	127.20000000	126.17000000
H03	80.19300000	75.85500000	82.44400000	-5.00050000	79.96000000	78.98600000
H05	0.58565000	0.70599000	0.55915000	0.66182000	0.60624000	0.59247000
H06	3.52500000	2.52050000	5.77290000	3.09890000	4.15140000	3.28270000
G01	0.38202000	0.40250000	0.40757000	0.30638000	0.37004000	0.28865000
G02	0.35321000	0.39310000	0.38699000	0.30193000	0.39899000	0.28950000
G04	0.66993000	0.77746000	1.45380000	2.44850000	5.00350000	1.83600000
G05	0.80035000	0.07374600	0.20851000	0.14979000	0.25132000	-0.36672000
CONSTANT	-167.88000000	-176.19000000	-160.58000000	-47.75800000	-169.98000000	-158.70000000
	-1.87321000	-2.43133000	-2.27118000	-2.96870000	-2.83412000	-2.57243000

VARIABLE	CLASSIFICATION FUNCTION NUMBER				
	7	8	9	10	11
S02	-0.00103390	-0.00088245	-0.00107210	-0.00102230	-0.00104740
S03	-0.00118990	-0.00920670	-0.01141500	-0.00908480	-0.14047000
S04	1.33890000	0.88885000	1.12280000	1.10080000	1.00090000
S05	0.79018000	1.66410000	0.95932000	0.92310000	0.61334000
L01	0.21990000	0.19082000	0.20993000	0.23231000	0.22595000
L02	0.17694000	0.12070000	0.15563000	0.18534000	0.18383000
L03	0.20512000	0.21845000	0.19700000	0.22053000	0.18957000
L04	0.14465000	1.55080000	0.14117000	0.17156000	0.24784000
L05	0.19200000	0.19169000	0.17187000	0.22190000	0.20114000
L07	0.15996000	0.13091000	0.18918000	0.12016000	1.95530000
L08	0.25025000	0.21502000	0.23602000	0.25773000	0.23571000
L13	5.35680000	4.84060000	5.74710000	6.39130000	5.74040000
A02	-0.00800720	-0.03442400	-0.01687500	-0.00667200	-0.06078500
A03	0.01655200	0.00965770	0.01467100	0.01933800	-0.04259000
A07	-0.26399000	-0.46751000	-0.30110000	-0.00379270	2.78790000
W01	0.41352000	0.83461000	0.42492000	0.35891000	0.24585000
W02	0.11332000	0.10344000	0.11681000	0.10847000	0.10119000
W04	0.21324000	0.23677000	0.25701000	0.23025000	0.23537000
W05	0.20826000	0.18558000	0.27139000	0.21265000	0.23395000
W06	0.17664000	0.11823000	0.13729000	0.14522000	0.15993000
W07	0.15725000	0.16025000	0.18377000	0.17347000	0.16419000
M02	-1.41520000	1.10720000	-1.50050000	-0.28283000	0.33280000
M03	-0.53130000	-0.38464000	-0.29366000	-0.26174000	1.28890000
M05	2.00780000	1.14340000	2.41620000	0.79596000	-1.18980000
M06	0.19631000	1.70930000	0.20118000	0.01224400	0.22671000
M07	10.65400000	13.24300000	11.25900000	5.85260000	11.89900000
H01	126.37000000	130.40000000	127.09000000	136.04000000	127.08000000
H03	79.35000000	80.62400000	81.03800000	-15.87300000	67.82900000
H05	0.58719000	0.53068000	0.48833000	0.66739000	0.55299000
H06	4.10130000	4.86870000	4.32340000	2.72200000	5.19850000
G01	0.37384000	0.37361000	0.37678000	0.36506000	0.37574000
G02	0.38001000	0.37425000	0.40248000	0.37137000	0.35655000
G04	1.95560000	1.97490000	0.87551000	1.29910000	1.85170000
G05	0.18440000	-0.41256000	0.28587000	0.20249000	0.00961370
CONSTANT	-165.51000000	-245.77000000	-164.52000000	-129.56000000	-220.44000000
	-1.60759000	-3.55121000	-1.86717000	-2.68107000	-6.09474000



Class Number	A Priori Classification		Classification I				Classification II			
			Priors Proportionate to Size		Priors Equal		Priors Proportionate to Size		Priors Equal	
	Sample D	Population	Sample D	Population	Sample D	Population	Sample D	Population	Sample D	Population
1	93 (4.3)	1130 (5.2)	201 (9.3)	2260 (9.5)	201 (9.3)	2246 (10.3)	345 (16.0)	3533 (16.2)	343 (15.9)	3520 (16.2)
2	52 (2.4)	399 (1.8)	31 (1.4)	290 (1.2)	32 (1.5)	307 (1.4)	181 (8.4)	1821 (8.4)	192 (8.9)	1920 (8.8)
3	498 (23.0)	4733 (21.8)	169 (7.8)	1653 (6.9)	173 (8.0)	1682 (7.7)	171 (7.9)	1738 (8.0)	183 (8.5)	1825 (8.4)
4	50 (2.3)	556 (2.6)	117 (5.4)	1248 (5.2)	122 (5.6)	1317 (6.1)	98 (4.5)	1117 (5.1)	98 (4.5)	1117 (5.1)
5	45 (2.1)	523 (2.4)	175 (8.1)	1569 (6.6)	175 (8.1)	1567 (7.2)	111 (5.1)	1079 (5.0)	121 (5.6)	1220 (5.6)
6	119 (5.5)	1068 (4.9)	136 (6.3)	1295 (5.4)	137 (6.3)	1291 (5.9)	148 (6.8)	1576 (7.2)	171 (7.9)	1739 (8.0)
7	163 (7.5)	1466 (6.7)	63 (2.9)	702 (2.9)	63 (2.9)	705 (3.2)	508 (23.5)	5048 (23.2)	457 (21.1)	4582 (21.1)
8	268 (12.4)	2670 (12.3)	91 (4.2)	1004 (4.2)	91 (4.2)	1002 (4.6)	65 (3.0)	702 (3.2)	65 (3.0)	704 (3.2)
9	101 (4.7)	1079 (5.0)	241 (11.2)	2540 (10.6)	233 (10.8)	2438 (11.2)	325 (15.0)	3185 (14.6)	322 (14.9)	3163 (14.5)
10	380 (17.6)	4058 (18.7)	240 (11.1)	2334 (9.8)	223 (10.3)	2114 (9.7)	178 (8.2)	1590 (7.3)	178 (8.2)	1590 (7.3)
11	52 (2.4)	563 (2.6)	97 (4.5)	924 (3.9)	103 (4.8)	1012 (4.7)	31 (1.4)	354 (1.6)	31 (1.4)	363 (1.7)
12	85 (3.9)	834 (3.8)	231 (10.7)	2153 (9.1)	213 (9.9)	2026 (9.3)	N.a.	N.a.	N.a.	N.a.
13	50 (2.3)	447 (2.1)	82 (3.8)	789 (3.3)	83 (3.8)	836 (3.8)	"	"	"	"
14	5 (0.2)	69 (0.3)	127 (5.9)	1335 (5.6)	141 (6.5)	1484 (6.8)	"	"	"	"
15	63 (2.9)	666 (3.1)	135 (6.2)	1291 (5.4)	145 (6.7)	1388 (6.4)	"	"	"	"
16	0 (0)	15 (0.1)	25 (1.2)	326 (1.4)	26 (1.2)	328 (1.5)	"	"	"	"
17	137 (6.3)	1467 (6.7)	N.a.	N.a.	N.a.	N.a.	"	"	"	"
	2161	21743	2161	21743	2161	21743	2161	21743	2161	21743
Explanatory Power	18.0%	16.3%	31.5%	28.3%	31.5%	28.3%	25.8%	24.6%	25.8%	24.6%

% of observations shown in parentheses.

Table 8.14  
 Classifications of the Population of Agricultural Holdings  
 Distributions and Explanatory Powers



### 6.5 Cost Considerations

The developmental and experimental stages of this approach to multivariate classification have quite obviously consumed substantial amounts of computer time and many man-hours. Having provided a validation of the total procedure a potential user will be interested in the costs associated with its implementation for new problems or data sets. The following information is for guidance only. It relates to the sampling of ten per cent of a population of 22000 members, the analysis of that sample in the manner described in this and earlier chapters, and the application of final assignment rules in classifying the population. Manpower costs are ignored and computer time and costs are based on the use of an I.C.L. 1904S machine of the configuration currently operating at the University of Aston Computer Centre. The further assumption is that the programs and packages listed in this text are employed without modification. It is quite certain that these programs could be made somewhat more efficient by a professional computer systems analyst and programmer. The costs are shown in terms of *central processor units* (CPU's) or *mill time* and in value terms at the present rate of charging at Aston for external commercial users (9p per CPU).

With the information from Table 6.15 and allowing for cluster analyses of both standardised and unstandardised component scores, the computation of six sets of classification functions and two population classification runs, the total cost would be a little over £3500. Even though this represents a fifteen-fold increase over the *a priori* classification of the same population, it nevertheless represents a trivial sum in comparison with data collection and analysis costs for large scale surveys.

Table 6.15

Implementation Costs for Multivariate Classification

Analysis Description	Program or Package	CPU's (in cc's)	Cost (in f's)
Selection of Sample, Conversion from Survey to Operational Variables	SYSTSAM or RANSAM	15	135
Full Principal Components Analysis	UASTATSXDS3	20	180
Preparation of Principal Component Scores for Cluster Analysis	PRINSORT	5	45
Cluster Analysis (per run)	CLUSTPROG	60	540
Computation of Classification Functions <sup>1</sup> (per classification)	SPSS MK 6.5	25	225
Classification of all observations (per classification)	POPCLASS	40	360
Classification of all observations using <i>a priori</i> classification scheme	POPPROG	25	225

1 SPSS MK 6.5 was not available at Aston and was implemented at Manchester University. The Manchester CDC 7600 is approximately 40-50 times more powerful than the ICL 1904S and this conversion factor has been employed to obtain an equivalent 'Aston Cost'.



CHAPTER VII

CONCLUSIONS AND RECOMMENDATIONS FOR FURTHER STUDY

7.1 General Conclusions

This research study has represented an initial pilot investigation of the feasibility and practicability of moving from a relatively simple, largely arbitrary and totally untested method of classifying agricultural holdings by principal activity to a more complex multivariate procedure which allows the incorporation of any number of classifying variables. An operational approach has been suggested which, although more costly to apply than the *a priori* method, produces much more distinctive classes of holdings with regard to their 'total production systems'. The relative improvement in the explanatory power of the polythetic data based classification more than justifies the cost increase, which is, in any event, marginal to the total costs involved in the exercise of conducting, analysing and publishing agricultural census data on an international scale.

The two alternative classification schemes which are proposed are in fact two of many available from the analysis. While they are in a statistical sense the 'best' classifications, there may be good agricultural, administrative or political reasons for preferring schemes with more classes or based on alternative patterns of classification parameters. Such factors are outside the competence of the author but may be validly allowed for by end-users in the final decisions about the precise form the classification should take. Further breakdown of the cluster-classes is also possible to the same end. For instance, the class characterised by high 'standard' livestock per hectare, small overall size and a larger proportion of non-agricultural land is made up of both very small peasant holdings

of a mainly subsistence type, and small but intensive pig and poultry producers. These could clearly be distinguished in separate sub-classes.

The enlarging of the European Economic Community to include the U.K., Eire and Denmark means that farms from these countries are included in the 1975/76 Farm Structure Survey. While it would appear necessary to re-estimate the classification scheme with data from these important agricultural producers included, there are few grounds for believing either that the structure of agriculture has changed within the founder members over the 1966 to 1975 decade, or that the classification based on 1966 data cannot accommodate the patterns of agriculture in the new member nations.

## 7.2 Remarks on the Classifactory Variables

The availability and selection of variables for analysis has been seen to be crucial insofar that the ultimate decisions taken here will dictate the weighting of the classification. The reported investigation contained fewer aggregated variables than were available in detail from the 1966 Farm Structure Survey. In practice, all survey variables were represented in some way in one or other of the operational variables which were constructed to reflect the balance of collected information. In so doing, the classifications arrived at were fairly heavily influenced by holding size considerations. This was as much due to the regular correlations in some classes between holding size and such variables as the ownership of capital equipment and the educational level of the holding managers as to the inclusion of five explicit measures of farm size.

The other dominant influence on the classification was the presence of binary variables. For at least two classes these



represent the most distinctive characteristic. In both instances the binary variables in question had a small minority of observations with unity values so that upon standardisation such observations were shown to be several standard deviation units from the overall sample mean. Inevitably their similarity in this respect may have outweighed less marked differences between them on other variables. However, the groups of female holders and corporate and joint holders do show other consistent patterns over a range of variates suggesting broad syndromes constituting genuine classes. This interpretation is supported by the fact that not all female holders or corporate and joint holders are in the two classes in question. Where a holding has other distinguishing features these have a greater influence than does its extremity on the relevant standardised binary scale.

Eventually the decision about the variables to incorporate in classification must depend upon the purpose(s) which the final scheme must serve. If there are numerous potential users there will need to be a large number of classifying variables built in, and the classes so formed will inevitably be sub-optimal in relationship to a specific use.

The classification study has also highlighted certain deficiencies in the data collected in the Farm Structure Surveys. The wording and nature of some questions has made analysis of results more difficult than necessary. The separation of 'agricultural land' and 'other land' appears sensible at first sight. It does, unfortunately, create difficulties when it is remembered that 'other land' includes farm buildings such as milking sheds, pig sties and battery hen houses. For some holdings there will be little or no 'agricultural land' and yet the holdings are very legitimately and significantly part of the commercial agricultural sector. Another problem occurs over the information

available for the holding manager compared with the holder. In the majority of cases these are one and the same person. In the few exceptional cases of joint or corporate holders they are not, and yet the only information provided for the managers of these holdings is their educational background. Knowledge of their sex and age, the proportion of time spent managing the holding and whether they have any non-holding employment, would be invaluable. It would also eradicate the need for "not applicable" answer codes to such questions when the holder is not an individual *natural person*.

Incompatibilities between the area of land under glass and the sum of the areas of heated and unheated greenhouses for certain horticultural holdings is illustrative of a further set of data deficiencies. It is either associated with ambiguities in definitions about the treatment of multi-storied greenhouses, or is purely response error. In either case, remedial action is possible. Other internal consistency checks should eliminate spurious holdings (no land at all) and those where the component land used declarations are at variance with the total land areas recorded.

Of potentially more significance is the absence of questions in the surveys on crops and livestock yields, input and output values, the proportion of output marketed, capital investment levels and capital equipment values. Without such data the validity of the classification produced in terms of the 'efficiency' and 'productivity' of holdings must be in doubt. The inputting of such values using, for example, 'average' yields is no remedy. Treating all hectares of wheat production or all dairy cows as homogeneous entities is clearly fallacious. It totally ignores differences in natural fertility and husbandry practices. Perhaps the solution is to reduce the number of



questions asked at present to allow the incorporation of these new elements. The evidence of principal component analysis has certainly suggested many fewer dimensions of difference between holding and holding than the 132 variables obtained from the survey in its current form.

### 7.3 Technical Considerations

There are clearly opportunities to refine and develop the computational procedures employed in the research. While a number of issues have been resolved in the preceding chapters, many others are in need of further investigation. Subjectivity rather than objectivity is still the order of the day in ultimate decisions about the number of 'significant' component dimensions, the 'best' number of clusters or the most 'discriminating' variables. Such statistical tests as are available either provide contradictory evidence, are suspect because of assumption contraventions, or are valueless in being designed within the constraints of small sample theory. Analytical methods are unlikely to provide solutions to these problems. Monte Carlo simulation studies of both synthesised and real data seem much more fruitful paths for future research in these areas.

Criticisms of the optimisation-partition techniques have been partly answered in the experiments with the Golder-Yeomans algorithm. That the clustering procedures may be made more efficient is not in doubt. Opportunities exist to speed the solution by coarsening the parameter which determines whether observations should be reallocated between clusters. It is apparent that such a move will no more than marginally affect the explanatory power of the classification. The possibility of splitting the most heterogeneous cluster and merging the two 'nearest' clusters at the termination of a round in the algorithm

has been suggested by other writers and seems worthy of experimentation. The inclusion of an assignment phase at the end of each round of clustering, employing classification functions of either component or original variables, also provides a potential basis for fine tuning in respect of the allocation of observations to classes. Such a step should counter any arguments concerning the use of only two iterations in the algorithm or the coarsening of the reallocation parameter described above. Finally, the development of the computer package to operate in two phases, firstly on quantitative and secondly on ranked and binary variables, is of interest. Observations would be clustered on such factors as size, land use and livestock levels, and each cluster so formed would be subdivided according to the values of the binary variable set. This may overcome some of the problems associated with the inclusion of binary variables mentioned earlier.

In addition to cluster analysis modifications, there are other potential improvements. Assignment rules may be better defined if observations at the periphery of cluster swarms are excluded. Such observations will, of course, be allocated to classes once the rules have been computed but will not have influenced the rules themselves. Further work on the distribution-free discrimination method discussed in Chapter IV will make it more applicable to a range of assignment tasks. It holds, it is believed, an appeal to non-statistically minded users of a classification who will be able to comprehend more easily the nature and meaning of assignment rules produced from the algorithm.

All of these areas, together with the synthesis of component analysis, clustering and assignment rule determination stages into one program suite, are the subject of ongoing research.



#### 7.4 Other Applications

Agriculture has provided the detailed background against which this operational approach to multivariate classification has been evaluated. There are equally many other economic or social scenarios which could have been used. It has been suggested that in the classification of industry, commodities, distribution, social class and occupations, benefit should accrue from the application of the proposed methodology. In fact, for any large scale census or survey, the need to present results succinctly leads inevitably to the requirement that the subjects of the enquiry should be classified. While there are numerous bases for such classification, the one which produces the maximum multivariate similarity in observations within classes and the greatest overall differences between classes must have the highest information content and be preferred.

APPENDIX A

"The Group of Experts' Farm Typology"



COMMISSION OF THE  
EUROPEAN COMMUNITIES

Luxembourg, 4th February 1977

DG VI - SOEC

CLASSEX 81

GROUP OF EXPERTS "FARM TYPOLOGY"

Community farm classification scheme :  
proposal by the services of the Commission.

COMMUNITY FARM CLASSIFICATION SCHEME : PROPOSAL BY THE SERVICES OF THE COMMISSION

INTRODUCTION

1. This paper sets out proposals by the services of the Commission for the Community farm classification scheme. These are at Appendix 1. Appendix 2 defines the various headings in terms of the characteristics of the 1975 Farm Structure Survey. The proposals reflect the detailed discussions in the farm classification working group in particular those at the most recent meeting on 24th and 25th November; they also reflect the French proposals set out in Classex 43.
2. The paper sets out for each of the various headings of the scheme the considerations relevant to that heading (para. 3 to 21). Paragraph 22 gives a general comment on the step 2 threshold.

STEP 1 (assumed threshold 2/3)

3. Field crops pose no particular problem in stage 1.
4. Horticulture has been maintained as an independent main heading and not merged with permanent crops. This meets the wishes of certain delegations, wishes having regard partly to the regional importance of certain permanent crops. Also since the combination of horticulture and permanent crops appears relatively unimportant there is not the argument for merging these two headings that there is for dairy and other grazing livestock (see para. 6 below).



5. Permanent crops - vineyards : showing vineyards as a separate heading satisfies the wishes of certain wine growing countries and reflects the political importance of this crop.

One disadvantage is the introduction of a step one heading for which less than half the 9 Member states are concerned. More important however, showing vineyards as a completely independent heading at step 1 would mean that combinations between vineyards and other permanent crops would be transferred to the class of mixed holdings, also the numbers of combinations for mixed classes would be undesirably increased while the total group "all permanent crops" would not anywhere be available. Accordingly there has been adopted the procedure proposed also for grazing livestock and dairy cows i.e. to give vineyards separately in step 1, but as an "of which" of permanent crops.

6. Grazing livestock I<sup>(1)</sup> and dairy cows : The approach proposed has the following advantages. It enables the totality of grazing livestock to be shown in one group, thus meeting the strongly expressed wishes of the German delegation and conceding with the French proposals in Classex 43. If the heading grazing livestock is simply split up into "dairy cows" and "other" a large number of holdings which combine dairying with other ruminants (and in particular rearing of dairy cow replacements) fall into the mixed group. This seems undesirable. This split has further complications when examining mixed field crop/livestock farms as proposed by the French in Classes 43. Firstly one has two headings or a

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(1) Category 5 "grazing livestock over 2/3" has been labelled "grazing livestock I" to distinguish it from the other grazing livestock category (9) (grazing livestock between one-third and two-thirds, all other main activities being less than one-third) which has been labelled "grazing livestock II".

need to choose between "field crop/dairy cows" and "field crops/other grazing livestock". Secondly certain holdings which would meet the requirements for this mixed group if both their dairy cows and their other grazing livestock be taken into account would not have sufficient of either taken separately. For these reasons the pragmatic solution proposed is to include the heading "of which dairy" as a separate heading in the first step.

7. Pigs and poultry : pose no particular problems here.
8. The combination of field crops and grazing livestock follows from the consideration set out in paragraph 6. Further analysis to isolate the dairy aspect is proposed in step 2.
9. Grazing livestock (between 1/3 and 2/3): involves the same comments as in the previous paragraph.
10. Others : is a rather heterogeneous group the main elements of which are shown separately in step 2 and discussed in more detail in paragraph 20.
11. No separate class of "unclassifiable" is included but it should not be forgotten that there are holdings where the information available is not sufficient to allow the farm type to be calculated, e.g. a holding producing only rabbits.

## STEP 2

12. For field crops a simple break-down into 3 broad groups is proposed. This takes into account the rotational constraints



which prevent any marked degree of specialisation. (The general argument for a threshold at 2/3 is set out in paragraph 22). It also takes account of the wish to see the combination\* at the last meeting though not in Classex 43. The definition proposed for the group (1.2) adopts the 1/3 to 2/3 approach proposed for mixed holdings. "Roots" are taken to include E 12 "forage roots" in the cases where these contribute a gross margin.

13. The breakdown for horticulture shows market garden vegetables at 2.1. At 2.2 is floriculture plus combinations of market garden vegetables and floriculture. It is necessary to pool the very small combination item with some other heading and if the telescopic principle is followed this has to be one of the enterprises within the main activity horticulture. Whether it would be better to pool with 2.1 could be discussed.
14. For permanent crops - wine the breakdown proposed by France in Classex 43 has been taken over. Table grapes are not however shown separately until step 3. Although the 1975 farm structure survey offers no possibility of distinguishing sub-categories of 4 (except under special arrangements for France) the Farm Accounts Data Network will allow the split.
15. A further major split is between fruit, olives and citrus fruit. If there were important combinations of these it would be possible to maintain a combined "group" in step 2, e.g. of fruit and olives and only split into the individual headings in step 3. The allocation of nurseries to this heading has aroused comment from some delegations.

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\*"cereals/roots" shown separately, expressed by the French delegation ....

16. The break-down proposed for grazing livestock and dairy cows shows non-dairy livestock separately and then in combination with dairying. Step 1 and 2 for grazing livestock thus have the advantage of showing all the major magnitudes, of treating dairying separately and with dairy cows\* have to be repeated from step 1 in order to maintain the exhaustive character of step 2 and in fact are split into the two classes 5.1 (dairy milk) and 5.2 (dairy other). 5.1 consists of those holdings where the purely milk element within the overall dairy cow gross margin is at least half of the total s.g.m. of the holding.
17. For pigs and poultry an analogous procedure to that for horticulture has been adopted. The negligible class of combined pig/poultry holdings has been included with the specialised poultry holdings for reasons analogous to those set out in paragraph 13.
18. The combined group field crops/grazing livestock is split up into "dairy cows" and "other g. l.", each combined with field crops. The category "others" thus includes those holdings where both dairy cows and other grazing livestock are found in combination with field crops. Just as step 1 and 2 of category 5 show all the major magnitudes for grazing livestock, dairying and other g.l. (as independent headings) so step 1 and 2 of category 8 show these magnitudes in combination with field crops. The only difference is that the dairying aspect is not brought forward to the first step since this would increase undesirably the number of headings.

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\* being shown in step 1. Dairy cows .....



19. A similar approach is adopted for the item grazing livestock between 1/3 and 2/3. Items 6, 8.1 and 9.1 should give the majority of holdings where dairying is over 1/3. The remaining possibilities for dairying over 1/3 involve dairying in combination with other main activities. These are in the residual category 10 "others", and can be isolated, if numerically significant, in analysing that category (of 10.6.1).
20. The category 10 "others" contains holdings of various types. Firstly there are the holdings where there are two main activities each between 1/3 and 2/3 (other than the important combination "field crops and grazing livestock" shown separately in Step 1 at category 8). Of the remaining possible combinations four are set out explicitly in 10.1, 10.2, 10.3, 10.4, the remaining five are included in 10.6 "others". A further set of holdings are those where on main activity lies between 1/3 and 2/3 (all other main activities being less than 1/3), other than the main activity "grazing livestock" shown separately at category 9. Of the four remaining possibilities one, field crop, is shown separately at 10.5, the rest are included in 10.6. The remaining item in 10.6 is the small number of holdings where all the main activities are under 1/3.

### STEP 3

21. The proposals for step 3 take account of (i) the groups of holdings currently used in the classification scheme for the Farm Accounts Data Network (ii) the desire expressed in the working group to highlight sheep and dairying. Step 3 differs from steps 1 and 2 in not being exhaustive. Member states can of course augment step 3 for their own purposes.

GENERAL

Step 2 threshold

22. In the choice of threshold the working assumption of the last meeting of a Step 1 threshold of 2/3 for specialised classes has been maintained. In Step 2 the same approach has been proposed (except for dairy milk) for the following reason. A lower value would imply adding the condition for specialisations that one was only considering holdings from the relevant main activity (in order to safeguard the telescopic principle). This would have the undesirable feature of distinguishing between holdings which reached a certain level of specialisation, in function of the other activities on that holding.

Example : threshold in Step 2 is less than the 2/3 of Step 1, say 60%. A holding which has 63% market garden vegetables but no other horticulture crops would not count as a specialised horticultural holding (category 2.1 in the appendix 1) since it would not fulfil the condition for inclusion under main activity 2. Another holding with not merely 63% of market gardening vegetables but also 4% of other horticultural crops would so count.



STEP 1	STEP 2	STEP 3
1 Field crops (>2/3)	1.1 Cereals (incl. rice (>2/3)) 1.2 Cereals and roots (both between 1/3 and 2/3) 1.3 Others (field scale vegetables (>2/3), industrial crops (>2/3), seeds (>2/3) and combinations from these cereals/roots)	1.1.1 Cereals (excl. rice) (>2/3) 1.1.2 Rice (>2/3)
2 Horticulture (>2/3)	2.1 Market gardening vegetables (>2/3) 2.2 Others (Flowers and ornamental plants (>2/3) and combinations of these with market garden vegetables)	2.1.1 Open-air (>2/3) 2.1.2 Under glass (>2/3) 2.2.1 Flowers etc - open-air (>2/3) 2.2.2 Flowers etc - under glass (>2/3)
3 Permanent crops (>2/3) of which	3.1 Quality wine of controlled vintage (>2/3)	
4 Vineyards (>2/3)	3.2 Ordinary wine (>2/3) 3.3 Other vineyards 3.4 Fruit (>2/3) 3.5 Citrus (>2/3) 3.6 Olives (>2/3) 3.7 Others (nurseries (>2/3), other permanent crops (>2/3), permanent crops under glass (>2/3) and combinations from these vineyards/fruit/citrus/olives)	3.3.1 Table grapes (>2/3)  3.7.1 Nurseries (>2/3)
5 Grazing livestock I (>2/3) of which	5.1 Dairy milk (milk >1/2)	
6 Dairy cows (>2/3) (= 5.1+5.2)	5.2 Dairy other (milk ( milk ≤1/2)) 5.3 Other grazing livestock (>2/3)  5.4 Others (Combinations from dairy cows and other grazing livestock (both between 1/3 and 2/3))	5.3.1 Cattle other than dairy cows (>2/3) 5.3.2 Sheep (>2/3) 5.4.1 Dairy cows and cattle other than dairy (both between 1/3 and 2/3)
7 Pigs and poultry (>2/3)	7.1 Pigs (>2/3) 7.2 Others (poultry (>2/3) and combinations of pigs and poultry)	7.1.1 Pigs rearing (>2/3) 7.1.2 Pigs fattening (>2/3) 7.2.1 Eggs (>2/3) 7.2.2 Table fowl (>2/3)
8 Field crops and grazing livestock (both between 1/3 and 2/3)	8.1 Field crops and dairy cows (both >1/3) 8.2 Field crops and other g.l. (both >1/3) 8.3 Others	
9 Grazing livestock II (1/3 < g.l. ≤ 2/3, all other main headings ≤ 1/3)	9.1 Dairy cows (>1/3) 9.2 Other g.l. (>1/3)  9.3 Others	9.2.1 Cattle other than dairy cows (>1/3) 9.2.2 Sheep (>1/3)
10 Others	10.1 Grazing livestock and pigs and poultry (both between 1/3 and 2/3)  10.2 Field crops and pigs and poultry (both between 1/3 and 2/3) 10.3 Field crops and permanent crops (both between 1/3 and 2/3) 10.4 Field crops and horticulture (both between 1/3 and 2/3) 10.5 Field crops (1/3 field < crops ≤ 2/3, all other main headings ≤ 1/3) 10.6 Others	10.1.1 Dairy cows and pigs and poultry (both between 1/3 and 2/3)  10.3.1 Field crops and wine (both between 1/3 and 2/3)  10.6.1 Dairy cows (>1/3) 10.6.2 Permanent crops and horticulture (both between 1/3 and 2/3)

Headings 1 - 7 of appendix 1 defined by characteristics in the 1975 Farm Structure Survey (1)

1	2	3
1 E/01 ...E/11, E/12*, E/13, E/14a, E/18*, E/19	1.1 E/01, ... E/08 1.2 E/01, ... E/06, E/08, E/10, E/11, E/12* 1.3 E/09, E/13, E/14a, E/18*, E/19 and combinations of these with items from 1.1 and 1.2	1.1.1 E/01 ... E/06, E/08 1.1.2 E/07
2 E/14b, E/15, E/16, E/17	2.1 E/14b, E/15 2.2 E/15, E/17 and combinations with items from 2.1	2.1.1 E/14b 2.1.2 E/15 2.2.1 E/16
3 H/01, ... H/07 4 H/04	3.1 } H/04 3.2 } 3.3 } 3.4 H/01 3.5 H/02 3.6 H/03 3.7 H/05, H/06, H/07 plus combinations	3.7.1 H/05
5 G/01*, K/01, ...K/10 6 K/07	5.1 } 2 K/07 5.2 } 5.3 G/01*, K/01 ..K/06, K/08 ... K/10 5.4 combinations from items in 5	5.3.1 K/01 ... K/06, K/08 5.3.2 K/09 5.4.1 combinations of 5.3.1 and 5.3.2
7 K/11, ... K/16	7.1 K/11, ... K/13 7.2 K/14, ... K/16 plus combinations of these with items in 7.1	7.1.1 K/11*, K/12 7.1.2 K/13 7.2.1 K/15 7.2.2 K/14, K/16

\* Only come into play in special circumstances

(1) Headings 8 - 10 follow from the definitions for headings 1 - 7

(2) Uses the share of standard gross margin for K/07 resulting from milk.



APPENDIX B

Operational Variables and the 1966/7  
EEC Farm Structure Survey Variables

The following operational variable definitions should be used in conjunction with the annotated summary of variables included in the 1966 Farm Structure Survey (Appendix B1). The survey variable numbers are as shown there.

Land use variables originally measured in square metres were converted to ares prior to the computation of the operational measures. The variables so modified were E15, E17, F, H07, L10 and L11 (survey variable codes). It should be noticed that the weighting factors for the construction of Annual Work Unit labour inputs and "standard" livestock are those proposed for the 1975/6 survey and are listed in Appendix B2.



Operational Variable	Survey Variable	Notes
<u>S01</u>	$C01 + C02 + C03 + I01 + I02 + I03$	
<u>S02</u>	$C01 + C02 + C03$	
<u>S03</u>	$0.6 * K01 + 0.4 * K02 + 0.5 * K06 + K07 + 0.8 * K08 + 0.1 * K09 + 0.1 * K10 + 0.027 * K11 + 0.5 * K12 + 0.3 * K13 + 0.007 * K14 + 0.014 * K15 + 0.03 * K16$	
<u>S04</u>	$((M01C - 1) * 0.25 + 0.125) + 0.125 * (M03C1 + M04C1) + 0.375 * (M03C2 + M04C2) + 0.625 * (M03C3 + M04C3) + 0.875 * (M03C4 + M04C4) + M03C5 + M04C5 + (M05 + M06) / 2200$	1
<u>S05</u>	$L02A + L02B * L02C + L022 + L023 + L031 + L032 + L033 + L041 + L042 + L043 + L051 + L052 / L053 + L061 + L062 + L063 + L071 + L072 + L073 * L081$	2
<u>L01</u>	$(E01 + E02 * E03 + E04 + E05 + E06 + E07 + E08 * E09) * 100 / \underline{S02}$	
<u>L02</u>	$(E10 + E11 + E12) * 100 / \underline{S02}$	
<u>L03</u>	$E13 * 100 / \underline{S02}$	
<u>L04</u>	$(E14B + E15 + E16 + E17) * 100 / \underline{S02}$	
<u>L05</u>	$(E14A + E18 + E19 + E20) * 100 / \underline{S02}$	
<u>L06</u>	$E21 * 100 / \underline{S02}$	
<u>L07</u>	$F * 100 / \underline{S02}$	
<u>L08</u>	$G01 * 100 / \underline{S02}$	
<u>L09</u>	$H04 * 100 / \underline{S02}$	
<u>L10</u>	$(H01 + H02 + H03 + H05 + H06 + H07) * 100 / \underline{S02}$	
<u>L11</u>	$(I01 / (OP1 + \underline{S02}) * 100$	
<u>L12</u>	$(I02 + I03) / \underline{S01} * 100$	
<u>L13</u>	J01A	3
<u>L14</u>	J02A	3
<u>A01</u>	$K01 * 0.6 * 100 / \underline{S03}$	
<u>A02</u>	$K07 * 100 / \underline{S03}$	
<u>A03</u>	$(0.4 * K02 + K05 + 0.5 * K06 + 0.8 * K08 * 100 / \underline{S03}$	
<u>A04</u>	$(0.1 * K09 + 0.1 * K10) * 100 / \underline{S03}$	
<u>A05</u>	$0.027 * K11 + 0.5 * K12 + 0.3 * K13) * 100 / \underline{S03}$	
<u>A06</u>	$(0.007 * K14 + 0.014 * K15 + 0.03 * K16) * 100 / \underline{S03}$	
<u>A07</u>	$S03 * 100 / \underline{S01}$	

Operational Variable	Survey Variable	Notes
<u>W01</u>	$S04 * 1000/S01$	
<u>W02</u>	$((M01C - 1) * 0.25 + 0.125) + 0.125 * M03C1 + 0.375 * M03C2 + 0.625 * M03C3 + 0.875 * M03C4 + M03C5 * 100/S04$	1
<u>W03</u>	$(P + M03B1 + M04B1) * 100/T$	4
<u>W04</u>	$(P + M03B2 + M04B2) * 100/T$	4
<u>W05</u>	$(P + M03B3 + M04B2) * 100/T$	4
<u>W06</u>	$(P + M03B4 + M04B4) * 100/T$	4
<u>W07</u>	$(P + M03B5 + M04B5) * 100/T$	4
<u>M01</u>	If $(L02A + L02B + L02C + L02D) \geq 1$ then <u>M01</u> =1, otherwise <u>M01</u> =0.	
<u>M02</u>	If $L031 \geq 1$ then <u>M02</u> =1, otherwise <u>M02</u> =0	
<u>M03</u>	If $(L041 + L051 + L061 + L071) \geq 1$ then <u>M03</u> =1, otherwise <u>M03</u> =0	
<u>M04</u>	If $(L022 + L023 + L032 + L033 + L042 + L043 + L052 + L053 + L062 + L063 + L072 + L073) \geq 1$ then <u>M04</u> =1, otherwise <u>M04</u> =0	
<u>M05</u>	If $L081 \geq 1$ then <u>M05</u> =1, otherwise <u>M05</u> =0	
<u>M06</u>	$(E15 + E17 + H07) * 100/S02$	
<u>M07</u>	L01	
<u>M08</u>	$S05 * 1000/S01$	
<u>H01</u>	$B01 * B02$	
<u>H02</u>	D05	
<u>H03</u>	If $M0IA=1$ then <u>H03</u> =1, otherwise <u>H03</u> =0	
<u>H04</u>	If $M0IA=2$ then <u>H04</u> =1, otherwise <u>H04</u> =0	
<u>H05</u>	M01B	7
<u>H06</u>	N01	8
<u>G01</u>	$C01 * 100/S02$	
<u>G02</u>	$C02 * 100/S02$	
<u>G03</u>	$C03 * 100/S02$	
<u>G04</u>	D01	
<u>G05</u>	$D04A1 + D04A2 + D04A3 + D04A4$	
<u>G06</u>	$D04B1 + D04B2 + D04B3 + D04B4 + D04B5 + D04B6 + D04B7$	9



- Notes:
1. This complicated expression to obtain the total Annual Work Units required the following recoding of MOIC. Code "5" was replaced by "4.5" and code "9" by "0.5". The assumption in the second step is that corporate and other non-natural person holders do not work on the holding. In the event there are relatively few of these so that the simplifying assumption should not affect the results greatly.
  2. This is a fairly crude estimate of capital equipment use and includes the number of machines owned plus the number of machines shared or rented at least once per year.
  3. J01A and J02A were originally coded "T Yes". Both were re-coded "1 = Yes".
  4. P takes a value "1" if the holder works regularly on the holding and is in the specified age range. T is the total number of regular workers (as opposed to casual labour) employed by the holding.
  5. B02 code "9" altered to code "0".
  6. M01A code "9" ignored.
  7. Where there is a non-natural or joint holder a default age of 52 years has been employed.
  8. Codes "8" and "9" are treated as "0".
  9. "Yes" answers to D04B1-D04B7 were originally coded "7". This was re-coded "1".

APPENDIX B1

Outline definition of Variables included  
in 1966 Farm Structure Survey



A. GEOGRAPHICAL SITUATION OF THE HOLDING

- A01\* Country
- A02\* Region
- A03\* District
- A04\* Holding Number
- A05\* Raising factor (5 decimals)

The codes of headings A01, A02, A03 are established jointly by the SOEC and the Member State concerned.

B. LEGAL PERSONALITY OF THE HOLDING

B01 Is the legal and economic responsibility .....

Codes:

Answer	Code
yes	1
no	0

B02 If yes, .....

Codes:

Answer	Code
yes	1
no	0
not applicable because B/01 answered as 'no'	9

C. TYPE OF TENURE

- C01 for owner farming
- C02 for tenant farming
- C03 for share cropping and other modes

D. MANAGEMENT OF THE HOLDING AND MANAGER'S EDUCATION

D01 Are accounts kept?

Codes:

Answer	Code
yes	1
no	0

04 a) Is the holding...for the purposes of

D04 a1)\* its supplies

D04 a2)\* marketing its produce

D04 a3)\* use of agricultural equipment...

D04 a4)\* supplies and/or marketing and/or  
use of equipment

member of a cooperative or other  
similar agr. organisation

Codes for the headings of D04 a1,  
D04 a2, D04 a3, D04 a4 in each case:

Answer	Code
yes	1
no	0

04 b) Whether production under contract

D04 b1)\* cereals

D04 b2)\* fruit and vegetables

O=No D04 b3)\* bovine animals

Y=Yes D04 b4)\* milk and milk products

D04 b5)\* pigs

D04 b6)\* poultry

D04 b7)\* eggs

D05 Manager's education and agricultural training

Codes:

Answer	Code
none	1
primary	2
secondary	3
higher	4



LAND USE

E. ARABLE LAND

- E01 Common wheat and spelt
- E02 Durum wheat
- E03 Rye
- E04 Barley
- E05 Oats
- E06 Grain maize
- E07 Rice
- E08 Other cereals
- E09 Dried vegetables (...)
- E10 Potatoes (...)
- E11 Sugar beet (...)
- E12 Fodder roots and brassicas (...)
- E13 Industrial plants (...)
- Fresh vegetables, melons, strawberries:
  - 14 - outdoor
- E14 a) open field
- E14 b) market gardening
- E15 - under glass (units are m<sup>2</sup>)
- Flowers and ornamental plants:
  - E16 - outdoor
  - E17 - under glass (units are m<sup>2</sup>)
- E18 Forage crops
- E19 Horticultural seeds .....
- E20 Other arable crops
- E21 Fallow

F. SUBSISTENCE PLOTS (units are m<sup>2</sup>)

G. PERMANENT PASTURE

- G01 Permanent pasture including mountain grazing

H. PERMANENT CROPS

- H01 Fruit and berry plantations
- H02 Citrus plantations
- H03 Olive plantations
- H04 Vineyards
- H05 Nurseries
- H06 Other permanent crops
- H07 Permanent crops under glass (units are m<sup>2</sup>)

I. OTHER LAND

- I01 Unutilised agricultural area (...)
- I02 Woodland
- I03 Other land (...)

J. COMBINED AND SUCCESSIVE CROPS  
(excluding...)

- 01 Land under crops combined with permanent crops
- J01 a)\* Are answers being furnished for this question?

Code:

Answer	Code
yes	7
no	0

K. LIVESTOCK (as of...)(...)

- K01 Equidae
  - Bovine animals
- K02 under 1 year old
  - 2 years old and over:
- K05 Male animals\*
- K06 Heifers
- K07 Dairy cows
- K08 Other cows
- K09 Sheep (all ages)
- K10 Goats (all ages)
- K11 Piglets of live weight...
- K12 Breeding sows weighing...
- K13 Other pigs
- K14 Broilers
- K15 Laying hens
- K16 Other poultry (...)

\* includes some cattle, mostly males under 2 years old.



L. TRACTORS, CULTIVATORS, MACHINERY AND EQUIPMENT

L01 Are draught animals used on the holding?

Codes:

Answer	Code
yes	1
no	0

02 4-wheeled tractors

(1) number belonging to the holding

L02 a)  $X < 25$  HP

L02 b)  $25 \leq X < 35$  HP

L02 c)  $35 \leq X < 51$  HP

L02 d)  $51 \text{ HP} \leq X$

(X = Horse-power rating)

L02 (2) used by several .....

L02 (3) belonging to a service supply agency

L03 Cultivators, hoeing machines

L03 (1) number belonging to the holding

L03 (2) used by several .....

L03 (3) belonging to a service supply agency

L04 Combine harvesters

L04 (1) number belonging to the holding

L04 (2) used by several holdings

L04 (3) belonging to a service supply agency

L05 Forage harvesters

L05 (1) number belonging to the holding

L05 (2) used by several holdings

L05 (3) belonging to a service supply agency

L06 Potato-harvesters (...)

L06 (1) number belonging to the holding

L06 (2) used by several holdings

L06 (3) belonging to a service supply agency

L07 Sugar-beet harvesters (...)

L07 (1) number belonging to the holding

L07 (2) used by several holdings

L07 (3) belonging to a service supply agency

- L08 Milking machinery (...)
- L08 (1) belonging to the holding
- L10 - without heating installation
- L11 - with heating installation

M. FARM LABOUR FORCE

- 01 Holder
- M01 a)\* Sex

Code:

Answer	Code
male	1
female	2
not applicable because the holder is not a natural person	9

- M01 b)\* Age  
(number of years)  
If M01 answered '9' put '0' in answer to  
this question
- M01 c)\* Time worked (classes)

Codes:

Answer	Code
$X < 25\%$	1
$25\% \leq X < 50\%$	2
$50\% \leq X < 75\%$	3
$75\% \leq X < 100\%$	4
$X = 100\%$	5
not applicable because the holder is not a natural person	9

X = hours worked expressed as  
a percentage of annual time  
worked by a full-time worker.



- 03 Other members of the holder's family
- a)\* Number
- MO3 a1) male
- MO3 a2) female
- b)\* Number in 5 classes of age:
- MO3 b1)  $X < 25$
- MO3 b2)  $25 \leq X < 35$
- MO3 b3)  $35 \leq X < 45$
- MO3 b4)  $45 \leq X < 65$
- MO3 b5)  $65 \leq X$
- (X = age in years)
- c)\* Number in 5 classes of time worked:
- MO3 c1)  $X < 25\%$
- MO3 c2)  $25\% \leq X < 50\%$
- MO3 c3)  $50\% \leq X < 75\%$
- MO3 c4)  $75\% \leq X < 100\%$
- MO3 c5)  $X = 100\%$
- (X = hours worked expressed as a percentage of annual time worked by a full-time worker).
- 04 Non-family labour regularly employed
- a)\* Number:
- MO4 a1) male
- MO4 a2) female
- b)\* Number in 5 age groups:
- MO4 b1)  $X < 25$
- MO4 b2)  $25 \leq X < 35$
- MO4 b3)  $35 \leq X < 45$
- MO4 b4)  $45 \leq X < 65$
- MO4 b5)  $65 \leq X$
- (X = age in years)
- c)\* Number in 5 classes of time worked:
- MO4 c1)  $X < 25\%$
- MO4 c2)  $25\% \leq X < 50\%$
- MO4 c3)  $50\% \leq X < 75\%$
- MO4 c4)  $75\% \leq X < 100\%$
- MO4 c5)  $X = 100\%$
- (X = hours worked expressed as a percentage of annual time worked by a full-time worker)

Non-family labour force not  
regularly employed.

Number of working days of:

M05 Males

M06 Females

07 Other members of the holder's family  
(item 03) working on the holding for  
at least 75% of annual working time

a)\* up to 25 years old

M07 a1)\* males

M07 a2)\* females

b)\* up to 35 years old

M07 b1)\* males

M07 b2)\* females

N. HOLDER'S GAINFUL ACTIVITIES OTHER THAN  
THE ACTIVITY REFERRED TO IN M.

N01 Does the holder engage in any other  
gainful activity

Codes for N01, N02a, N02b, N03a),  
N03b), N04:

Answer	Code
yes	1
no	0
not applicable because holder is not the same person as the manager, or is not a natural person	8
for N04 no information is being provided	9



APPENDIX B2

Conversion Codes for Annual Work  
Units and Standard Livestock

S.O.E.C.

ANNEX 11

1975 FARM STRUCTURE SURVEY

Calculation of Annual Work Units

M.01 - M.04

<u>Class of time worked</u>	<u>Mid Point for calculation of Annual Work Units</u>
X < 25%	0.125
25% ≤ X < 50%	0.375
50% ≤ X < 75%	0.625
75% ≤ X < 100%	0.875
X = 100%	1.0

(X = hours worked expressed as a percentage of full time worked by a full-time worker).

M.05 - M.06

Number of working days	$\frac{8}{2200}$ Annual Work Units
100 working days	0.36363 a.w.u.'s



S.O.E.C.

APPENDIX 12

1966/67 LIVESTOCK COEFFICIENTS ADJUSTED TO CONFORM TO 1975 FARM  
STRUCTURE SURVEY HEADINGS

<u>K</u>		
01	Equidae	0.8
	<u>BOVINE ANIMALS</u>	
02	Under one year old	0.4
	Over one but under two years old	
03	Male	0.7
04	Female	0.7
	Two years old and over	
05	Male	1.0
06	Heifers	0.5
07	Dairy cows	1.0
08	Other cows	0.8
09	Sheep (all ages)	0.1
10	Goats (all ages)	0.1
	<u>PIGS</u>	
11	Piglets of live weight under 20 kg (100 head)	2.7
12	Breeding sows weighing 50 kg and over	0.5
13	Other pigs	0.3
	<u>POULTRY</u>	
14	Table fowl (100 head)	0.7
15	Laying hens (100 head)	1.4
16	Other poultry (ducks, turkeys, geese, guinea-fowl)(100 head)	3.0

APPENDIX C

Computer Programs Written for the Research



```

PROGRAM(SYST)
INPUT 1=MT0/FORMATTED(EECDATA)/512
OUTPUT 2=CP0
OUTPUT 3=CP1
OUTPUT 4=CP2
COMPRESS INTEGER AND LOGICAL
TRACE 1
END
MASTER SYST
DIMENSION Y(200),X(200),W(5),NW(5),NX(200)
NV=127
IND=1
DO 7 I=1,2202
IF(I,NE,1) GOTO 8
J=3
GOTO 9
8 J=9
9 DO 10 K=1,J
10 READ(1,501) ID
501 FORMAT(I3,//////////)
READ(1,200) (W(K),K=1,5),(X(J),J=1,127)
200 FORMAT(F1.0,F3.0,F2.0,2F10.0,2F1.0,3F10.0,F1.0,2X,12F1.0/
18F10.0/8F10.0/8F10.0/
210X,7F10.0/3F10.0,F1.0,9X,F1.0,9X,2F10.0,10X/10X,7F10.0/5F10.0,F1.
30,4F4.0,2F1.0,F4.0,2F1.0/4(F4.0,2F1.0),F4.0,5X,2F10.0,10X,F1.0,F4.
40,F1.0,5X/19F4.0/5F4.0,2F10.0,4F4.0,F1.0)
DO 307 K9=1,3
307 NW(K9)=IFIX(W(K9))
NW(4)=IFIX(W(4)/10000)
NW(5)=IFIX(W(5)/10000)
DO 308 K9=1,NV
308 NX(K9)=IFIX(X(K9))
WRITE(3,209)(NW(K),K=1,5),(NX(J),J=1,127)
209 FORMAT(I1,I3,I2,2I10,2I1,3I10,I1,2X,12I1/
18I10/8I10/8I10/
210X,7I10/3I10,I1,9X,I1,9X,2I10,10X/10X,7I10/5I10,I1
3,4I4,2I1,I4,2I1/4(I4,2I1),I4,5X,2I10,10X,I1,I4,
4I1,3X/19I4/5I4,2I10,4I4,I1)
DO 20 M=1,200
Y(M)=0.0
20 CONTINUE
X(34)=X(34)/100
X(36)=X(36)/100
X(41)=X(41)/100
X(49)=X(49)/100
TOT=0.0
DO 30 K=19,49
30 TOT=TOT+X(K)
Y(45)=X(3)+X(4)+X(5)
Y(46)=Y(45)+X(50)+X(51)+X(52)
IF(TOT,NE,Y(45))GOTO 40
IF(Y(45),EQ,0.0)GOTO 40
IF(X(96),EQ,9.0)X(96)=0.5
IF(X(96),EQ,5.0)X(96)=4.5
Y(48)=(X(96)-1)*0.25+0.125+0.125*(X(104)+X(116))+0.375*(X(105)+X(

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1117)))+0,625*(X(106)+X(118))+0,875*(X(107)+X(119))+X(108)+X(120)+(8
2*(X(121)+X(122))/2200))
IF(Y(48).EQ,0)GOTO 40
IF (Y(40).NE,0,0)GOTO 501
40 CALL OUT(W,X,NV,IND)
GOTO 7
501 IF(X(2).EQ,9,0)X(2)=0
Y(1)=X(2)+X(1)
Y(2)=X(3)/(Y(45)*0,01)
Y(3)=X(4)/(Y(45)*0,01)
Y(4)=X(5)/(Y(45)*0,01)
Y(5)=X(6)
Y(6)=X(7)+X(8)+X(9)+X(10)
Y(7)=X(11)/7+X(12)/7+X(13)/7+X(14)/7+X(15)/7+X(16)/7+X(17)/7
Y(8)=X(18)
Y(9)=(X(19)+X(20)+X(21)+X(22)+X(23)+X(24)+X(25)+X(26)
1+X(27))/(Y(45)*0,01)
Y(10)=(X(28)+X(29)+X(30))/(Y(45)*0,01)
Y(11)=X(31)/(Y(45)*0,01)
Y(12)=(X(33)+X(34)+X(35)+X(36))/(Y(45)*0,01)
Y(13)=(X(37)+X(38)+X(32)+X(39))/(Y(45)*0,01)
Y(14)=X(40)/(Y(45)*0,01)
Y(15)=(X(41))/(Y(45)*0,01)
Y(16)=X(42)/(Y(45)*0,01)
Y(17)=(X(43)+X(44)+X(45)+X(47)+X(48)+X(49))/(Y(45)*0,01)
Y(52)=X(46)/(Y(45)*0,01)
Y(18)=X(50)/((Y(45)+X(50))*0,01)
Y(19)=(X(51)+X(52))/(Y(46)*0,01)
IF(X(53).EQ,7,0)X(53)=1,0
IF(X(54).EQ,7,0)X(54)=1,0
Y(20)=X(53)
Y(21)=X(54)
Y(22)=0,6*X(55)
Y(53)=X(59)
Y(23)=0,4*X(56)+X(57)+0,5*X(58)+0,8*X(60)
Y(24)=0,1*(X(61)+X(62))
Y(25)=0,027*X(63)+0,5*X(64)+0,3*X(65)
Y(26)=X(66)*0,007+X(67)*0,014+X(68)*0,03
Y(47)=Y(22)+Y(23)+Y(24)+Y(25)+Y(26)+Y(53)
IF(Y(47).EQ,0,0)GOTO 50
Y(22)=Y(22)*100/Y(47)
Y(23)=Y(23)*100/Y(47)
Y(24)=Y(24)*100/Y(47)
Y(25)=Y(25)*100/Y(47)
Y(26)=Y(26)*100/Y(47)
Y(53)=Y(53)*100/Y(47)
50 Y(50)=Y(47)*100/Y(46)
Y(27)=X(69)
IF((X(70)+X(71)+X(72)+X(73)).GT,0)Y(28)=1
IF(X(76).GT,0)Y(29)=1
IF((X(79)+X(82)+X(85)+X(88)).GT,0)Y(30)=1
IF((X(74)+X(75)+X(77)+X(78)+X(80)+X(81)+X(83)+X(84)+
1 X(86)+X(87)+X(89)+X(90)).GT,0)Y(31)=1
DO 51 K=70,91
51 Y(49)=Y(49)+X(K)
Y(51)=Y(49)/(Y(46)*0,001)

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IF(X(91),GT,0,0) Y(32)=1
Y(33)=(X(36)+X(34)+X(49))/(Y(45)*0.01)
IF(X(94),EQ,1)Y(34)=1
IF(X(94),EQ,2)Y(35)=1
IF(X(95),EQ,0,0)X(95)=52.0
Y(36)=X(95)
Y(38)=((X(96)-1)*0.25+0.125+0.125*X(104)+0.375*X(105)+0.625*X(106)
1+0.875*X(107)+X(108))
Y(37)=Y(48)/(Y(46)*0.001)
Y(38)=Y(38)*100/Y(48)
IF(X(96),EQ,0,5)P=0,0
IF(X(96),NE,0,5)P=1,0
T=P+X(97)+X(98)+X(109)+X(110)
IF(T,NE,0,0) GO TO 502
T = 0,00001
502 IF(X(95),LT,25,0,AND,P,EQ,1,0)Y(39)=1.0
Y(39)=(Y(39)+X(99)+X(111))/(T*0.01)
IF((X(95),GE,25,0,AND,X(95),LT,35,0),AND,P,EQ,1,0)Y(40)=1.0
Y(40)=(Y(40)+X(100)+X(112))/(T*0.01)
IF((X(95),GE,35,0,AND,X(95),LT,45,0),AND,P,EQ,1,0)Y(41)=1.0
Y(41)=(Y(41)+X(101)+X(113))/(T*0.01)
IF((X(95),GE,45,0,AND,X(95),LT,65,0),AND,P,EQ,1,0)Y(42)=1.0
Y(42)=(Y(42)+X(102)+X(114))/(T*0.01)
IF((X(95),GE,65,0),AND,P,EQ,1)Y(43)=1
Y(43)=(Y(43)+X(103)+X(115))/(T*0.01)
IF(X(127),EQ,8,0)X(127)=0
Y(44)=X(127)
C1=0,0
C2=0,0
C3=0,0
C4=0,0
C5=0,0
C6=0,0
C7=0,0
C8=0,0
C9=0,0
CLASS=17
IF((Y(9)+Y(10)+Y(11)+Y(13)),GT,66,6)CLASS=3
IF(Y(9),GT,66,6)CLASS=1
IF(Y(9),LE,66,6,AND,Y(9),GT,33,3,AND,Y(10),LE,66,6,AND,
1Y(10),GT,33,3)CLASS=2
IF(Y(12),GT,66,6)CLASS=4
IF((Y(52)+Y(17)),GT,66,6)CLASS=6
IF(Y(52),GT,66,6)CLASS=5
IF(CLASS,NE,17) GOTO 70
IF(Y(16),GT,66,6)C1=1
IF(Y(16),LE,66,6,AND,Y(16),GT,33,3)C2=1
A=Y(22)+Y(53)+Y(23)+Y(24)
IF(A,GT,66,6)C3=1
IF(A,LE,66,6,AND,A,GT,33,3)C4=1
A=Y(25)+Y(26)
IF(A,GT,66,6)C5=1
IF(A,LE,66,6,AND,A,GT,33,3)C6=1
A=Y(9)+Y(10)+Y(11)+Y(13)
IF(A,LE,66,6,AND,A,GT,33,3)C7=1
IF(Y(12),LE,66,6,AND,Y(12),GT,33,3)C8=1

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```
IF((Y(52)+Y(17)),LE,66.0,AND,(Y(52)+Y(17)),GT,33.3)C9=1
IF(C1*C5,EQ,1)CLASS=8
IF(C1,EQ,1,AND,Y(53),GT,66.6)CLASS=7
IF(C5,EQ,1)CLASS=9
IF(CLASS,NE,17)GOTO 70
IF(C2*C4*C7,EQ,1,OR,C3*C2*C7,EQ,1,OR,C4*C1*C7,EQ,1)CLASS=10
IF(C2*C4*C6,EQ,1,OR,C3*C2*C6,EQ,1,OR,C4*C1*C6,EQ,1)CLASS=11
IF(C7*C6,EQ,1)CLASS=12
IF(C7*C9,EQ,1)CLASS=13
IF(C7*C8,EQ,1)CLASS=14
IF(CLASS,NE,17)GOTO 70
IF(C7,EQ,1)CLASS=15
IF(CLASS,NE,17)GOTO 70
IF(C4,EQ,1)CLASS=16
70 CONTINUE
WRITE(2,300) IND,Y(46),Y(45),Y(47),Y(48),Y(49)
300 FORMAT(2X,1HD,I4,8(1X,F8.2))
WRITE(2,300)IND,(Y(J),J=9,15 )
WRITE(2,300)IND,Y(16),Y(52),(Y(J),J=17,21)
WRITE(2,300)IND,Y(22),Y(53),(Y(J),J=23,26),Y(50)
WRITE(2,300)IND,(Y(J),J=37,43)
WRITE(2,300)IND,(Y(J),J=28,33),Y(27),Y(51)
WRITE(2,300)IND,Y(1),Y(8),Y(34),Y(35),Y(36),Y(44)
WRITE(2,300)IND,(Y(J),J=2,7)
WRITE(2,300)IND,W(1),CLASS
IND=IND+1
7 CONTINUE
STOP
END
```



```
SUBROUTINE OUT(W,X,NV,IND)
DIMENSION X(200),U(5)
WRITE(4,104)IND
104 FORMAT(////,9H BEFORE D,I4)
DO 100 I = 1,5
WRITE(4,101)W(I)
101 FORMAT(10X,F16,2)
100 CONTINUE
DO 102 I = 1,NV
IF(X(I),EQ,0,0)GOTO 102
WRITE(4,103)I,X(I)
102 CONTINUE
103 FORMAT(5H X(,I3,2H)=,F16,2)
RETURN
END
FINISH
```

```

PROGRAM(RANSAM)
INPUT 1=MT0/FORMATTED(EECDATA)/512
OUTPUT 2=CP1
OUTPUT 3=CP2
OUTPUT 4=LPO
OUTPUT 5=CPO
COMPRESS INTEGER AND LOGICAL
TRACE 1
END
MASTER RANSAM
DIMENSION IX(500),Y(200),NX(500),X(200),NIX(200),W(5),NW(5)
NV=127
IND=1
DO 1 I=1,500
NX(I)=0
18 XM=G05ABF(1,0,22026,0)
MX=IFIX(XM)
IX(I)=MX
IF(I.EQ,1)GOTO 1
DO 17 K=1,I=1
IF (IX(I).EQ,IX(K)) GOTO 18
17 CONTINUE
1 CONTINUE
DO 2 J=1,500
ICOUNT =0
DO 3 I=1,500
3 IF(IX(J),GE,IX(I))ICOUNT =ICOUNT+1
IEND=ICOUNT
DO 4 I=1,IEND
IF(NX(ICOUNT).EQ,0) GOTO 5
4 ICOUNT=ICOUNT-1
5 NX(ICOUNT)=IX(J)
2 CONTINUE
WRITE(3,100)
100 FORMAT(1X,'SAMPLE MEMBER POPULATION MEMBER')
DO 6 I=1,500
6 WRITE(3,207)I,NX(I)
207 FORMAT(5X,13,12X,15)
DO 7 I=1,500,
IF(I.NE,1) GOTO 8
J=NX(I)=1
GOTO 0
8 J=NX(I)-NX(I=1)=1
IF(J.EQ,0)GOTO 727
9 DO 10 K=1,J
10 READ(1,305) ID
305 FORMAT(I3,//////////)
727 READ(1,200) (W(K),K=1,5 ),(X(J),J=1,127)
200 FORMAT(F1.0,F3.0,F2.0,2F10.0,2F1.0,3F10.0,F1.0,2X,12F1.0/
18F10.0/8F10.0/8F10.0/
210X,7F10.0/3F10.0,F1.0,9X,F1.0,9X,2F10.0,10X/10X,7F10.0/5F10.0,F1.
30,4F4.0,2F1.0,F4.0,2F1.0/4(F4.0,2F1.0),F4.0,5X,2F10.0,10X,F1.0,F4.
40,F1.0,5X/19F4.0/5F4.0,2F10.0,4F4.0,F1.0)
DO 307 K9=1,3
307 NW(K9)=IFIX(W(K9))

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```

NW(4)=IFIX(W(4)/10000)
NW(5)=IFIX(W(5)/10000)
DO 308 K9=1,NV
508 NIX(K9)=IFIX(X(K9))
WRITE(5,209)(NW(K),K=1,5),(NIX(J),J=1,127)
209 FORMAT(I1,I3,I2,2I10,2I1,3I10,I1,2X,12I1/
18I10/8I10/8I10/
210X,7I10/3I10,I1,9X,I1,9X,2I10,10X/10X,7I10/5I10,I1
3,4I4,2I1,I4,2I1/4(I4,2I1),I4,5X,2I10,10X,I1,I4,
4I1,3X/19I4/5I4,2I10,4I4,I1)
DO 20 M=1,200
Y(M)=0.0
20 CONTINUE
X(34)=X(34)/100
X(36)=X(36)/100
X(41)=X(41)/100
X(49)=X(49)/100
TOT=0.0
DO 30 X=19,49
30 TOT=TOT+X(K)
Y(45)=X(3)+X(4)+X(5)
Y(46)=Y(45)+X(50)+X(51)+X(52)
IF(TOT.NE.Y(45))GOTO 40
IF(Y(45).EQ.0.0)GOTO 40
IF(X(96).EQ.9.0)X(96)=0.5
IF(X(96).EQ.5.0)X(96)=4.5
Y(48)=(X(96)-1)*0.25+0.125+0.125*(X(104)+X(116))+0.375*(X(105)+X(
1117))+0.625*(X(106)+X(118))+0.875*(X(107)+X(119))+X(108)+X(120)+(8
2*(X(121)+X(122))/2200)
IF(Y(48).EQ.0)GOTO 40
IF(Y(46).NE.0.0)GOTO 501
40 CALL OUT(W,X,NV,IND)
GOTO 7
501 IF(X(2).EQ.9.0)X(2)=0
Y(1)=X(2)*X(1)
Y(2)=X(3)/(Y(45)*0.01)
Y(3)=X(4)/(Y(45)*0.01)
Y(4)=X(5)/(Y(45)*0.01)
Y(5)=X(6)
Y(6)=X(7)+X(8)+X(9)+X(10)
Y(7)=X(11)/7+X(12)/7+X(13)/7+X(14)/7+X(15)/7+X(16)/7+X(17)/7
Y(8)=X(18)
Y(9)=(X(19)+X(20)+X(21)+X(22)+X(23)+X(24)+X(25)+X(26)
1+X(27))/(Y(45)*0.01)
Y(10)=(X(28)+X(29)+X(30))/(Y(45)*0.01)
Y(11)=X(31)/(Y(45)*0.01)
Y(12)=(X(33)+X(34)+X(35)+X(36))/(Y(45)*0.01)
Y(13)=(X(37)+X(38)+X(32)+X(39))/(Y(45)*0.01)
Y(14)=X(40)/(Y(45)*0.01)
Y(15)=(X(41))/(Y(45)*0.01)
Y(16)=X(42)/(Y(45)*0.01)
Y(17)=(X(43)+X(44)+X(45)+X(47)+X(48)+X(49))/(Y(45)*0.01)
Y(52)=X(46)/(Y(45)*0.01)
Y(18)=X(50)/(Y(45)+X(50))*0.01)
Y(19)=(X(51)+X(52))/(Y(46)*0.01)
IF(X(53).EQ.7.0)X(53)=1.0

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IF(X(54),EQ,7,0)X(54)=1,0
Y(20)=X(53)
Y(21)=X(54)
Y(22)=0,6*X(55)
Y(53)=X(59)
Y(23)=0,4*X(56)+X(57)+0,5*X(58)+0,8*X(60)
Y(24)=0,1*(X(61)+X(62))
Y(25)=0,027*X(63)+0,5*X(64)+0,3*X(65)
Y(26)=X(66)*0,007+X(67)*0,014+X(68)*0,03
Y(47)=Y(22)+Y(23)+Y(24)+Y(25)+Y(26)+Y(53)
IF(Y(47),EQ,0,0)GOTO 50
Y(22)=Y(22)*100/Y(47)
Y(23)=Y(23)*100/Y(47)
Y(24)=Y(24)*100/Y(47)
Y(25)=Y(25)*100/Y(47)
Y(26)=Y(26)*100/Y(47)
Y(53)=Y(53)*100/Y(47)
50 Y(50)=Y(47)*100/Y(46)
Y(27)=X(69)
IF((X(70)+X(71)+X(72)+X(73)),GT,0)Y(28)=1
IF(X(76),GT,0)Y(29)=1
IF((X(79)+X(82)+X(85)+X(88)),GT,0)Y(30)=1
IF((X(74)+X(75)+X(77)+X(78)+X(80)+X(81)+X(83)+X(84)+
1 X(86)+X(87)+X(89)+X(90)),GT,0)Y(31)=1
DO 51 K=70,91
51 Y(49)=Y(49)+X(K)
Y(51)=Y(49)/(Y(46)*0,001)
IF(X(91),GT,0,0) Y(32)=1
Y(33)=(X(36)+X(34)+X(49))/(Y(45)*0,01)
IF(X(94),EQ,1)Y(34)=1
IF(X(94),EQ,2)Y(35)=1
IF(X(95),EQ,0,0)X(95)=52,0
Y(36)=X(95)
Y(38)=((X(96)-1)*0,25+0,125+0,125*X(104)+0,375*X(105)+0,625*X(106)
1+0,875*X(107)+X(108))
Y(37)=Y(48)/(Y(46)*0,001)
Y(38)=Y(38)*100/Y(48)
IF(X(96),EQ,0,5)P=0,0
IF(X(96),NE,0,5)P=1,0
T=P+X(97)+X(98)+X(109)+X(110)
IF(T,NE,0,0) GO TO 502
T = 0,00001
502 IF(X(95),LT,25,0,AND,P,EQ,1,0)Y(39)=1,0
Y(39)=(Y(39)+X(99)+X(111))/(T*0,01)
IF((X(95),GE,25,0,AND,X(95),LT,35,0),AND,P,EQ,1,0)Y(40)=1,0
Y(40)=(Y(40)+X(100)+X(112))/(T*0,01)
IF((X(95),GE,35,0,AND,X(95),LT,45,0),AND,P,EQ,1,0)Y(41)=1,0
Y(41)=(Y(41)+X(101)+X(113))/(T*0,01)
IF((X(95),GE,45,0,AND,X(95),LT,65,0),AND,P,EQ,1,0)Y(42)=1,0
Y(42)=(Y(42)+X(102)+X(114))/(T*0,01)
IF((X(95),GE,65,0),AND,P,EQ,1)Y(43)=1
Y(43)=(Y(43)+X(103)+X(115))/(T*0,01)
IF(X(127),EQ,8,0)X(127)=0
Y(44)=X(127)
C1=0,0
C2=0,0

```



```

C3=0.0
C4=0.0
C5=0.0
C6=0.0
C7=0.0
C8=0.0
C9=0.0
CLASS=17
IF((Y(9)+Y(10)+Y(11)+Y(13)),GT,66.6)CLASS=3
IF(Y(9),GT,66.6)CLASS=1
IF(Y(9),LE,66.6,AND,Y(9),GT,33.3,AND,Y(10),LE,66.6,AND,
1 Y(10),GT,33.3)CLASS=2
IF(Y(12),GT,66.6)CLASS=4
IF((Y(52)+Y(17)),GT,66.6)CLASS=6
IF(Y(52),GT,66.6)CLASS=5
IF(CLASS,NE,17)GOTO 70
IF(Y(16),GT,66.6)C1=1
IF(Y(16),LE,66.6,AND,Y(16),GT,33.3)C2=1
A=Y(22)+Y(53)+Y(23)+Y(24)
IF(A,GT,66.6)C3=1
IF(A,LE,66.6,AND,A,GT,33.3)C4=1
A=Y(25)+Y(26)
IF(A,GT,66.6)C5=1
IF(A,LE,66.6,AND,A,GT,33.3)C6=1
A=Y(9)+Y(10)+Y(11)+Y(13)
IF(A,LE,66.6,AND,A,GT,33.3)C7=1
IF(Y(12),LE,66.6,AND,Y(12),GT,33.3)C8=1
IF((Y(52)+Y(17)),LE,66.6,AND,(Y(52)+Y(17)),GT,33.3)C9=1
IF(C1*C3,EQ,1)CLASS=8
IF(C1,EQ,1,AND,Y(53),GT,66.6)CLASS=7
IF(C5,EQ,1)CLASS=9
IF(CLASS,NE,17)GOTO 70
IF(C2*C4*C7,EQ,1,OR,C3*C2*C7,EQ,1,OR,C4*C1*C7,EQ,1)CLASS=10
IF(C2*C4*C6,EQ,1,OR,C3*C2*C6,EQ,1,OR,C4*C1*C6,EQ,1)CLASS=11
IF(C7*C6,EQ,1)CLASS=12
IF(C7*C9,EQ,1)CLASS=13
IF(C7*C8,EQ,1)CLASS=14
IF(CLASS,NE,17)GOTO 70
IF(C7,EQ,1)CLASS=15
IF(CLASS,NE,17)GOTO 70
IF(C4,EQ,1)CLASS=16
70 CONTINUE
WRITE(2,300)IND,Y(46),Y(45),Y(47),Y(48),Y(49)
300 FORMAT(2X,1HC,14,8(1X,F8.2))
WRITE(2,300)IND,(Y(J),J=9,15)
WRITE(2,300)IND,Y(16),Y(52),(Y(J),J=17,21)
WRITE(2,300)IND,Y(22),Y(53),(Y(J),J=23,26),Y(50)
WRITE(2,300)IND,(Y(J),J=37,43)
WRITE(2,300)IND,(Y(J),J=28,33),Y(27),Y(51)
WRITE(2,300)IND,Y(1),Y(8),Y(34),Y(35),Y(36),Y(44)
WRITE(2,300)IND,(Y(J),J=2,7)
WRITE(2,300)IND,W(1),CLASS
IND=IND+1
7 CONTINUE
STOP
END

```



```

PROGRAM(CCLASS)
INPUT 3=MT0/FORMATTED(EECDATA)/512
OUTPUT 6=CP0
OUTPUT 4=LP0
OUTPUT 7=LP1
INPUT 1=CR0
INPUT 2=CR1
COMPRESS INTEGER AND LOGICAL
TRACE 1
END
MASTER CLASS
DIMENSION Z(60),NO(30),SUMZ(30,60),SUMZ2(30,60),ZMIN(30,60)
DIMENSION ZMAX(30,60),TSUMZ(60),TSUMZ2(60),TZMIN(60),TZMAX(60)
DIMENSION SMEAN(30,60),SMIN(30,60),SMAX(30,60)
DIMENSION LABEL(80),LABELA(440),NLAND(30,6),NTLAND(6)
REAL LABEL,LABELA
COMMON LABEL,LABELA
READ(2,59)(LABEL(I),I=1,10)
READ(2,59)(LABELA(I),I=1,53)
59 FORMAT(10A8)
READ(2,119) NOBS,NV,NCLASS,NCV
119 FORMAT(4I0)
DO 1 J=1,NV=2
TSUMZ(J)=0
TSUMZ2(J)=0
TZMIN(J)=100000
TZMAX(J)=-100000
DO 1 K=1,NCLASS
NO(K)=0
DO 14 L=1,6
14 NLAND(K,L)=0
SUMZ(K,J)=0
SUMZ2(K,J)=0
ZMIN(K,J)=100000
ZMAX(K,J)=-100000
1 CONTINUE
DO 13 L=1,6
13 NTLAND(L)=0
DO 2 I=1,NOBS
READ(1,200) (Z(J),J=1,NV)
200 FORMAT(7X,5F0,0/4(7X,7F0,0/),7X,8F0,0/2(7X,6F0,0/),7X,2F0,0)
K=Z(NCV)
NO(K)=NO(K)+1
L=Z(54)
NLAND(K,L)=NLAND(K,L)+1
DO 3 J=1,NV=2
SUMZ(K,J)=SUMZ(K,J)+Z(J)
SUMZ2(K,J)=SUMZ2(K,J)+Z(J)**2
IF(Z(J),GE,ZMIN(K,J))GOTO 7
ZMIN(K,J)=Z(J)
7 IF(Z(J),LE,ZMAX(K,J))GO TO 6
ZMAX(K,J)=Z(J)
6 TSUMZ(J)=TSUMZ(J)+Z(J)
TSUMZ2(J)=TSUMZ2(J)+Z(J)**2

```



```

      IF(Z(J),GE,TZMIN(J)) GOTO 9
      TZMIN(J)=Z(J)
9     IF(Z(J),LE,TZMAX(J)) GOTO 8
      TZMAX(J)=Z(J)
8     CONTINUE
3     CONTINUE
2     CONTINUE
      DO 4 J=1,NV=2
      IF(TSUMZ2(J),EQ,0)GOTO 4
      TSUMZ(J)=TSUMZ(J)/NOBS
      TSUMZ2(J)=SQRT(TSUMZ2(J)/NOBS-TSUMZ(J)**2)
      DO 4 K=1,NCLASS
      IF(NO(K),EQ,0)GOTO 4
      SUMZ(K,J)=SUMZ(K,J)/NO(K)
      SUMZ2(K,J)=SQRT(SUMZ2(K,J)/NO(K)-SUMZ(K,J)**2)
      SMEAN(K,J)=(SUMZ(K,J)-TSUMZ(J))/TSUMZ2(J)
      SMIN(K,J)=(ZMIN(K,J)-TSUMZ(J))/TSUMZ2(J)
      SMAX(K,J)=(ZMAX(K,J)-TSUMZ(J))/TSUMZ2(J)
4     CONTINUE
      WRITE(4,309)(LABEL(M),M=1,10)
309  FORMAT(1X///,10A8/)
      WRITE(4,300)NOBS
300  FORMAT(1X/' TOTAL SAMPLE/'/' NO. OF OBSERVATIONS =' ,I5//
1'  VARIABLE      MEAN      STAN.DEV.    MINIMUM    MAXIMUM'//)
      DO 10 J=1,NV=2
      WRITE(4,400)LABELA(J),TSUMZ(J),TSUMZ2(J),TZMIN(J),TZMAX(J)
400  FORMAT(1X,A8,4(1X,E10,4))
10   CONTINUE
      WRITE(4,700)
700  FORMAT(//' FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG'//)
      WRITE(4,800)(NTLAND(L),L=1,6)
800  FORMAT(2X,I4,4X,I4,3X,I4,4X,I4,4X,I4,4X,I4)
      DO 11 K=1,NCLASS
      WRITE(4,309)(LABEL(M),M=1,10)
      WRITE(4,500)K,NO(K)
500  FORMAT(1X/' CLASS ' ,I3,/' NO. OF OBSERVATIONS =' ,I5//
1'  VARIABLE      MEAN      STAN.DEV.    MINIMUM    MAXIMUM      SMEAN
2'  SMINIMUM      SMAXIMUM '//)
      DO 12 J=1,NV=2
      WRITE(4,600)LABELA(J),SUMZ(K,J),SUMZ2(K,J),ZMIN(K,J),ZMAX(K,J),
1SMEAN(K,J),SMIN(K,J),SMAX(K,J)
600  FORMAT(1X,A8,4(1X,E10,4),3(1X,F10,2))
12   CONTINUE
      WRITE(4,700)
      WRITE(4,800)(NLAND(K,L),L=1,6)
11   CONTINUE
      CALL ANOVA(SUMZ,TSUMZ2,TSUMZ,NO,NOBS,NCLASS,NV=2)
      STOP
      END

```



```

SUBROUTINE ANOVA(GM,SD,ZMEAN,NOBSG,NOBTOT,NG,NVAR)
REAL LABEL,LABELA
DIMENSION GM(30,60),SD(60),ZMEAN(60),NOBSG(30)
DIMENSION LABEL(80),LABELA(440)
COMMON LABEL,LABELA
TSS=NOBTOT*NVAR
BSS=0.0
DO 2 I=1,NVAR
DO 3 J=1,NG
SS=NOBSG(J)*((GM(J,I)-ZMEAN(I))/SD(I))**2
3 BSS=BSS+SS
2 CONTINUE
K=1
L=9
DO 98 M=1,6
WRITE(7,70)(LABEL(I),I=1,10)
70 FORMAT(1H1,10A8//1X,'GROUP MEANS',46X,'VARIABLES',50X,'SIZE')
WRITE(7,500)(LABELA(I),I=K,K+L)
IF(M.EQ,6)GOTO 103
DO 101 J=1,NG
101 WRITE(7,600) J,(GM(J,I),I=K,K+L),NOBSG(J)
WRITE(7,605)(ZMEAN(I),I=K,K+L),NOBTOT
605 FORMAT(/1X,'TOTAL',1X,9(E10.4,1X),E10.4,15)
K=K+10
GOTO 97
103 DO 104 J=1,NG
104 WRITE(7,700)J,(GM(J,I),I=K,K+L),NOBSG(J)
WRITE(7,705)(ZMEAN(I),I=K,K+L),NOBTOT
705 FORMAT(/1X,'TOTAL',1X,3(E10.4,1X),76X,15)
700 FORMAT(2X,12,3X,3(E10.4,1X),77X,14)
97 IF(M.EQ,5)L=2
98 CONTINUE
500 FORMAT(1X,'GROUP',1X,10(A8,3X))
600 FORMAT(2X,12,3X,10(E10.4,1X),14)
WSS=TSS-BSS
P1=WSS*100/TSS
P2=BSS*100/TSS
P3=P1+P2
WRITE(7,60)(LABEL(I),I=1,10),NG,NVAR,NOBTOT
60 FORMAT(1H1,10A8//5X,'NO. OF GROUPS= ',13/5X,'NO. OF VARIABLES= ',
113/5X,'NO. OF OBSERVATIONS= ',15)
WRITE(7,901)WSS,P1
901 FORMAT(/,30X,7HSUMMARY,//20X,15H SUM OF SQUARES ,5X,
110HPERCENTAGE,/,5X,15HWITHIN GROUPS,3X,E12.4,4X,E11.4)
WRITE(7,902)BSS,P2,TSS,P3
902 FORMAT(2X,14HBETWEEN GROUPS,2X,E12.4,4X,E11.4,/,5X,5HTOTAL,11X,
1E12.4,4X,E11.4)
RETURN
END
FINISH

```



```

PROGRAM(POPU)
INPUT 1=MTU/FORMATTED(EECDATA)/512
OUTPUT 4=CP2
OUTPUT 5=LPO
OUTPUT 6=LP1
INPUT 8=CR0
COMPRESS INTEGER AND LOGICAL
TRACE 1
END
MASTER POPU
DIMENSION Z(60),NO(30),SUMZ(30,60),SUMZ2(30,60),ZMIN(30,60)
DIMENSION ZMAX(30,60),TSUMZ(60),TSUMZ2(60),TZMIN(60),TZMAX(60)
DIMENSION SMEAN(30,60),SMIN(30,60),SMAX(30,60)
DIMENSION LABEL(80),LABELA(440),NLAN(30,6),NTLAND(6)
DIMENSION Y(200),X(200),W(5)
REAL LABEL,LABELA
COMMON LABEL,LABELA
READ(8,59)(LABEL(I),I=1,10)
READ(8,59)(LABELA(I),I=1,53)
59 FORMAT(10A8)
READ(8,119) NV,NCLASS,NCV
119 FORMAT(3I0)
NOUT=0
DO 1 J=1,NV-2
TSUMZ(J)=0
TSUMZ2(J)=0
TZMIN(J)=100000
TZMAX(J)=-100000
DO 1 K=1,NCLASS
NO(K)=0
DO 14 L=1,6
14 NLAN(K,L)=0
SUMZ(K,J)=0
SUMZ2(K,J)=0
ZMIN(K,J)=100000
ZMAX(K,J)=-100000
1 CONTINUE
DO 13 L=1,6
13 NTLAND(L)=0
DO 17 I=1,22026
READ(1,200) (W(K);K=1,5 ),(X(J);J=1,127)
200 FORMAT(F1.0,F3.0,F2.0,2F10.0,2F1.0,3F10.0,F1.0,2X,12F1.0/
18F10.0/8F10.0/8F10.0/
210X,7F10.0/3F10.0,F1.0,9X,F1.0,9X,2F10.0,10X/10X,7F10.0/5F10.0,F1.
30,4F4.0,2F1.0,F4.0,2F1.0/4(F4.0,2F1.0),F4.0,5X,2F10.0,10X,F1.0,F4.
40,F1.0,5X/19F4.0/5F4.0,2F10.0,4F4.0,F1.0)
X(34)=X(34)/100
X(36)=X(36)/100
X(41)=X(41)/100
X(49)=X(49)/100
DO 20 M=1,200
Y(M)=0.0
20 CONTINUE
TOT=0.0
DO 30 K=19,49

```



```

30 TOT=TOT+X(K)
   Y(45)=X(3)+X(4)+X(5)
   Y(46)=Y(45)+X(50)+X(51)+X(52)
   IF(TOT.NE.Y(45))GOTO 40
   IF(Y(45).EQ.0,0)GOTO 40
   IF(X(96).EQ.9,0)X(96)=0,5
   IF(X(96).EQ.5,0)X(96)=4,5
   Y(48)=(X(96)-1)*0,25+0,125*(X(104)+X(116))+0,375*(X(105)+X(
1117))+0,625*(X(106)+X(118))+0,875*(X(107)+X(119))+X(108)+X(120)+(8
2*(X(121)+X(122))/2200))
   IF(Y(48).EQ.0)GOTO 40
   IF (Y(46).NE.0,0)GOTO 501
40 CALL OUT(W,X,NV,IND)
   NOUT=NOUT+1
   GOTO 17
501 IF(X(2).EQ.9,0)X(2)=0
   Y(1)=X(2)+X(1)
   Y(2)=X(3)/(Y(45)*0,01)
   Y(3)=X(4)/(Y(45)*0,01)
   Y(4)=X(5)/(Y(45)*0,01)
   Y(5)=X(6)
   Y(6)=X(7)+X(8)+X(9)+X(10)
   Y(7)=X(11)/7+X(12)/7+X(13)/7+X(14)/7+X(15)/7+X(16)/7+X(17)/7
   Y(8)=X(18)
   Y(9)=(X(19)+X(20)+X(21)+X(22)+X(23)+X(24)+X(25)+X(26)
1+X(27))/(Y(45)*0,01)
   Y(10)=(X(28)+X(29)+X(30))/(Y(45)*0,01)
   Y(11)=X(31)/(Y(45)*0,01)
   Y(12)=(X(33)+X(34)+X(35)+X(36))/(Y(45)*0,01)
   Y(13)=(X(37)+X(38)+X(32)+X(39))/(Y(45)*0,01)
   Y(14)=X(40)/(Y(45)*0,01)
   Y(15)=(X(41))/(Y(45)*0,01)
   Y(16)=X(42)/(Y(45)*0,01)
   Y(17)=(X(43)+X(44)+X(45)+X(47)+X(48)+X(49))/(Y(45)*0,01)
   Y(52)=X(46)/(Y(45)*0,01)
   Y(18)=X(50)/((Y(45)+X(50))*0,01)
   Y(19)=(X(51)+X(52))/(Y(46)*0,01)
   IF(X(53).EQ.7,0)X(53)=1,0
   IF(X(54).EQ.7,0)X(54)=1,0
   Y(20)=X(53)
   Y(21)=X(54)
   Y(22)=0,6*X(55)
   Y(53)=X(59)
   Y(23)=0,4*X(56)+X(57)+0,5*X(58)+0,8*X(60)
   Y(24)=0,1*(X(61)+X(62))
   Y(25)=0,027*X(63)+0,5*X(64)+0,3*X(65)
   Y(26)=X(66)*0,007+X(67)*0,014+X(68)*0,03
   Y(47)=Y(22)+Y(23)+Y(24)+Y(25)+Y(26)+Y(53)
   IF(Y(47).EQ.0,0)GOTO 50
   Y(22)=Y(22)*100/Y(47)
   Y(23)=Y(23)*100/Y(47)
   Y(24)=Y(24)*100/Y(47)
   Y(25)=Y(25)*100/Y(47)
   Y(26)=Y(26)*100/Y(47)
   Y(53)=Y(53)*100/Y(47)
50 Y(50)=Y(47)*100/Y(46)

```



```

Y(27)=X(69)
IF((X(70)+X(71)+X(72)+X(73)),GT,0)Y(28)=1
IF(X(76),GT,0)Y(29)=1
IF((X(79)+X(82)+X(85)+X(88)),GT,0)Y(30)=1
IF((X(74)+X(75)+X(77)+X(78)+X(80)+X(81)+X(83)+X(84)+
1 X(86)+X(87)+X(89)+X(90)),GT,0)Y(31)=1
DO 51 K=70,91
51 Y(49)=Y(49)+X(K)
Y(51)=Y(49)/(Y(46)*0,001)
IF(X(91),GT,0,0) Y(32)=1
Y(33)=(X(36)+X(34)+X(49))/(Y(45)*0,01)
IF(X(94),EQ,1)Y(34)=1
IF(X(94),EQ,2)Y(35)=1
IF(X(95),EQ,0,0)X(95)=52,0
Y(36)=X(95)
Y(38)=((X(96)-1)*0,25+0,125+0,125*X(104)+0,375*X(105)+0,625*X(106)
1+0,875*X(107)+X(108))
Y(37)=Y(48)/(Y(46)*0,001)
Y(38)=Y(38)+100/Y(48)
IF(X(96),EQ,0,5)P=0,0
IF(X(96),NE,0,5)P=1,0
T=P+X(97)+X(98)+X(109)+X(110)
IF(T,NE,0,0) GO TO 502
T = 0,00001
502 IF(X(95),LT,25,0,AND,P,EQ,1,0)Y(39)=1,0
Y(39)=(Y(39)+X(99)+X(111))/(T*0,01)
IF((X(95),GE,25,0,AND,X(95),LT,35,0),AND,P,EQ,1,0)Y(40)=1,0
Y(40)=(Y(40)+X(100)+X(112))/(T*0,01)
IF((X(95),GE,35,0,AND,X(95),LT,45,0),AND,P,EQ,1,0)Y(41)=1,0
Y(41)=(Y(41)+X(101)+X(113))/(T*0,01)
IF((X(95),GE,45,0,AND,X(95),LT,65,0),AND,P,EQ,1,0)Y(42)=1,0
Y(42)=(Y(42)+X(102)+X(114))/(T*0,01)
IF((X(95),GE,65,0),AND,P,EQ,1)Y(43)=1
Y(43)=(Y(43)+X(103)+X(115))/(T*0,01)
IF(X(127),EQ,8,0)X(127)=0
Y(44)=X(127)
C1=0,0
C2=0,0
C3=0,0
C4=0,0
C5=0,0
C6=0,0
C7=0,0
C8=0,0
C9=0,0
CLASS=17
IF((Y(9)+Y(10)+Y(11)+Y(13)),GT,66,6)CLASS=3
IF(Y(9),GT,66,6)CLASS=1
IF(Y(9),LE,66,6,AND,Y(9),GT,33,3,AND,Y(10),LE,66,6,AND,
1 Y(10),GT,33,3)CLASS=2
IF(Y(12),GT,66,6)CLASS=4
IF((Y(52)+Y(17)),GT,66,6)CLASS=6
IF(Y(52),GT,66,6)CLASS=5
IF(CLASS,NE,17) GOTO 70
IF(Y(16),GT,66,6)C1=1
IF(Y(16),LE,66,6,AND,Y(16),GT,33,3)C2=1

```



```

A=Y(22)+Y(53)+Y(23)+Y(24)
IF(A.GT,66.6)C3=1
IF(A.LE,66.6,AND,A.GT,33.3)C4=1
A=Y(25)+Y(26)
IF(A.GT,66.6)C5=1
IF(A.LE,66.6,AND,A.GT,33.3)C6=1
A=Y(9)+Y(10)+Y(11)+Y(13)
IF(A.LE,66.6,AND,A.GT,33.3)C7=1
IF(Y(12).LE,66.6,AND,Y(12).GT,33.3)C8=1
IF((Y(52)+Y(17)).LE,66.6,AND,(Y(52)+Y(17)).GT,33.3)C9=1
IF(C1*C5,EQ,1)CLASS=8
IF(C1,EQ,1,AND,Y(53).GT,66.6)CLASS=7
IF(C5,EQ,1)CLASS=9
IF(CLASS,NE,17)GOTO 70
IF(C2*C4*C7,EQ,1,OR,C3*C2*C7,EQ,1,OR,C4*C1*C7,EQ,1)CLASS=10
IF(C2*C4*C6,EQ,1,OR,C3*C2*C6,EQ,1,OR,C4*C1*C6,EQ,1)CLASS=11
IF(C7*C6,EQ,1)CLASS=12
IF(C7*C9,EQ,1)CLASS=13
IF(C7*C8,EQ,1)CLASS=14
IF(CLASS,NE,17)GOTO 70
IF(C7,EQ,1)CLASS=15
IF(CLASS,NE,17)GOTO 70
IF(C4,EQ,1)CLASS=16
70 CONTINUE
Z(42)=Y(1)
Z(43)=Y(8)
DO 77 K1=2,7
77 Z(46+K1)=Y(K1)
DO 78 K1=9,16
78 Z(K1-3)=Y(K1)
Z(14)=Y(52)
DO 79 K1=17,22
79 Z(K1-2)=Y(K1)
Z(21)=Y(53)
DO 80 K1=23,26
80 Z(K1-1)=Y(K1)
Z(40)=Y(27)
DO 81 K1=28,33
81 Z(K1+6)=Y(K1)
DO 82 K1=34,36
82 Z(K1+10)=Y(K1)
DO 83 K1=37,43
83 Z(K1-10)=Y(K1)
Z(47)=Y(44)
Z(2)=Y(45)
Z(1)=Y(46)
DO 84 K1=47,49
84 Z(K1-44)=Y(K1)
Z(26)=Y(50)
Z(41)=Y(51)
Z(54)=W(1)
Z(55)=CLASS
K=Z(NCV)
NO(K)=NO(K)+1
L=Z(54)
NTLAND(L)=NTLAND(L)+1

```



```

NLAND(K,L)=NLAND(K,L)+1
DO 3 J=1,NV=2
SUMZ(K,J)=SUMZ(K,J)+Z(J)
SUMZ2(K,J)=SUMZ2(K,J)+Z(J)**2
IF(Z(J),GE,ZMIN(K,J))GOTO 7
ZMIN(K,J)=Z(J)
7 IF(Z(J),LE,ZMAX(K,J))GO TO 6
ZMAX(K,J)=Z(J)
6 TSUMZ(J)=TSUMZ(J)+Z(J)
TSUMZ2(J)=TSUMZ2(J)+Z(J)**2
IF(Z(J),GE,TZMIN(J)) GOTO 9
TZMIN(J)=Z(J)
9 IF(Z(J),LE,TZMAX(J)) GOTO 8
TZMAX(J)=Z(J)
8 CONTINUE
3 CONTINUE
17 CONTINUE
NOBS=22026-NOUT
DO 4 J=1,NV=2
IF(TSUMZ2(J),EQ,0)GOTO 4
TSUMZ(J)=TSUMZ(J)/NOBS
TSUMZ2(J)=SQRT(TSUMZ2(J)/NOBS-TSUMZ(J)**2)
DO 4 K=1,NCLASS
IF(NO(K),EQ,0)GOTO 4
SUMZ(K,J)=SUMZ(K,J)/NO(K)
SUMZ2(K,J)=SQRT(SUMZ2(K,J)/NO(K)-SUMZ(K,J)**2)
SMEAN(K,J)=(SUMZ(K,J)-TSUMZ(J))/TSUMZ2(J)
SMIN(K,J)=(ZMIN(K,J)-TSUMZ(J))/TSUMZ2(J)
SMAX(K,J)=(ZMAX(K,J)-TSUMZ(J))/TSUMZ2(J)
4 CONTINUE
WRITE(5,309)(LABEL(M),M=1,10)
309 FORMAT(1X///10A8/)
WRITE(5,300)NOBS
300 FORMAT(1X/' TOTAL SAMPLE'/' NO. OF OBSERVATIONS =' ,I5//
1' VARIABLE MEAN STAN.DEV. MINIMUM MAXIMUM '/')
DO 10 J=1,NV=2
WRITE(5,400)LABELA(J),TSUMZ(J),TSUMZ2(J),TZMIN(J),TZMAX(J)
400 FORMAT(1X,A8,4(1X,E10,4))
10 CONTINUE
WRITE(5,700)
700 FORMAT(//' FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG'//)
WRITE(5,800)(NLAND(L),L=1,6)
800 FORMAT(2X,I4,4X,I4,3X,I4,4X,I4,4X,I4,4X,I4)
DO 11 K=1,NCLASS
WRITE(5,309)(LABEL(M),M=1,10)
WRITE(5,500)K,NO(K)
500 FORMAT(1X/' CLASS ' ,I3,/' NO. OF OBSERVATIONS =' ,I5//
1' VARIABLE MEAN STAN.DEV. MINIMUM MAXIMUM SMEAN
2 SMINIMUM SMAXIMUM '/')
DO 12 J=1,NV=2
WRITE(5,600)LABELA(J),SUMZ(K,J),SUMZ2(K,J),ZMIN(K,J),ZMAX(K,J),
1SMEAN(K,J),SMIN(K,J),SMAX(K,J)
600 FORMAT(1X,A8,4(1X,E10,4),3(1X,F10,2))
12 CONTINUE
WRITE(5,700)
WRITE(5,800)(NLAND(K,L),L=1,6)

```

```
11 CONTINUE
   CALL ANOVA(SUMZ,TSUMZ2,TSUMZ,NO,NOBS,NCLASS,NV=2)
   STOP
   END
```



```
PROGRAM(TEMP)
USE 1=MT0/UNFORMATTED(SCRATCH1)
USE 2=MT1/UNFORMATTED(SCRATCH2)
INPUT 3=CRO
OUTPUT 4=CP0
TRACE 2
COMPRESS INTEGER AND LOGICAL
END
MASTER TEMP
DIMENSION X(8)
REAL IND
READ(3,100)NOBS
100 FORMAT(I0)
DO 1 I=1,NOBS
READ(3,200)IND,INO,(X(J),J=1,8)
200 FORMAT(A8,I0,8F0,0)
1 WRITE(1)IND,(X(J),J=1,8)
ENDFILE 1
REWIND 1
DO 2 I=1,NOBS
READ(3,200)IND,INO,(X(J),J=1,8)
WRITE(2)IND,(X(J),J=1,8)
2 CONTINUE
ENDFILE 2
REWIND 2
DO 3 I=1,NOBS
READ(1)IND,(X(J),J=1,8)
WRITE(4,300)IND,(X(J),J=1,8)
300 FORMAT(A8,8(1X,F8,4))
READ(2)IND,(X(J),J=1,8)
WRITE(4,300)IND,(X(J),J=1,8)
READ(3,200)IND,INO,(X(J),J=1,8)
WRITE(4,300)IND,(X(J),J=1,8)
3 CONTINUE
STOP
END
FINISH
```

```

PROGRAM (ANYL)
COMPRESS INTEGER AND LOGICAL
INPUT 3 = TR0
INPUT 1 = CR0
OUTPUT2 = LP0
OUTPUT4 = CP0
OUTPUT5=CP1
TRACE1
END
MASTER ANYL
INTEGER XDIAG
DIMENSION COMMENT(10) ,FORM(100)
DIMENSION TD(3),W(40)
COMMON /A/ XTX(1600),XDIAG(40) /B/XMEAN(40) ,XSTD(40),NM(40)
COMMON /E/ CONST,BETA(40),STER(40),TVAL(40),F,RR,SS,RSS,SIGMAT
COMMON /C/ LVAR(40), TITLE(40) /D/ N1,N2
COMMON/F/X(40000)
COMMON /G/NX(2500),WSSQ(40)
DATA TD(1) / 24HCOMP 1 COMP 2 COMP 3 /
WRITE(2,300)
300 FORMAT(1H1,////,20X,34HUNIVERSITY OF ASTON IN BIRMINGHAM /19X,
1 39H MANAGEMENT CENTRE /22X,8HCLUSTER ,
1 23H ANALYSIS OCTOBER 1976 /31X,25HP.A.GOLDER & K.A.YEOMANS )
NC = 1
NY = 1
CALL COMIN(NV,NOBS,COMMENT,FORM,1)
CALL DATAFO(X,NOBS,NV,FORM,1)
CALL ADATA(X,NV,NOBS)
CALL HOUT(NV,NOBS)
100 FORMAT(40I1)
READ(NC,100) (LVAR(I),I=1,NV)
NVAR=0
DO 1201 KL=1,NV
1201 NVAR=NVAR+LVAR(KL)
READ(NC,400) NW
IF(NW.LE,1) GO TO 10
DO 10 I=1,NV
IF(LVAR(I).EQ,0) GO TO 10
READ(NC,500) W(I)
500 FORMAT(F0.0)
10 CONTINUE
IF(NW.EQ,0.OR,NW.EQ,2)GO TO 11
CALL CORR(X,NV,NOBS,0)
CALL COUT(NV,1,NV,NV)
CALL ADATA(X,NV,NOBS)
CALL HOUT(NV,NOBS)
11 IF(NW.LE,1)GO TO 13
DO 12 I=1,NV
IF(LVAR(I).EQ,0) GO TO 12
WI=W(I)
KJ=(I-1)*NOBS
XSTD(I)=XSTD(I)*WI
XMEAN(I)=XMEAN(I)*WI
DO 12 J=1,NOBS
KJ=KJ+1

```



```
X(KJ)=X(KJ)*WI
12 CONTINUE
CALL HOUT(NV,NOBS)
13 CONTINUE
READ(NC,200) N1,N2,N3,MZ
400 FORMAT(I0)
200 FORMAT(4I0)
IF(N1.LE.0) GO TO 19
NXBS=NOBS+1
CALL RANK(X(NXBS),NOBS,NX(NXBS),NXBS)
JB = NOBS
XNGR=(1.0+FLOAT(NOBS))/FLOAT(N1)
DO 30 I=1,NOBS
JB = JB + 1
XNX=FLOAT(NX(JB))/XNGR
NX(I)=INT(XNX)+1
30 CONTINUE
GO TO 20
19 N1 = -N1
READ(NC,209) (NX(I),I=1,NOBS)
209 FORMAT(20I0)
20 NZ=N1+1
N7A=N1
NAC = 1
CALL XMSS(NOBS,NV,X,1,NZ=1)
DO 40 I= 1,N1
NZ=NZ-1

NR = 0
IF(NZ.LE.N2.AND.NZ.GE.N5) NR =1
IF(I.LE.2)GOTO 77
CALL CLUST(NZ,NOBS,NV,X,MZ,1)
GOTO 78
77 CALL CLUST(NZ,NOBS,NV,X,MZ+2,1)
78 CALL ANOUT(NZ,NOBS,NV,X,1,NR)
CALL KLESS(NZ,NOBS,NV,X,1)
40 CONTINUE
CALL ADATA(X,NV,NOBS)
CALL HOUT(NV,NOBS)
CALL BEALE(NOBS,NVAR,N7A)
STOP
END
```

```
SUBROUTINE NULL  
COMMON /A/ XM(1600),NX(40)  
DO 10 I=1,40  
10 NX(I) = 0  
DO 20 I=1,1600  
20 XM(I) = 0.0  
RETURN  
END
```



```
SUBROUTINE XMSS(NOBS,NV,X,NG,NZ)
DIMENSION X(NOBS,NV)
COMMON /C/LVAR(40),TITLE(40)
COMMON /A/ XM(40,40),NX(40)
COMMON /G/NK(<500),WSSQ(40)
CALL NULL
DO 20 J=1,NOBS
K = NK(J)
DO 50 IA=NG,NV
IF(LVAR(IA),NE,1) GO TO 50
XT = X(J,IA)
XH(IA,K) = XM(IA,K) * XT
50 CONTINUE
NX(K) = NX(K) + 1
20 CONTINUE
RETURN
END
```

```

SUBROUTINE ANOUT(KLUST,NOBS,NV,X,NG,NZ)
DIMENSION X(NOBS,NV),JCOUNT(2500),YSS(2500)
DIMENSION Z(40)
COMMON /C/LVAR(40),TITLE(40)
COMMON /A/ XM(40,40),NX(40) /B/XMEAN(40),XSTD(40),NM(40)
COMMON /G/NK(2500),WSSQ(40)
WRITE(2,301)
WRITE(5,775)(NK(J),J=1,NOBS)
775 FORMAT(20(1X,I3))
WRITE(5,776)
776 FORMAT(//,'****',//)
301 FORMAT(1H1)
TSSK=0.0
DO 20 K=1,KLUST
DO 27 MA=1,NOBS
JCOUNT(MA)=0
YSS(MA)=0.0
27 CONTINUE
IF(NZ,NE,1)GOTO 58
300 FORMAT(///, 8H GROUP ,I2 ,/, 40H OBSERVATION DISTANCE FROM GROUP
1 MEAN ,40H OBSERVATION DISTANCE FROM GROUP MEAN ,40H OBSERVATIO
2H DISTANCE FROM GROUP MEAN ,//)
WRITE(2,300) K
58 SSK=0.0
NNK=0
DO 30 J=1,NOBS
IF(NK(J),NE,K) GO TO 30
NNK=NNK+1
SS= 0.0
DO 40 I=NG,NV
IF(LVAR(I),NE,1) GO TO 40
XT = X(J,I)-XM(I,K)/NX(K)
SS = SS+ XT*XT
40 CONTINUE
SSK=SSK+SS
JCOUNT(NNK)=J
YSS(NNK)=SS
30 CONTINUE
IF(NZ,NE,1)GOTO 59
WRITE(2,400)(JCOUNT(I),YSS(I),JCOUNT(I+1),YSS(I+1),JCOUNT(I+2),
1YSS(I+2),I=1,NNK,3)
400 FORMAT(3(5X,I3,10X,E10.4,12X))
WRITE(2,401)
401 FORMAT(' OBSERVATIONS IN GROUP &WITHIN GROUP S.S. ')
402 FORMAT(34H FINAL COL. SHOWS CONTRIBUTION TO ,
146H TOTAL SUM OF SQUARES EXPLAINED BY CLUSTERING )
WRITE(2,400) NNK,SSK
WRITE(4,737)NNK
737 FORMAT(5X,I4)
WRITE(4,739)(JCOUNT(I),JCOUNT(I+1),JCOUNT(I+2),I=1,NNK,3)
739 FORMAT(2X,3(2X,I4))
59 TSSK=TSSK+SSK
20 CONTINUE
WSSQ(KLUST)=TSSK
IF(NZ,NE,1)GOTO 61
WRITE(2,500)

```



```

00  FORMAT(1H0, 5X, 23H ANALYSIS BY VARIABLE  ,//, 5X, 8HVARIABLE, 5X,
120H GROUP MEANS                               //)
    WRITE(2,402)
61  SST = 0
    DO 70 I=NG,NV
    IF(LVAR(I) ,NE,1) GO TO 70
    RSS = 0
    DO80K=1,KLUST
    IF(NX(K),EQ,0) GO TO 80
    Z(K) = XM(I,K)/NX(K)
    RSS = RSS+Z(K)*Z(K)*NX(K)
80  CONTINUE
    SST =SST+RSS
    IF(NZ.NE,1)GOTO 70
    WRITE(2,600)  TITLE(I),(Z(K),K=1,KLUST),RSS
600  FORMAT(5X,A8,8(2X,E11.4))
70  CONTINUE
    K = K -1
    WRITE(2,700) K,SST
    K = K + 1
700  FORMAT(//,10X,12,2X,10HCLUSTERS /
1 ,48H TOTAL SUM OF SQUARES EXPLAINED BY CLUSTERING ,3H = ,E10.4)
    TSS=0.0
    DO 900 I=1,NV
    IF(LVAR(I),NE,1)GOTO 900
    TSS=TSS+XSTD(I)**2*NOBS
900  CONTINUE
    P1=TSSK*100.0/TSS
    P2=SST*100.0/TSS
    P3=P1+P2
    WRITE(2,901)TSSK,P1
901  FORMAT(///,30X,7HSUMMARY,//20X,15H SUM OF SQUARES ,5X,
110HPERCENTAGE,/,5X,15HWITHIN GROUPS,3X,E12.4,4X,E11.4)
    WRITE(2,902)SST,P2,TSS,P3
902  FORMAT(5X,14HBETWEEN GROUPS,2X,E12.4,4X,E11.4,/,5X,5HTOTAL,11X,
1E12.4,4X,E11.4)
    RETURN
    END

```

```
SUBROUTINE KLESS(KLUST,NOBS,NV,X,NG)
DIMENSION X(NOBS,NV)
COMMON /C/LVAR(40),TITLE(40)
COMMON /A/ XM(40,40),NX(40)
COMMON /G/NK(2500),WSSQ(40)
DELTA(AX,BX,NA,NB) = AX*AX/NA + BX*BX/NB - (AX+BX)*(AX+BX)/(NA+NB)
DMIN = 100000
DO 20 K=1,KLUST
DO 30 K2 = K,KLUST
IF(K,EQ,K2) GO TO 30
DE = 0,0
IF(NX(K),LT,1) GO TO 40
IF(NX(K2),LT,1) GO TO 40
DO 40 I=NG,NV
IF(LVAR(I),NE,1) GO TO 40
DE=DE+DELTA(XM(I,K),XM(I,K2),NX(K),NX(K2))
40 CONTINUE
IF(DE,GT,DMIN) GO TO 30
DMIN = DE
I1 = K
I2 = K2
30 CONTINUE
20 CONTINUE
DO 50 J=1,NOBS
IF(NK(J)-I2) 50,51,52
51 NK(J)= I1
GO TO 50
52 NK(J)= NK(J)-1
50 CONTINUE
IF(KLUST-1,EQ,0)RETURN
KL=KLUST-1
CALL XMSS(NOBS,NV,X,NG,KL)
RETURN
END
```



```

SUBROUTINE CLUST(KLUST,NOBS,NV,X,NDMAX,NG)
DIMENSION X(NOBS,NV)
COMMON /G/NK(2500),WSSQ(40)
COMMON /A/ XM(40,40),NX(40)
COMMON /C/LVAR(40),TITLE(40)
CUTOFF=0.001
ND = 0
DHIN= 100000
8 NC = 0
DO 70 J=1,NOBS
  DMIN = 100000
  DO 80 K=1,KLUST
    L = 1
    IF(NK(J),NE,K) GO TO 81
    L = -1
81  NXT = NX(K) + (L-1)/2
    DE=CUTOFF
    IF(NXT,LE,0) GO TO 90
    DO 90 I=NG,NV
      IF(LVAR(I),NE,1) GO TO 90
    XT = X(J,I)
    XMT = X(I,K) + XT*(L-1)/2
    DE=DE+XT*XT+XMT*XMT/NXT*(XMT+XT)*(XMT+XT)/(NXT+1)
90  CONTINUE
    IF(DE,GT,DMIN) GO TO 80
    KC = K
    DMIN = DE
80  CONTINUE
    IF(DHIN,LT,CUTOFF)GOTO 70
    IF(NK(J),EQ,KC)GO TO 70
    NC = NC + 1
    KD = NK(J)
    NK(J) = KC
    NX(KD) = NX(KD) - 1
    NX(KC) = NX(KC) + 1
    DO 100 I=NG,NV
      IF(LVAR(I),NE,1) GO TO 100
    XM(I,KD) = XM(I,KD) - X(J,I)
    XM(I,KC) = XM(I,KC) + X(J,I)
100 CONTINUE
70  CONTINUE
    IF(NC,EQ,0) RETURN
    ND = ND + 1
    WRITE(2,200)ND
200 FORMAT(10X,3HND=,I5)
    IF(ND,EQ,NDMAX) RETURN
    GO TO 8
END

```

```
SUBROUTINE ADATA(X,NV,NOBS)
INTEGER XDIAG
DIMENSION X(NOBS,NV)
COMMON /A/ XTX(1600),XDIAG(40) /B/ XMEAN(40),XSTD(40),NM(40)
COMMON /D/ N1, N2 /C/ LVAR(40), TITLE(40)
XDIAG(1) = 0
DO 20 I=2,NV
  XDIAG(I) = XDIAG(I-1) + NV - I + 1
20 CONTINUE
XTX(1)=0,0
CALL FMOVE(XTX(1),XTX(2),1599)
DO 30 KI=1,NOBS
DO 30 I=1,NV
  L= XDIAG(I)
DO 40 J=I,NV
  K= L+J
  XTX(K) = XTX(K) + X(KI,I) * X(KI,J)
40 CONTINUE
30 CONTINUE
DO 50 I=1,NV
  L= XDIAG(I)
  XMEAN(I) = XTX(I)/NOBS
  XSTD(I) = XTX(L+I)/NOBS = XMEAN(I)* XMEAN(I)
  XSTD(I) = SQRT (XSTD(I))
50 CONTINUE
N1 = -1
N2 = NOBS
RETURN
END
```



```

SUBROUTINE MOUT(NV,NOBS)
  COMMON/B/XMEAN(40),XSTD(40),NM(40) /C/LVAR(40),TITLE(40)
  WRITE(2,100) NOBS , NV
100  FORMAT (1H1 , 10X, 34H MEANS AND STANDARD DEVIATIONS OF ,14,16H 0
1BSERVATIONS ON , 14 , 11H VARIABLES      /// 23X, 30H MEAN
2  STANDARD          ,/,36X,9HDEVIATION  /)
  DO 10 I=1,NV
200  FORMAT(1H , 3X, I2, 3X, A8, 5X, E10.4, 4X, E10.4)
  WRITE(2,200) I, TITLE(I), XMEAN(I), XSTD(I)
10  CONTINUE
  RETURN
  END
```

```
SUBROUTINE CORR(X,NV,NOBS,IN)
INTEGER XDIAG
DIMENSION X(NOBS,NV)
COMMON/A/ XTX(1600),XDIAG(40) /B/XMEAN(40),XSTD(40),NM(40)
DO 60 I=2,NV
L=XDIAG(I)
DO 59 J=I,NV
K=L+J
XTX(K) = XTX(K)/NOBS
XTX(K) = XTX(K)-XMEAN(I)*XMEAN(J)
XTX(K) = XTX(K)/(XSTD(I)*XSTD(J))
59 CONTINUE
XMN = XMEAN(I)
XSD = XSTD(I)
IF(IN,EQ,1) GO TO 60
XMEAN(I) = 0,0
XSTD(I) = 1,0
DO 30 J=1,NOBS
X(J,I) = (X(J,I)-XMN)/XSD
30 CONTINUE
60 CONTINUE
RETURN
END
```



```
SUBROUTINE COMIN(NV,NOBS,COMMENT,FORM,N)
DIMENSION FORM(100),COMMENT(10)
COMMON /C/ LVAR(40), TITLE(40)
READ(N,200) NC
READ(N,300)(FORM(I),I=1,10)
WRITE(2,400)(FORM(I),I=1,10)
400 FORMAT(////10A8)
IF(NC.EQ.1) GO TO 10
DO 10 K=2,NC
READ(N,300) COMMENT
300 FORMAT(10A8)
WRITE(2,500) COMMENT
500 FORMAT( 10A8)
10 CONTINUE
CALL COPY(80,COMMENT(1),1,FORM(1),1)
READ(N,200) NV,NOBS
200 FORMAT(2I0)
WRITE(2,600) NOBS,NV
600 FORMAT( 20X, 14,17H OBSERVATIONS ON ,12,11H VARIABLES )
NV = NV * 1
CALL COPY8(TITLE(1),8HCUNSTANT )
READ(N,800) (TITLE(I),I=2,NV)
800 FORMAT(8( 1X,A8))
READ(N,200) NC
NC = 10*NC
READ(N,300)(FORM(I),I=1,NC)
RETURN
END
```

```
SUBROUTINE DATAFO(X,NOBS,NV,FORM,N)
DIMENSION X(NOBS,NV),FORM(100)
DO 10 J=1,NOBS
X(J,1)= 1.0
READ(H,FORM)(X(J,I),I=2,NV)
10 CONTINUE
RETURN
END
```



```
      SUBROUTINE RANK(X,NOBS,NX,NXRS)
      DIMENSION X(NOBS), NX(NOBS)
      DO 10 I=1,NOBS
10     NX(I) = I
      DO 30 I=1,NOBS
      DO 30 J = I,NOBS
      NA = NX(I)
      NB = NX(J)
      IF(X(I),GE,X(J)) GO TO 30
      NX(I) = NB
      NX(J) = NA
30     CONTINUE
      RETURN
      END
```

```
SUBROUTINE DOUT(X,NV,NOBS,IA,IB)
DIMENSION X(NOBS,NV)
COMMON /C/ LVAR(40), TITLE(40)
ID = IA + 1
IC = NV
IF(IB.EQ,2) GO TO 4
ID=1
IC = IA
4 CONTINUE
DO 10 K=ID,IC,6
IF(K.GT,IC) GO TO 10
NK = K + 5
IF(NK.LT,IC) GO TO 5
NK = IC
5 CONTINUE
WRITE(2,100) (TITLE(I),I=K,NK)
100 FORMAT(1H1,////,6H DATA ///, 11X,6(A8,8X))
300 FORMAT(//)
WRITE(2,300)
DO 20 J=1,NOBS
WRITE(2,200) J,(X(J,I),I=K,NK)
200 FORMAT(4X,13,5X,6(E13.6,3X))
20 CONTINUE
10 CONTINUE
RETURN
END
```



```
SUBROUTINE COUT(NV,ND,NY,NZ)
INTEGER XDIAG
COMMON /C/ LVAR(40),TITLE(40)
COMMON /A/ XTX(1600),XDIAG(40)
COMMON /E/ XA,XTEMP(40)
NA = NY
NB = NZ
GO TO (1,2,3,4),ND
1 IA=2
  IB=2
  GO TO 10
2 IA=2
  IB = NB
  IB = IB+1
  NB = NV
  GO TO 10
3 IB=2
  IA = NA
  IA = IA +1
  NA = NV
  GO TO 10
4 IA = NA
  IA = IA +1
  IB = NB
  IB = IB+1
  NA = NV
  NB = NV
10 WRITE(2,100)(I,I=IB,NB)
100 FORMAT(1H1,9X,20(I2,3X))
DO 20 J=IA,NA
  K = XDIAG(J)
  SQ= XTX(K+J)
DO 30 I=IB,NB
  SR = XTX(I+XDIAG(I))
  IF(J,LT,I) GO TO 25
  XTEMP(I) = XTX( J+ XDIAG(I))
GO TO 29
25 CONTINUE
  XTEMP(I) = XTX(I+K)
29 XTEMP(I) = XTEMP(I)/SQRT(SQ+SR)
30 CONTINUE
  WRITE(2,200) J,(XTEMP(I),I=IB,NB)
200 FORMAT(5X,I2,3X,20(1X,F4.2))
20 CONTINUE
RETURN
END
```

```
SUBROUTINE BEALE(NOBS,NV,N1)
COMMON/G/NX(2500),WSSQ(40)
DIMENSION RVAR(40)
DO 1 J=1,N1
1 RVAR(J)=WSSQ(J)
DO 2 I=1,N1
L1=2
IF(I,EQ,1)L1=0
IF(I,EQ,2)L1=1
CALL BEALETEST(I,NOBS,NV,RVAR,L1)
2 CONTINUE
RETURN
END
```



```

SUBROUTINE BEALETEST(I,NOBS,NV,RVAR,L1)
DIMENSION RVAR(40)
IF(L1.EQ.0)RETURN
ANOBS=FLOAT(NOBS)
ANV=FLOAT(NV)
NTEST=0
DO 10 J=1,I-1
F=(RVAR(I-J)-RVAR(I))/RVAR(I)
A=(ANOBS-I+J)/(ANOBS-I)
AI=FLOAT(I)
B=(AI/(AI-J))**(2.0/ANV)
F=F/(A*B-1.0)
DF1=NV*J
DF2=NV*(NOBS-I)
IF (F,GE,0)GOTO 909
PF=0.0
GOTO 900
909 PF=PRBF(DF1,DF2,F)
900 IF (L1,GT,1)GOTO 203
WRITE(2,100)
100 FORMAT(///,10X,11HBEALES TEST,///,5X,25HHYPOTHESES: K2 CLUSTERS ,
11X,27HNO BETTER THAN K1 CLUSTERS )
WRITE(2,201)
201 FORMAT(5X,2HK2,3X,2HK1,4X,1HF,5X,16HPROBABILITY OF F ,
112H RVAR(K2) ,10H RVAR(K1) )
203 IJ=I-J
WRITE(2,202)I,IJ,F,PF,RVAR(I),RVAR(I-J)
202 FORMAT(5X,I2,3X,I2,3X,F5.2,7X,F6.4,8X,F7.1,4X,F7.1)
NTEST=NTEST+1
IF(NTEST,GT,6)RETURN
10 CONTINUE
RETURN
END
FUNCTION PRBF(DA,DB,FR)
PRBF=1.0
IF(DA*DB*FR,EQ,0.0)RETURN
IF(FR,LT,1.0)GO TO 5
A=DA
B=DB
F=FR
GO TO 10
5 A=DB
B=DA
F=1.0/FR
10 AA=2.0/(9.0*A)
BB=2.0/(9.0*B)
Z=ABS(((1.0-BB)*F**0.333333-1.0+AA)/SQRT(BB*F
1**0.666667+AA))
IF(B,LT,4.0)Z=Z*(1.0+0.08*Z**4/B**3)
PRBF=0.5/(1.0+Z*(0.196854+Z*(0.115194+Z*
1(0.000344+Z*0.019527))))**4
IF(FR,LT,1.0)PRBF=1.0-PRBF
RETURN
END
FINISH

```

```

PROGRAM(CLASS)
OUTPUT 6=CP0
OUTPUT 4=LP0
OUTPUT 7=LP1
INPUT 1=CR0
INPUT 2=CR1
INPUT 8=CR2
USE 9=MT1/UNFORMATTED(SCRATCH1)
USE 5=MT0/UNFORMATTED(SCRATCH2)
USE 3=MT2/UNFORMATTED(SCRATCH3)
COMPRESS INTEGER AND LOGICAL
TRACE 1
END
MASTER CLASS
DIMENSION Z(300),NO(30),SUMZ(30,60),SUMZ2(30,60),ZMIN(30,60)
DIMENSION ZMAX(30,60),TSUMZ(60),TSUMZ2(60),TZMIN(60),TZMAX(60)
DIMENSION SMEAN(30,60),SMIN(30,60),SMAX(30,60)
DIMENSION LABEL(30),LABELA(440),NLAN(30,6),NTLAND(6)
DIMENSION W(2200,11)
REAL LABEL,LABELA
COMMON LABEL,LABELA
READ(2,59)(LABEL(I),I=1,10)
READ(2,59)(LABELA(I),I=1,53)
59  FORMAT(10A8)
READ(2,119) NOBS,NV,NCLASS,NCV,NSTEP,NSAM,NEXTRA
119  FORMAT(7I0)
DO 333 K1=1,NSTEP
N2=NCLASS-K1+1
DO 334 IN=1,N2
READ(8,1001) K2
K21=K2/3
AK21=FLOAT(K2)/3.0
IF(FLOAT(K21)-AK21.LT.0.0)K21=K21+1
DO 335 L=1,K21
READ(8,1002) I1,I2,I3
1001  FORMAT(I0)
1002  FORMAT(3I0)
W(I1,K1)=IN+(NSAM-1)*20
IF(I2.EQ.0)GOTO 335
W(I2,K1)=IN+(NSAM-1)*20
IF(I3.EQ.0)GOTO 335
W(I3,K1)=IN+(NSAM-1)*20
335  CONTINUE
334  CONTINUE
333  CONTINUE
DO 2 I=1,NOBS
READ(1,200) (Z(J),J=1,NV)
200  FORMAT(7X,5F0.0/4(7X,7F0.0/),7X,8F0.0/2(7X,6F0.0/),
17X,2F0.0)
IB=9
IF(I.GT.800)IB=5
IF(I.GT.1600)IB=3
WRITE(IB)(Z(J),J=1,NV)
WRITE(6,1003)I,(Z(J),J=1,5)
1003  FORMAT(2X,1HA,14,8(1X,F8.2))

```



```

WRITE(6,1003)I,(Z(J),J=6,12)
WRITE(6,1003)I,(Z(J),J=13,19)
WRITE(6,1003)I,(Z(J),J=20,26)
WRITE(6,1003)I,(Z(J),J=27,33)
WRITE(6,1003)I,(Z(J),J=34,41)
WRITE(6,1003)I,(Z(J),J=42,47)
WRITE(6,1003)I,(Z(J),J=48,53)
WRITE(6,1003)I,(Z(J),J=54,55)
1004 FORMAT(2X,1HA,I4,11(1X,F4.1))
IF(NEXTRA.EQ.0)GOTO 342
DO 517 K7=1,NEXTRA
READ(1,204)(Z(J1),J1=Nv+1,Nv+11)
204 FORMAT(7X,11(1X,F4.1))
WRITE(IB)(Z(J1),J1=Nv+1,Nv+11)
WRITE(6,1004)I,(Z(J1),J1=Nv+1,Nv+11)
517 CONTINUE
342 DO 337 K1=1,NSTEP
337 Z(Nv+K1)=W(I,K1)
WRITE(IB)(Z(J1),J1=Nv+1,Nv+NSTEP)
WRITE(6,1004)I,(Z(J1),J1=Nv+1,Nv+NSTEP)
2 CONTINUE
ENDFILE 9
REWIND 9
ENDFILE 5
REWIND 5
ENDFILE 3
REWIND 3
DO 17 K1=1,NSTEP
N2=NCLASS-K1+1
DO 1 J=1,Nv-2
TsumZ(J)=0
TsumZ2(J)=0
TZMIN(J)=100000
TZMAX(J)=-100000
DO 1 K=1,N2
NO(K)=0
DO 14 L=1,6
14 NLAND(K,L)=0
SUMZ(K,J)=0
SUMZ2(K,J)=0
ZHIN(K,J)=100000
ZMAX(K,J)=-100000
1 CONTINUE
DO 13 L=1,6
13 NTLAND(L)=0
DO 12 I=1,NOBS
IB=9
IF(I.GT.800)IB=5
IF(I.GT.1600)IB=3
READ(IB)(Z(J),J=1,Nv)
DO 79 K11=1,NEXTRA+1
NX1=K11*11-10
NX2=K11*11
79 READ(IB)(Z(J),J=Nv+NX1,Nv+NX2)
K=Z(Nv+(NEXTRA*NSTEP)+K1)-20*(NSAM-1)
NO(K)=NO(K)+1

```

```

L=Z(54)
NTLAND(L)=NTLAND(L)+1
NLAND(K,L)=NLAND(K,L)+1
DO 3 J=1,NV-2
SUMZ(K,J)=SUMZ(K,J)+Z(J)
SUMZ2(K,J)=SUMZ2(K,J)+Z(J)**2
IF(Z(J).GE.ZMIN(K,J))GOTO 7
ZMIN(K,J)=Z(J)
7 IF(Z(J).LE.ZMAX(K,J))GO TO 6
ZMAX(K,J)=Z(J)
6 TSUMZ(J)=TSUMZ(J)+Z(J)
TSUMZ2(J)=TSUMZ2(J)+Z(J)**2
IF(Z(J).GE.TZMIN(J)) GOTO 9
TZMIN(J)=Z(J)
9 IF(Z(J).LE.TZMAX(J)) GOTO 8
TZMAX(J)=Z(J)
8 CONTINUE
3 CONTINUE
12 CONTINUE
DO 4 J=1,NV-2
IF(TSUMZ2(J).EQ.0)GOTO 4
TSUMZ(J)=TSUMZ(J)/NOBS
TSUMZ2(J)=SQRT(TSUMZ2(J)/NOBS-TSUMZ(J)**2)
DO 4 K=1,N2
IF(NO(K).EQ.0)GOTO 4
SUMZ(K,J)=SUMZ(K,J)/NO(K)
SUMZ2(K,J)=SQRT(SUMZ2(K,J)/NO(K)-SUMZ(K,J)**2)
SMEAN(K,J)=(SUMZ(K,J)-TSUMZ(J))/TSUMZ2(J)
SMIN(K,J)=(ZMIN(K,J)-TSUMZ(J))/TSUMZ2(J)
SMAX(K,J)=(ZMAX(K,J)-TSUMZ(J))/TSUMZ2(J)
4 CONTINUE
WRITE(4,309)(LABEL(H),M=1,10)
309 FORMAT(///10A8/)
WRITE(4,300)NOBS
300 FORMAT(1X/' TOTAL SAMPLE'/' NO. OF OBSERVATIONS =' ,I5//
1' VARIABLE MEAN STAN.DEV. MINIMUM MAXIMUM'//)
DO 10 J=1,NV-2
WRITE(4,400)LABELA(J),TSUMZ(J),TSUMZ2(J),TZMIN(J),TZMAX(J)
400 FORMAT(1X,A8,4(1X,E10.4))
10 CONTINUE
WRITE(4,700)
700 FORMAT(//' FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG'//)
WRITE(4,800)(NTLAND(L),L=1,6)
800 FORMAT(2X,I4,4X,I4,3X,I4,4X,I4,4X,I4,4X,I4)
DO 11 K=1,N2
WRITE(4,309)(LABEL(H),M=1,10)
WRITE(4,500)K,NO(K)
500 FORMAT(1X/' CLASS ' ,I3,/' NO. OF OBSERVATIONS =' ,I5//
1' VARIABLE MEAN STAN.DEV. MINIMUM MAXIMUM SMEAN
2 SMINIMUM SMAXIMUM '//)
DO 15 J=1,NV-2
WRITE(4,600)LABELA(J),SUMZ(K,J),SUMZ2(K,J),ZMIN(K,J),ZMAX(K,J),
1SMEAN(K,J),SMIN(K,J),SMAX(K,J)
600 FORMAT(1X,A8,4(1X,E10.4),3(1X,F10.2))
15 CONTINUE
WRITE(4,700)

```



```
WRITE(4,800)(NLAND(K,L),L=1,6)
11 CONTINUE
CALL ANOVA(SUMZ,TSUMZ2,TSUMZ,NO,NOBS,N2,NV=2)
REWIND 9
REWIND 5
REWIND 3
17 CONTINUE
STOP
END
```

```

PROGRAM(BART)
COMPRESS INTEGER AND LOGICAL
INPUT 1=CR0
OUTPUT 2=LPO
INPUT 4=CR1
TRACE 2
END
MASTER BART
REAL LABEL
DIMENSION LABEL(80)
DIMENSION XLAMDA(100)
READ(1,50)(LABEL(I),I=1,10)
50 FORMAT(10A8)
WRITE(2,70)(LABEL(I),I=1,10)
70 FORMAT(1H1,10A8)
WRITE(2,400)
400 FORMAT(1X,/, ' K          L          R          DF          PROB')
READ(1,100)NP,NOBS
100 FORMAT(2I0)
READ(1,200)(XLAMDA(I),I=1,NP)
200 FORMAT(F0,0)
K=-1
DO 1 I=1,NP
SIGL=0.0
PRDL=1.0
K=K+1
DO 2 J=K+1,NP
SIGL=SIGL+XLAMDA(J)
PRDL=PRDL*XLAMDA(J)
2 CONTINUE
SIGL=(SIGL/(NP-K))**(NP-K)
XL=SIGL/PRDL
STAT=((NOBS-K-0.5)*(ALOG(XL)))
DF=((NP-K-1)*(NP-K+2))*0.5
P=PRBF(DF,1000.0,STAT/DF)
WRITE(2,500)K,XL,STAT,DF,P
500 FORMAT(1X,I2,2X,F10.1,2X,F10.1,2X,F10.1,2X,F5.4)
1 CONTINUE
STOP
END
FUNCTION PRBF(DA,DB,FR)
PRBF=1.0
IF(DA*DB*FR.EQ.0.0)RETURN
IF(FR.LT.1.0)GO TO 5
A=DA
B=DB
F=FR
GO TO 10
5 A=DB
B=DA
F=1.0/FR
10 AA=2.0/(9.0*A)
BB=2.0/(9.0*B)
Z=ABS(((1.0-BB)*F**0.333333+1.0+AA)/SQRT(BB*F
1**0.666667+AA))

```



```
IF(B.LT,4.0)Z=Z*(1.0+0.08*Z**4/B**3)
PRBF=0.5/(1.0+Z*(0.196854+Z*(0.115194+Z*
1(0.000344+Z*0.019527))))**4
IF(FR.LT,1.0)PRBF=1.0-PRBF
RETURN
END
FINISH
```

```

PROGRAM(POPU)
INPUT 1=CR1
OUTPUT 2=CP1
OUTPUT 7=LP2
INPUT 8=CRO
COMPRESS INTEGER AND LOGICAL
TRACE 1
END
MASTER POPU
DIMENSION Z(60),NO(30),SUMZ(30,60),SUMZ2(30,60),ZMIN(30,60)
DIMENSION ZMAX(30,60),TSUMZ(60),TSUMZ2(60),TZMIN(60),TZMAX(60)
DIMENSION SMEAN(30,60),SMIN(30,60),SMAX(30,60)
DIMENSION LABEL(10),LABELA(60),NLAND(30,6),NTLAND(6)
DIMENSION X(200),W(5),N7(30)
DIMENSION SC(30),COEF(30,60),CONST1(30),CONST2(30),N(60)
REAL LABEL,LABELA
COMMON LABEL,LABELA
READ(8,59)(LABEL(I),I=1,10)
READ(8,59)(LABELA(I),I=1,53)
59  FORMAT(10A8)
READ(8,119) NV,NCLASS,NCV,NDISVR
119  FORMAT(4I0)
DO 118 K=1,NCLASS
CONST1(K)=0.0
CONST2(K)=0.0
DO 118 J=1,NV-2
118  COEF(K,J)=0.0
READ(8,120)(N(I),I=1,NDISVR)
120  FORMAT(20I0)
KL=1
KU=6
TEST=FLOAT(NCLASS)/6.0
ITEST=NCLASS/6
IF(TEST.GT.FLOAT(ITEST)) GOTO 124
K3=ITEST
GOTO 126
124  K3=ITEST+1
126  DO 137 K=1,NCLASS
137  N7(K)=K
WRITE(7,399)(LABEL(M),M=1,10)
399  FORMAT(1X,///,10A8,/)
DO 123 J=1,K3
WRITE(7,132)(N7(K),K=KL,KU)
132  FORMAT(25X,'CLASSIFICATION FUNCTION NUMBER'/
11X,'VARIABLE',6X,5(I2,12X),I2)
DO 122 I=1,NDISVR
READ(8,121)(COEF(K,N(I)),K=KL,KU)
122  WRITE(7,129)LABELA(N(I)),(COEF(K,N(I)),K=KL,KU)
129  FORMAT(1X,A8,6F14.8)
READ(8,121)(CONST1(K),K=KL,KU)
WRITE(7,130)(CONST1(K),K=KL,KU)
130  FORMAT(1X,'CONSTANT',6F14.8)
READ(8,121)(CONST2(K),K=KL,KU)
WRITE(7,131)(CONST2(K),K=KL,KU)
131  FORMAT(9X,6F14.8)

```



```

KL=KL+6
IF((KU+6).GE.NCLASS) GOTO 125
KU=KU+6
GOTO 123
25 KU=NCLASS
23 CONTINUE
21 FORMAT(8F0.0)
NOUT=0
DO 1 J=1,NV=2
TSUMZ(J)=0
TSUMZ2(J)=0
TZMIN(J)=100000
TZMAX(J)=-100000
DO 1 K=1,NCLASS
NO(K)=0
DO 14 L=1,6
14 NLAND(K,L)=0
SUMZ(K,J)=0
SUMZ2(K,J)=0
ZMIN(K,J)=100000
ZMAX(K,J)=-100000
1 CONTINUE
DO 13 L=1,6
13 NTLAND(L)=0
DO 17 I=1,22026
DO 18 K2=1,60
18 Z(K2)=0.0
READ(1,200) (W(K),K=1,5), (X(J),J=1,127)
200 FORMAT(F1.0,F3.0,F2.0,2F10.0,2F1.0,3F10.0,F1.0,2X,12F1.0/
18F10.0/8F10.0/8F10.0/
210X,7F10.0/3F10.0,F1.0,9X,F1.0,9X,2F10.0,10X/10X,7F10.0/5F10.0,F1.
30,4F4.0,2F1.0,F4.0,2F1.0/4(F4.0,2F1.0),F4.0,5X,2F10.0,10X,F1.0,F4.
40,F1.0,5X/19F4.0/5F4.0,2F10.0,4F4.0,F1.0)
X(34)=X(34)/100
X(36)=X(36)/100
X(41)=X(41)/100
X(49)=X(49)/100
TOT=0.0
DO 30 K=19,49
30 TOT=TOT+X(K)
Z(2)=X(3)+X(4)+X(5)
Z(1)=Z(2)+X(50)+X(51)+X(52)
IF(TOT.NE.Z(2))GOTO 40
IF(Z(2).EQ.0.0)GOTO 40
IF(X(96).EQ.9.0)X(96)=0.5
IF(X(96).EQ.5.0)X(96)=4.5
Z(4)=((X(96)-1)*0.25+0.125+0.125*(X(104)+X(116)))+0.375*(X(105)+X(
1117))+0.625*(X(106)+X(118))+0.875*(X(107)+X(119))+X(108)*X(120)+(8
2*(X(121)+X(122))/2200))
IF(Z(4).EQ.0)GOTO 40
IF(Z(1).NE.0.0)GOTO 501
40 CONTINUE
NOUT=NOUT+1
GOTO 117
501 IF(X(2).EQ.9.0)X(2)=0
Z(42)=X(2)*X(1)

```



```

Z(48)=X(3)/(Z(2)*0.01)
Z(49)=X(4)/(Z(2)*0.01)
Z(50)=X(5)/(Z(2)*0.01)
Z(51)=X(6)
Z(52)=X(7)+X(8)+X(9)+X(10)
Z(53)=X(11)/7+X(12)/7+X(13)/7+X(14)/7+X(15)/7+X(16)/7+X(17)/7
Z(43)=X(18)
Z(6)=(X(19)+X(20)+X(21)+X(22)+X(23)+X(24)+X(25)+X(26)
1+X(27))/(Z(2)*0.01)
Z(7)=(X(28)+X(29)+X(30))/(Z(2)*0.01)
Z(8)=X(31)/(Z(2)*0.01)
Z(9)=(X(33)+X(34)+X(35)+X(36))/(Z(2)*0.01)
Z(10)=(X(37)+X(38)+X(32)+X(39))/(Z(2)*0.01)
Z(11)=X(40)/(Z(2)*0.01)
Z(12)=(X(41))/(Z(2)*0.01)
Z(13)=X(42)/(Z(2)*0.01)
Z(15)=(X(43)+X(44)+X(45)+X(47)+X(48)+X(49))/(Z(2)*0.01)
Z(14)=X(46)/(Z(2)*0.01)
Z(16)=X(50)/((Z(2)+X(50))*0.01)
Z(17)=(X(51)+X(52))/(Z(1)*0.01)
IF(X(53).EQ.7.0)X(55)=1.0
IF(X(54).EQ.7.0)X(54)=1.0
Z(18)=X(53)
Z(19)=X(54)
Z(20)=0.6*X(55)
Z(21)=X(59)
Z(22)=0.4*X(56)+X(57)+0.5*X(58)+0.8*X(60)
Z(23)=0.1*(X(61)+X(62))
Z(24)=0.027*X(63)+0.5*X(64)+0.3*X(65)
Z(25)=X(66)*0.007+X(67)*0.014+X(68)*0.03
Z(3)=Z(20)+Z(22)+Z(23)+Z(24)+Z(25)+Z(21)
IF(Z(3).EQ.0.0)GOTO 50
Z(20)=Z(20)*100/Z(3)
Z(22)=Z(22)*100/Z(3)
Z(23)=Z(23)*100/Z(3)
Z(24)=Z(24)*100/Z(3)
Z(25)=Z(25)*100/Z(3)
Z(21)=Z(21)*100/Z(3)
50 Z(26)=Z(3)*100/Z(1)
Z(40)=X(69)
IF((X(70)+X(71)+X(72)+X(73)).GT.0)Z(34)=1
IF(X(76).GT.0)Z(35)=1
IF((X(79)+X(82)+X(85)+X(88)).GT.0)Z(36)=1
IF((X(74)+X(75)+X(77)+X(78)+X(80)+X(81)+X(83)+X(84)+
1 X(86)+X(87)+X(89)+X(90)).GT.0)Z(37)=1
DO 51 K=70,91
51 Z(5)=Z(5)+X(K)
Z(41)=Z(5)/(Z(1)*0.001)
IF(X(91).GT.0.0)Z(38)=1
Z(39)=(X(36)+X(34)+X(49))/(Z(2)*0.01)
IF(X(94).EQ.1)Z(44)=1
IF(X(94).EQ.2)Z(45)=1
IF(X(95).EQ.0.0)X(95)=52.0
Z(46)=X(95)
Z(28)=((X(96)-1)*0.25+0.125+0.125*X(104)+0.375*X(105)+0.625*X(106)
1+0.875*X(107)+X(108))

```



```

Z(27)=Z(4)/(Z(1)*0.001)
Z(28)=Z(28)*100/Z(4)
IF(X(96).EQ.0.5)P=0.0
IF(X(96).NE.0.5)P=1.0
T=P+X(97)+X(98)+X(109)+X(110)
IF(T.NE.0.0)GO TO 502
T = 0.00001
02 IF(X(95).LT.25.0.AND.P.EQ.1.0)Z(29)=1.0
Z(29)=(Z(29)+X(99)+X(111))/(T*0.01)
IF((X(95).GE.25.0.AND.X(95).LT.35.0).AND.P.EQ.1.0)Z(30)=1.0
Z(30)=(Z(30)+X(100)+X(112))/(T*0.01)
IF((X(95).GE.35.0.AND.X(95).LT.45.0).AND.P.EQ.1.0)Z(31)=1.0
Z(31)=(Z(31)+X(101)+X(113))/(T*0.01)
IF((X(95).GE.45.0.AND.X(95).LT.65.0).AND.P.EQ.1.0)Z(32)=1.0
Z(32)=(Z(32)+X(102)+X(114))/(T*0.01)
IF((X(95).GE.65.0).AND.P.EQ.1)Z(33)=1
Z(33)=(Z(33)+X(103)+X(115))/(T*0.01)
IF(X(127).EQ.8.0)X(127)=0
Z(47)=X(127)
Z(54)=W(1)
DO 177 K=1,NCLASS
SC(K)=0.0
DO 178 J=1,NV-2
78 SC(K)=SC(K)+COEF(K,J)*Z(J)
SC(K)=SC(K)+CONST1(K)+CONST2(K)
IF(K.EQ.1)GOTO 179
IF(SC(K).LT.SCMAX)GOTO 177
KMAX=K
SCMAX=SC(K)
GOTO 177
79 KMAX=1
SCMAX=SC(1)
77 CONTINUE
Z(55)=KMAX
K=Z(NCV)
NO(K)=NO(K)+1
L=Z(54)
NTLAND(L)=NTLAND(L)+1
NLAND(K,L)=NLAND(K,L)+1
DO 3 J=1,NV-2
SUMZ(K,J)=SUMZ(K,J)+Z(J)
SUMZ2(K,J)=SUMZ2(K,J)+Z(J)**2
IF(Z(J).GE.ZMIN(K,J))GOTO 7
ZMIH(K,J)=Z(J)
7 IF(Z(J).LE.ZMAX(K,J))GO TO 6
ZMAX(K,J)=Z(J)
6 TSUMZ(J)=TSUMZ(J)+Z(J)
TSUMZ2(J)=TSUMZ2(J)+Z(J)**2
IF(Z(J).GE.TZMIN(J))GOTO 9
TZMIN(J)=Z(J)
9 IF(Z(J).LE.TZMAX(J))GOTO 8
TZMAX(J)=Z(J)
8 CONTINUE
3 CONTINUE
17 IF(I.NE.20000)GOTO 17
WRITE(2,340)NOUT

```



```

340 FORMAT(I6)
WRITE(2,349)(NTLAND(L),L=1,6)
DO 347 J=1,NV=2
347 WRITE(2,345)TSUMZ(J),TSUMZ2(J),TZMIN(J),TZMAX(J)
345 FORMAT(4(E20.11))
DO 348 K=1,NCLASS
WRITE(2,340)NO(K)
WRITE(2,349)(NLAND(K,L),L=1,6)
DO 348 J=1,NV=2
348 WRITE(2,345)SUMZ(K,J),SUMZ2(K,J),ZMIN(K,J),ZMAX(K,J)
349 FORMAT(6I5)
17 CONTINUE
NOBS=22026-NOUT
DO 4 J=1,NV=2
IF(TSUMZ2(J).EQ.0)GOTO 4
TSUMZ(J)=TSUMZ(J)/NOBS
TSUMZ2(J)=SQRT(TSUMZ2(J)/NOBS-TSUMZ(J)**2)
DO 4 K=1,NCLASS
IF(NO(K).EQ.0)GOTO 4
SUMZ(K,J)=SUMZ(K,J)/NO(K)
SUMZ2(K,J)=SQRT(SUMZ2(K,J)/NO(K)-SUMZ(K,J)**2)
SMEAN(K,J)=(SUMZ(K,J)-TSUMZ(J))/TSUMZ2(J)
SMIN(K,J)=(ZMIN(K,J)-TSUMZ(J))/TSUMZ2(J)
SMAX(K,J)=(ZMAX(K,J)-TSUMZ(J))/TSUMZ2(J)
4 CONTINUE
WRITE(5,309)(LABEL(M),M=1,10)
309 FORMAT(1X///10A8/)
WRITE(5,300)NOBS
300 FORMAT(1X/' TOTAL SAMPLE'/' NO. OF OBSERVATIONS =' ,I5//
1' VARIABLE MEAN STAN.DEV. MINIMUM MAXIMUM'//)
DO 10 J=1,NV=2
WRITE(5,400)LABELA(J),TSUMZ(J),TSUMZ2(J),TZMIN(J),TZMAX(J)
400 FORMAT(1X,A8,4(1X,E10.4))
10 CONTINUE
WRITE(5,700)
700 FORMAT(//' FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG'//)
WRITE(5,800)(NTLAND(L),L=1,6)
800 FORMAT(2X,I4,4X,I4,3X,I4,4X,I4,4X,I4,4X,I4)
DO 11 K=1,NCLASS
WRITE(5,309)(LABEL(M),M=1,10)
WRITE(5,500)K,NO(K)
500 FORMAT(1X/' CLASS ' ,I3,/' NO. OF OBSERVATIONS =' ,I5//
1' VARIABLE MEAN STAN.DEV. MINIMUM MAXIMUM SMEAN
2 SMINIMUM SMAXIMUM '//)
DO 12 J=1,NV=2
WRITE(5,600)LABELA(J),SUMZ(K,J),SUMZ2(K,J),ZMIN(K,J),ZMAX(K,J),
1SMEAN(K,J),SMIN(K,J),SMAX(K,J)
600 FORMAT(1X,A8,4(1X,E10.4),3(1X,F10.2))
12 CONTINUE
WRITE(5,700)
WRITE(5,800)(NLAND(K,L),L=1,6)
11 CONTINUE
CALL ANOVA(SUMZ,TSUMZ2,TSUMZ,NO,NOBS,NCLASS,NV=2)
STOP
END

```



APPENDIX D

Output from CLUSTPROG

SAMPLE A - 15 Groups  
10 Component Variables

GROUP 1	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
	7	0.1491E 02	9	0.8049E 01	26	0.1462E 02
	49	0.6425E 01	58	0.7446E 01	157	0.9840E 01
	161	0.5493E 01	177	0.1234E 02	217	0.9980E 01
	229	0.7686E 01	242	0.7240E 01	275	0.4615E 01
	281	0.7059E 01	283	0.8986E 01	292	0.1045E 02
	302	0.5988E 01	308	0.7383E 01	311	0.3250E 01
	313	0.3025E 01	321	0.3169E 01	329	0.2501E 01
	345	0.1032E 02	445	0.5667E 01	446	0.8066E 01
	447	0.2570E 01	448	0.2884E 01	449	0.1695E 02
	450	0.5230E 01	451	0.5209E 01	453	0.5503E 01
	454	0.1267E 02	456	0.5207E 01	459	0.4268E 01
	460	0.4857E 01	463	0.7066E 01	464	0.1529E 02
	465	0.1191E 02	466	0.992E 01	469	0.6244E 01
	470	0.3920E 01	473	0.4623E 01	474	0.7800E 01
	475	0.7402E 01	476	0.1816E 02	477	0.1442E 01
	478	0.5289E 01	479	0.1308E 02	484	0.6091E 01
	48	0.5638E 03				

OBSERVATIONS IN GROUP 1 WITHIN GROUP S.S.

GROUP 2	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
	10	0.4676E 01	16	0.7741E 01	18	0.5326E 01
	27	0.5853E 01	36	0.4272E 01	37	0.2770E 02
	76	0.5291E 01	78	0.1191E 02	81	0.3862E 01
	82	0.5544E 01	85	0.5564E 01	87	0.9820E 01
	89	0.4022E 01	91	0.4145E 01	93	0.6427E 01
	95	0.1093E 01	96	0.1153E 02	106	0.8356E 01
	107	0.4776E 01	108	0.5032E 01	115	0.3870E 01
	123	0.4976E 01	148	0.5325E 01	150	0.3708E 02
	166	0.5760E 01	169	0.4283E 01	179	0.9453E 01
	180	0.1188E 02	216	0.6380E 01	219	0.9588E 01
	220	0.9566E 01	221	0.1497E 02	225	0.2333E 02
	226	0.1727E 02	232	0.7961E 01	237	0.4921E 01
	245	0.1413E 02	250	0.4945E 01	253	0.4832E 01
	254	0.6188E 01	258	0.4554E 01	260	0.4798E 01
	262	0.4045E 01	268	0.4690E 02	263	0.1790E 01
	280	0.1279E 02	285	0.2971E 01	289	0.2274E 01
	310	0.1032E 02	312	0.1876E 02	322	0.2514E 01
	323	0.2669E 01	371	0.7251E 01	379	0.1778E 02
	392	0.1542E 02	397	0.4234E 01	402	0.6037E 01
	443	0.7817E 01	458	0.7095E 01	467	0.7058E 01
	482	0.5676E 01	0	0.0000E 00	0	0.0000E 00
	61	0.5419E 03				

OBSERVATIONS IN GROUP 2 WITHIN GROUP S.S.



GROUP 3			
OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
12	0.8294E 01	34	0.1341E 02
172	0.1464E 02	218	0.2244E 02
246	0.1771E 02	293	0.8796E 01
303	0.1606E 02	309	0.2042E 02
335	0.2098E 02	341	0.1929E 02
363	0.1530E 02	366	0.8738E 01
414	0.5063E 02	415	0.2425E 02
435	0.1652E 02	439	0.1385E 02
OBSERVATIONS IN GROUP WITHIN GROUP S.S.			
24	0.4364E 03		

GROUP 4			
OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
331	0.4583E 01	338	0.6816E 01
350	0.7650E 01	354	0.5193E 01
360	0.1622E 02	362	0.4673E 01
365	0.9677E 01	367	0.1417E 01
369	0.1189E 02	370	0.6578E 01
375	0.7924E 01	377	0.4653E 01
381	0.6706E 01	382	0.2180E 02
386	0.9504E 01	389	0.1297E 02
398	0.2971E 01	399	0.5583E 01
427	0.4369E 02	0	0.0000E 00
OBSERVATIONS IN GROUP WITHIN GROUP S.S.			
28	0.2848E 03		

GROUP 5			
OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
8	0.4554E 01	75	0.1728E 02
240	0.1642E 02	241	0.8093E 01
272	0.1659E 02	286	0.9592E 01
485	0.4448E 02	0	0.0000E 00
OBSERVATIONS IN GROUP WITHIN GROUP S.S.			
10	0.2553E 03		



6	0.5517E 01	31	0.9417E 01	41	0.2466E 01
47	0.7456E 01	50	0.1174E 02	68	0.1834E 02
70	0.1402E 02	92	0.1486E 02	104	0.7328E 01
141	0.8195E 01	186	0.8437E 01	196	0.4356E 01
198	0.6935E 01	210	0.7475E 01	212	0.5960E 01
238	0.9765E 01	248	0.2399E 01	261	0.2291E 02
267	0.1016E 02	269	0.1041E 02	294	0.5854E 01
501	0.2492E 02	305	0.1253E 02	307	0.7562E 01
552	0.1606E 02	394	0.1254E 02	410	0.1083E 02
433	0.9263E 01	434	0.7328E 01	460	0.5572E 01
483	0.2115E 02	486	0.5832E 01	487	0.3140E 02
53	0.5567E 03				
OBSERVATIONS IN GROUP WITHIN GROUP S.S.					

GROUP 7	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
97	0.2520E 02	114	0.2237E 02	332	0.1007E 02
337	0.1705E 02	349	0.1612E 02	409	0.7537E 01
417	0.2533E 02	422	0.1653E 02	425	0.5891E 01
450	0.2541E 02	0	0.0000E 00	0	0.0000E 00
OBSERVATIONS IN GROUP WITHIN GROUP S.S.					
10	0.1680E 03				

GROUP 8	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
19	0.7739E 01	20	0.5256E 01	22	0.1697E 01
23	0.7123E 01	25	0.4984E 01	30	0.3615E 01
43	0.1260E 01	44	0.3040E 01	51	0.3547E 00
56	0.3246E 01	59	0.3687E 01	60	0.4071E 01
77	0.5266E 01	80	0.5445E 01	86	0.4241E 01
88	0.5243E 01	90	0.6151E 01	110	0.5078E 01
121	0.4949E 01	127	0.2380E 01	129	0.1871E 01
130	0.1138E 02	132	0.4249E 01	134	0.2728E 01
135	0.2164E 01	138	0.3569E 01	160	0.1872E 01
162	0.3443E 01	163	0.3724E 01	164	0.2602E 01
167	0.3751E 01	171	0.1997E 01	174	0.1227E 02
190	0.7967E 01	191	0.1020E 02	194	0.7576E 01
201	0.5462E 01	205	0.5298E 01	206	0.1183E 02
208	0.4922E 01	214	0.1239E 02	223	0.9384E 01
230	0.3901E 01	235	0.3042E 01	251	0.3425E 01
255	0.5039E 01	259	0.7074E 01	266	0.7872E 01
270	0.4994E 01	282	0.1196E 02	290	0.4138E 01
296	0.7408E 01	304	0.2695E 01	306	0.4016E 01
316	0.4625E 01	317	0.3114E 01	318	0.4915E 01
334	0.6080E 01	336	0.7804E 01	342	0.5292E 01
343	0.9740E 01	346	0.6488E 01	348	0.1630E 02
353	0.4553E 01	403	0.8865E 01	458	0.8787E 01
441	0.1054E 02	452	0.1533E 01	457	0.3051E 01
463	0.3904E 01	471	0.6031E 01	481	0.1743E 01
72	0.5918E 03				
OBSERVATIONS IN GROUP WITHIN GROUP S.S.					





GROUP 11		GROUP 12	
OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
1	0.8919E 01	2	0.1021E 01
11	0.8071E 01	14	0.7018E 00
17	0.6304E 01	24	0.8756E 00
20	0.8427E 01	45	0.2713E 01
54	0.6664E 01	103	0.9010E 01
117	0.7568E 01	120	0.5459E 01
124	0.2940E 01	125	0.7222E 01
131	0.3246E 01	133	0.5967E 01
143	0.7205E 01	145	0.7166E 01
151	0.3903E 01	156	0.3500E 01
166	0.1701E 02	192	0.6226E 01
243	0.7118E 01	244	0.6988E 01
257	0.9187E 01	263	0.1925E 02
271	0.6055E 01	279	0.3309E 01
297	0.3363E 01	298	0.4238E 01
324	0.1201E 01	461	0.9891E 01
48	0.2732E 03		
OBSERVATIONS IN GROUP WITHIN GROUP S.S.		OBSERVATIONS IN GROUP WITHIN GROUP S.S.	

GROUP 11		GROUP 12	
OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
3	0.6949E 00	21	0.3520E 01
15	0.5400E 01	48	0.1326E 02
28	0.3098E 01	84	0.7306E 01
46	0.5350E 01	100	0.1751E 02
111	0.8729E 00	112	0.5719E 01
122	0.4886E 01	139	0.3041E 01
128	0.3794E 01	183	0.1475E 02
136	0.6807E 01	207	0.3038E 01
146	0.5579E 01	277	0.1040E 02
165	0.3340E 01	315	0.1220E 02
199	0.7067E 01	327	0.2938E 01
249	0.8701E 01	385	0.1117E 02
264	0.8542E 01	408	0.8969E 01
288	0.2755E 01	0	0.0000E 00
300	0.1520E 01		
472	0.6139E 01		
OBSERVATIONS IN GROUP WITHIN GROUP S.S.		OBSERVATIONS IN GROUP WITHIN GROUP S.S.	



GROUP 13	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
35	0.6687E 01	38	0.6129F 01	59	0.7277E 01		
55	0.3502E 02	61	0.1033F 02	62	0.1748E 02		
63	0.3139E 01	67	0.3130F 02	71	0.4630E 01		
73	0.2948E 02	83	0.4541E 01	99	0.1525E 02		
149	0.3765E 01	155	0.3989E 01	158	0.1121E 02		
209	0.7615E 01	252	0.1973F 01	274	0.9094E 01		
319	0.1426E 02	330	0.1230E 02	333	0.8889E 01		
351	0.1081E 02	356	0.8199E 01	374	0.5315E 01		
376	0.6446E 01	378	0.3432E 02	384	0.1004E 02		
387	0.8149E 01	388	0.2002E 02	391	0.6013E 01		
405	0.4987E 01	406	0.1242F 02	407	0.1305E 02		
411	0.1191E 02	412	0.1344E 01	413	0.5965E 01		
416	0.4055E 01	418	0.4452E 01	420	0.8945E 01		
426	0.1374E 02	429	0.7923E 01	431	0.3519E 01		
432	0.1410E 02	436	0.4270E 01	437	0.1083E 02		
442	0.1241E 01	444	0.4672F 01	0	0.0000E 00		
47	0.4632E 03						
OBSERVATIONS IN GROUP WITHIN GROUP S.S.							

GROUP 14	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
33	0.4549E 01	42	0.8620E 01	53	0.6966E 01		
57	0.7877E 01	64	0.5490E 01	74	0.1172E 02		
101	0.2008E 02	113	0.1781E 02	116	0.1122E 02		
118	0.5210E 02	119	0.1275E 02	153	0.4654E 01		
154	0.5587E 01	159	0.2677E 02	170	0.1795E 02		
197	0.6185E 01	200	0.5746F 01	211	0.7841E 01		
215	0.1115E 02	291	0.1411E 02	340	0.9972E 01		
355	0.1460E 02	358	0.2357F 02	365	0.1762E 02		
401	0.6581E 01	404	0.3014E 02	421	0.6010E 01		
428	0.4714E 01	455	0.2399E 01	0	0.0000E 00		
29	0.5542E 03						
OBSERVATIONS IN GROUP WITHIN GROUP S.S.							

GROUP 15	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN	OBSERVATION	DISTANCE FROM GROUP MEAN
65	0.6491E 02	66	0.3584E 02	69	0.3474E 02		
178	0.7840E 01	189	0.3137F 02	222	0.1471E 02		
265	0.5153E 02	0	0.0000E 00	0	0.0000E 00		
7	0.2409E 03						
OBSERVATIONS IN GROUP WITHIN GROUP S.S.							



ANALYSIS BY VARIABLE  
VARIABLE GROUP MEANS

FINAL COL.	SHOWS CONTRIBUTION TO TOTAL	SUM OF SQUARES EXPLAINED BY CLUSTERING	BY CLUSTERING			
COMPON 1	0.3415E 01	-0.8107E 00	-0.1937E 00	-0.2695E 01	-0.3686E 01	0.1514E 01
0.8042E 00	0.4295E 01	0.2441E 01	-0.7522E 00	-0.1893E 01	0.2217E 04	
COMPON 2	0.6478E 00	-0.1401E 01	0.5207E 01	-0.4652E 00	0.1997E 01	-0.4591E 00
-0.9496E 00	0.1459E 01	-0.1115E 01	-0.1487E 01	0.1110E 01	0.5096E-01	0.1115E 04
COMPON 3	0.4715E 00	-0.5255E 00	-0.5653E 00	-0.6169E 01	-0.9979E-01	0.4716E 00
0.8562E 00	-0.2880E 01	0.1948E 00	0.2767E 00	0.5957E 00	-0.8641E 00	0.6079E 03
COMPON 4	-0.4494E-01	0.5501E 00	-0.7977E 00	0.7141E 00	0.4623E 00	0.2183E 01
-0.1393E 01	0.3720E 00	-0.5501E 00	-0.8272E 00	-0.2116E 00	-0.6052E 01	0.5941E 03
COMPON 5	-0.6655E 00	-0.4565E 00	0.6276E 00	-0.5325E 00	-0.1208E 01	0.1444E 01
-0.8623E 00	0.8308E 00	0.1425E 01	0.1959E 01	-0.1784E 01	-0.1601E 01	0.5742E 03
COMPON 6	0.9410E 00	-0.8408E-01	-0.1354E 01	0.1010E 01	0.5645E 00	0.3478E 00
-0.1248E 01	-0.2499E 00	-0.5739E 00	-0.5244E 00	-0.2704E 01	0.2839E 01	0.5171E 03
COMPON 7	0.8151E 00	-0.5251E 00	-0.3374E 00	0.6184E 00	0.1724E 01	0.1458E 01
0.3597E 01	0.9998E 00	-0.4397E-01	-0.5060E-01	-0.1325E 01	-0.3649E 01	0.4744E 03
COMPON 8	-0.7959E 00	0.6581E 00	0.6925E 00	0.6583E 00	-0.1670E 01	-0.1022E 01
0.2926E 01	0.7414E 00	-0.6131E 00	-0.3843E 00	-0.9834E 00	-0.8526E 00	0.3750E 03
COMPON 9	0.4331E 00	-0.9627E 00	-0.4999E 00	0.3997E 01	-0.4625E 00	0.1049E 01
0.3670E 01	-0.1505E 01	0.1977E 00	0.5305E-01	-0.9497E-01	0.9345E 00	0.3897E 03
COMPON 10	0.5269E 00	-0.9039E-01	0.2195E 00	0.2205E 01	-0.2507E 00	-0.4108E 01
-0.4815E 00	-0.1325E 01	-0.2089E-01	0.4537E 00	0.4078E 00	-0.2935E 01	0.3463E 03

15 CLUSTERS  
TOTAL SUM OF SQUARES EXPLAINED BY CLUSTERING = 0.7212E 04

SUMMARY

	SUM OF SQUARES	PERCENTAGE
WITHIN GROUPS	0.4764E 04	0.5978E 02
BETWEEN GROUPS	0.7212E 04	0.6022E 02
TOTAL	0.1198E 05	0.1000E 03

ND= 1  
ND= 2



APPENDIX E

Means of 10 and 20 Cluster Classes

- Experimental Analysis I

CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES										SIZE
	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05	
1	0.3912E 04	0.3501E 04	0.3178E 04	0.2758E 02	0.4570E 01	0.3699E 02	0.9110E 01	0.9078E 00	0.2897E-01	0.1026E 02	107
2	0.6493E 03	0.7462E 03	0.9269E 01	0.1629E 01	0.2269E 01	0.2561E 02	0.1045E 02	0.6944E 00	0.2049E 01	0.9354E 01	108
3	0.4820E 04	0.4175E 04	0.1251E 02	0.2513E 02	0.2148E 01	0.1747E 02	0.3693E 01	0.5026E 00	0.4000E-01	0.1074E 02	27
4	0.1597E 04	0.1150E 04	0.5792E 01	0.2375E 01	0.1811E 01	0.3652E 02	0.2651E 01	0.0000E 00	0.6635E 00	0.2915E 02	37
5	0.2474E 03	0.2192E 03	0.5000E-01	0.2717E 01	0.2000E 01	0.0000E 00	0.6472E 01	0.0000E 00	0.7365E 02	0.4027E 01	12
6	0.2651E 03	0.2560E 03	0.9636E 00	0.8753E 00	0.1029E 01	0.1864E 02	0.2206E 01	0.0000E 00	0.1000E 00	0.1140E 01	34
7	0.1136E 04	0.1079E 04	0.1210E 02	0.1450E 01	0.2645E 01	0.1082E 02	0.1131E 02	0.1042E 00	0.3700E 00	0.8355E 01	76
8	0.5859E 03	0.6674E 03	0.2928E 01	0.8804E 00	0.3844E 00	0.1322E 02	0.5793E 01	0.0000E 00	0.3077E-02	0.2042E 01	52
9	0.7474E 03	0.6267E 03	0.5973E 01	0.1290E 01	0.1481E 01	0.1807E 02	0.6684E 01	0.0000E 00	0.9259E-01	0.7073E 01	27
10	0.7687E 03	0.6747E 03	0.9310E 02	0.1246E 01	0.1000E 01	0.1841E 01	0.3890E 01	0.0000E 00	0.8929E 01	0.6303E 01	7
TOTAL	0.1754E 04	0.1551E 04	0.1475E 02	0.1826E 01	0.2435E 01	0.2610E 02	0.7848E 01	0.3976E 00	0.2520E 01	0.9352E 01	487

GROUP	VARIABLES										SIZE
	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01	
1	0.2822E 00	0.1991E 00	0.4182E 02	0.5720E-01	0.3448E 00	0.3353E 00	0.8737E 01	0.0000E 00	0.2056E 00	0.2524E 01	107
2	0.6686E 00	0.8521E 00	0.4768E 02	0.1274E 01	0.1213E 01	0.6103E 00	0.5579E 01	0.5556E-01	0.2778E 00	0.5166E 01	108
3	0.3072E 01	0.5548E 00	0.3252E 02	0.3748E 00	0.2803E 02	0.2401E 01	0.1689E 02	0.2222E 00	0.0000E 00	0.1270E 00	27
4	0.1599E 01	0.5878E 00	0.1860E 02	0.4688E 01	0.5541E 01	0.3051E 01	0.2102E 02	0.6757E 00	0.3514E 00	0.1556E 01	57
5	0.1172E 00	0.0000E 00	0.5176E 01	0.5208E 00	0.9633E 01	0.4972E 01	0.1809E 02	0.6333E-01	0.8333E-01	0.0000E 00	12
6	0.1687E 01	0.1685E 01	0.2627E 02	0.2658E 02	0.2178E 02	0.2645E 01	0.8667E 01	0.1471E 00	0.2941E-01	0.1193E 02	54
7	0.6839E 00	0.4661E 00	0.4244E 02	0.8792E 00	0.1388E 01	0.3909E 00	0.4664E 01	0.5265E-01	0.2763E 00	0.1569E 01	76
8	0.5103E 01	0.4749E 01	0.3127E 02	0.7648E 01	0.3211E 02	0.5770E 01	0.1514E 02	0.9615E-01	0.3646E-01	0.4621E 01	52
9	0.4674E 00	0.7281E 00	0.5635E 02	0.1450E 01	0.9051E 01	0.1885E 01	0.5581E 01	0.3704E-01	0.3533E 00	0.4576E 01	27
10	0.0000E 00	0.1812E 02	0.4679E 02	0.1416E 02	0.0000E 00	0.4977E 01	0.1645E 02	0.1429E 00	0.2657E 00	0.4657E 00	7
TOTAL	0.1097E 01	0.1502E 01	0.3938E 02	0.3781E 01	0.8225E 01	0.1734E 01	0.9600E 01	0.1109E 00	0.2074E 00	0.3657E 01	487

GROUP	VARIABLES										SIZE
	A02	A03	A04	A05	A06	A07	W01	W02	W03	W04	
1	0.4150E 02	0.3516E 02	0.2718E 00	0.1444E 00	0.2175E 01	0.9942E 00	0.9476E 00	0.8420E 02	0.1373E 02	0.2228E 02	107
2	0.4075E 02	0.2825E 02	0.6706E 00	0.9756E 00	0.3371E 01	0.1225E 01	0.3158E 01	0.9727E 02	0.9901E 01	0.6846E 01	108
3	0.9404E 01	0.6600E 01	0.1035E 02	0.1381E 02	0.7859E 01	0.6322E 00	0.1586E 01	0.4783E 01	0.3595E 01	0.1321E 02	27
4	0.3092E 02	0.4297E 02	0.1921E 01	0.7264E 01	0.4541E 01	0.5181E 00	0.3231E 01	0.8888E 02	0.1203E 02	0.1031E 02	37
5	0.0000E 00	0.0000E 00	0.8333E 01	0.6333E 01	0.0000E 00	0.1167E-01	0.2581E 02	0.7783E 02	0.1431E 02	0.1542E 02	12
6	0.9679E 01	0.5107E 01	0.0000E 00	0.1583E 00	0.1573E 01	0.6744E 00	0.4175E 01	0.8301E 02	0.1961E 01	0.3561E 01	54
7	0.5621E 02	0.3567E 02	0.7249E 00	0.1833E 02	0.9029E 00	0.1456E 01	0.2762E 01	0.9803E 02	0.3509E 01	0.2752E 02	76
8	0.5325E 01	0.6361E 01	0.1424E 02	0.9456E 01	0.1000E 02	0.5702E 00	0.4135E 01	0.6460E 02	0.2884E 01	0.7852E 01	52
9	0.5602E 02	0.1745E 02	0.1243E 01	0.1305E 02	0.5406E 01	0.1415E 01	0.3687E 01	0.8713E 02	0.5556E 01	0.6173E 01	27
10	0.1744E 01	0.2939E 01	0.1257E 00	0.9157E 00	0.3129E 01	0.2239E 01	0.1230E 02	0.8488E 02	0.1667E 02	0.1429E 02	7
TOTAL	0.2994E 02	0.2523E 02	0.2840E 01	0.1392E 02	0.3671E 01	0.1501E 01	0.3423E 01	0.6518E 02	0.8207E 01	0.1378E 02	487

CENTROIDS OF 10 CLUSTER CLASSES - SAMPLE A



CLUSTER CLASSIFICATION - SAMPLE A

GROUP MEANS		VARIABLES										SIZE
GROUP	M05	M06	M07	M01	M02	M03	M04	M05	M06	M07		
1	0.1924E	02 0.3553E	02 0.9221E	01 0.9626E	00 0.4673E	-01 0.5514E	00 0.7850E	00 0.7290E	00 0.0000E	00 0.2346E	-02 107	
2	0.5124E	01 0.6500E	02 0.1513E	02 0.3476E	00 0.1019E	00 0.1852E	-01 0.8611E	00 0.1574E	00 0.8694E	-01 0.0000E	00 108	
3	0.1896E	02 0.5261E	02 0.2901E	01 0.6296E	00 0.1481E	00 0.7407E	-01 0.5185E	00 0.1111E	00 0.0000E	00 0.1852E	00 47	
4	0.2856E	02 0.4577E	02 0.3535E	01 0.2703E	00 0.2973E	00 0.5405E	-01 0.6757E	00 0.8108E	-01 0.0000E	00 0.5405E	-01 37	
5	0.2085E	02 0.5347E	02 0.1597E	02 0.0000E	00 0.8333E	00 0.0000E	00 0.3333E	00 0.0000E	00 0.1997E	02 0.1667E	00 12	
6	0.1292E	02 0.1443E	02 0.6753E	02 0.8824E	-01 0.2059E	00 0.2941E	-01 0.5588E	00 0.0000E	00 0.0000E	00 0.4706E	00 34	
7	0.5855E	02 0.4715E	01 0.5702E	01 0.5921E	00 0.5243E	-01 0.6579E	-01 0.8421E	00 0.2765E	00 0.1008E	00 0.0000E	00 76	
8	0.1667E	02 0.6651E	02 0.6090E	01 0.7692E	-01 0.1146E	00 0.0000E	00 0.1923E	00 0.0000E	00 0.0000E	00 0.5769E	-01 52	
9	0.1298E	02 0.5247E	02 0.2284E	02 0.2222E	00 0.1111E	00 0.0000E	00 0.7037E	00 0.1111E	00 0.0000E	00 0.0000E	00 27	
10	0.1429E	02 0.5476E	02 0.0000E	00 0.2857E	00 0.0000E	00 0.0000E	00 0.4286E	00 0.1429E	00 0.1786E	01 0.0000E	00 7	
TOTAL	0.2184E	02 0.4104E	02 0.1570E	02 0.4661E	00 0.1243E	00 0.1458E	00 0.6879E	00 0.2587E	00 0.5529E	00 0.5955E	-01 487	

GROUP MEANS		VARIABLES										SIZE
GROUP	M08	M01	M02	M03	M04	M05	M06	M01	M02	M03		
1	0.1607E	01 0.1000E	01 0.1398E	01 0.9720E	00 0.2804E	-01 0.5115E	02 0.3738E	-01 0.5822E	02 0.4116E	02 0.6275E	00 107	
2	0.4998E	01 0.1000E	01 0.1107E	01 0.1000E	01 0.0000E	00 0.5868E	02 0.1750E	00 0.4937E	02 0.5032E	02 0.5106E	00 108	
3	0.1268E	01 0.1481E	00 0.1481E	01 0.1111E	00 0.3704E	-01 0.5111E	02 0.0000E	00 0.8908E	02 0.3510E	01 0.7407E	01 27	
4	0.2340E	01 0.1000E	01 0.1000E	01 0.1000E	01 0.0000E	00 0.5211E	02 0.1622E	00 0.5720E	02 0.4964E	01 0.5734E	02 37	
5	0.1146E	02 0.1000E	01 0.1007E	01 0.9167E	00 0.8333E	-01 0.5542E	02 0.1667E	00 0.4843E	02 0.5157E	02 0.0000E	00 12	
6	0.6258E	01 0.1000E	01 0.1425E	01 0.9118E	00 0.8824E	-01 0.6266E	02 0.3235E	00 0.8485E	02 0.3382E	01 0.1176E	02 34	
7	0.4166E	01 0.1000E	01 0.1437E	01 0.9868E	00 0.1316E	-01 0.5808E	02 0.4474E	00 0.3535E	02 0.6452E	02 0.1555E	00 76	
8	0.2514E	01 0.1000E	01 0.1135E	01 0.1000E	01 0.0000E	00 0.5304E	02 0.6923E	00 0.9151E	02 0.8487E	01 0.0000E	00 52	
9	0.4808E	01 0.9630E	00 0.1000E	01 0.0000E	00 0.9670E	00 0.5793E	02 0.0000E	00 0.7804E	02 0.2196E	02 0.0000E	00 27	
10	0.3325E	01 0.1000E	01 0.1000E	01 0.7143E	00 0.2857E	00 0.4771E	02 0.7143E	00 0.8571E	02 0.1429E	02 0.0000E	00 7	
TOTAL	0.3662E	01 0.9507E	00 0.1479E	01 0.8747E	00 0.7598E	-01 0.5254E	02 0.2402E	00 0.6099E	02 0.3468E	02 0.4355E	01 487	

GROUP MEANS		VARIABLES										SIZE
GROUP	G04	G05	G06	G04	G05	G06	G04	G05	G06	G04		
1	0.3564E	00 0.2701E	01 0.1402E	00							107	
2	0.2407E	00 0.1552E	01 0.5506E	-01							108	
3	0.1852E	00 0.1037E	01 0.1111E	00							27	
4	0.8108E	-01 0.4865E	00 0.5405E	-01							37	
5	0.6667E	00 0.1833E	01 0.0000E	00							12	
6	0.1765E	00 0.1235E	01 0.0000E	00							34	
7	0.1974E	00 0.1711E	01 0.5265E	-01							76	
8	0.5769E	-01 0.2115E	00 0.3846E	-01							52	
9	0.7407E	-01 0.1111E	01 0.7407E	-01							27	
10	0.5714E	00 0.1286E	01 0.2857E	00							7	
TOTAL	0.2218E	00 0.1469E	01 0.7592E	-01							487	



UNIVARIATE F TESTS : SAMPLE A - 10 CLUSTER CLASSES

WILKS LAMBDA (U-STATISTIC) AND UNIVARIATE F-RATIO

VARIABLE	WILKS LAMBDA	F
S01	.6680	26,3369
S02	.6879	24,0434
S03	.6182	32,7304
S04	.6982	22,9058
S05	.5054	51,8742
L01	.8299	10,8653
L02	.9341	3,7416
L03	.9746	1,3792
L04	.2669	145,5921
L05	.8361	10,3881
L06	.9672	1,7958
L07	.8722	7,7676
L08	.8964	6,1237
L09	.7942	13,7352
L10	.7705	15,7886
L11	.9396	3,4099
L12	.8665	8,1647
L13	.7030	22,3935
L14	.9245	4,3262
A01	.9553	2,4778
A02	.7537	17,3208
A03	.7560	17,1012
A04	.8934	6,3217
A05	.8238	11,3367
A06	.9613	2,1357
A07	.3850	84,6646
W01	.7052	22,1554
W02	.4861	56,0223
W03	.9287	4,0689
W04	.8812	7,1430
W05	.7452	18,1224
W06	.6899	23,8250
W07	.6884	23,9880
M01	.5994	35,4164
M02	.8391	10,1649
M03	.6235	32,0016
M04	.7880	14,2551
M05	.6382	30,0451
M06	.6668	26,4887
M07	.7304	19,5611
M08	.8574	8,8143
H01	.1915	223,7075
H02	.8676	8,0881
H03	.2183	189,7521
H04	.3191	113,0996
H05	.6147	33,2212
H06	.7305	19,5500
G01	.7944	13,7181
G02	.6919	23,5953
G03	.7435	18,2816
G04	.9102	5,2304
G05	.7401	18,6081
G06	.9654	1,9006

WITH 9 AND 477 DEGREES OF FREEDOM

FO.01 = 3.11



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES										SIZE
	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05	
1	0.6235E 04	0.5387E 04	0.6640E 02	0.3203E 01	0.5202E 01	0.4260E 02	0.6917E 01	0.9735E 00	0.8125E 01	0.8145E 01	24
2	0.2519E 04	0.2181E 04	0.2288E 02	0.2657E 01	0.4103E 01	0.3725E 02	0.8294E 01	0.1744E 00	0.8333E 01	0.1223E 02	39
3	0.5140E 03	0.2949E 03	0.1935E 00	0.1561E 01	0.3600E 01	0.2865E 02	0.2061E 02	0.1581E 01	0.1366E 02	0.1268E 02	15
4	0.5390E 04	0.4672E 04	0.1745E 02	0.2748E 01	0.2375E 01	0.1709E 02	0.4065E 01	0.5656E 00	0.4500E 01	0.7875E 01	24
5	0.6350E 03	0.5653E 03	0.5758E 02	0.1574E 01	0.1182E 01	0.2572E 02	0.1060E 02	0.0000E 00	0.1352E 01	0.7475E 01	33
6	0.1960E 04	0.1471E 04	0.7989E 01	0.2356E 01	0.2429E 01	0.3798E 02	0.3788E 01	0.0000E 00	0.1625E 00	0.2673E 02	26
7	0.1217E 03	0.9610E 02	0.6000E 01	0.2484E 01	0.1500E 01	0.0000E 01	0.0000E 00	0.0000E 00	0.7812E 02	0.2867E 01	10
8	0.2360E 03	0.2056E 03	0.4971E 00	0.1027E 01	0.1000E 01	0.9774E 01	0.8629E 00	0.0000E 00	0.0000E 00	0.0000E 00	17
9	0.5480E 03	0.4904E 03	0.6071E 01	0.1183E 01	0.1590E 01	0.2537E 02	0.4387E 01	0.0000E 00	0.0000E 00	0.5724E 01	45
10	0.1254E 04	0.8888E 03	0.5918E 01	0.2454E 01	0.1462E 01	0.3893E 02	0.2507E 01	0.0000E 00	0.0000E 00	0.3544E 02	13
11	0.5035E 03	0.2441E 03	0.3429E 00	0.8987E 00	0.5714E 00	0.3169E 02	0.3887E 01	0.0000E 00	0.0000E 00	0.5675E 01	7
12	0.2210E 04	0.2115E 04	0.2906E 02	0.2540E 02	0.3521E 01	0.2982E 02	0.7548E 01	0.3648E 00	0.1558E 00	0.901E 01	48
13	0.1988E 04	0.1855E 04	0.2817E 02	0.1487E 01	0.1600E 01	0.0000E 00	0.3133E 01	0.0000E 00	0.0000E 00	0.0000E 00	15
14	0.6757E 04	0.6211E 04	0.1104E 02	0.3500E 01	0.6400E 01	0.4808E 02	0.3534E 02	0.5396E 01	0.0000E 00	0.6450E 01	10
15	0.1802E 04	0.1737E 04	0.2430E 02	0.1852E 01	0.3711E 01	0.3445E 02	0.1160E 02	0.2433E 00	0.4318E 00	0.9194E 01	45
16	0.6594E 03	0.6211E 03	0.7599E 01	0.1541E 01	0.2139E 01	0.2687E 02	0.9209E 01	0.1216E 01	0.2598E 01	0.1047E 02	36
17	0.4475E 03	0.4186E 03	0.4939E 01	0.8801E 00	0.2139E 01	0.2687E 02	0.9508E 01	0.0000E 00	0.0000E 00	0.5242E 01	33
18	0.4519E 03	0.3262E 03	0.8487E 00	0.7520E 00	0.1667E 00	0.9019E 01	0.4973E 01	0.0000E 00	0.5333E 02	0.1245E 01	30
19	0.6877E 03	0.6051E 03	0.4527E 01	0.1144E 01	0.1345E 01	0.1729E 02	0.6489E 01	0.0000E 00	0.8621E 01	0.1003E 02	29
20	0.5445E 03	0.2700E 03	0.7209E 02	0.9750E 02	0.6667E 00	0.0000E 00	0.3687E 01	0.0000E 00	0.1042E 02	0.6010E 01	6
TOTAL	0.1754E 04	0.1551E 04	0.1475E 02	0.1826E 01	0.2435E 01	0.2610E 02	0.7848E 01	0.3976E 00	0.2520E 01	0.9352E 01	487

GROUP	VARIABLES										SIZE
	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01	
1	0.0000E 00	0.1329E 00	0.4074E 02	0.0000E 00	0.4075E 00	0.2908E 00	0.1070E 02	0.0000E 00	0.2917E 00	0.1471E 00	24
2	0.5500E 00	0.3082E 00	0.4309E 02	0.0000E 00	0.1821E 01	0.6428E 00	0.1198E 02	0.0000E 00	0.2565E 01	0.1822E 01	30
3	0.4291E 01	0.1494E 01	0.3105E 01	0.4053E 01	0.1807E 01	0.1467E 01	0.9011E 01	0.0000E 00	0.2000E 00	0.0000E 00	15
4	0.2712E 01	0.5979E 00	0.3939E 02	0.3312E 00	0.2711E 02	0.1797E 01	0.1827E 02	0.1667E 00	0.0000E 00	0.1429E 00	24
5	0.7970E 00	0.2005E 01	0.3589E 02	0.2822E 01	0.1033E 02	0.2247E 01	0.8032E 01	0.6061E 01	0.3030E 01	0.3649E 01	53
6	0.1724E 01	0.3121E 00	0.2269E 02	0.1507E 01	0.5118E 01	0.3303E 01	0.1741E 02	0.5357E 00	0.2500E 00	0.1665E 01	28
7	0.6210E 00	0.0000E 00	0.6411E 01	0.6250E 00	0.1154E 02	0.5966E 01	0.2065E 02	0.1000E 00	0.0000E 00	0.0000E 00	10
8	0.1358E 01	0.1413E 01	0.1195E 02	0.4735E 02	0.2759E 02	0.1858E 01	0.1131E 02	0.1176E 00	0.0000E 00	0.0000E 00	17
9	0.1950E 00	0.1662E 01	0.6116E 02	0.1004E 01	0.4082E 01	0.6504E 00	0.6342E 01	0.4000E 01	0.2000E 00	0.1920E 01	25
10	0.8558E 00	0.5692E 00	0.6081E 01	0.8158E 01	0.6828E 01	0.3395E 01	0.2439E 02	0.7692E 00	0.3846E 00	0.1846E 01	13
11	0.7400E 01	0.9871E 00	0.5714E 01	0.5071E 01	0.3970E 02	0.8567E 01	0.4774E 01	0.5714E 00	0.0000E 00	0.5714E 02	7
12	0.0000E 00	0.2992E 00	0.5164E 02	0.7542E 00	0.4143E 00	0.8708E 01	0.3797E 01	0.2083E 01	0.3750E 00	0.1568E 01	48
13	0.0000E 00	0.1533E 01	0.9995E 02	0.0000E 00	0.0000E 00	0.0000E 00	0.6953E 01	0.0000E 00	0.0000E 00	0.3045E 01	15
14	0.1200E 00	0.1430E 00	0.4471E 01	0.0000E 00	0.0000E 00	0.0000E 00	0.8446E 01	0.0000E 00	0.4000E 00	0.1500E 02	10
15	0.6755E 00	0.4040E 00	0.4135E 02	0.8629E 00	0.5834E 00	0.5622E 01	0.5511E 01	0.4444E 01	0.3111E 00	0.1328E 01	45
16	0.0000E 00	0.4544E 00	0.6733E 02	0.5878E 00	0.1067E 01	0.7355E 00	0.4370E 01	0.8333E 01	0.4444E 00	0.2562E 01	36
17	0.8809E 00	0.1473E 00	0.4752E 02	0.7315E 00	0.1169E 02	0.3055E 00	0.4388E 01	0.6061E 01	0.2727E 00	0.3357E 01	53
18	0.4601E 01	0.6036E 01	0.3152E 02	0.9943E 01	0.3240E 02	0.8006E 01	0.2058E 02	0.1333E 00	0.3333E 01	0.4963E 01	30
19	0.4354E 00	0.6997E 00	0.4902E 02	0.1358E 01	0.1450E 01	0.1755E 01	0.5509E 01	0.6807E 01	0.3103E 00	0.4261E 01	29
20	0.0000E 00	0.2112E 02	0.4224E 02	0.1642E 02	0.0000E 00	0.5807E 01	0.1813E 02	0.1667E 00	0.1667E 00	0.4983E 00	6
TOTAL	0.1097E 01	0.1302E 01	0.3938E 02	0.3741E 01	0.8225E 01	0.1734E 01	0.9600E 01	0.1109E 00	0.2074E 00	0.3657E 01	487



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES																				SIZE
	A02	A03	A04	A05	A06	A07	A07	W01	W02	W03	W04	W04	W04	W04	W04	W04	W04	W04	W04	W04	
1	0.3903E	02	0.3996E	02	0.3712E	00	0.1888E	02	0.11617E	01	0.1196E	01	0.5796F	00	0.7862E	02	0.1563E	02	0.3271E	02	24
2	0.3909E	02	0.3811E	02	0.1305E	-01	0.1707E	02	0.2992E	01	0.9956E	00	0.1350E	01	0.9635E	02	0.5854E	01	0.2102E	02	39
3	0.0000E	00	0.3617E	01	0.1607E	01	0.1958E	02	0.0000E	00	0.9067E	-01	0.5273E	01	0.9549L	02	0.1478E	02	0.9070F	01	15
4	0.1058E	02	0.7425E	01	0.1104E	02	0.1553E	02	0.8841F	01	0.7113E	00	0.9475F	00	0.5380E	01	0.3819E	01	0.1456E	02	24
5	0.2009E	02	0.2025E	02	0.1031E	02	0.1578E	02	0.8642F	01	0.1113E	01	0.4118E	01	0.8998E	02	0.5959E	01	0.2222E	01	33
6	0.3431E	02	0.4668E	02	0.2134E	01	0.5834E	01	0.2215E	01	0.5986E	00	0.2038E	01	0.8799E	01	0.1321E	02	0.1000E	02	28
7	0.0000E	00	0.0000E	00	0.1000E	02	0.1000E	02	0.0000E	00	0.3800E	-01	0.3006F	02	0.7687E	02	0.9166E	01	0.1250E	02	18
8	0.3691E	02	0.3068E	02	0.1128E	00	0.6194E	00	0.7477F	01	0.7465E	00	0.5190E	01	0.7875E	02	0.0000E	00	0.6743E	01	17
9	0.3539E	02	0.3812E	02	0.8054E	00	0.6315E	01	0.3987F	01	0.1109E	01	0.2903F	01	0.8665F	02	0.0000E	00	0.5000E	01	25
10	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.2055F	01	0.8138E	00	0.4757F	01	0.9191E	02	0.1474E	02	0.1070E	02	13
11	0.5119E	02	0.3154E	02	0.3494F	00	0.1336E	02	0.1986E	01	0.1362E	01	0.1416E	01	0.9418E	02	0.2353E	02	0.9846E	01	7
12	0.7036E	02	0.1852E	02	0.6007E	00	0.6970E	01	0.4080E	01	0.2111E	01	0.1993F	01	0.8680E	02	0.6666E	01	0.1556E	02	15
13	0.1120E	02	0.2074E	02	0.0000E	00	0.1000E	02	0.3058E	01	0.1480E	00	0.6770E	00	0.3403E	02	0.3424E	01	0.2509E	02	10
14	0.4100E	02	0.5872E	02	0.5335E	-02	0.1700E	02	0.1250F	01	0.1474E	01	0.1390F	01	0.9730E	02	0.7037E	01	0.2832E	02	45
15	0.4198E	02	0.2971E	02	0.1728E	00	0.8795F	01	0.1446F	01	0.1145E	01	0.3403F	01	0.9861E	02	0.1018E	02	0.6944E	00	36
16	0.2710E	02	0.3003E	02	0.3003E	01	0.1767E	02	0.6585E	00	0.1278E	01	0.4164E	01	0.9783E	02	0.0000E	00	0.3036E	02	33
17	0.0000E	00	0.2222E	02	0.1689E	02	0.6289E	01	0.1687E	02	0.4680E	00	0.4327E	01	0.8267E	02	0.1111E	01	0.6607E	01	50
18	0.5241E	02	0.1579E	02	0.1137E	01	0.1031E	02	0.5033F	01	0.1140E	01	0.3705F	01	0.8379E	02	0.4023E	01	0.5767E	01	29
19	0.1047E	01	0.2372E	01	0.1733E	00	0.9511E	02	0.2800E	01	0.2502E	02	0.1421E	02	0.8446E	02	0.1111E	02	0.1667E	02	6
20	0.2994E	02	0.2523E	02	0.2840E	01	0.1302E	02	0.3671E	01	0.1301E	01	0.3423E	01	0.8518E	02	0.8207E	01	0.1378E	02	37

GROUP	VARIABLES																				SIZE
	W05	W06	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	W07	
1	0.1993E	02	0.2861E	02	0.3619E	01	0.1000E	01	0.8333E	-01	0.7500E	00	0.4250E	00	0.9747E	00	0.0000E	00	0.0000E	00	24
2	0.1812E	02	0.3047E	02	0.2593E	02	0.1000E	01	0.7692E	-01	0.6667E	00	0.6923F	00	0.8205E	00	0.8974E	-02	0.0000E	00	39
3	0.3000E	02	0.4289E	02	0.3333E	01	0.4667E	00	0.6667E	-01	0.6667E	00	0.1000E	01	0.0000E	00	0.5107E	00	0.0000E	00	15
4	0.2133E	02	0.4006E	02	0.3204F	01	0.7083E	00	0.1667E	00	0.8333E	-01	0.5417F	00	0.1250E	00	0.0000E	00	0.1250E	00	24
5	0.4640E	01	0.8717E	02	0.0000E	00	0.2121E	00	0.1515F	00	0.0000E	00	0.3664F	00	0.0000E	00	0.0000E	00	0.0000E	00	35
6	0.2454E	02	0.5065E	02	0.1607E	01	0.5357E	00	0.2857E	00	0.3571E	-01	0.7857E	00	0.7143E	-01	0.0000E	00	0.0000E	00	28
7	0.2500E	02	0.5417E	02	0.1917E	02	0.0000E	00	0.8000E	00	0.0000E	00	0.2000F	00	0.0000E	00	0.2397E	02	0.2000E	00	10
8	0.1113E	02	0.1807E	02	0.6408E	02	0.1176E	00	0.4118E	00	0.0000E	00	0.4118E	00	0.0000E	00	0.0000E	00	0.5294E	00	17
9	0.4267E	01	0.7800E	01	0.8295E	02	0.8000E	-01	0.4000E	-01	0.0000E	00	0.8400F	00	0.6000E	-01	0.0000E	00	0.4000E	-01	15
10	0.3462E	02	0.3526E	02	0.4487F	01	0.2368E	00	0.3844F	00	0.7692E	-01	0.5385E	00	0.7692E	-01	0.0000E	00	0.7672E	-01	23
11	0.1429E	02	0.1905E	02	0.2637E	02	0.0000E	00	0.0000E	00	0.0000E	00	0.4286F	00	0.0000E	00	0.0000E	00	0.1000E	01	7
12	0.6424E	01	0.5753E	02	0.2649E	01	0.2500E	00	0.2083E	-01	0.1250E	00	0.8750E	00	0.6042E	00	0.1379E	00	0.0000E	00	48
13	0.2000E	02	0.4444E	02	0.1353E	02	0.2667E	00	0.0000E	00	0.0000E	00	0.6667F	00	0.5335E	00	0.0000E	00	0.0000E	00	18
14	0.3119E	02	0.3969E	02	0.0000E	00	0.1000F	01	0.0000E	00	0.7000E	00	0.1000E	01	0.1000E	01	0.0000E	00	0.1000E	00	10
15	0.5566E	02	0.1852E	01	0.7037E	01	0.8444F	00	0.2222F	-01	0.1778E	00	0.9556E	00	0.4889E	00	0.0000E	00	0.0000E	00	45
16	0.2778E	01	0.8032E	02	0.6078E	01	0.1944F	01	0.2778F	-01	0.2778E	-01	0.8889E	00	0.5556E	-01	0.6722E	-01	0.0000E	00	36
17	0.6364E	02	0.2273E	01	0.3235E	01	0.2424F	00	0.3080F	-01	0.0000E	00	0.6061F	00	0.0000E	00	0.0000E	00	0.0000E	00	33
18	0.1278E	02	0.7222E	02	0.7222E	01	0.3333E	-01	0.3333E	-01	0.0000E	00	0.1000E	00	0.0000E	00	0.0000E	00	0.1000E	00	30
19	0.1724E	02	0.4655E	02	0.2499E	02	0.2049F	00	0.1034F	00	0.0000E	00	0.6552F	00	0.6897E	-01	0.0000E	00	0.6897E	-01	29
20	0.8333E	01	0.6389E	02	0.0000E	00	0.1667E	00	0.0000E	00	0.0000E	00	0.5000E	00	0.0000E	00	0.2083E	01	0.0000E	00	6
TOTAL	0.2184E	02	0.4104E	02	0.1570E	02	0.4661E	00	0.1243E	00	0.1458E	00	0.6879E	00	0.2587E	00	0.5529E	00	0.5955E	-01	387





UNIVARIATE F TESTS : SAMPLE A - 20 CLUSTER CLASSES

WILKS LAMBDA (U-STATISTIC) AND UNIVARIATE F-RATIO

VARIABLE	WILKS LAMBDA	F
S01	.5463	20.3747
S02	.5770	18.0185
S03	.5455	20.4764
S04	.6359	14.0727
S05	.3871	38.9086
L01	.7526	8.0777
L02	.7289	9.1435
L03	.8764	3.4651
L04	.2826	62.3980
L05	.8030	6.0296
L06	.9218	2.0840
L07	.8511	4.2986
L08	.7020	10.4326
L09	.6507	13.1915
L10	.7806	6.5485
L11	.9090	2.4620
L12	.8178	5.4771
L13	.6978	10.6432
L14	.8540	4.2023
A01	.7135	9.8701
A02	.6285	14.5303
A03	.7229	9.4215
A04	.9060	2.5490
A05	.8151	5.5772
A06	.9120	2.3717
A07	.3297	49.9760
W01	.6408	13.7772
W02	.4316	32.3655
W03	.8420	4.6114
W04	.8428	4.5840
W05	.7086	10.1099
W06	.5391	21.0135
W07	.4570	29.2088
M01	.5214	22.5635
M02	.7222	9.4549
M03	.5395	20.9789
M04	.7550	7.9746
M05	.4918	25.4032
M06	.5978	16.5354
M07	.5795	17.8333
M08	.5987	16.4719
H01	.2903	60.0868
H02	.7435	8.4801
H03	.2109	91.9696
H04	.3098	54.7629
H05	.5116	23.4670
H06	.6761	11.7752
G01	.5960	16.6632
G02	.5907	17.0300
G03	.3461	46.4379
G04	.7434	8.4852
G05	.7135	9.8710
G06	.8433	4.5656

WITH 19 AND 467 DEGREES OF FREEDOM  
 FO.01 = 2.38



APPENDIX F

Results from Experiments A to F

CLUSTER ANALYSIS

EXPERIMENT A

EFFECT OF CHANGING NUMBER OF ITERATIONS

No. of Classes	Analysis I			Analysis II			Analysis III		
	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)
30	3663	-		3596	1.14		3595	1.14	
29	3635	1.79		3633	1.58		3633	1.58	
28	3695	1.51		3686	1.71		3686	1.69	
27	3748	1.39		3746	1.37		3746	1.37	
26	3799	1.57		3796	1.60		3796	1.62	
25	3859	1.92		3857	1.97		3857	1.95	
24	3936	1.44		3936	1.11		3936	0.12	
23	3997	0.74		3983	0.47		3940	2.10	
22	4030	2.03		4004	2.04		4032	1.42	
21	4124	1.36		4098	1.47		4098	1.47	
20	4181	1.40	35.5	4170	1.65	35.6	4170	1.60	35.6
19	4264	1.62	35.1	4256	1.73	35.0	4253	1.79	35.0
18	4354	1.95	34.3	4352	2.14	34.6	4352	2.14	34.6
17	4470	1.93	33.6	4479	2.08	33.5	4479	2.08	33.5
16	4594	2.44*	32.6	4613	1.89	33.1	4613	1.89	33.1
15	4764	2.29	31.5	4745	1.83	32.4	4745	1.83	32.4
14	4939	1.80	31.1	4844	2.81*	31.6	4884	2.81*	31.6
13	5091	1.92	30.3	5118	1.92	30.4	5118	1.92	30.3
12	5270	2.04	29.4	5298	2.17	29.2	5298	2.17	29.2
11	5482	2.40*	27.9	5524	2.02	27.8	5524	2.02	27.8
10	5763	2.25	26.5	5763	2.23	26.6	5763	2.23	26.6
9	6067	2.33*		6064	2.37*		6064	2.37*	
8	6434	2.25		6438	2.22		6438	2.22	
7	6856	1.77		6856	1.77		6856	1.77	
6	7261	1.62		7261	1.62		7261	1.62	
Total sum of squares	11980			11980			11980		



EXPERIMENTAL ANALYSIS II - CLASS NUMBERS

		1	4	3	5	6	7	8	9	2	10	11	12	13	14	15	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	46							1		1						48	
	2		45							14			1	1			61	
	3			24													24	
	4				28												28	
	5					10											10	
	6			2			29			2								33
	7							10										10
	8	17	22							26	2		5					72
	9		3				1		11							1		16
	10									1	12							13
	11	2								3			43					45
	12		2								2		1	36				41
	13			1		1		1						3	41			47
	14				1											28		29
	15																7	7
Tot	65	75	25	29	10	31	10	41	21	13	49	40	42	29	7	7	487	

EXPERIMENTAL ANALYSIS II - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	106	1									107
	2		108									108
	3			27								27
	4				37							37
	5					12						12
	6						34					34
	7							76				76
	8								52			52
	9									27		27
	10										7	7
Tot	106	109	27	37	12	34	76	52	27	7	487	

EXPERIMENTAL ANALYSIS III - CLASS NUMBERS

		1	4	3	5	6	7	8	9	2	10	11	12	13	14	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	46							1		1					48
	2		45							14			1	1		61
	3			24												24
	4				28											28
	5					10										10
	6	2					29			2						33
	7							10								10
	8	18	22						26	2		4				72
	9		3				1		11						1	16
	10									1	12					13
	11	2							3			43				45
	12		2							2		5	32			41
	13		1		1		1						4	40		47
	14			1											28	29
	15															7
Tot	66	75	25	29	10	31	10	41	21	13	52	37	41	29	7	487

EXPERIMENTAL ANALYSIS III - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	106	1									107
	2		108									108
	3			27								27
	4				37							37
	5					12						12
	6						34					34
	7							76				76
	8								52			52
	9									27		27
	10										7	7
Tot	106	109	27	37	12	34	76	52	27	7	487	



CLUSTER ANALYSIS

EXPERIMENT B

EFFECT OF CHANGING SEEDING NUMBER OF CLUSTERS

No. of Classes	Analysis I			Analysis IV			Analysis V		
	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)
30	3663	-							
29	3635	1.79							
28	3695	1.51							
27	3748	1.39							
26	3799	1.57							
25	3859	1.92		3882	0.62				
24	3936	1.44		3915	1.40				
23	3997	0.74		3973	1.21				
22	4030	2.03		4027	1.17				
21	4124	1.36		4081	2.18				
20	4191	1.40	35.5	4187	1.71	35.4	4198	1.20	35.0
19	4264	1.62	35.1	4277	1.33	35.0	4261	2.07	34.7
18	4354	1.95	34.3	4351	1.60	34.2	4376	1.62	34.0
17	4470	1.93	33.6	4446	2.16	33.5	4473	1.88	33.4
16	4594	2.44*	32.6	4584	2.21	32.9	4593	2.16	32.5
15	4764	2.29	31.5	4738	2.28	32.1	4744	2.39*	31.5
14	4939	1.80	31.1	4911	2.61*	31.2	4925	1.66	30.5
13	5091	1.92	30.3	5130	2.01	30.0	5065	2.40*	30.0
12	5270	2.04	29.4	5318	2.24	29.4	5287	1.83	28.9
11	5482	2.40*	27.9	5552	1.75	27.8	5478	2.45*	28.0
10	5763	2.25	26.5	5760	2.56*	26.6	5764	2.24	26.5
9	6067	2.33*		6106	2.09		6067	2.36*	
8	6434	2.25		6438	2.22		6438	2.22	
7	6856	1.77		6856	1.77		6856	1.76	
6	7261	1.62		7261	1.63		7261	1.63	
Total sum of squares	11980	* = Sig at 1% level	25810	11980	* = Sig at 1% level	25810	11980	* = Sig at 1% level	25810

EXPERIMENTAL ANALYSIS IV - CLASS NUMBERS

	2	12	1	3	9	7	5	14	10	8	6	4	15	11	13	Tot
1	47															48
2		44				6						11				61
3			24													24
4				28												28
5					10											10
6						20	10					2	1			33
7							10									10
8		5				1		65				1				72
9								1	15							16
10										12		1				13
11	6							4			38					45
12		2		2					1		29	2	5			41
13		5		1		1	2						38			47
14							1							28		29
15															7	7
Tot	53	56	24	31	10	28	23	71	16	12	67	17	44	28	7	487

EXPERIMENTAL ANALYSIS IV - CLASS NUMBERS

	2	4	1	3	7	5	6	10	8	9	Tot
1	104	2				1					107
2		107						1			108
3			25			2					27
4				36		1					37
5					12						12
6		7				19		8			34
7	1			1			74	50			76
8									27		52
9										7	27
10											7
Tot	105	116	25	37	12	25	74	59	27	7	487



EXPERIMENTAL ANALYSIS V - CLASS NUMBERS

		1	12	2	3	6	15	7	8	5	11	10	13	14	9	4	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	43									4	1					48	
	2		47										1	1			61	
	3			24														24
	4				28													28
	5					10												10
	6		5		1		25		2									33
	7							10										10
	8	36	25						2	1	2	6						72
	9									16								16
	10								1		12							13
	11											48						45
	12		1						2			1	37					41
	13		1		1									45				47
	14														29			29
	15																7	7
Tot	79	79	24	30	10	25	10	19	17	18	56	38	46	29	7	7	487	

EXPERIMENTAL ANALYSIS V - CLASS NUMBERS

		1	7	2	3	5	6	9	10	8	4	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	106					1					107
	2		107					1				108
	3			27								27
	4				36		1					37
	5					12						12
	6						32			2		34
	7	2							74			76
	8									52		52
	9									27		27
	10										7	7
Tot	108	107	27	36	12	34	75	52	29	7	7	487

CLUSTER ANALYSIS

EXPERIMENT C

EFFECT OF CHANGING NUMBER OF COMPONENTS IN ANALYSIS

No. of Classes	Analysis I			Analysis VI			Analysis VII		
	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)
30	3633	-		5828	-		7474	0.48	
29	3635	1.79		5821	1.20		7494	1.54	
28	3695	1.51		5869	1.52		7560	2.00*	
27	3748	1.39		5932	1.54		7648	1.82	
26	3799	1.57		5998	1.59		7731	1.55	
25	3859	1.92		6069	1.58		7804	2.31*	
24	3936	1.44		6142	1.84		7917	2.67*	
23	3997	0.74		6231	2.08*		8053	2.70*	
22	4030	2.03		6336	1.96		8197	3.24*	
21	4124	1.36		6440	1.79		8378	3.13*	
20	4191	1.40	35.5	6540	2.98*	37.0	8563	2.95*	38.7
19	4264	1.62	35.1	6710	2.44*	36.0	8747	2.72*	37.7
18	4354	1.95	34.3	6870	2.32*	35.4	8927	2.32*	36.7
17	4470	1.93	33.6	7026	2.18*	34.6	9090	2.82*	35.5
16	4594	2.44*	32.6	7183	2.29*	33.4	9301	2.66*	34.3
15	4764	2.29	31.5	7360	1.99	32.5	9514	2.70*	33.3
14	4939	1.80	31.1	7527	2.42*	31.4	9747	2.48*	32.0
13	5091	1.92	30.3	7724	2.30*	30.2	9978	3.21*	31.6
12	5270	2.04	29.4	7976	2.83*	29.8	10304	3.14*	30.3
11	5482	2.40*	27.9	8287	2.60*	28.4	10655	2.84*	28.9
10	5763	2.25	26.5	8608	2.42*	26.8	11009	2.87*	27.2
9	6067	2.33*		8947	2.51*		11411	2.70*	
8	6434	2.25		9350	2.28*		11842	2.51*	
7	6856	1.77		9779	2.05*		12305	2.14*	
6	7261	1.62		10239	2.10*		12769	2.36*	
Total sum of squares	11980	* = Sig at 1% level	26810	15125	* = Sig at 1% level		17735	* = Sig at 1% level	



EXPERIMENTAL ANALYSIS VI - CLASS NUMBERS

		1	9	2	4	8	7	3	6	10	11	12	15	5	14	13	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	44									4						48	
	2		38				9		13					1			61	
	3			21								1			1	1		24
	4		1		27													28
	5					10												10
	6						17		2				13	1				33
	7			2	1			4						3				10
	8	26	35				5		2		2	2						72
	9		1							14		1						16
	10							1	1		11							13
	11	7									4	37						45
	12		1		1				2	2		27			8			41
	13		2		1		1		1					3	39			47
	14			2												27		29
	15																7	7
Tot	77	78	25	30	10	32	5	21	16	22	67	19	50	28	7		487	

EXPERIMENTAL ANALYSIS VI - CLASS NUMBERS

		1	6	2	4	7	3	8	5	10	8	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	103					1	3				107
	2	4	100					2	2			108
	3			26	1							27
	4	1			36							37
	5					12						12
	6		10				21		1	2		34
	7		1					73	1	1		76
	8						2		50			52
	9			1						26		27
	10										7	7
Tot	108	111	27	37	12	24	78	54	29	7		487

EXPERIMENTAL ANALYSIS VII - CLASS NUMBERS

		1	5	11	6	8	9	12	15	7	3	10	4	2	14	13	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	43									5						48	
	2		50				9					1		1			61	
	3			22								1			1		24	
	4		1		26								1					28
	5						10											10
	6							18		11				4				33
	7			2	3				4	1								10
	8	29	30					4				5	3		1			72
	9		1								14		1					16
	10								1			12						13
	11	9										4	34				1	45
	12		2		1						2		30	4	2			41
	13		6		1			2		4				15	18		1	47
	14				2									4			23	29
	15	1								1								5
Tot	82	90	26	31	10	33	5	17	16	27	70	27	23	24	6		487	

EXPERIMENTAL ANALYSIS VII - CLASS NUMBERS

		1	3	7	4	6	8	5	2	10	9	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	103					1	3				107
	2		106					2				108
	3			26				1				27
	4	1	3		30			2	1			37
	5		2			10						12
	6		4		1		4		23	2		34
	7		1					74		1		76
	8		2					1	48		1	52
	9			1						26		27
	10	1								1	5	7
Tot	105	118	27	31	10	5	83	72	30	6	487	



CLUSTER ANALYSIS

EXPERIMENT D

EFFECT OF STANDARDISATION OR UNSTANDARDISATION

OF OPERATIONAL AND COMPONENT VARIABLES

No. of Classes	Analysis I			Analysis VIII			Analysis IX			Analysis X		
30	3663	-		1624	-		0.2121	28.35*		1434	1.11	
29	3635	1.79		1623	0.60		0.2661	29.34*		1448	2.20	
28	3695	1.51		1632	1.16		0.3383	-		1478	1.34	
27	3748	1.39		1650	1.18		0.2910	11.19*		1497	1.69	
26	3789	1.57		1669	1.37		0.3228	2.58*		1521	1.08	
25	3859	1.92		1691	1.82		0.3312	5.09*		1538	1.53	
24	3936	1.44		1723	1.57		0.3487	-		1562	2.12	
23	3997	0.74		1752	1.64		0.3378	2.15		1598*	2.43*	
22	4030	2.03		1784	1.70		0.3459	1.60		1641	1.31	
21	4124	1.36		1819	1.33		0.3523	-		1666	1.93	
20	4191	1.40	35.5	1848	1.39	35.4	0.3509	-	6.8	1704	1.80	27.0
19	4264	1.62	35.1	1880	1.47	34.7	0.3485	0.54	6.8	1742	1.72	26.9
18	4354	1.95	34.3	1916	1.64	34.3	0.3510	1.09	6.2	1781	1.68	26.3
17	4470	1.93	33.6	1959	1.96	33.6	0.3562	1.04	5.9	1822	1.97	25.9
16	4594	2.44	32.6	2014	1.61	32.5	0.3616	1.95	4.7	1873	1.82	25.0
15	4764	2.29*	31.5	2063	1.57	31.5	0.3722	0.81	4.7	1925	1.47	24.9
14	4939	1.80	31.1	2115	1.91	30.9	0.3770	0.16	4.2	1971	2.06	24.1
13	5091	1.92	30.3	2184	2.76*	29.6	0.3781	-	4.7	2040	1.92	22.5
12	5270	2.04*	29.4	2294	2.90*	27.9	0.3714	1.71	4.7	2112	2.01	21.6
11	5482	2.50*	27.9	2425	2.60*	26.8	0.3839	0.19	4.2	2195	2.55*	20.7
10	5763	2.25	26.5	2560	2.68*	25.6	0.3855	-	3.0	2314	2.39*	18.7
9	6067	2.33*		2721	2.56*		0.3843	0.96		2444	2.95*	
8	6434	2.25		2902	1.84		0.3939	0.76		2631	2.63*	
7	6856	1.77		3058	2.24		0.4026	1.21		2833	2.70*	
6	7261	1.62		3287	1.80		0.4190	-		3089	2.37*	
Total sum of squares	11980	*Sig at 1% level	25810	4870	*Sig at 1% level	25810	?	*Sig at 1% level	4870	4510	*Sig at 1% level	25810

EXPERIMENTAL ANALYSIS VIII - CLASS NUMBERS

		2	4	8	6	10	12	11	7	14	1	3	5	9	13	15	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	45							2						1		48
	2		32				4		8				13	4			61
	3			21								3					24
	4				23				5								28
	5					10											10
	6						30		1		1		1				33
	7						1	9									10
	8	3	37				2		30								72
	9		1							14						1	16
	10		1					1			10		1				13
	11	2	3		1						3		38			1	45
	12		1		1				4	3		29	2	1			41
	13		1						7	1		1	2	35			47
	14			1									1		27		29
	15																7
Tot	50	76	22	25	10	37	10	57	21	14	68	20	40	30	7	487	

EXPERIMENTAL ANALYSIS VIII - CLASS NUMBERS

		2	1	5	4	7	8	3	6	9	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	64	29	3			1	9		1	107
	2	5	92		1		4	1	5		108
	3			26						1	27
	4	1	1		30		1		4		37
	5		1			11					12
	6	1					31			2	34
	7		2		1			72		1	76
	8	1	1					3	47		52
	9									27	27
	10									7	7
Tot	72	126	29	32	11	37	85	56	32	7	487



EXPERIMENTAL ANALYSIS IX - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	4	1	2	1	4		3	1	6		2	6	13	2	3	48	
	2	3	2	1		2		8		1		5	5	29	1	4	61	
	3	3		3			1	3		1		1	1	9		2	24	
	4	8	2										2	16			28	
	5			1				1				2		5		1	10	
	6	3	1	1					3				2	3	14		6	33
	7	2									2			2	4			10
	8	9	5	3		3		7		2		10	11	16	2	4	72	
	9	1						6		1		2		6				16
	10	1	1					4				1	2	1	2	1		13
	11	4	2	1		2	1	3				10	10	11	3	1	45	
	12	3					1	3		1	1	4	6	22				41
	13	5				1		2		6		4	2	23		4	47	
	14	2		2		1		1		1		4	4	13		1	29	
	15	1						1						2		3	7	
Tot	49	14	14	1	13	3	45	1	21	2	48	53	185	9	29	487		

EXPERIMENTAL ANALYSIS IX - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	19	19	1	1	14	17	1	8	26	1	107
	2	17	36			13	7		6	28	1	108
	3	3	7			5	1	2	2	6	1	27
	4	2	16			5	5			9		37
	5	2	5			1			1	2	1	12
	6	3	12			4	3			12		34
	7	13	28	1		8	8	1	3	11	3	76
	8	5	23			6	4	1	1	12		52
	9	5	10			3	2	1	1	5		27
	10		4							3		7
Tot	69	160	2	1	59	47	6	22	114	7	487	

EXPERIMENTAL ANALYSIS X - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	19	1	5	18				1	3				1			48	
	2	2		16				9		1	3		2		19	9	61	
	3		3		1	9	6		1	1	2				1		24	
	4	1		2	1	1			7	2			11			3	28	
	5					1				1		1		1		6	10	
	6					1			1	2		4		22		2	1	33
	7					1					1		7	1			10	
	8	6		37	5				5	3				1	2	1	12	72
	9			9	1						3			1	2			16
	10	1	1	1	1		7					1			1			13
	11	6		2	1				2		20	1		1	14	1		45
	12	2		1					4	10	11	2	1		9		1	41
	13	1		1	1	25	1	1	1	6		1	1	2	1	2	4	47
	14	1		3		7				3	3			4		1	7	29
	15											7						7
Tot	39	5	77	29	45	14	29	26	46	22	20	20	35	30	33	37	487	

EXPERIMENTAL ANALYSIS X - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	10	2	28	28	5	10	3		5	16	107
	2	16		60	2	9	3	1		9	8	108
	3	7	3	1	7		2	3	2		2	27
	4	8		2	2	9	1		14		1	37
	5	1		7			1	1		1	1	12
	6	2		1			3	4	4	20		34
	7			3		6	34	5		3	25	76
	8	32		2	1	2	6	2		4	3	52
	9	12		4			4			5	2	27
	10							7				7
Tot	8	5	108	40	31	64	26	20	47	58	487	



CLUSTER ANALYSIS

EXPERIMENT E

EFFECT OF A PRIORI SEEDING

	Analysis I			Analysis XI		
17	4470	1.93	33.6	4505	1.46	33.1
16	4594	2.44*	32.6	4599	1.91	32.4
15	4764	2.29	31.5	4732	1.97	31.7
14	4939	1.80	31.1	4881	2.37*	31.5
13	5091	1.92	30.3	5079	1.67	30.4
12	5270	2.04	29.4	5234	2.36*	29.3
11	5482	2.40*	27.9	5477	2.41*	28.0
10	5763	2.25	26.5	5759	2.26	26.6
9	6067	2.33*		6064	2.37*	25.4
8	6434	2.25		6438	2.22	23.6
7	6856	1.77		6856	1.76	21.2
6	7261	1.62		7261	1.62	
	11980	* Sig at 1% level	25810	11980	* Sig at 1% level	25810

EXPERIMENTAL ANALYSIS XI - CLASS NUMBERS

	10	1	6	3	4	5	12	13	7	14	2	8	15	11	9	Tot
1	41									7						48
2		42						17				1	1			61
3			24													24
4				28												28
5					10											10
6		2				29		2								33
7							10									10
8	23	32						2	2	2	11					72
9									16							16
10								1		12						13
11	2	1									45	1				45
12		1						2				38				41
13													46			47
14														29		29
15															7	7
Tot	66	78	24	28	10	29	10	24	18	21	56	40	47	29	7	487

EXPERIMENTAL ANALYSIS XI - CLASS NUMBERS

	2	1	6	3	4	5	7	10	9	8	Tot
1	105					1	1				107
2		105		1			2				108
3			27								27
4				37							37
5					12						12
6		6				27		1			34
7							76				76
8						2		50			52
9									27		27
10										7	7
Tot	105	111	27	38	12	30	79	51	27	7	487



CLUSTER ANALYSIS

EXPERIMENT F

EFFECT OF CHANGING

THE VARIABLE SET AND NUMBER OF COMPONENTS

of res	Analysis XII			Analysis XIV			Analysis XV			Analysis XVII		
	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)	tr W	Beale F-test	Explan. Power(%)
	2519	-		1030	-		1975	-		802	-	
	2511	1.51		1004	0.55		1957	1.05		796	0.66	
	2546	1.28		1013	0.41		1976	1.12		804	0.90	
	2577	1.19		1020	0.84		1997	1.49		816	1.23	
	2607	1.22		1035	1.05		2026	1.96		834	0.79	
	2639	1.64		1055	1.07		2066	1.91		846	1.32	
	2684	2.01		1076	1.10		2107	1.46		866	1.57	
	2742	1.90		1099	1.27		2140	1.43		893	1.57	
	2800	1.58		1127	0.68		2174	1.92		921	1.26	
	2851	1.87		1143	0.68		2222	2.37*		945	1.63	
	2915	1.95	30.0	1160	1.24	26.5	2285	2.00	33.2	979	1.93	29.9
	2986	1.52	29.6	1193	1.39	26.0	2342	2.92*	32.6	1023	2.12	29.4
	3045	1.64	29.0	1233	1.28	25.6	2431	1.87	31.0	1075	1.58	28.9
	3113	1.50	28.7	1273	1.44	24.4	2493	2.49*	30.6	1118	1.46	28.6
	3180	1.60	28.1	1322	1.44	23.6	2582	2.20	29.8	1161	1.56	27.7
	3257	1.65	27.3	1376	1.28	23.2	2668	2.50*	29.0	1213	1.87	27.4
	3343	1.65	26.4	1429	1.24	22.6	2775	1.75	28.1	1281	1.27	26.7
	3437	1.89	25.5	1486	1.16	22.0	2858	2.47*	26.7	1333	1.29	26.1
	3556	2.44*	24.5	1546	1.27	21.6	2987	3.35*	25.5	1393	1.55	24.5
	3727	2.41*	22.9	1620	1.28	21.0	3184	2.22	25.3	1474	1.22	23.6
	3919	2.57*	20.9	1705	1.26	20.4	3335	2.99*	24.1	1548	1.13	22.6
	4155	2.03		1802	1.55		3569	3.37*		1627	1.56	
	4374	2.42*		1943	1.42		3881	3.21*		1755	2.09	
	4683	1.59		2100	1.28		4245	2.54*		1963	1.41	
	4932	1.83		2277	1.33		4606	2.40*		2146	1.58	
of res	7788	*Sig at 1% level	25810	4936	*Sig at 1% level	25810	8006	*Sig at 1% level	25810	5291	Sig at 1% level	25810

EXPERIMENTAL ANALYSIS XII - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	5				23	2	8					7	2		1	48	
	2	15	1		1		5	2			10	10	13	4			61	
	3		3	5	2	6		1	3	1			1	1		1	24	
	4	22	1	1		1			1		1		1				28	
	5		1										1			8	10	
	6	2		3			22		2		2	2						33
	7	1		4			3					1					1	10
	8	14				8	1	16			1	3	21	8				72
	9	1							1		14							16
	10								1				1		11			13
	11	3				3			3			4		27	7		1	45
	12	7		3		1	1			2	2	19	2	4				41
	13	7	7	12	7					12		1	1					47
	14	1		3									1	1			23	29
	15	1					1		1	2							1	1
Tot	79	13	31	10	43	34	33	22	17	39	21	75	33	9	28	487		

EXPERIMENTAL ANALYSIS XII - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	22				44	12	3	1	25		107
	2	50	1	1	1	6	22	7	10	10		108
	3	1	3	8	2	5	2	3		3		27
	4	8	1	4	1	7	14		2			37
	5		1						3		8	12
	6	1		11	1		19		2			34
	7	53		3	1		3	5	4	7		76
	8		8	27	8		4	4	1			52
	9	5		1	1		18	1	1			27
	10			2		2	1			1	1	7
Tot	140	14	57	15	64	95	23	24	46	9	487	



EXPERIMENTAL ANALYSIS XIII - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	11			14	2	16		3				1		1		48	
	2	8		2		14		1			8		5		17	6	61	
	3	1	5	2	11		1		1			1		2			24	
	4	3	2		8	11									3	1	28	
	5							4		6							10	
	6	1	2	10		7										13		33
	7		5		1	1									2	1	10	
	8	44			6	9	5		2				3		3		72	
	9							1				13		2			16	
	10							1	12								13	
	11	19			2	3	3		3				15		1	2	45	
	12		3		2	11					2		5	6		12	41	
	13		24	4	3	8								6		2	47	
	14	1	3	1	4	3								1	15	1	29	
	15				1	1	2	1						2			7	
Tot	88	44	19	52	70	27	8	21	6	10	14	29	19	55	25	487		

EXPERIMENTAL ANALYSIS XIII - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	32			25	3	26	19		1	1	107
	2	37	1	7	7	30	1	2		7	16	108
	3	1	9		11	1	1	1		3		27
	4	2	3	1	18	10					3	37
	5			2					10			12
	6		13	2	1	17					1	34
	7	21		4	2	6		2		9	32	76
	8		33	2	4	2				7	4	52
	9	1	1	1	4	17				2	1	27
	10		2		1		2		1		1	7
Tot	94	62	19	73	86	30	24	11	29	59	487	

EXPERIMENTAL ANALYSIS XIV - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	3	43								2						48	
	2	6							14			8	30	3			61	
	3				18					4	1				1		24	
	4					11		1	14							2	28	
	5	1										1	7		1		10	
	6	1						11		2			2	17			33	
	7			4	2	3										1	10	
	8	50	10							7			3		1	1	72	
	9	4	1									3	1	7			16	
	10	4	4	1							1					3	13	
	11	19	4							1		21	2		1		45	
	12	4				1				1		15	14	6			41	
	13					1	3			4		1	3	29		5	1	47
	14	3			2					2			2	19		1		29
	15		1				1										5	7
Tot	95	63	5	22	16	15	1	45	5	43	36	115	9	11	6	487		

EXPERIMENTAL ANALYSIS XIV - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	16	71	1				7	10	2		107
	2	42	4					4	4	54		108
	3				24			2	1			27
	4	20				15			1	1		37
	5	1				1			2	8		12
	6			4		3	11			16		34
	7	6	10						53	7		76
	8	1					4		3	43	1	52
	9	2			1				3	21		27
	10		1				1				5	7
Tot	88	86	5	25	19	16	13	77	152	6	487	



EXPERIMENTAL ANALYSIS XV - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Tot	
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	1	38					8		1							48	
	2											8	35	7	11		61	
	3				7				3		1	13						24
	4					11			2		1				13	1		28
	5							2		2	1		1	2	1	1		10
	6							10	1				3	15	1	2	1	33
	7				7		1					2						10
	8		12						1		10		6	1	1	41		72
	9	2	1						1		2		2	5		3		16
	10		2	1					9		1							13
	11	15	6								26		1					45
	12	10				1					6		12	5	6	1		41
	13	1						6		8			2	25	4	1		47
	14							2		21	2	2	1				1	29
	15							1					1				5	7
Tot	29	59	8	7	13	21	25	31	51	17	37	88	33	61	7		487	

EXPERIMENTAL ANALYSIS XV - CLASS NUMBERS

		1	2	3	4	5	6	7	8	9	10	Tot
EXPERIMENTAL ANALYSIS I - CLASS NUMBERS	1	11	69	1					4	22		107
	2		1			2		54	8	43		108
	3	1	2		24							27
	4	1		1		26		4		5		37
	5					1	2	5	1	3		12
	6			6		1	13	10	3		1	34
	7	51				5		3	13	4		76
	8	2					6	37	6	1		52
	9	1			1			18	3	3	1	27
	10	1					1				5	7
Tot	68	72	8	25	35	22	131	38	81	7	487	

APPENDIX G

Means of 20, 15 and 10 Cluster Classes

Experimental Analysis VIII



CLUSTER CLASSIFICATION - SAMPLE R

GROUP	VARIABLES										SIZE
	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05	
1	0.1355E 04	0.1278E 04	0.1415E 02	0.1858E 01	0.2810E 01	0.2597E 02	0.1170E 02	0.1021E 01	0.2154E 01	0.9641E 01	126
2	0.3606E 04	0.3090E 04	0.3023E 02	0.2745E 01	0.4202E 01	0.3823E 02	0.6262E 01	0.1893E 01	0.7222E-01	0.1069E 02	85
3	0.1351E 04	0.1274E 04	0.1063E 02	0.1479E 01	0.2753E 01	0.3157E 02	0.1117E 02	0.3372E 00	0.3308E 00	0.8347E 01	72
4	0.1312E 04	0.1009E 04	0.5753E 01	0.2282E 01	0.1875E 01	0.3747E 02	0.2968E 01	0.0000E 00	0.7672E 00	0.3172E 02	32
5	0.5738E 04	0.5005E 04	0.1752E 02	0.2862E 01	0.2690E 01	0.2183E 02	0.6954E 01	0.7810E 00	0.3724E-01	0.6930E 01	29
6	0.609E 03	0.7876E 03	0.3355E 01	0.1059E 01	0.5000E 00	0.1420E 02	0.4734E 01	0.0000E 00	0.2857E-02	0.3620E 01	56
7	0.2197E 03	0.1928E 03	0.5455E-01	0.2723E 01	0.1909E 01	0.0000E 00	0.4506E 01	0.0000E 00	0.7560E 02	0.2006E 01	11
8	0.3635E 03	0.3297E 03	0.1269E 01	0.1097E 01	0.1216E 01	0.2099E 02	0.3198E 01	0.0000E 00	0.4000E 00	0.229E 01	37
9	0.7975E 03	0.7208E 03	0.6039E 01	0.1228E 01	0.1562E 01	0.1709E 02	0.5953E 01	0.0000E 00	0.7813E-01	0.923E 01	32
10	0.7687E 03	0.6747E 03	0.9310E 02	0.1246E 01	0.1000E 01	0.1841E 01	0.3850E 01	0.0000E 00	0.8929E 01	0.6303E 01	7
TOTAL	0.1754E 04	0.1551E 04	0.1475E 02	0.1826E 01	0.2435E 01	0.2610E 02	0.7848E 01	0.3976E 00	0.2520E 01	0.9352E 01	487

GROUP	VARIABLES										SIZE
	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01	
1	0.5343E 00	0.6034E 00	0.4013E 02	0.1127E 01	0.1114E 01	0.3813E 00	0.5012E 00	0.3968E-01	0.3492E 00	0.4593E 01	126
2	0.2979E 00	0.2682E 00	0.4277E 02	0.8444E 00	0.3768E 00	0.5092E 00	0.1156E 02	0.0000E 00	0.8333E-01	0.1302E 01	72
3	0.6995E 00	0.4496E 00	0.4139E 00	0.8319E 00	0.4871E 01	0.3695E 00	0.4754E 01	0.3529E-01	0.2706E 00	0.1411E 01	85
4	0.8350E 00	0.7175E 00	0.1344E 02	0.4201E 01	0.5876E 01	0.2198E 01	0.1980E 01	0.7813E 00	0.3750E 00	0.1638E 01	32
5	0.2863E 01	0.5166E 00	0.3064E 02	0.3490E 00	0.2609E 02	0.2836E 01	0.1724E 02	0.1724E 00	0.3448E-01	0.1133E 00	29
6	0.3461E 01	0.4526E 01	0.3087E 02	0.7478E 02	0.2481E 01	0.6492E 01	0.1575E 02	0.1071E 00	0.3571E-01	0.5048E 01	56
7	0.5645E 00	0.0000E 00	0.5046E 01	0.5682E 00	0.1051E 02	0.5424E 01	0.1907E 02	0.9091E-01	0.0000E 00	0.0000E 00	11
8	0.1715E 01	0.1669E 01	0.3176E 02	0.2324E 02	0.1490E 02	0.2327E 01	0.8229E 01	0.1622E 00	0.3405E-01	0.1405E 02	37
9	0.3944E 00	0.6406E 00	0.5210E 02	0.1231E 01	0.1323E 02	0.1591E 01	0.5094E 01	0.6250E-01	0.2813E 00	0.3964E 01	32
10	0.0000E 00	0.1812E 02	0.4079E 02	0.1416E 02	0.4000E 00	0.4977E 01	0.1645E 01	0.1429E 00	0.2857E 00	0.4657E 00	7
TOTAL	0.1097E 01	0.1302E 01	0.3938E 02	0.3781E 01	0.8225E 01	0.1734E 01	0.9600E 01	0.1109E 00	0.2074E 00	0.3657E 01	487

GROUP	VARIABLES										SIZE
	A02	A03	A04	A05	A06	A07	W01	W02	W03	W04	
1	0.4026E 02	0.2708E 02	0.2519E 02	0.1050E 02	0.35647E 01	0.1726E 01	0.2718E 01	0.9232E 02	0.1481E 02	0.6825E 01	126
2	0.4235E 02	0.3804E 02	0.1697E 00	0.1600E 02	0.2143E 01	0.625E 00	0.1169E 00	0.9167E 01	0.9629E 01	0.2514E 02	72
3	0.3502E 02	0.3373E 02	0.9313E 00	0.1967E 02	0.1008E 01	0.1377E 01	0.2615E 01	0.5644E 02	0.3333E 01	0.2637E 02	85
4	0.3035E 02	0.4643E 02	0.1824E 01	0.8249E 01	0.2154E 01	0.5878E 00	0.3474E 01	0.8798E 02	0.1234E 02	0.8802E 01	32
5	0.8917E 01	0.9383E 01	0.9637E 01	0.1630E 02	0.7366E 01	0.6134E 00	0.1336E 01	0.6772E 01	0.3653E 01	0.1530E 02	29
6	0.1198E 02	0.9269E 01	0.1410E 02	0.5662E 01	0.9299E 01	0.5571E 00	0.3816E 01	0.8557E 02	0.3274E 01	0.8631E 01	56
7	0.0000E 00	0.0000E 00	0.9091E 01	0.9091E 01	0.0000E 00	0.3455E-01	0.2771E 02	0.7677E 02	0.1015E 02	0.1682E 02	11
8	0.1388E 02	0.1116E 02	0.0000E 00	0.1262E 02	0.2346E 01	0.7395E 00	0.4074E 01	0.8325E 02	0.1802E 01	0.1758E 01	37
9	0.3315E 02	0.1753E 02	0.1049E 01	0.1151E 02	0.4673E 01	0.1264E 01	0.3520E 01	0.8531E 02	0.5469E 01	0.7552E 01	32
10	0.1744E 01	0.2939E 01	0.1557E 01	0.9157E 00	0.3129E 02	0.2239E 02	0.1230E 02	0.8482E 02	0.1667E 02	0.1429E 02	7
TOTAL	0.2994E 02	0.2523E 02	0.2840E 01	0.1392E 02	0.3671E 01	0.1301E 01	0.3423E 01	0.8518E 02	0.8207E 01	0.1378E 02	487

CENTROIDS OF 10 CLUSTER CLASSES : SAMPLE A - STANDARDISED COMPONENT SCORES







CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES															SIZE							
	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05	L06	L07	L08	L09	L10		L11	L12	L13	L14	A01		
1	0.6727E	04	0.6340E	04	0.1440E	02	0.4099E	01	0.5000E	01	0.3683E	02	0.2519E	02	0.4393E	01	0.0000E	00	0.0000E	00	0.6188E	01	14
2	0.4249E	04	0.3649E	04	0.3352E	02	0.2817E	01	0.4600E	01	0.3957E	02	0.2548E	01	0.2726E	00	0.6200E	-01	0.9428E	01	0.9428E	01	50
3	0.1333E	04	0.1268E	04	0.1516E	02	0.1481E	01	0.2745E	01	0.3409E	02	0.1221E	02	0.3546E	00	0.2857E	00	0.7669E	01	0.7669E	01	68
4	0.1385E	04	0.1307E	04	0.1746E	02	0.1935E	01	0.2684E	01	0.2648E	02	0.8290E	01	0.8066E	00	0.1329E	01	0.7244E	01	0.7244E	01	76
5	0.2422E	03	0.2251E	03	0.2090E	00	0.1331E	01	0.3050E	01	0.2326E	02	0.1966E	02	0.1183E	01	0.1248E	02	0.1701E	02	0.1701E	02	20
6	0.1437E	04	0.1078E	04	0.6215E	01	0.2352E	01	0.1800E	01	0.3817E	02	0.3070E	01	0.0000E	00	0.0000E	00	0.3493E	02	0.3493E	02	25
7	0.1682E	04	0.1421E	04	0.1264E	02	0.2149E	01	0.2789E	01	0.3532E	02	0.6003E	01	0.5596E	-01	0.7982E	-01	0.1557E	02	0.1557E	02	57
8	0.4803E	04	0.4018E	04	0.1056E	02	0.2321E	01	0.2344E	01	0.1691E	02	0.4407E	01	0.2727E	01	0.4909E	-01	0.1210E	02	0.1210E	02	22
9	0.5741E	03	0.4807E	03	0.2791E	01	0.8847E	00	0.3500E	00	0.1210E	02	0.8529E	01	0.0000E	00	0.4000E	-02	0.2125E	01	0.2125E	01	40
10	0.1217E	03	0.9610E	02	0.6100E	-01	0.2484E	01	0.1500E	01	0.0000E	00	0.0000E	00	0.0000E	00	0.7812E	02	0.2867E	01	0.2867E	01	10
11	0.6152E	03	0.5025E	03	0.6000E	00	0.1434E	01	0.1200E	01	0.3375E	02	0.6304E	01	0.0000E	00	0.0000E	00	0.4081E	01	0.4081E	01	10
12	0.3634E	03	0.5426E	03	0.3256E	01	0.9343E	00	0.1378E	00	0.1882E	02	0.5086E	01	0.0000E	00	0.5676E	-01	0.3164E	01	0.3164E	01	37
13	0.8434E	03	0.7619E	03	0.7295E	01	0.1291E	01	0.1567E	01	0.1823E	02	0.6350E	01	0.0000E	00	0.8333E	-01	0.6900E	01	0.6900E	01	30
14	0.1649E	04	0.1541E	04	0.2128E	02	0.1314E	01	0.1476E	01	0.2505E	00	0.2238E	-01	0.0000E	00	0.0000E	00	0.2305E	00	0.2305E	00	21
15	0.7687E	03	0.6747E	03	0.9310E	02	0.1246E	01	0.1000E	01	0.1841E	01	0.3850E	01	0.0000E	00	0.8929E	01	0.6303E	01	0.6303E	01	7
TOTAL	0.1754E	04	0.1551E	04	0.1475E	02	0.1826E	01	0.2435E	01	0.2610E	02	0.7848E	01	0.3976E	01	0.2520E	01	0.9352E	01	0.9352E	01	487

GROUP	VARIABLES															SIZE							
	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01	L14	L13	L12	L11	L10		L09	L08	L07	L06			
1	0.1514E	01	0.3343E	00	0.5366E	01	0.6383E	01	0.1380E	02	0.0000E	00	0.6321E	01	0.7143E	-01	0.2857E	00	0.3746E	01	0.3746E	01	14
2	0.4290E	00	0.2228E	00	0.4426E	02	0.0000E	00	0.2098E	00	0.2682E	00	0.1194E	02	0.0000E	00	0.1000E	00	0.1104E	01	0.1104E	01	50
3	0.8744E	00	0.5841E	00	0.3040E	02	0.8365E	00	0.6691E	01	0.8475E	00	0.4240E	01	0.4412E	-01	0.3088E	00	0.1372E	01	0.1372E	01	68
4	0.0000E	00	0.4454E	00	0.5281E	02	0.1368E	01	0.7286E	00	0.3538E	00	0.4580E	01	0.5263E	-01	0.4868E	00	0.5688E	01	0.5688E	01	76
5	0.3218E	01	0.1802E	01	0.6273E	01	0.3460E	01	0.1155E	02	0.1101E	01	0.9622E	01	0.0000E	00	0.1500E	00	0.0000E	00	0.0000E	00	20
6	0.1669E	01	0.8280E	00	0.1050E	02	0.3092E	01	0.2334E	01	0.2348E	01	0.2086E	02	0.8400E	00	0.4400E	00	0.1619E	01	0.1619E	01	25
7	0.6211E	00	0.5360E	00	0.3000E	00	0.2660E	01	0.5154E	01	0.2715E	01	0.9846E	01	0.1053E	00	0.3263E	-01	0.2233E	01	0.2233E	01	57
8	0.1995E	01	0.6450E	00	0.4208E	02	0.3614E	00	0.2115E	02	0.1961E	01	0.1994E	02	0.1818E	00	0.0000E	00	0.1539E	00	0.1539E	00	22
9	0.4034E	01	0.5653E	01	0.3065E	01	0.8227E	01	0.2838E	02	0.5238E	01	0.1515E	02	0.1000E	00	0.5000E	-01	0.6208E	01	0.6208E	01	40
10	0.6310E	00	0.0000E	00	0.6211E	01	0.6250E	00	0.1156E	02	0.5966E	01	0.2065E	02	0.1000E	00	0.0000E	00	0.0000E	00	0.0000E	00	10
11	0.5342E	01	0.6910E	00	0.5438E	01	0.1201E	02	0.5228E	02	0.5997E	01	0.1123E	02	0.5000E	00	0.0000E	00	0.0000E	02	0.0000E	02	10
12	0.7559E	00	0.1692E	01	0.3921E	02	0.1868E	02	0.1754E	02	0.1293E	01	0.7120E	01	0.8108E	-01	0.8108E	-01	0.9697E	00	0.9697E	00	37
13	0.4207E	00	0.6623E	00	0.5557E	02	0.1313E	02	0.1077E	02	0.1697E	01	0.5226E	01	0.3335E	-01	0.5000E	00	0.4229E	01	0.4229E	01	30
14	0.0000E	00	0.2100E	-01	0.9946E	02	0.0000E	00	0.0000E	00	0.0000E	00	0.8540E	01	0.0000E	00	0.4762E	-01	0.2175E	01	0.2175E	01	21
15	0.1000E	00	0.1012E	02	0.4079E	02	0.1416E	02	0.0000E	00	0.4977E	01	0.1645E	02	0.1429E	00	0.2857E	00	0.4657E	00	0.4657E	00	7
TOTAL	0.1097E	01	0.1302E	01	0.3938E	02	0.3781E	01	0.6225E	01	0.1734E	01	0.9600E	01	0.1109E	01	0.2074E	00	0.3657E	01	0.3657E	01	487

CENTROIDS OF 15 CLUSTER CLASSES : SAMPLE A - STANDARDISED COMPONENT SCORES



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES							SIZE			
	A02	A03	A04	A05	A06	A07	A07				
1	0.8001E	01 0.1645E	02 0.7143E	01 0.1207E	02 0.2504E	01 0.2157E	00 0.2239E	01 0.3725E	02 0.4830E	01 0.2890E	02 14
2	0.4220E	02 0.3907E	02 0.1772E	00 0.1511E	02 0.2262E	01 0.9610E	00 0.9470E	00 0.9133E	02 0.9067E	01 0.2773E	02 50
3	0.3642E	02 0.3470E	02 0.5054E	00 0.1937E	02 0.9165E	00 0.1285E	01 0.2752E	01 0.9653E	02 0.2941E	01 0.2561E	02 68
4	0.4465E	02 0.2858E	02 0.2401E	00 0.1337E	02 0.4290E	01 0.1432E	01 0.2539E	01 0.9547E	02 0.1701E	02 0.6009E	01 76
5	0.0000E	00 0.6253E	01 0.6250E	01 0.1697E	02 0.5255E	00 0.1315E	00 0.5620E	01 0.9224E	02 0.1108E	02 0.6750E	01 20
6	0.3273E	02 0.4205E	02 0.2335E	01 0.6990E	01 0.2277E	01 0.5904E	00 0.3613E	01 0.9242E	02 0.1580E	02 0.9266E	01 25
7	0.3994E	02 0.5923E	02 0.1438E	01 0.1003E	02 0.1815E	01 0.8593E	00 0.1847E	01 0.9164E	02 0.1020E	02 0.1284E	02 57
8	0.1134E	02 0.8100E	01 0.8158E	01 0.1695E	02 0.9645E	01 0.7723E	00 0.9286E	00 0.6627E	00 0.2651E	01 0.1318E	02 22
9	0.3536E	01 0.6831E	01 0.1536E	02 0.1145E	02 0.1411E	02 0.6935E	00 0.6604E	01 0.8407E	02 0.4416E	01 0.5000E	02 40
10	0.0000E	00 0.0000E	00 0.1000E	02 0.1000E	02 0.0000E	00 0.3800E	01 0.3006E	02 0.7687E	02 0.9166E	01 0.1250E	02 10
11	0.6667E	01 0.5335E	01 0.0000E	00 0.0000E	00 0.1470E	00 0.6045E	01 0.5457E	02 0.6667E	01 0.3600E	00 0.0000E	01 10
12	0.1915E	02 0.1904E	02 0.5022E	01 0.1642E	02 0.3118E	01 0.9632E	00 0.5535E	01 0.9131E	02 0.0000E	00 0.3604E	01 37
13	0.3536E	02 0.1870E	02 0.1119E	01 0.1228E	02 0.4944E	01 0.1349E	01 0.3419E	01 0.8767E	02 0.5833E	01 0.8056E	01 30
14	0.6213E	02 0.1861E	02 0.1204E	01 0.5366E	01 0.9933E	00 0.1927E	01 0.1668E	01 0.9053E	02 0.4761E	01 0.2540E	02 21
15	0.1746E	01 0.2939E	01 0.1557E	00 0.9157E	02 0.3129E	01 0.2239E	02 0.1230E	02 0.8482E	02 0.1667E	02 0.1429E	02 7
TOTAL	0.2994E	02 0.2523E	02 0.2640E	01 0.1392E	02 0.3671E	01 0.1301E	01 0.3423E	01 0.8518E	02 0.8207E	01 0.1378E	02 487

GROUP	VARIABLES							SIZE			
	M05	M06	M07	M01	M02	M03	M03				
1	0.2806E	02 0.3719E	02 0.1021E	01 0.1000E	01 0.0000E	00 0.5000E	00 0.8571E	00 0.7143E	01 0.0000E	00 0.7143E	01 14
2	0.1870E	02 0.2617E	02 0.1933E	02 0.1000E	01 0.4000E	01 0.7800E	00 0.6200E	00 0.9200E	00 0.0000E	00 0.0000E	00 50
3	0.6324E	02 0.1838E	01 0.6573E	01 0.6029E	00 0.2911E	01 0.1029E	00 0.8676E	00 0.2647E	00 0.0000E	00 0.0000E	00 68
4	0.5088E	01 0.6541E	02 0.6485E	01 0.4079E	02 0.2682E	01 0.0000E	00 0.8816E	00 0.2895E	00 0.1189E	00 0.0000E	00 76
5	0.2300E	02 0.6217E	02 0.0000E	00 0.2500E	00 0.7500E	00 0.5000E	01 0.9000E	00 0.0000E	00 0.3830E	00 0.0000E	00 20
6	0.3500E	02 0.3560E	02 0.3533E	01 0.2400E	00 0.2800E	00 0.4000E	01 0.7200E	00 0.4000E	01 0.0000E	00 0.0000E	00 25
7	0.8977E	01 0.6456E	02 0.3421E	01 0.6842E	00 0.1404E	00 0.2105E	00 0.7895E	00 0.2982E	00 0.0000E	00 0.0000E	00 57
8	0.1872E	02 0.3914E	02 0.3260E	01 0.6364E	00 0.1818E	00 0.6091E	01 0.5455E	00 0.1364E	00 0.0000E	00 0.9091E	00 22
9	0.9167E	01 0.7600E	02 0.5417E	01 0.1000E	00 0.5000E	01 0.0000E	00 0.1500E	00 0.0000E	00 0.0000E	00 0.7500E	01 40
10	0.2300E	02 0.3417E	02 0.1917E	02 0.1000E	00 0.8000E	00 0.0000E	00 0.2000E	00 0.0000E	00 0.2397E	02 0.2000E	00 10
11	0.1667E	02 0.2667E	02 0.3000E	02 0.1000E	00 0.0000E	00 0.1000E	00 0.6000E	00 0.0000E	00 0.0000E	00 0.1000E	01 10
12	0.8064E	01 0.9549E	01 0.7788E	02 0.1351E	00 0.2482E	00 0.0000E	00 0.6757E	00 0.5405E	01 0.9459E	02 0.2432E	00 37
13	0.1335E	02 0.4556E	02 0.2222E	02 0.2667E	00 0.6667E	01 0.3333E	01 0.6667E	00 0.1667E	00 0.0000E	00 0.6667E	01 30
14	0.3016E	02 0.3016E	02 0.9324E	01 0.3333E	00 0.0000E	00 0.0000E	00 0.5238E	00 0.4762E	00 0.0000E	00 0.0000E	00 21
15	0.1429E	02 0.5476E	02 0.0000E	00 0.2857E	00 0.0000E	00 0.0000E	00 0.4286E	00 0.1429E	00 0.1786E	01 0.0000E	00 7
TOTAL	0.2184E	02 0.4104E	02 0.1370E	02 0.4661E	00 0.1243E	00 0.1458E	00 0.6879E	00 0.2587E	00 0.5529E	00 0.5955E	01 487



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES															SIZE
	H01	H02	H03	H04	H05	H06	G01	G02	G03							
1	0.1229E 01	0.1000E 01	0.2500E 01	0.1000E 01	0.0000E 00	0.4821E 02	0.7143E-01	0.5208E 02	0.4792E 02	0.0000E 00	14					
2	0.1513E 01	0.1000E 01	0.1220E 01	0.9600E 01	0.4000E-01	0.5206E 02	0.4000E-01	0.7316E 02	0.2572E 02	0.1113E 01	50					
3	0.5345E 01	0.1000E 01	0.1221E 01	0.1000E 01	0.0000E 00	0.3778E 02	0.4118E 00	0.4099E 02	0.5886E 02	0.1515E 00	68					
4	0.5042E 01	0.1000E 01	0.1289E 01	0.1000E 01	0.0000E 00	0.5543E 02	0.7895E-01	0.3943E 02	0.5920E 02	0.1370E 01	76					
5	0.1394E 02	0.1000E 01	0.1250E 01	0.9500E 01	0.5000E-01	0.5180E 02	0.3500E 00	0.6008E 02	0.3992E 02	0.0000E 00	20					
6	0.2374E 01	0.1000E 01	0.1000E 01	0.1000E 01	0.0000E 00	0.5020E 02	0.2000E 00	0.4110E 02	0.1090E 02	0.4800E 02	25					
7	0.2638E 01	0.1000E 01	0.1018E 01	0.1000E 01	0.0000E 00	0.5598E 02	0.1579E 00	0.8035E 02	0.1965E 02	0.0000E 00	57					
8	0.1462E 01	0.4545E-01	0.1500E 01	0.0000E 00	0.4545E-01	0.5232E 02	0.0000E 00	0.9569E 02	0.4307E 01	0.0000E 00	22					
9	0.1789E 01	0.1000E 01	0.1175E 01	0.1000E 01	0.0000E 00	0.5433E 02	0.8000E 00	0.8647E 02	0.1353E 02	0.0000E 00	40					
10	0.1271E 02	0.1000E 01	0.1700E 01	0.5000E 01	0.5470E 02	0.2000E 00	0.2000E 00	0.4660E 02	0.5340E 02	0.0000E 00	10					
11	0.1821E 01	0.8000E 00	0.1200E 01	0.7000E 00	0.1000E 00	0.5680E 02	0.2000E 00	0.2401E 02	0.1599E 02	0.6000E 02	10					
12	0.6714E 01	0.1000E 01	0.1243E 01	0.1000E 01	0.0000E 00	0.6946E 02	0.2432E 00	0.8176E 02	0.1463E 02	0.3609E 01	37					
13	0.5169E 01	0.9667E 00	0.1000E 01	0.0000E 01	0.9667E 00	0.5723E 02	0.3333E-01	0.7526E 02	0.2449E 02	0.2337E 00	30					
14	0.1306E 01	0.1000E 01	0.1476E 01	0.1000E 01	0.0000E 00	0.4686E 02	0.3810E 00	0.2700E 02	0.7300E 02	0.0000E 00	21					
15	0.5323E 01	0.1000E 01	0.1000E 01	0.7143E 00	0.2857E 00	0.4771E 02	0.7143E 00	0.8571E 02	0.1429E 02	0.0000E 00	7					
TOTAL	0.3662E 01	0.9507E 00	0.1279E 01	0.8747E 00	0.7508E-01	0.5254E 02	0.2402E 00	0.6099E 02	0.3468E 02	0.4335E 01	487					

GROUP	VARIABLES						SIZE
	G04	G05	G06				
1	0.7857E 00	0.2643E 01	0.5714E 00	14			
2	0.1800E 00	0.3020E 01	0.2000E-01	50			
3	0.1324E 00	0.1779E 01	0.7553E-01	68			
4	0.5816E 00	0.1592E 01	0.1516E 00	76			
5	0.5000E 00	0.1500E 01	0.5000E-01	20			
6	0.8000E-01	0.4800E 00	0.8000E-01	25			
7	0.0000E 00	0.1386E 01	0.1754E-01	57			
8	0.818E 00	0.1136E 01	0.5091E-01	22			
9	0.7500E-01	0.1000E 00	0.5000E-01	40			
10	0.6000E 00	0.1400E 01	0.0000E 00	10			
11	0.2000E 00	0.8000E 00	0.0000E 00	37			
12	0.1592E 00	0.1405E 01	0.0000E 00	30			
13	0.1000E 00	0.1100E 01	0.6067E-01	21			
14	0.6190E 00	0.1381E 01	0.0000E 00	7			
15	0.5714E 00	0.1286E 01	0.2857E 00	487			
TOTAL	0.2218E 00	0.1489E 01	0.7592E-01				



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES																				SIZE
	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05											
1	0.6507E 04	0.6025E 04	0.1738E 02	0.3447E 01	0.6000E 01	0.4412E 02	0.3206E 02	0.4905E 01	0.0000E 00	0.6361E 01	11										
2	0.4133E 04	0.3546E 04	0.3700E 02	0.2833E 01	0.4622E 01	0.4075E 02	0.5427E 01	0.1511E 00	0.4333E-01	0.9734E 01	45										
3	0.5016E 03	0.4071E 03	0.2584E 01	0.8565E 00	0.6522E 00	0.1016E 02	0.3543E 00	0.0000E 00	0.0000E 00	0.3434E 01	23										
4	0.3988E 03	0.3834E 03	0.4064E 01	0.1097E 01	0.1500E 01	0.2898E 02	0.1256E 02	0.7983E 00	0.1259E 01	0.1145E 02	36										
5	0.1878E 03	0.1731E 03	0.4317E 00	0.1237E 01	0.3617E 01	0.2591E 02	0.1718E 02	0.1976E 01	0.2391E 01	0.1838E 02	12										
6	0.1437E 04	0.1078E 04	0.6215E 01	0.2352E 01	0.1800E 01	0.3817E 02	0.3070E 01	0.0000E 00	0.0000E 00	0.3493E 02	25										
7	0.2207E 04	0.1911E 04	0.1433E 02	0.2410E 01	0.3339E 01	0.3788E 02	0.6222E 01	0.1483E 00	0.1896E 00	0.1600E 02	46										
8	0.4803E 04	0.4018E 04	0.1058E 02	0.2321E 01	0.2344E 01	0.1691E 02	0.4407E 01	0.2727E 00	0.4909E-01	0.1210E 02	22										
9	0.1302E 04	0.1137E 04	0.2308E 00	0.2132E 01	0.3077E 00	0.5692E 01	0.1076E 01	0.0000E 00	0.0000E 00	0.0000E 00	13										
10	0.1111E 03	0.8400E 02	0.7500E-01	0.2497E 01	0.1500E 01	0.0000E 00	0.0000E 00	0.0000E 00	0.7459E 02	0.3584E 01	8										
11	0.1520E 04	0.1431E 04	0.1778E 02	0.1611E 01	0.3161E 01	0.3744E 02	0.1463E 02	0.4305E 00	0.370E 00	0.8437E 01	56										
12	0.6155E 03	0.5025E 03	0.6000E 00	0.1434E 01	0.1200E 01	0.3375E 02	0.6304E 01	0.0000E 00	0.0000E 00	0.4081E 01	10										
13	0.4034E 03	0.3814E 03	0.1521E 01	0.2171E 01	0.2375E 01	0.7198E 01	0.2227E 02	0.0000E 00	0.5159E 02	0.2456E 01	8										
14	0.4835E 03	0.4655E 03	0.6035E 01	0.1132E 01	0.1786E 01	0.2617E 02	0.6138E 01	0.0000E 00	0.0000E 00	0.4615E 01	28										
15	0.8630E 03	0.7637E 03	0.7547E 01	0.1330E 01	0.1691E 01	0.1886E 02	0.6569E 01	0.0000E 00	0.8621E-01	0.6828E 01	29										
16	0.1874E 04	0.1739E 04	0.2430E 02	0.1469E 01	0.1567E 01	0.2922E 00	0.2611E-01	0.0000E 00	0.0000E 00	0.2922E 00	18										
17	0.1315E 04	0.1101E 04	0.2408E 01	0.8453E 00	0.3684E 00	0.1349E 02	0.7718E 01	0.3984E 00	0.8421E-02	0.2666E 01	19										
18	0.1735E 04	0.1673E 04	0.2204E 02	0.2203E 01	0.3017E 01	0.2509E 02	0.8018E 01	0.6085E 00	0.8293E 00	0.7962E 01	59										
19	0.7687E 03	0.6747E 03	0.9310E 02	0.1246E 01	0.1000E 01	0.1841E 01	0.3850E 01	0.0000E 00	0.8929E 01	0.6303E 01	7										
20	0.2205E 03	0.2213E 03	0.7042E 00	0.6542E 00	0.1083E 01	0.1128E 02	0.1222E 01	0.0000E 00	0.0000E 00	0.0000E 00	12										
TOTAL	0.1754E 04	0.1531E 04	0.1475E 02	0.1826E 01	0.2435E 01	0.2610E 02	0.7848E 01	0.3976E 01	0.2520E 01	0.9352E 01	487										

GROUP	VARIABLES																				SIZE
	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01											
1	0.0000E 00	0.1627E 00	0.4627E 01	0.0000E 00	0.7761E 00	0.0000E 00	0.7140E 01	0.9091E-01	0.3636E 00	0.4768E 01	11										
2	0.4767E 00	0.2138E 00	0.4297E 02	0.0000E 00	0.2347E 00	0.2933E 01	0.1231E 02	0.0000E 00	0.8889E-01	0.3933E 00	45										
3	0.0000E 00	0.2132E 01	0.4222E 02	0.0000E 00	0.3870E 00	0.1957E 01	0.9368E 01	0.1304E 00	0.4348E-01	0.2929E 01	23										
4	0.7309E 00	0.1532E 01	0.3059E 02	0.3539E 01	0.8761E 01	0.7844E 00	0.3178E 01	0.1111E 00	0.1389E 00	0.9864E 01	36										
5	0.5363E 01	0.1027E 01	0.3778E 01	0.5067E 01	0.1893E 02	0.3192E 00	0.1104E 02	0.0000E 00	0.1667E 00	0.0000E 00	12										
6	0.1069E 01	0.8230E 00	0.1050E 02	0.3098E 01	0.2534E 01	0.2548E 01	0.2086E 02	0.8400E 00	0.4600E 00	0.1619E 01	25										
7	0.7052E 00	0.2974E 00	0.3436E 02	0.1144E 01	0.3110E 01	0.2792E 01	0.1078E 02	0.8696E-01	0.6522E-01	0.2149E 01	46										
8	0.1995E 01	0.6630E 00	0.4208E 02	0.3614E 00	0.2115E 02	0.1991E 02	0.1818E 00	0.0000E 00	0.0000E 00	0.1559E 00	22										
9	0.0000E 00	0.1003E 02	0.1036E 02	0.5420E 02	0.3314E 02	0.1298E 02	0.2179E 02	0.1538E 00	0.7692E-01	0.1709E 01	13										
10	0.7753E 00	0.0000E 00	0.7764E 01	0.7813E 00	0.1250E 02	0.7458E 01	0.2136E 02	0.1250E 00	0.0000E 00	0.0000E 00	8										
11	0.1082E 01	0.4927E 00	0.3538E 02	0.7482E 00	0.5289E 00	0.2252E 00	0.4013E 01	0.1786E-01	0.3571E 00	0.1599E 01	56										
12	0.5342E 01	0.6910E 00	0.5538E 01	0.1231E 02	0.3228E 02	0.5997E 01	0.1123E 02	0.5000E 00	0.0000E 00	0.5000E 02	10										
13	0.0000E 00	0.9252E 00	0.1538E 02	0.0000E 00	0.2184E 01	0.2272E 01	0.1070E 02	0.0000E 00	0.1250E 00	0.0000E 00	8										
14	0.1746E 00	0.1575E 01	0.5722E 02	0.9764E 00	0.3104E 01	0.5807E 00	0.5336E 01	0.3571E-01	0.2500E 00	0.1846E 01	28										
15	0.4352E 00	0.6822E 00	0.5748E 02	0.1358E 01	0.7688E 01	0.1755E 01	0.5406E 01	0.3448E-01	0.3103E 00	0.4374E 01	29										
16	0.0000E 00	0.2333E-01	0.9937E 02	0.0000E 00	0.0000E 00	0.0000E 00	0.1151E 01	0.0000E 00	0.5556E-01	0.2538E 01	18										
17	0.8331E 01	0.2789E 01	0.4087E 02	0.1533E 02	0.1612E 02	0.3696E 01	0.1685E 02	0.0000E 00	0.0000E 00	0.7031E 01	19										
18	0.0000E 00	0.3080E 00	0.5604E 02	0.6615E 00	0.4741E 00	0.4686E 00	0.5168E 01	0.5085E-01	0.5085E 00	0.2926E 01	59										
19	0.0000E 00	0.1812E 02	0.4679E 02	0.1416E 02	0.0000E 00	0.4977E 01	0.1645E 02	0.1429E 00	0.2857E 00	0.4657E 00	7										
20	0.1923E 01	0.1765E 01	0.1156E 02	0.5578E 02	0.1667E 02	0.0000E 00	0.7237E 01	0.1667E 00	0.0000E 00	0.0000E 00	12										
TOTAL	0.1097E 01	0.1302E 01	0.3938E 02	0.3781E 01	0.8225E 01	0.1734E 01	0.9600E 01	0.1109E 01	0.2074E 00	0.3657E 01	487										

CENTROIDS OF 20 CLUSTER CLASSES : SAMPLE A - STANDARDISED COMPONENT SCORES



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES																				SIZE
	A02	A03	A04	A05	A06	A07	W01	W02	W03	W04	W05	W06	W07	W08	W09	W10	W11	W12	W13	W14	
1	0.1018E	02	0.2094E	02	0.0000E	00	0.1536E	02	0.3301E	01	0.2673E	00	0.6791E	00	0.3717E	02	0.6147E	01	0.3548E	02	11
2	0.4294E	02	0.3875E	02	0.1969E	00	0.1520E	02	0.2514E	01	0.9904E	00	0.9556E	00	0.9042E	02	0.8592E	01	0.2915E	02	45
3	0.1576E	02	0.1464E	02	0.8602E	01	0.5054E	01	0.4989E	01	0.6813E	00	0.2881E	01	0.8908E	02	0.0000E	00	0.2754E	02	23
4	0.2028E	02	0.2376E	02	0.1768E	01	0.1862E	02	0.3484E	01	0.1027E	01	0.4119E	01	0.9330E	02	0.3750E	01	0.6944E	00	36
5	0.0000E	00	0.1042E	02	0.2083E	01	0.2829E	02	0.8758E	00	0.2050E	00	0.6241E	01	0.8998E	02	0.6250E	01	0.6250E	01	12
6	0.3275E	02	0.4205E	02	0.2535E	01	0.6990E	01	0.2277E	01	0.5904E	00	0.3613E	01	0.9242E	02	0.1580E	02	0.9266E	01	25
7	0.3905E	02	0.4355E	02	0.1470E	00	0.1126E	02	0.1845E	01	0.8372E	00	0.1621E	01	0.9040E	02	0.1083E	02	0.1862E	02	46
8	0.1154E	02	0.8158E	01	0.8158E	01	0.1695E	02	0.9645E	01	0.7723E	00	0.9286E	00	0.6627E	00	0.2651E	01	0.1518E	02	22
9	0.0000E	00	0.5128E	01	0.8546E	00	0.0000E	00	0.7692E	01	0.8462E	01	0.5855E	01	0.6203E	02	0.2564E	01	0.1099E	01	13
10	0.0000E	00	0.0000E	00	0.1250E	02	0.0000E	02	0.0000E	00	0.4750E	01	0.3306E	02	0.7338E	02	0.7291E	01	0.1563E	02	8
11	0.3693E	02	0.3674E	02	0.1673E	00	0.2167E	02	0.1133E	01	0.1419E	01	0.2794E	01	0.9765E	02	0.3571E	01	0.2396E	02	56
12	0.6667E	01	0.3333E	01	0.0000E	00	0.0000E	00	0.0000E	00	0.1470E	00	0.4045E	01	0.5457E	02	0.6667E	01	0.0000E	00	10
13	0.9461E	01	0.2129E	01	0.0000E	00	0.9100E	00	0.0000E	00	0.1863E	00	0.8081E	01	0.9340E	02	0.3083E	02	0.7500E	01	8
14	0.3448E	02	0.2823E	02	0.7429E	01	0.6351E	01	0.4014E	01	0.1114E	01	0.2977E	01	0.9699E	02	0.0000E	00	0.5357E	01	28
15	0.3658E	02	0.1934E	02	0.1157E	01	0.1270E	02	0.5156E	01	0.1394E	01	0.3494E	01	0.8802E	02	0.6034E	01	0.8333E	01	29
16	0.7248E	02	0.1832E	02	0.5856E	00	0.5734E	01	0.3400E	00	0.2099E	01	0.1734E	01	0.8895E	02	0.5555E	01	0.2407E	02	18
17	0.0000E	00	0.0000E	00	0.3433E	02	0.6880E	01	0.2018E	02	0.5984E	00	0.3393E	01	0.8968E	02	0.3508E	01	0.2632E	01	19
18	0.5124E	02	0.3216E	02	0.3093E	00	0.1022E	02	0.3138E	01	0.1466E	01	0.2038E	01	0.9552E	02	0.2233E	02	0.5622E	01	59
19	0.1744E	01	0.2939E	01	0.1557E	00	0.9157E	02	0.3129E	01	0.2239E	02	0.1230E	02	0.8482E	02	0.1667E	02	0.1429E	02	7
20	0.0000E	00	0.0000E	00	0.0000E	00	0.3233E	02	0.9983E	00	0.1058E	01	0.4406E	01	0.8373E	02	0.0000E	00	0.4167E	01	12
TOTAL	0.2994E	02	0.2523E	02	0.2840E	01	0.1392E	02	0.3671E	01	0.1301E	01	0.3423E	01	0.8518E	02	0.8207E	01	0.1378E	02	487

GROUP	VARIABLES																				SIZE
	W05	W06	W07	W08	W09	W10	W11	W12	W13	W14	W15	W16	W17	W18	W19	W20	W21	W22	W23	W24	
1	0.2532E	02	0.3305E	02	0.0000E	00	0.1000E	01	0.0000E	00	0.6364E	00	0.1000E	01	0.9091E	01	0.0000E	00	0.0000E	00	11
2	0.1818E	02	0.2461E	02	0.1926E	02	0.1000E	01	0.4444E	01	0.8222E	00	0.5778E	00	0.9333E	00	0.0000E	00	0.0000E	00	45
3	0.6377E	02	0.6522E	01	0.2174E	01	0.2174E	01	0.1304E	00	0.0000E	00	0.2609E	00	0.0000E	00	0.0000E	00	0.4348E	01	23
4	0.2315E	01	0.9185E	02	0.1389E	01	0.1944E	00	0.2778E	01	0.0000E	00	0.7500E	00	0.0000E	00	0.6167E	01	0.0000E	00	36
5	0.3335E	02	0.5417E	02	0.0000E	00	0.4167E	00	0.9167E	00	0.8333E	01	0.9167E	00	0.0000E	00	0.6383E	00	0.0000E	00	12
6	0.3600E	02	0.3560E	02	0.3233E	01	0.2400E	00	0.2800E	01	0.4000E	01	0.7200E	00	0.4000E	01	0.0000E	00	0.0000E	00	25
7	0.1221E	02	0.5337E	02	0.4964E	01	0.8696E	00	0.1739E	00	0.2826E	00	0.8043E	00	0.3913E	00	0.7609E	02	0.0000E	00	46
8	0.1872E	02	0.3916E	02	0.3560E	01	0.6364E	00	0.1818E	00	0.9091E	01	0.5455E	00	0.1364E	00	0.0000E	00	0.9091E	01	22
9	0.1099E	01	0.7875E	02	0.1648E	02	0.2308E	00	0.0000E	00	0.0000E	00	0.7692E	01	0.0000E	00	0.0000E	00	0.3077E	00	13
10	0.3125E	02	0.3229E	02	0.1554E	02	0.0000E	00	0.7500E	00	0.0000E	00	0.1250E	00	0.0000E	00	0.2934E	02	0.0000E	00	8
11	0.6250E	02	0.2232E	01	0.7038E	01	0.6786E	00	0.1786E	01	0.1250E	00	0.9466E	00	0.3214E	00	0.0000E	00	0.0000E	00	56
12	0.1667E	02	0.2667E	02	0.3000E	02	0.1000E	00	0.4000E	00	0.1000E	00	0.6000E	00	0.0000E	00	0.0000E	00	0.1000E	01	10
13	0.0000E	00	0.5125E	02	0.1042E	02	0.0000E	00	0.7500E	00	0.0000E	00	0.6250E	00	0.1250E	00	0.1452E	01	0.2500E	00	8
14	0.7976E	01	0.6071E	01	0.8059E	02	0.1071E	00	0.7143E	01	0.0000E	00	0.8571E	00	0.1429E	00	0.0000E	00	0.3571E	01	28
15	0.1552E	02	0.4713E	02	0.2459E	02	0.2759E	00	0.6807E	01	0.3448E	01	0.6897E	00	0.1724E	00	0.0000E	00	0.3448E	01	29
16	0.2407E	02	0.3519E	02	0.1111E	02	0.3333E	00	0.0000E	00	0.0000E	00	0.6111E	00	0.5556E	00	0.0000E	00	0.0000E	00	18
17	0.7017E	01	0.8070E	02	0.6141E	01	0.5263E	01	0.1043E	00	0.0000E	00	0.2103E	00	0.0000E	00	0.0000E	00	0.0000E	00	19
18	0.4576E	01	0.6392E	02	0.3551E	01	0.5254E	00	0.1605E	01	0.1695E	01	0.8983E	00	0.3729E	00	0.3390E	02	0.0000E	00	59
19	0.1429E	02	0.5476E	02	0.0000E	00	0.2857E	00	0.0000E	00	0.0000E	00	0.4286E	00	0.1429E	00	0.1786E	01	0.0000E	00	7
20	0.1458E	02	0.2083E	02	0.6042E	02	0.8333E	01	0.4167E	00	0.0000E	00	0.5000E	00	0.0000E	00	0.0000E	00	0.6667E	00	12
TOTAL	0.2184E	02	0.4104E	02	0.1370E	02	0.4661E	00	0.1253E	00	0.1458E	00	0.6879E	00	0.2587E	00	0.5529E	00	0.5955E	01	487

CENTROIDS OF 20 CLUSTER CLASSES : SAMPLE A - STANDARDISED COMPONENT SCORES



CLUSTER CLASSIFICATION - SAMPLE A

GROUP	VARIABLES										SIZE
	H08	H01	H02	H03	H04	H05	H06	G01	G02	G03	
1	0.1246E 01	0.1000E 01	0.2636E 01	0.1000E 01	0.0000E 01	0.4718E 02	0.9091E-01	0.3969E 02	0.6031E 02	0.0000E 00	11
2	0.1527E 01	0.1000E 01	0.1511E 01	0.9556E 00	0.4444E-01	0.5189E 02	0.4444E-01	0.7179E 02	0.2697E 02	0.1236E 01	45
3	0.2626E 01	0.1000E 01	0.1217E 01	0.9565E 00	0.4348E-01	0.4061E 02	0.7824E 02	0.7950E 02	0.2050E 02	0.0000E 00	23
4	0.5241E 01	0.1000E 01	0.1167E 01	0.1000E 01	0.0000E 01	0.5494E 02	0.4167E 02	0.5963E 02	0.4637E 02	0.0000E 00	36
5	0.2266E 02	0.1000E 01	0.1250E 01	0.9167E 00	0.8333E-01	0.4942E 02	0.2500E 00	0.6988E 02	0.5012E 02	0.0000E 00	12
6	0.2374E 01	0.1000E 01	0.1000E 01	0.1000E 01	0.0000E 00	0.5020E 02	0.2000E 00	0.4110E 02	0.1090E 02	0.4800E 02	25
7	0.2363E 01	0.1000E 01	0.1087E 01	0.1000E 01	0.0000E 00	0.5528E 02	0.1522E 02	0.7970E 02	0.2030E 02	0.0000E 00	46
8	0.1462E 01	0.4545E-01	0.1500E 01	0.0000E 00	0.6545E-01	0.5232E 02	0.0000E 00	0.9569E 02	0.4307E 01	0.0000E 00	22
9	0.4192E 00	0.1000E 01	0.1154E 01	0.1000E 01	0.0000E 00	0.5938E 02	0.5385E 00	0.8404E 02	0.5731E 00	0.1538E 02	13
10	0.1334E 02	0.1000E 01	0.1625E 01	0.8750E 00	0.1250E 00	0.5242E 02	0.1250E 00	0.5825E 02	0.4175E 02	0.0000E 00	8
11	0.3268E 01	0.1000E 01	0.1250E 01	0.1000E 01	0.0000E 00	0.371E 02	0.3571E 00	0.3498E 02	0.6484E 02	0.1839E 00	56
12	0.1821E 01	0.8000E 00	0.1200E 01	0.7000E 00	0.1000E 00	0.5680E 02	0.2000E 00	0.2401E 02	0.1599E 02	0.6000E 02	10
13	0.624E 01	0.1000E 01	0.1625E 01	0.1000E 01	0.0000E 00	0.5750E 02	0.3750E 00	0.3376E 02	0.6624E 02	0.0000E 00	8
14	0.5745E 01	0.1000E 01	0.1143E 01	0.1000E 01	0.0000E 00	0.7000E 02	0.7143E-01	0.7144E 02	0.2736E 02	0.1198E 01	28
15	0.5279E 01	0.9625E 00	0.1000E 01	0.0000E 00	0.9655E 00	0.5774E 02	0.0000E 00	0.7441E 02	0.2533E 02	0.2624E 00	29
16	0.1369E 01	0.1000E 01	0.1556E 01	0.1000E 01	0.0000E 00	0.4844E 02	0.2778E 00	0.1484E 02	0.8516E 02	0.0000E 00	18
17	0.214E 01	0.1000E 01	0.1053E 01	0.1000E 01	0.0000E 00	0.5605E 02	0.7895E 02	0.9515E 02	0.4847E 01	0.0000E 00	19
18	0.2475E 01	0.1000E 01	0.1505E 01	0.1000E 01	0.0000E 00	0.5466E 02	0.1695E-01	0.4000E 02	0.5993E 02	0.6966E-01	59
19	0.5523E 01	0.1000E 01	0.1000E 01	0.7143E 00	0.2857E 00	0.4771E 02	0.7143E 00	0.8571E 02	0.1429E 02	0.0000E 00	7
20	0.8113E 01	0.1000E 01	0.1417E 01	0.1000E 01	0.0000E 00	0.6783E 02	0.4167E 00	0.1000E 03	0.0000E 00	0.0000E 00	12
TOTAL	0.3662E 01	0.9507E 00	0.1279E 01	0.8747E 00	0.7508E-01	0.5254E 02	0.2402E 00	0.6099E 02	0.3468E 02	0.4335E 01	487

GROUP	VARIABLES										SIZE
	G04	G05	G06	G07	G08	G09	G10	G11	G12	G13	
1	0.9091E 00	0.3182E 01	0.7273E 00								11
2	0.179E 00	0.3089E 01	0.0000E 00								45
3	0.8696E-01	0.7391E 00	0.4548E-01								23
4	0.1389E 00	0.6667E 00	0.1111E 00								36
5	0.1667E 00	0.1353E 01	0.8333E-01								12
6	0.8000E-01	0.4800E 00	0.8000E-01								25
7	0.0000E 00	0.1650E 01	0.4348E-01								46
8	0.1813E 00	0.1156E 01	0.9091E-01								22
9	0.7694E-01	0.5385E 00	0.0000E 00								13
10	0.6250E 00	0.1750E 01	0.0000E 00								8
11	0.1429E 00	0.1893E 01	0.8929E-01								56
12	0.2000E 00	0.8000E 00	0.0000E 00								10
13	0.7500E 00	0.2000E 01	0.0000E 00								8
14	0.2857E 00	0.1393E 01	0.371E-01								28
15	0.1034E 00	0.1158E 01	0.6897E-01								29
16	0.6667E 00	0.1444E 01	0.0000E 00								18
17	0.5263E-01	0.1053E 00	0.5263E-01								19
18	0.4068E 00	0.1780E 01	0.8475E-01								59
19	0.5714E 00	0.1286E 01	0.2857E 00								7
20	0.8333E-01	0.1417E 01	0.0000E 00								12
TOTAL	0.2218E 00	0.1489E 01	0.7392E-01								487

CENTROIDS OF 20 CLUSTER CLASSES : SAMPLE A - STANDARDISED COMPONENT SCORES



APPENDIX H

Results of Experiment G

DISCRIMINANT ANALYSIS - HITS AND MISSES

Experimental Analysis XVI

PREDICTED GROUP

	1	2	3	4	5	6	7	8	9	10	Total	% HITS
1	87	11					6		3		107	81
2	6	99			1	1		1			108	92
3			23					3	1		27	85
4	2	4		29			2				37	78
5					12						12	100
6		3				25	1	2	3		34	74
7	5	3		1			65	1	1		76	86
8		7		1			1	43			52	83
9						1			26		27	96
10										7	7	100
											487	85.4

Variables	25
% Trace	100
Functions	9
Priors	Si

43 out of 73 misses correctly predicted by the second highest probability

Experimental Analysis XVII

PREDICTED GROUP

	1	2	3	4	5	6	7	8	9	10	Total	% HITS
1	88	9					7		3		107	82
2	8	93		2	1	1	1	2			108	86
3		1	23			1		1	1		27	85
4	1	7		29							37	78
5					12						12	100
6		4				26		1	3		34	76
7	8	6		2			57	2	1		76	75
8		6		1		2		43			52	83
9			1						26		27	96
10							1		1	5	7	71
											487	82.5

Variables	25
% Trace	90
Functions	7
Priors	Si

39 out of 85 misses correctly predicted by the second highest probability.



DISCRIMINANT ANALYSIS HITS AND MISSES

Experimental Analysis XVIII

	PREDICTED GROUP										Total	% HITS
	1	2	3	4	5	6	7	8	9	10		
1	93	6					5		3		107	87
2	5	89			1		11	2			108	82
3			23	1			2	1			27	85
4	9	17		4			4	3			37	11
5					12						12	100
6		6				16		9	3		34	47
7	23	20					31	1	1		76	41
8		9						39			52	75
9			1						26		27	96
10							1	1	5		7	71
											487	69.4

Variables	25
% Trace	80
Functions	5
Priors	Si

80 out of 149 misses correctly predicted by the second highest probability

Experimental Analysis XIX

	PREDICTED GROUP										Total	% HITS
	1	2	3	4	5	6	7	8	9	10		
1	96	6					4		1		107	90
2	4	101			1	2		1			108	94
3		1	23					2	1		27	85
4		2		34			1				37	92
5					12						12	100
6		2				27		1	4		34	79
7	3	2					70		1		76	92
8		5						47			52	90
9						1			26		27	96
10											7	100
											487	91.0%

Variables	50
% Trace	100
Functions	9
Priors	Si

20 out of 44 misses correctly predicted by the second highest probability.

ACTUAL  
GROUP

ACTUAL  
GROUP

DISCRIMINANT ANALYSIS HITS AND MISSES

Experimental Analysis XX

PREDICTED GROUP

	1	2	3	4	5	6	7	8	9	10	Total	% HITS
1	95	4					5		3		107	89
2	5	99				3		1			108	92
3		1	23					2	1		27	85
4		3		33			1				37	89
5					12						12	100
6		2				28		1	3		34	82
7	4	2					69		1		76	91
8		6						46			52	88
9			1						26		27	96
10	1									6	7	86

Variables	50
% Trace	95
Functions	8
Priors	Si

31 out of 50 misses correctly predicted by the second highest probability

487 89.7

Experimental Analysis XXI

PREDICTED GROUP

	1	2	3	4	5	6	7	8	9	10	Total	% HITS
1	95	3					6		3		107	89
2	5	100					2	1			108	93
3		1	23					2	1		27	85
4		5		32							37	86
5					12						12	100
6		5				26			3		34	76
7	3	4					67	1	1		76	88
8		5		1		3		43			52	83
9			1						26		27	96
10	1									6	7	86

Variables	50
% Trace	90
Functions	7
Priors	Si

33 out of 57 misses correctly predicted by the second highest probability

487 88.3



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DISCRIMINANT ANALYSIS HITS AND MISSES

Experimental Analysis XXII

ACTUAL GROUP	PREDICTED GROUP										Total	% HITS
	1	2	3	4	5	6	7	8	9	10		
1	95	3					6		3		107	89
2	1	89					17	1			108	82
3			23	1				2	1		27	85
4		11		24			1	1			37	65
5					12						12	100
6		8				9		14	3		34	26
7	23	32					19	1	1		76	25
8		6		1				45			52	86
9			1						26		27	96
10	1									6	7	86
											487	71.5

Variables	50
% Trace	80
Functions	5
Priors	Si

95 out of 139 misses correctly predicted by the second highest probability

Experimental Analysis XXIII

ACTUAL GROUP	PREDICTED GROUP										Total	% HITS
	1	2	3	4	5	6	7	8	9	10		
1	85	8					11		3		107	79
2	8	85		4	1	5	1	4			108	79
3		1	23					2	1		27	85
4	1	4		30		1	1				37	81
5					12						12	100
6						28	1	2	3		34	82
7	5	2		1			66	1	1		76	87
8		6		1			1	44			52	85
9			1						26		27	96
10							1		1	5	7	71
											487	83

Variables	25
% Trace	95
Functions	8
Priors	Eq

50 out of 83 misses correctly predicted by the second highest probability

DISCRIMINANT ANALYSIS HITS AND MISSES

Experimental Analysis XXIV

PREDICTED GROUP

	1	2	3	4	5	6	7	8	9	10	Total	% HITS
1	95	3					6		3		107	89
2	5	95		1	1	4	1	1			108	88
3		1	23					2	1		27	85
4		3		33			1				37	89
5					12						12	100
6						30		1	3		34	88
7	3	2					70		1		76	92
8		4		1				47			52	90
9			1						26		27	96
10	1									6	7	86
											487	89.7

ACTUAL  
GROUP

Variables	50
% Trace	95
Functions	8
Priors	Eq

30 out of 50 misses correctly predicted by the second highest probability.



Step-Wise MANOVA - 15 Groups

SUMMARY TABLE

STEP NUMBER	VARIABLE ENTERED	REMOVED	F TO ENTER OR REMOVE
1	H03		118.96433
2	L04		78.10467
3	H04		55.23024
4	A07		53.78203
5	S05		47.38327
6	M06		34.19105
7	H05		25.46650
8	G03		24.09248
9	W06		20.17978
10	M05		17.39752
11	M03		16.14444
12	M07		15.68379
13	L13		13.42342
14	W07		10.83100
15	G02		10.25933
16	W02		9.56666
17	L09		8.29538
18	L02		7.01597
19	A01		6.36077
20	S04		6.32333
21	H02		5.10562
22	A02		4.62715
23	A03		5.13323
24	M08		4.62947
25	W03		4.03136
26	H06		3.98897
27	M01		3.90062
28	W01		3.49717
29	L07		3.76990
30	L05		3.26156
31	S01		2.99787
32	G05		2.43773
33	L01		2.52905
34	S03		2.48324
35	L03		2.45254
36	G06		2.57662
37	A04		2.35872
38	L08		2.70527
39	M04		2.19785
40	L14		1.97151
41	W05		1.93536
42	W04		3.47139
43	L12		2.23769
44	L11		1.87899
45	G04		1.48735
46	A06		1.46847
47	H02		1.22747
48	S02		1.08207
49	A05		.87410
50	L06		.44914

SIGNIFICANCE

D.F.

CHI-SQUARE

WILKS LAMBDA

PERCENT OF TRACE

CANONICAL CORRELATION

EIGENVALUE

NUMBER REMOVED

NUMBER REMOVED	EIGENVALUE	CANONICAL CORRELATION	PERCENT OF TRACE	WILKS LAMBDA	CHI-SQUARE	D.F.	SIGNIFICANCE
0	6.35752	.92956	26.0	.00001	5442.86658	350	0.000
1	4.61488	.90659	18.9	.00006	4510.86408	312	0.000
2	3.10341	.86966	12.7	.00036	3705.09274	276	0.000
3	2.37416	.83883	9.7	.00147	3045.77352	242	0.000
4	1.72109	.79530	7.0	.00496	2477.83310	210	0.000
5	1.58700	.78323	6.5	.01350	2010.35082	180	0.000
6	1.51452	.77609	6.2	.03493	1566.46827	152	0.000
7	1.08015	.72060	4.4	.08784	1135.86655	126	0.000
8	.79523	.66556	3.3	.18272	793.80679	102	0.000
9	.55886	.59773	2.3	.32802	520.54890	80	0.000
10	.39312	.53121	1.6	.51037	314.11546	60	0.000
11	.20535	.41276	.8	.71100	169.28436	42	0.000
12	.12033	.32772	.5	.85701	72.06157	26	0.000
13	.04153	.19967	.2	.96013	15.00068	12	.089

10 FUNCTIONS WILL BE USED IN REMAINING ANALYSES

STANDARDIZED DISCRIMINANT FUNCTION COEFFICIENTS

	1	2	3	4	5	6	7	8	9	10
S04	.00990	.39792	.09090	-.20853	.07484	.02258	-.08819	-.22195	.15018	-.09119
S05	.05209	.59971	.26632	-.02150	.14685	.07727	.17105	.18530	.49090	.35890
L02	.21761	.11743	.06419	-.03351	.12511	.16945	.02646	.07962	.48524	.02253
L04	1.81462	.56228	.29793	.28774	.04061	.09207	.24514	.11272	.12702	-.04558
L09	.07414	.07240	.11331	.10530	.26160	.36210	.12890	.39958	.08093	.02948
L13	.02373	.00734	.14116	.29976	.21807	.22579	.51633	.33129	.18517	.19923
A01	.03583	.05376	.06746	.29592	.04811	.02066	.27981	.01523	.27513	.32357
A02	.06238	.18511	.15737	.05525	-.17460	.11700	.30018	.18107	.15080	.41057
A03	.08769	.23157	.08027	-.06410	.10550	.04254	.29356	.00090	.28751	.17638
A07	.12855	.09698	.11973	.65026	1.42287	.28973	.00446	.05714	.13971	.18716
W02	.06914	.28489	.04810	.13565	.24365	.18357	.03357	.02484	.51142	.25933
W03	.14205	.02919	.07410	.06144	.22801	.18245	.08090	.08477	.18053	.31702
W06	.02458	.24402	.28413	.15212	.02071	.35778	.49247	.73002	.07307	.30677
W07	.06680	.34776	.11536	.16658	.20284	.89135	.05140	.41436	.02460	.11343
M03	.08138	.23268	.32668	.01066	.19581	.38980	.16160	.17786	.10853	.65053
M05	.01677	.30442	.28371	.00628	.25969	.31655	.06442	.30020	.62892	.22022
M06	1.19991	.18596	.10368	.09352	.08008	.02126	.02190	.01023	.03751	.11901
M07	.09546	.23925	.01245	.37011	.17835	.28716	.35312	.39833	.16310	.32045
M08	.01001	.06592	.25673	.03690	.13322	.18678	.03454	.08547	.17638	.14414
H02	.04216	.01252	.22824	.01217	.14829	.14829	.07320	.01498	.39430	.06267
H03	.82016	1.93196	.69732	.69732	.09502	.12585	.50009	.34270	.98460	.84851
H04	.21125	.64486	.127102	1.61159	.38997	.27823	1.12635	.91002	.19781	.68002
H05	.01557	.11474	.07462	.06014	.44636	.44636	.25785	.54465	.19781	.21189
G02	.20623	.11489	.08961	.17393	.21815	.21815	.25785	.18219	.31069	.52380
G03	.04054	.03368	.28362	.52379	.16195	.17150	.72681	.27861	.16823	.22233



Experimental Analysis XXV

PREDICTED GROUP

ACTUAL GROUP	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	Total	% HITS
1	38							3			4					48	79
2		45		1		2		5				2	6			61	73
3			20	1								1	1	1		24	83
4				25				2				1				28	89
5					10											10	100
6						30							1			33	91
7							9									10	90
8	5	9				1		56			1					72	78
9						1		5			4			1		16	0
10								1		11	1					13	85
11	5							2			34	6		1		48	71
12											1	37				41	90
13												4	37			47	79
14														27		29	93
15								1						1	5	7	71
																487	78.9

Variables	25
% Trace	95
Functions	10
Priors	Si

64 out of 103 misses correctly predicted by the second highest probability.

Step-Wise MANOVA - 20 Groups

SUMMARY TABLE

STEP NUMBER	VARIABLE ENTERED	VARIABLE REMOVED	F TO ENTER OR REMOVE
1	H03		91.96962
2	L04		62.55499
3	A07		50.12281
4	G03		47.53707
5	H04		41.03111
6	S05		36.24601
7	W07		27.94450
8	M06		26.50679
9	W06		19.59978
10	M07		15.56138
11	S03		13.80652
12	L09		12.66621
13	M08		11.17146
14	G02		10.88335
15	W02		9.24988
16	A01		9.02166
17	M03		8.92514
18	M05		7.02835
19	H06		6.68669
20	L13		6.42997
21	W03		5.35028
22	L02		5.04480
23	G04		4.98308
24	H05		4.57412
25	S01		4.53790
26	A02		4.33985
27	A03		4.90637
28	L07		3.39761
29	M01		3.39725
30	M02		3.33082
31	W01		3.26675
32	H02		2.92608
33	L03		2.34208
34	L08		2.53970
35	L10		3.00475
36	L12		2.42899
37	S04		2.34859
38	A04		1.91027
39	A06		2.02987
40	G06		1.83196
41	L14		1.77414
42	M04		1.76026
43	G05		1.85719
44	L06		1.34842
45	L11		1.32294
46	S02		1.50711
47	W05		.97643
48	W04		3.35390
49	A05		.84798
50	L01		.77937



Discriminant Analysis - 20 Groups

NUMBER REMOVED	EIGENVALUE	CANNICAL CORRELATION	PERCENT OF TRACE	MILKS LAMBDA	CHI-SQUARE	D.F.	SIGNIFICANCE
0	7.53760	.93961	24.8	.00000	6419.26778	475	0.000
1	5.53046	.92026	18.2	.00001	5423.15677	432	0.000
2	3.74838	.88848	12.3	.00006	4551.53315	391	0.000
3	2.93587	.86367	9.7	.00026	3827.93316	352	0.000
4	2.32651	.83629	7.7	.00104	3191.50740	315	0.000
5	1.84267	.80512	6.1	.00345	2633.21317	280	0.000
6	1.72618	.79573	5.7	.00981	2147.92971	247	0.000
7	1.25447	.74595	4.1	.02675	1682.08241	216	0.000
8	.87776	.68370	2.9	.06030	1304.48432	187	0.000
9	.68395	.63731	2.3	.11324	1011.81247	160	0.000
10	.54226	.59296	1.8	.19068	769.74207	135	0.000
11	.40784	.53823	1.3	.29408	568.49861	112	0.000
12	.35163	.51003	1.2	.41402	409.61428	91	0.000
13	.27103	.46178	.9	.55960	269.65476	72	0.000
14	.16430	.37565	.5	.71127	158.25387	55	0.000
15	.10958	.31426	.4	.82814	87.59470	40	0.000
16	.06107	.23991	.2	.91888	39.29444	27	0.060
17	.01687	.12679	.1	.97500	11.75901	16	.760
18	.00663	.09249	.0	.99145	3.99039	7	.781

11 FUNCTIONS WILL BE USED IN REMAINING ANALYSES

STANDARDIZED DISCRIMINANT FUNCTION COEFFICIENTS

	1	2	3	4	5	6	7	8	9	10	11
S01	.17347	.04208	-.32464	-.12877	.39736	-.14412	.04231	-.10607	-.26277	-.05267	
S03	-.47279	-.41169	-.43909	-.16996	-.26245	.13351	.26350	-.18140	-.05343		
S05	.15205	.22047	.36020	.07434	.17494	-.17682	.16079	-.32899	-.07960		
L02	.13986	-.20225	.03902	-.04884	-.00825	.05906	-.14320	-.14885	-.40746		
L04	-.167486	.105153	-.35277	.07229	.32855	.32855	.01631	.34275	-.16342		
L09	-.06492	.16166	.38460	-.09608	.22898	.41430	.28613	-.11634	-.14113		
L13	.05945	.03125	.09420	-.25671	.23298	.21969	.09739	-.08257	-.09984		
A01	.05504	.02855	.00677	-.48096	.10049	.15442	.00359	-.00517	-.08188		
A07	.69243	.75363	.73683	.69853	1.57326	-.02040	.16645	-.00561	-.08188		
A02	-.27627	-.27540	.23205	.02153	-.32246	.34461	.02195	-.21867	1.9024		
A03	.11063	-.10087	.06345	-.07552	.06446	-.09790	.09955	-.24388	.36623		
A05	.03521	.11710	.06500	.09799	.14404	.31133	.06998	-.19259	.20885		
A07	.00612	.33287	.11788	-.49443	-.14404	-.19318	.39838	-.16476	.07787		
A03	-.12367	-.26620	-.31757	-.02000	-.32247	-.45276	.65642	-.00571	-.07787		
A05	.00530	.30888	-.17990	.03095	.22049	.08299	.35835	-.04654	.31354		
A05	-.13568	.42089	.15795	-.10675	.19039	.04099	.38548	-.28592	-.52721		
A07	.01909	.28463	.04703	.10675	.16289	-.09388	.02004	-.07526	.25307		
A03	-.11947	-.06466	.14854	-.49443	.11653	-.18081	.36080	-.18180	.14368		
A03	-.124613	1.36129	.68424	.95772	-.22267	-.01553	.12614	-.61973	.04050		
A04	.13394	.78299	.13918	1.20863	.09929	.28391	.03041	-.22125	-.12598		
A05	.03602	.00390	.18545	-.05846	-.39181	1.36448	.41094	-.22521	.90437		
A06	.00790	.09221	.20739	.11504	-.18665	-.12256	.31532	-.14425	-.90402		
G02	-.25226	-.15292	-.10745	.07188	.04651	-.20199	.38546	-.29424	-.16738		
G03	.19341	.31929	.68424	-.14045	-.03192	.14096	-.08779	-.42099	.31244		
G04	-.01382	-.07820	-.00616	-.02716	.31213	.77051	.16868	-.08746	.02880		
					.08060	-.03720	.01450	-.44998	.14470		

ACTUAL GROUP	PREDICTED GROUP																				Total	% HITS	
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20			
1	21														3						24	88	
2	2	24			1	3		1			4				1			3			39	62	
3			12		1										1	1					15	80	
4				20		2											1	1			24	83	
5					21				1			1			5						33	64	
6					1	19				2					1	2	2	1			28	68	
7							10														10	100	
8								13	3	1											17	76	
9						1			24												25	96	
10						1				12											13	92	
11											7										7	100	
12												38			2	3					48	79	
13													3	1	4	3		1	1		15	7	
14													1								10	90	
15															35		4	1			45	78	
16																29					36	88	
17																		30			33	91	
18																		4	20		30	67	
19																			27		29	93	
20																				1	5	6	83

487 77.4

Variables	25
% Trace	95
Functions	11
Priors	Si

56 out of 110 misses correctly predicted by the second highest probability.



APPENDIX I

Means of 15 and 10 Cluster Classes

Samples B and C

CENTROIDS OF 10 CLUSTER CLASSES - SAMPLE B

CLUSTER CLASSIFICATION - SAMPLE B

GROUP	MEANS	VARIABLES										SIZE									
GROUP	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05											
1	0.4374E	04	0.8946E	04	0.4965E	02	0.5729E	01	0.6900E	01	0.4639E	02	0.1289E	02	0.6110E	01	0.0000E	00	0.1327E	02	20
2	0.4774E	03	0.7844E	03	0.4759E	01	0.1956E	01	0.1842E	01	0.2318E	02	0.2533E	01	0.1432E	00	0.1850E	01	0.2017E	02	81
3	0.4943E	03	0.7212E	03	0.5176E	00	0.1104E	01	0.8824E	00	0.2593E	02	0.1246E	01	0.2024E	00	0.3255E	01	0.6598E	01	17
4	0.3242E	04	0.2903E	04	0.3051E	02	0.2563E	01	0.4544E	01	0.3253E	02	0.8000E	01	0.4038E	00	0.1178E	01	0.7515E	01	101
5	0.3418E	03	0.5067E	03	0.5569E	01	0.9858E	00	0.1476E	01	0.2491E	02	0.1507E	02	0.7031E	00	0.1638E	01	0.5872E	01	84
6	0.7022E	02	0.5667E	02	0.0000E	00	0.2344E	01	0.1111E	01	0.0000E	00	0.4908E	01	0.0000E	00	0.8782E	02	0.1010E	01	9
7	0.1885E	04	0.1717E	04	0.9216E	01	0.1713E	01	0.2000E	01	0.2593E	02	0.6699E	01	0.4920E	00	0.2514E	01	0.2030E	02	30
8	0.8500E	02	0.7075E	02	0.2085E	02	0.7525E	00	0.5000E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	4
9	0.1560E	04	0.1358E	04	0.1417E	02	0.1574E	01	0.1644E	01	0.1371E	02	0.2759E	01	0.3854E	01	0.3050E	01	0.5566E	01	82
0	0.1293E	04	0.1246E	04	0.1958E	02	0.1626E	01	0.2441E	01	0.2690E	02	0.6781E	01	0.2033E	00	0.3616E	00	0.5951E	01	58
TOTAL	0.1852E	04	0.1666E	04	0.1689E	02	0.1918E	01	0.2539E	01	0.2487E	02	0.7209E	01	0.5510E	00	0.2489E	01	0.1032E	02	486

GROUP	MEANS	VARIABLES										SIZE									
GROUP	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01											
1	0.1740E	00	0.6450E	01	0.1484E	02	0.2732E	01	0.1534E	01	0.3600E	00	0.4350E	01	0.5000E	01	0.2500E	00	0.9820E	00	20
2	0.3246E	01	0.6416E	00	0.1087E	02	0.1479E	02	0.1684E	02	0.3603E	01	0.1418E	02	0.4568E	00	0.2546E	00	0.2533E	01	81
3	0.1016E	02	0.4429E	00	0.1019E	02	0.2054E	02	0.1536E	02	0.2929E	01	0.1115E	02	0.0000E	00	0.5362E	01	0.6471E	02	17
4	0.7043E	00	0.2657E	00	0.4947E	02	0.8030E	01	0.2148E	00	0.4186E	00	0.8218E	01	0.4950E	01	0.4257E	00	0.9723E	00	101
5	0.5258E	00	0.3293E	01	0.3371E	02	0.3926E	01	0.4948E	01	0.3026E	01	0.9677E	01	0.1190E	01	0.2500E	00	0.5876E	01	84
6	0.1852E	01	0.0000E	00	0.1083E	01	0.0000E	00	0.1911E	01	0.0000E	00	0.2006E	02	0.0000E	00	0.0000E	00	0.0000E	00	9
7	0.5555E	00	0.5023E	00	0.2093E	02	0.5502E	01	0.8594E	01	0.1372E	01	0.1068E	02	0.1333E	00	0.2000E	00	0.2051E	01	30
8	0.2500E	02	0.5104E	02	0.0000E	00	0.0000E	00	0.2366E	02	0.0000E	00	0.4920E	02	0.0000E	00	0.0000E	00	0.0000E	00	4
9	0.6135E	04	0.4344E	00	0.7552E	02	0.3573E	00	0.9860E	00	0.3031E	01	0.7899E	01	0.4878E	01	0.4878E	01	0.2131E	01	82
0	0.2052E	00	0.6236E	00	0.5074E	02	0.8026E	00	0.1436E	01	0.7155E	01	0.3531E	01	0.1034E	00	0.3276E	00	0.1924E	01	58
TOTAL	0.1543E	01	0.1348E	01	0.4178E	02	0.4488E	01	0.5407E	01	0.1932E	01	0.9479E	01	0.1195E	00	0.2428E	00	0.4726E	01	486

GROUP	MEANS	VARIABLES										SIZE									
GROUP	A02	A03	A04	A05	A06	A07	A08	A09	A10	A11											
1	0.3195E	02	0.3227E	02	0.9070E	01	0.9222E	01	0.6511E	01	0.5435E	00	0.7050E	00	0.3665E	02	0.1574E	02	0.2445E	02	20
2	0.1624E	02	0.5075E	02	0.5935E	01	0.8414E	01	0.5209E	01	0.6698E	00	0.4424E	01	0.8284E	02	0.6913E	01	0.6132E	01	81
3	0.0000E	00	0.5802E	01	0.0000E	00	0.0000E	00	0.0000E	00	0.1424E	00	0.2606E	01	0.7273E	02	0.5362E	01	0.4932E	01	17
4	0.3965E	02	0.3632E	02	0.1951E	00	0.1725E	02	0.3437E	01	0.1372E	01	0.1037E	01	0.8986E	02	0.1756E	02	0.1745E	02	101
5	0.2546E	04	0.1098E	02	0.1097E	01	0.2871E	02	0.6445E	01	0.1647E	01	0.5024E	01	0.9747E	02	0.4762E	01	0.5040E	01	84
6	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.3831E	02	0.8255E	02	0.2667E	02	0.1689E	02	9
7	0.2037E	04	0.2614E	02	0.2527E	00	0.1560E	02	0.1444E	01	0.6917E	00	0.2159E	01	0.7407E	00	0.8389E	01	0.1561E	02	30
8	0.0000E	00	0.0000E	00	0.5025E	00	0.2500E	02	0.7444E	02	0.7419E	02	0.1044E	02	0.1000E	03	0.0000E	00	0.2500E	02	4
9	0.5116E	02	0.2607E	02	0.5507E	01	0.7524E	01	0.8566E	00	0.1281E	01	0.1420E	01	0.9791E	02	0.5122E	01	0.7500E	01	82
0	0.4395E	02	0.3573E	02	0.7550E	00	0.1162E	02	0.4351E	01	0.1623E	01	0.1711E	01	0.9630E	02	0.2566E	01	0.3147E	02	58
TOTAL	0.3180E	02	0.2652E	02	0.2036E	01	0.1415E	02	0.4326E	01	0.1395E	01	0.3419E	01	0.8379E	02	0.8693E	01	0.1515E	02	486

GROUP	MEANS	VARIABLES										SIZE									
GROUP	A08	A09	A10	A11	A12	A13	A14	A15	A16	A17											
1	0.1712E	02	0.3542E	02	0.7498E	01	0.1000E	01	0.3000E	00	0.8500E	00	0.7500E	00	0.3500E	00	0.0000E	00	0.0000E	00	20
2	0.3239E	02	0.4241E	02	0.1216E	02	0.3210E	00	0.3951E	00	0.4938E	01	0.6174E	00	0.1235E	01	0.3342E	00	0.3704E	01	81
3	0.2255E	02	0.4706E	02	0.1961E	02	0.0000E	00	0.1745E	00	0.0000E	00	0.5294E	00	0.0000E	00	0.2747E	00	0.1000E	01	17
4	0.1725E	04	0.3882E	02	0.8722E	01	0.9307E	00	0.5941E	01	0.5347E	00	0.7228E	00	0.7921E	00	0.1178E	01	0.0030E	00	101
5	0.6944E	01	0.5438E	02	0.2087E	02	0.1905E	00	0.3571E	01	0.3571E	01	0.7024E	00	0.2581E	01	0.2132E	00	0.0030E	00	84
6	0.0000E	00	0.4611E	02	0.8333E	01	0.0000E	00	0.5556E	00	0.0000E	00	0.3533E	00	0.0000E	00	0.4404E	02	0.0000E	00	9
7	0.1000E	04	0.3611E	02	0.1006E	02	0.4333E	00	0.1667E	00	0.1667E	00	0.5667E	00	0.1667E	00	0.4767E	01	0.6667E	01	30
8	0.2500E	02	0.5000E	02	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.2500E	00	0.0000E	00	0.0000E	00	0.0000E	00	4
9	0.8252E	01	0.6699E	02	0.1413E	02	0.4756E	00	0.7317E	01	0.1220E	01	0.5854E	00	0.3295E	00	0.0000E	00	0.1220E	01	82
0	0.5316E	02	0.3879E	01	0.8908E	01	0.6207E	00	0.5172E	01	0.4897E	01	0.8103E	00	0.3448E	00	0.0000E	00	0.0000E	00	58
TOTAL	0.2024E	02	0.4290E	02	0.1419E	02	0.5021E	00	0.1450E	00	0.1811E	00	0.6626E	00	0.2922E	00	0.9231E	00	0.4733E	01	486

GROUP	MEANS	VARIABLES										SIZE									
GROUP	A18	A19	A20	A21	A22	A23	A24	A25	A26	A27											
1	0.9435E	00	0.9000E	00	0.2050E	01	0.8500E	00	0.5000E	01	0.5435E	02	0.5000E	01	0.3864E	02	0.6136E	02	0.0000E	00	20
2	0.4849E	01	0.1000E	01	0.1074E	01	0.9753E	00	0.2469E	01	0.5416E	02	0.2593E	00	0.7516E	02	0.9466E	01	0.1335E	02	81
3	0.1385E	01	0.9412E	00	0.1174E	01	0.6235E	00	0.1176E	00	0.5400E	02	0.1765E	00	0.8158E	02	0.1842E	02	0.0000E	00	17
4	0.1892E	01	0.1000E	01	0.1073E	01	0.9901E	00	0.9901E	02	0.4836E	02	0.1980E	01	0.6501E	02	0.3419E	02	0.8009E	00	101
5	0.6931E	01	0.1000E	01	0.1071E	01	0.8690E	00	0.1340E	00	0.5939E	02	0.3571E	00	0.7544E	02	0.2446E	02	0.1000E	00	84
6	0.1764E	04	0.1000E	01	0.1444E	01	0.8889E	00	0.1111E	00	0.5367E	02	0.2227E	00	0.6667E	02	0.3333E	02	0.0000E	00	9
7	0.2205E	01	0.6667E	01	0.1333E	01	0.0000E	00	0.6667E	01	0.5323E	02	0.3533E	01	0.7046E	02	0.1953E	02	0.1000E	02	30
8	0.3703E	01	0.1000E	01	0.1650E	01	0.7500E	00	0.2500E	00	0.4500E	02	0.7500E	00	0.7500E	02	0.2500E	02	0.0000E	00	4
9	0.1835E	01	0.1000E	01	0.1073E	01	0.9512E	00	0.4872E	01	0.5713E	02	0.3049E	00	0.6972E	02	0.2492E	02	0.5022E	00	82
0	0.2625E	01	0.1000E	01	0.1362E	01	0.9828E	00	0.1724E	01	0.3650E	02	0.2566E	00	0.2161E	02	0.7799E	02	0.3486E	00	58
TOTAL	0.3605E	01	0.9392E	00	0.1317E	01															



CENTROIDS OF 15 CLUSTER CLASSES - SAMPLE B

CLUSTER CLASSIFICATION - SAMPLE B

P MEANS		VARIABLES										SIZE								
P	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05										
0,9054E	04	0,8640E	04	0,4910E	02	0,5572E	01	0,6840E	01	0,4663E	02	0,1231E	02	0,6366E	01	0,0000E	00	0,1568E	02	21
0,1315E	04	0,1097E	04	0,7014E	01	0,2675E	01	0,2444E	01	0,3512E	02	0,3855E	01	0,0000E	00	0,1528E	01	0,3447E	02	36
0,8675E	03	0,8401E	03	0,6000E	00	0,1032E	01	0,1000E	01	0,3391E	02	0,1020E	01	0,0000E	00	0,4256E	01	0,8285E	01	13
0,4185E	04	0,3653E	04	0,4051E	02	0,2812E	01	0,4880E	01	0,3778E	02	0,5775E	01	0,2702E	00	0,0000E	00	0,8363E	01	30
0,5870E	03	0,3889E	03	0,1459E	01	0,1314E	01	0,1200E	01	0,4437E	01	0,8090E	00	0,2650E	00	0,3725E	01	0,2592E	01	30
0,4563E	03	0,3421E	03	0,6062E	01	0,9745E	00	0,1000E	01	0,1615E	02	0,8201E	01	0,1875E	01	0,7853E	01	0,3450E	01	20
0,6912E	02	0,5637E	02	0,0000E	00	0,2544E	01	0,1250E	01	0,0000E	00	0,3402E	01	0,0000E	00	0,9053E	02	0,1811E	01	8
0,1931E	04	0,1767E	04	0,9796E	01	0,1755E	01	0,2107E	01	0,2706E	02	0,6078E	01	0,5271E	00	0,2694E	01	0,2175E	02	28
0,2107E	04	0,1993E	04	0,3385E	02	0,1954E	01	0,4041E	01	0,2008E	02	0,1004E	02	0,1359E	00	0,0000E	00	0,2935E	01	49
0,2059E	03	0,1895E	03	0,5950E	01	0,7217E	00	0,1583E	01	0,2316E	02	0,2003E	02	0,0000E	00	0,2225E	00	0,7528E	01	24
0,8500E	02	0,7075E	02	0,2085E	02	0,7525E	00	0,5000E	00	0,0000E	00	0,0000E	00	0,0000E	00	0,0000E	00	0,0000E	00	4
0,2055E	04	0,1893E	04	0,1023E	02	0,2195E	01	0,2766E	01	0,3222E	02	0,7561E	01	0,6491E	00	0,4675E	01	0,1180E	02	64
0,1051E	04	0,8404E	03	0,1412E	02	0,1258E	01	0,1070E	01	0,5832E	01	0,2768E	01	0,0000E	00	0,0000E	00	0,1307E	01	43
0,1157E	04	0,1143E	04	0,1594E	02	0,1600E	01	0,2209E	01	0,3070E	02	0,7258E	01	0,2742E	00	0,4377E	00	0,5013E	01	43
0,4871E	03	0,3599E	03	0,3307E	01	0,1079E	01	0,1226E	01	0,2125E	02	0,9551E	01	0,0000E	00	0,0000E	00	0,1417E	02	53

L 0,1852E 04 0,1666E 04 0,1089E 02 0,1918E 01 0,2539E 01 0,2487E 02 0,7209E 01 0,5510E 00 0,2489E 01 0,1032E 02 400

P MEANS		VARIABLES										SIZE								
P	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01										
0,1657E	00	0,6524E	01	0,1470E	02	0,2602E	01	0,1461E	01	0,3429E	00	0,4359E	01	0,4762E	01	0,2381E	00	0,9352E	00	21
0,4061E	00	0,5733E	00	0,1468E	02	0,5286E	01	0,6081E	01	0,8981E	00	0,1104E	02	0,5278E	00	0,4107E	00	0,2387E	01	36
0,1329E	02	0,4508E	00	0,1032E	02	0,6899E	01	0,1205E	02	0,6408E	00	0,4578E	01	0,0000E	00	0,7692E	01	0,8462E	02	13
0,1343E	01	0,2502E	00	0,4368E	02	0,8660E	01	0,2478E	00	0,4516E	00	0,1107E	02	0,1000E	00	0,5000E	00	0,6616E	00	30
0,6117E	01	0,2750E	01	0,7923E	01	0,3181E	02	0,3957E	02	0,8065E	01	0,1372E	02	0,3333E	00	0,0000E	00	0,5920E	00	30
0,0000E	00	0,2113E	01	0,4365E	02	0,9804E	01	0,6917E	01	0,1039E	02	0,1218E	02	0,0000E	00	0,5000E	01	0,3334E	01	20
0,2084E	01	0,0000E	00	0,0000E	00	0,0000E	00	0,2172E	01	0,0000E	00	0,1940E	02	0,0000E	00	0,0000E	00	0,0000E	00	8
0,5950E	00	0,5302E	00	0,2721E	02	0,5181E	01	0,7758E	01	0,3961E	00	0,9472E	01	0,1429E	00	0,2143E	00	0,3055E	01	28
0,0000E	00	0,2624E	00	0,6019E	02	0,0000E	00	0,3067E	00	0,2247E	00	0,4762E	00	0,0000E	00	0,4393E	00	0,1576E	01	49
0,1190E	01	0,2014E	01	0,3499E	02	0,0000E	00	0,1070E	02	0,1630E	01	0,9543E	01	0,0000E	00	0,2505E	00	0,1093E	01	24
0,2500E	02	0,5104E	02	0,0000E	00	0,0000E	00	0,2306E	02	0,0000E	00	0,4200E	02	0,0000E	00	0,0000E	00	0,0000E	00	4
0,1228E	01	0,5739E	00	0,4406E	02	0,1393E	01	0,6750E	00	0,2209E	01	0,6275E	01	0,1583E	01	0,2413E	00	0,2713E	01	64
0,0000E	00	0,6391E	00	0,3775E	02	0,3019E	00	0,1406E	01	0,3197E	01	0,9979E	01	0,9302E	01	0,4651E	01	0,2995E	01	43
0,2553E	00	0,7484E	00	0,5182E	02	0,8891E	00	0,1754E	01	0,0000E	00	0,3016E	01	0,1395E	00	0,3024E	00	0,1400E	01	43
0,1076E	01	0,2378E	01	0,4088E	02	0,7664E	01	0,3028E	01	0,1490E	01	0,1601E	02	0,1509E	00	0,2264E	00	0,7751E	01	53

L 0,1543E 01 0,1348E 01 0,4178E 02 0,4488E 01 0,5407E 01 0,1932E 01 0,9479E 01 0,1193E 00 0,2428E 00 0,4726E 01 400

P MEANS		VARIABLES										SIZE								
P	A02	A03	A04	A05	A06	A07	W01	W02	W03	W04										
0,3043E	02	0,3334E	02	0,8039E	01	0,8783E	01	0,8356E	01	0,5910E	00	0,7162E	00	0,3932E	02	0,1618E	02	0,2326E	02	21
0,2653E	02	0,5121E	02	0,1724E	01	0,7049E	01	0,5544E	01	0,7894E	00	0,3737E	01	0,8613E	02	0,1509E	02	0,8472E	01	36
0,0000E	00	0,0000E	00	0,0000E	00	0,0000E	00	0,0000E	00	0,1731E	00	0,2768E	01	0,7980E	02	0,0000E	00	0,3646E	01	13
0,3794E	02	0,4530E	02	0,1440E	01	0,1456E	02	0,1335E	01	0,9866E	00	0,8342E	00	0,9061E	02	0,1997E	02	0,1982E	02	30
0,1900E	00	0,5026E	01	0,9037E	01	0,5344E	01	0,2745E	01	0,1517E	00	0,6073E	01	0,7079E	02	0,4444E	01	0,3011E	01	30
0,2229E	02	0,1285E	02	0,0000E	00	0,8327E	01	0,3206E	01	0,1418E	01	0,8997E	01	0,8394E	02	0,1500E	02	0,9300E	01	20
0,0000E	00	0,0000E	00	0,0000E	00	0,0000E	00	0,0000E	00	0,0000E	00	0,4192E	02	0,8036E	02	0,2375E	02	0,2125E	02	8
0,2023E	02	0,2603E	02	0,2707E	00	0,1672E	02	0,1547E	01	0,7139E	00	0,2245E	01	0,0000E	00	0,9524E	01	0,1458E	02	28
0,4843E	02	0,1999E	02	0,5341E	00	0,1868E	02	0,6702E	01	0,2034E	01	0,1143E	01	0,8919E	02	0,1207E	02	0,1497E	02	49
0,1260E	02	0,5272E	01	0,9071E	00	0,5696E	02	0,6434E	01	0,3125E	01	0,4712E	01	0,9844E	02	0,3472E	01	0,0000E	00	24
0,0000E	00	0,0000E	00	0,5025E	00	0,2500E	02	0,7444E	02	0,2419E	02	0,1043E	02	0,1000E	03	0,0000E	00	0,2300E	02	4
0,4532E	02	0,3178E	02	0,4932E	01	0,1158E	02	0,2111E	01	0,9711E	00	0,1572E	01	0,9560E	02	0,6953E	01	0,7916E	01	64
0,5270E	02	0,2246E	02	0,5012E	01	0,9226E	01	0,5926E	00	0,1590E	01	0,1881E	01	0,9880E	02	0,3488E	01	0,7170E	01	43
0,4050E	02	0,3940E	02	0,3002E	00	0,1163E	02	0,3545E	01	0,1568E	01	0,1913E	01	0,9638E	02	0,3488E	01	0,5895E	02	43
0,2569E	02	0,2141E	02	0,2465E	01	0,1690E	02	0,7121E	01	0,9875E	00	0,4003E	01	0,9694E	02	0,6289E	00	0,6761E	01	53

L 0,3180E 02 0,2632E 02 0,2030E 01 0,1415E 02 0,4326E 01 0,1395E 01 0,3410E 01 0,8379E 02 0,8693E 01 0,1315E 02 400











CENTROIDS OF 15 CLUSTER CLASSES - SAMPLE C

CLUSTER CLASSIFICATION - RANDOM SAMPLE C

GROUP MEANS		VARIABLES																		
GROUP	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05	L06	L07	L08	L09	L10					
1	0.3290E	04	0.1800E	04	0.8728E	01	0.2245E	01	0.1917E	01	0.1899E	02	0.5130E	01	0.3787E	00	0.6688E	01	0.1051E	02
2	0.4560E	03	0.7372E	03	0.1293E	01	0.1288E	01	0.1576E	01	0.4400E	02	0.3548E	01	0.8570E	00	0.0000E	00	0.2039E	02
3	0.2477E	04	0.2194E	04	0.2710E	02	0.2485E	01	0.2618E	01	0.1968E	02	0.3176E	01	0.2091E	-01	0.9873E	-01	0.1073E	02
4	0.3759E	03	0.3298E	03	0.2031E	01	0.1263E	01	0.1561E	01	0.1928E	02	0.6710E	01	0.0000E	00	0.2858E	01	0.2561E	00
5	0.3000E	04	0.2632E	04	0.3103E	02	0.2722E	01	0.4840E	01	0.4087E	02	0.1039E	04	0.0000E	00	0.1954E	00	0.1067E	02
6	0.1742E	03	0.1505E	03	0.1003E	03	0.9709E	01	0.5740E	01	0.2551E	02	0.2712E	01	0.8500E	00	0.0000E	00	0.2544E	02
7	0.8010E	03	0.6508E	03	0.4001E	01	0.1081E	01	0.1349E	01	0.1593E	02	0.2015E	01	0.8209E	-01	0.1551E	03	0.1348E	02
8	0.2282E	04	0.1935E	04	0.1290E	02	0.3625E	01	0.2959E	01	0.4187E	02	0.3315E	01	0.6361E	00	0.5796E	00	0.3720E	02
9	0.5350E	03	0.4121E	03	0.5635E	01	0.8683E	00	0.9167E	00	0.1267E	02	0.5172E	01	0.0000E	00	0.0000E	00	0.2625E	01
10	0.6687E	03	0.6471E	03	0.1023E	02	0.1097E	01	0.2400E	01	0.4316E	02	0.2144E	02	0.1332E	01	0.1780E	00	0.9777E	01
11	0.5218E	04	0.5038E	04	0.3074E	02	0.2719E	01	0.5559E	01	0.4691E	02	0.1159E	02	0.4955E	01	0.1188E	01	0.1029E	02
12	0.1143E	03	0.9637E	02	0.6103E	00	0.2298E	01	0.1822E	01	0.0000E	00	0.4921E	01	0.0000E	00	0.2540E	02	0.5942E	01
13	0.1590E	04	0.1509E	04	0.2443E	02	0.1591E	01	0.3000E	01	0.2571E	02	0.4660E	01	0.5778E	00	0.9630E	00	0.7784E	01
14	0.7422E	02	0.2867E	02	0.8091E	01	0.5288E	00	0.2500E	00	0.7500E	01	0.5000E	01	0.0000E	00	0.0000E	00	0.0000E	00
15	0.9720E	03	0.6277E	03	0.3070E	01	0.9034E	00	0.6000E	00	0.3699E	01	0.1329E	01	0.0000E	00	0.3676E	01	0.7666E	00
TOTAL	0.2051E	04	0.1756E	04	0.1290E	02	0.1944E	01	0.2566E	01	0.2607E	02	0.6748E	01	0.6137E	00	0.4021E	01	0.1048E	02

GROUP MEANS		VARIABLES																		
GROUP	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01										
1	0.8974E	01	0.9800E	00	0.2094E	02	0.4466E	01	0.1784E	02	0.1816E	01	0.2390E	02	0.2085E	00	0.8533E	-01	0.9799E	01
2	0.4187E	01	0.3901E	00	0.4428E	01	0.1489E	02	0.7602E	01	0.4716E	01	0.7595E	01	0.3030E	00	0.6061E	-01	0.4556E	02
3	0.4878E	00	0.4244E	00	0.6445E	02	0.8529E	00	0.2721E	00	0.2162E	01	0.7875E	01	0.1818E	-01	0.2364E	00	0.2415E	01
4	0.1630E	01	0.2021E	01	0.1091E	02	0.2503E	02	0.2241E	02	0.1740E	01	0.6927E	01	0.9756E	-01	0.7317E	-01	0.1529E	01
5	0.1817E	00	0.2392E	00	0.3038E	02	0.6629E	00	0.3910E	00	0.1705E	00	0.9629E	01	0.6349E	-01	0.3810E	00	0.9373E	00
6	0.6172E	01	0.4000E	-01	0.3706E	02	0.2942E	00	0.3515E	01	0.1969E	01	0.9937E	01	0.3750E	00	0.3750E	01	0.9217E	00
7	0.2750E	01	0.1641E	01	0.4304E	02	0.3038E	01	0.8372E	01	0.3087E	01	0.9087E	01	0.6977E	-01	0.1628E	00	0.1310E	01
8	0.1002E	01	0.4065E	00	0.9138E	01	0.3085E	01	0.2267E	01	0.4040E	01	0.1217E	02	0.6522E	00	0.5652E	01	0.2598E	01
9	0.2371E	00	0.8021E	00	0.6035E	02	0.1029E	02	0.7787E	01	0.4390E	01	0.1204E	02	0.8333E	-01	0.1450E	00	0.9471E	00
10	0.0000E	00	0.1822E	01	0.1009E	02	0.2288E	01	0.1920E	01	0.0000E	00	0.4794E	01	0.1000E	00	0.3333E	01	0.9745E	00
11	0.4853E	-01	0.1262E	00	0.2394E	02	0.0000E	00	0.2985E	00	0.8009E	00	0.2891E	01	0.0000E	00	0.2647E	01	0.1322E	01
12	0.0000E	00	0.6263E	00	0.2236E	01	0.0000E	00	0.1023E	02	0.0000E	00	0.1805E	02	0.1053E	00	0.5263E	-01	0.5263E	01
13	0.3540E	-01	0.4464E	00	0.6109E	02	0.1912E	00	0.5422E	00	0.1726E	01	0.4330E	01	0.6000E	-01	0.2800E	00	0.1741E	01
14	0.0000E	00	0.3823E	02	0.3732E	02	0.0000E	00	0.1104E	02	0.0000E	00	0.2630E	02	0.0000E	00	0.0000E	01	0.0000E	00
15	0.8469E	00	0.2139E	01	0.6671E	02	0.1390E	01	0.1944E	02	0.2768E	01	0.2020E	02	0.5714E	-01	0.5714E	-01	0.9313E	01
TOTAL	0.1404E	01	0.1498E	01	0.3746E	02	0.4676E	01	0.6824E	01	0.1965E	01	0.1004E	02	0.1165E	00	0.2163E	00	0.5332E	01

GROUP MEANS		VARIABLES																		
GROUP	A02	A03	A04	A05	A06	A07	W01	W02	W03	W04										
1	0.1430E	02	0.2091E	02	0.1901E	01	0.1155E	02	0.4133E	00	0.2975E	00	0.2178E	01	0.9400E	00	0.0000E	00	0.3093E	01
2	0.3341E	01	0.1740E	02	0.2791E	01	0.2550E	01	0.1134E	01	0.3033E	01	0.2844E	01	0.8240E	02	0.7575E	01	0.3333E	01
3	0.5591E	02	0.2894E	02	0.2433E	01	0.5072E	01	0.3303E	01	0.1180E	01	0.1578E	01	0.9139E	02	0.1771E	02	0.6782E	01
4	0.1044E	02	0.7430E	01	0.1401E	01	0.3875E	02	0.6445E	01	0.8329E	00	0.6635E	01	0.8667E	02	0.6501E	01	0.2073E	02
5	0.4122E	02	0.3352E	02	0.1935E	00	0.1898E	02	0.4174E	01	0.1276E	01	0.1404E	01	0.8713E	02	0.1098E	02	0.1590E	02
6	0.3094E	02	0.3729E	02	0.1144E	02	0.6328E	01	0.4650E	00	0.7637E	00	0.6600E	00	0.2934E	02	0.3311E	01	0.1319E	02
7	0.2231E	02	0.2638E	02	0.1802E	02	0.3614E	01	0.1850E	01	0.6379E	00	0.5025E	01	0.9366E	02	0.7751E	00	0.2132E	01
8	0.2077E	02	0.3224E	02	0.1893E	01	0.1540E	02	0.7299E	01	0.9381E	00	0.3032E	01	0.7726E	02	0.1916E	02	0.1674E	02
9	0.2702E	02	0.1711E	02	0.6403E	01	0.1347E	02	0.1687E	01	0.1167E	01	0.2983E	01	0.9192E	02	0.0000E	00	0.1458E	02
10	0.2154E	02	0.8455E	01	0.4333E	00	0.2393E	02	0.2003E	02	0.1949E	01	0.3697E	01	0.9528E	02	0.1667E	01	0.4348E	01
11	0.3394E	02	0.4317E	02	0.4794E	-01	0.2917E	01	0.9670E	01	0.7265E	00	0.7077E	00	0.7436E	02	0.9363E	01	0.2324E	02
12	0.3907E	01	0.1204E	01	0.1035E	02	0.7521E	00	0.1023E	02	0.7684E	00	0.3264E	02	0.7109E	02	0.8070E	01	0.2784E	02
13	0.3270E	02	0.3263E	02	0.1132E	01	0.1073E	02	0.1058E	01	0.1578E	01	0.1264E	01	0.9658E	02	0.3000E	01	0.3567E	02
14	0.0000E	00	0.0000E	00	0.2235E	01	0.7426E	02	0.2318E	02	0.2436E	02	0.5341E	02	0.9870E	02	0.4166E	01	0.0000E	00
15	0.1990E	02	0.2200E	02	0.4628E	01	0.7619E	01	0.4912E	01	0.7960E	00	0.3487E	01	0.9388E	02	0.5258E	01	0.2225E	00
TOTAL	0.2873E	02	0.2469E	02	0.3603E	01	0.1326E	02	0.5347E	01	0.1387E	01	0.4221E	01	0.8303E	02	0.7272E	01	0.1334E	02



CENTROIDS OF 15 CLUSTER CLASSES - SAMPLE C

CLUSTER CLASSIFICATION - RANDOM SAMPLE C

GROUP	VARIABLES											SIZE										
	MEANS	M05	M06	M07	M01	M02	M03	M04	M05	M06	M07											
1	0.1632E	02	0.3849E	02	0.1415E	02	0.3750E	00	0.2500E	00	0.8333E-01	0.3700E	00	0.1667E	00	0.7746E	00	0.3553E	00	24		
2	0.1630E	02	0.6708E	02	0.4245E	01	0.6041E-01	0.6041E-01	0.0000E	00	0.8788E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.6667E	00	53	
3	0.1030E	02	0.0704E	02	0.4732E	01	0.7636E	00	0.9001E-01	0.1818E-01	0.7818E	00	0.3818E	00	0.0000E	00	0.0000E	00	0.0000E	00	55	
4	0.3610E	02	0.2981E	02	0.1077E	02	0.3171E	00	0.3650E	00	0.7317E-01	0.4390E	00	0.2439E-01	0.3422E	00	0.4678E-01	0.0000E	0.0000E	00	41	
5	0.2167E	02	0.3614E	02	0.1022E	02	0.9683E	00	0.1587E	00	0.7937E	00	0.7502E	00	0.7778E	00	0.8587E-01	0.0000E	0.0000E	00	63	
6	0.1549E	02	0.0061E	02	0.1209E	01	0.6250E	00	0.5000E	00	0.5000E	00	0.6250E	00	0.5000E	00	0.0000E	00	0.0000E	00	8	
7	0.8914E	01	0.7170E	01	0.8101E	02	0.1305E	00	0.1123E	00	0.0000E	00	0.6977E	00	0.6977E-01	0.0000E	0.0000E	00	0.4651E-01	0.0000E	43	
8	0.2627E	02	0.3467E	02	0.3140E	01	0.3915E	00	0.3478E	00	0.1304E	00	0.9565E	00	0.1304E	00	0.0000E	00	0.0000E	00	23	
9	0.1520E	02	0.3819E	02	0.3194E	02	0.4167E-01	0.4167E-01	0.0000E	00	0.6250E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	24	
10	0.1111E	01	0.7972E	02	0.8011E	01	0.3333E	00	0.0000E	00	0.0000E	00	0.9667E	00	0.0000E	00	0.0000E	00	0.0000E	00	50	
11	0.1922E	02	0.3826E	02	0.7917E	01	0.1000E	01	0.2941E-01	0.5288E	00	0.9118E	00	0.5882E	00	0.0000E	00	0.0000E	00	0.0000E	00	34
12	0.3150E	02	0.2544E	02	0.7200E	01	0.5263E-01	0.5780E	00	0.0000E	00	0.5789E	00	0.0000E	00	0.2951E	02	0.5263E-01	0.0000E	0.0000E	00	19
13	0.3732E	02	0.2533E	01	0.3007E	01	0.0800E	00	0.0000E	00	0.6000E-01	0.8800E	00	0.5600E	00	0.0000E	00	0.0000E	00	0.0000E	00	50
14	0.1250E	02	0.3417E	02	0.2917E	02	0.1250E	00	0.0000E	00	0.0000E	00	0.1250E	00	0.0000E	00	0.0000E	00	0.0000E	00	8	
15	0.4280E	01	0.8476E	02	0.4702E	01	0.3714E-01	0.2857E-01	0.0000E	00	0.4286E	00	0.0000E	00	0.0000E	00	0.0000E	00	0.0000E	00	35	
TOTAL	0.2080E	02	0.4103E	02	0.1575E	02	0.4694E	00	0.1408E	00	0.1735E	00	0.7102E	00	0.2714E	00	0.1222E	01	0.7143E-01	0.0000E	490	

GROUP	VARIABLES											SIZE										
	MEANS	M01	M02	M03	M04	M05	M06	G01	G02	G03												
1	0.2271E	01	0.4167E-01	0.1292E	01	0.0000E	00	0.4167E-01	0.5267E	02	0.0000E	00	0.8538E	02	0.6282E	01	0.8333E	01	0.8333E	01	24	
2	0.5874E	01	0.1000E	01	0.1000E	01	0.9697E	00	0.3040E-01	0.5545E	02	0.1818E	00	0.7650E	02	0.1441E	02	0.2018E	01	0.2018E	01	53
3	0.1789E	01	0.1000E	01	0.1073E	01	0.1000E	01	0.0000E	00	0.5427E	02	0.1273E	00	0.5252E	02	0.4667E	02	0.8156E	00	55	
4	0.4589E	01	0.1000E	01	0.1146E	01	0.1000E	01	0.0000E	00	0.4498E	02	0.6093E	00	0.8311E	02	0.1413E	02	0.2739E	01	41	
5	0.2607E	01	0.9841E	00	0.1571E	01	0.9524E	00	0.3195E-01	0.5086E	02	0.7937E-01	0.7282E	02	0.2322E	02	0.3954E	01	0.3954E	01	63	
6	0.4250E	00	0.0750E	00	0.1209E	01	0.8750E	00	0.0000E	00	0.5375E	02	0.0000E	00	0.5081E	02	0.3669E	02	0.1250E	02	8	
7	0.4107E	01	0.1000E	01	0.1103E	01	0.1000E	01	0.0000E	00	0.7109E	02	0.2558E	00	0.8386E	02	0.1341E	02	0.2726E	01	43	
8	0.2559E	01	0.9130E	00	0.1000E	01	0.7826E	00	0.1304E	00	0.4961E	02	0.4348E-01	0.2968E	02	0.1380E	02	0.5622E	02	0.5622E	02	23
9	0.2362E	01	0.1000E	01	0.1000E	01	0.0000E	00	0.1000E	01	0.5792E	02	0.1250E	00	0.7079E	02	0.2504E	02	0.4167E	01	24	
10	0.8561E	01	0.1000E	01	0.1300E	01	0.1000E	01	0.0000E	00	0.5933E	02	0.5000E	00	0.4670E	02	0.5350E	02	0.0000E	00	50	
11	0.1394E	01	0.1000E	01	0.1500E	01	0.9706E	00	0.2941E-01	0.4791E	02	0.5882E-01	0.9071E	01	0.9093E	02	0.0000E	00	0.0000E	00	34	
12	0.2210E	02	0.1000E	01	0.1220E	01	0.8947E	00	0.1043E	00	0.4305E	02	0.5263E-01	0.6364E	02	0.3636E	02	0.0000E	00	0.0000E	00	19
13	0.2510E	01	0.1000E	01	0.1320E	01	0.1000E	01	0.0000E	00	0.3838E	02	0.1600E	00	0.2726E	02	0.7274E	02	0.0000E	00	50	
14	0.2522E	01	0.1000E	01	0.1145E	01	0.7500E	00	0.2500E	00	0.5400E	02	0.5000E	00	0.1000E	03	0.0000E	00	0.0000E	00	8	
15	0.3464E	01	0.1000E	01	0.1000E	01	0.1000E	01	0.0000E	00	0.5531E	02	0.6857E	00	0.8344E	02	0.1656E	02	0.0000E	00	35	
TOTAL	0.4330E	01	0.9449E	00	0.1401E	01	0.8714E	00	0.7347E-01	0.5237E	02	0.2163E	00	0.6092E	02	0.3392E	02	0.5152E	01	0.5152E	01	490

GROUP	VARIABLES			SIZE			
	MEANS	G04	G05				
1	0.2083E	00	0.3417E	00	0.0000E	00	24
2	0.3030E-01	0.3030E	00	0.3030E-01	0.0000E	00	33
3	0.1630E	00	0.1745E	01	0.5435E-01	0.0000E	55
4	0.4678E-01	0.1244E	01	0.0000E	00	0.0000E	41
5	0.1746E	00	0.3111E	01	0.0000E	00	63
6	0.3750E	00	0.7500E	00	0.5000E	00	8
7	0.6977E-01	0.1047E	01	0.4031E-01	0.0000E	00	43
8	0.2174E	00	0.3217E	00	0.3045E	00	23
9	0.1250E	00	0.1125E	01	0.4167E-01	0.0000E	24
10	0.2333E	00	0.1400E	01	0.1067E	00	50
11	0.3204E	00	0.1971E	01	0.3435E	00	34
12	0.3789E	00	0.1737E	01	0.5263E-01	0.0000E	19
13	0.3800E	00	0.1720E	01	0.4000E-01	0.0000E	50
14	0.2500E	00	0.0000E	00	0.1250E	00	8
15	0.1714E	00	0.3429E	00	0.2057E-01	0.0000E	35
TOTAL	0.2143E	00	0.1420E	01	0.7959E-01	0.0000E	490

APPENDIX J

Class Means for Classifications I and II

- Sample D



CLUSTER CLASSIFICATION - SAMPLE D

GROUP	VARIABLES																SIZE				
	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05	L06	L07	L08	L09	L10	L11		L12	L13	L14	A01
1	0.4048E	04	0.3537E	04	0.4000E	02	0.3244F	01	0.6861E	01	0.3791E	02	0.6288F	01	0.3723E	00	0.0030E	00	0.1466E	02	194
2	0.1373E	05	0.1170E	05	0.5900E	02	0.6510E	01	0.5607E	01	0.4117E	02	0.7348F	01	0.3232E	01	0.6529E	-02	0.1233E	02	29
3	0.6524E	03	0.5124F	03	0.3949E	01	0.9507E	00	0.1140E	01	0.1878E	02	0.7948E	01	0.3920E	00	0.1033E	01	0.7662E	01	163
4	0.1501E	04	0.1230E	04	0.7599E	01	0.2730E	01	0.2104E	01	0.3670E	02	0.2645E	01	0.7489E	00	0.3647E	00	0.3505E	02	135
5	0.5046E	03	0.4529F	03	0.6576E	01	0.1163F	01	0.1644E	01	0.1686E	02	0.6728E	01	0.4013E	00	0.1433E	01	0.2587E	01	133
6	0.9085E	03	0.7486E	03	0.9474E	00	0.1487F	01	0.1258E	01	0.2101E	02	0.1875F	01	0.2559E	01	0.9598E	01	0.6745E	01	163
7	0.1094E	03	0.9113E	02	0.1685E	00	0.2137F	01	0.1433E	01	0.4125E	00	0.3354E	01	0.0000E	00	0.7970E	02	0.5952E	01	60
8	0.1774E	04	0.1451E	04	0.5420E	01	0.1961E	01	0.1584E	01	0.2131E	02	0.3862E	01	0.6811E	00	0.1449E	01	0.1237E	02	101
9	0.7324E	03	0.6464E	03	0.7482E	01	0.1150F	01	0.1115E	01	0.1352E	02	0.6214E	01	0.3962E	-01	0.5109E	00	0.6292E	01	208
10	0.1675E	04	0.1593F	04	0.1968E	02	0.2179F	01	0.3603E	01	0.4168E	02	0.1557E	02	0.1186E	01	0.5069E	00	0.1067E	02	234
11	0.2948E	03	0.2929E	03	0.3612E	01	0.9081E	00	0.2129E	01	0.3106E	02	0.1538E	02	0.1487E	01	0.3757E	01	0.1166E	02	116
12	0.1503E	04	0.1325E	04	0.2034E	02	0.2002F	01	0.3184E	01	0.2657E	02	0.7178E	01	0.1940E	00	0.1633E	00	0.1050E	02	228
13	0.4641E	04	0.4411E	04	0.1499E	02	0.5114E	01	0.6356E	01	0.4860E	02	0.2711E	02	0.4380E	00	0.7961E	00	0.1015E	02	90
14	0.3160E	04	0.2982E	04	0.4464E	02	0.2165E	01	0.3576E	01	0.1037E	02	0.2515E	01	0.4485E	-01	0.1357E	00	0.2693E	01	132
15	0.9610E	03	0.7751E	03	0.1026E	02	0.1016F	01	0.1178E	01	0.1294E	02	0.3940E	01	0.1195E	00	0.5327E	00	0.4293E	01	146
16	0.2191E	03	0.1558E	03	0.5282E	02	0.8752E	00	0.4628E	00	0.2993E	01	0.6499E	01	0.0000E	00	0.3448E	01	0.3701E	01	29
TOTAL	0.1757E	04	0.1522E	04	0.1582E	02	0.1905E	01	0.2545E	01	0.2515E	.02	0.7543E	01	0.8193E	00	0.2986E	01	0.1017E	02	2161

GROUP	VARIABLES																SIZE				
	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01	L14	L13	L12	L11	L10	L09		L08	L07	L06	A01
1	0.8424E	00	0.2102E	00	0.3670E	02	0.6272E	00	0.3939E	00	0.6028E	00	0.9981E	01	0.7732E	-01	0.2113E	00	0.5551E	00	194
2	0.1852E	01	0.1193E	00	0.2852E	02	0.1728E	00	0.5240E	01	0.1892E	01	0.1024E	02	0.1579E	00	0.2039E	00	0.9243E	00	29
3	0.2459E	01	0.1220F	01	0.4885E	02	0.2996F	01	0.8657E	01	0.2614E	01	0.1243E	02	0.7975E	-01	0.1238E	00	0.5283E	01	163
4	0.1338E	01	0.6143E	00	0.9667E	01	0.7540E	01	0.7317E	01	0.2519E	01	0.1156E	02	0.6000E	00	0.3926E	00	0.2623E	01	135
5	0.1557E	01	0.1405E	01	0.4929E	02	0.4624F	01	0.8384E	01	0.2117E	01	0.3335E	01	0.7519E	-01	0.1729E	00	0.2357E	01	133
6	0.4887E	01	0.1073E	01	0.7631E	01	0.1770E	02	0.3756E	02	0.6349E	01	0.4630E	01	0.2331E	00	0.1840E	-01	0.2231E	02	163
7	0.1876E	01	0.1032F	01	0.2427E	01	0.0000E	00	0.7246E	01	0.1512E	01	0.1605E	02	0.1667E	-01	0.0000E	00	0.2500E	01	60
8	0.3839E	01	0.4257E	00	0.2445E	02	0.1064E	02	0.2008E	02	0.3814E	01	0.1185E	02	0.2079E	00	0.8911E	-01	0.4768E	01	101
9	0.2735E	00	0.1056E	01	0.6907E	02	0.1115E	01	0.1308E	01	0.1438E	01	0.7920E	01	0.3365E	-01	0.2019E	00	0.5040E	01	208
10	0.2853E	00	0.2903E	00	0.3066E	02	0.6340E	00	0.2974E	00	0.2378E	00	0.3841E	01	0.3346E	-01	0.5855E	00	0.2371E	01	234
11	0.6657E	00	0.2396F	01	0.1118E	01	0.1456E	02	0.7311E	01	0.2744E	01	0.1000E	02	0.1293E	00	0.1273E	00	0.6547E	00	116
12	0.3659E	00	0.4376F	00	0.5310E	02	0.7839E	00	0.7389E	00	0.1179E	01	0.7895E	01	0.5263E	-01	0.3333E	00	0.1410E	01	228
13	0.1598E	00	0.1482E	00	0.8331E	00	0.1882E	00	0.1882E	00	0.1370E	00	0.4753E	01	0.3333E	00	0.5333E	00	0.6570E	01	90
14	0.3258E	00	0.1285E	00	0.8329E	02	0.0000E	00	0.5043E	00	0.1561E	00	0.5144E	01	0.3788E	-01	0.1439E	00	0.8742E	00	132
15	0.8417E	00	0.8240E	00	0.7148E	02	0.6141E	00	0.4300E	01	0.1794E	01	0.8757E	01	0.8904E	-01	0.1027E	00	0.3427E	01	146
16	0.0000E	00	0.3634E	02	0.3413E	02	0.4271E	01	0.8621E	01	0.5616E	01	0.2981E	02	0.0000E	00	0.0000E	00	0.4897E	-01	29
TOTAL	0.1284E	01	0.1243E	01	0.3988E	02	0.4017E	01	0.6384E	01	0.1913E	01	0.8910E	01	0.1145E	00	0.2300E	00	0.4235E	01	2161

CLASS MEANS : CLASSIFICATION I - SAMPLE D



CLUSTER CLASSIFICATION - SAMPLE D

GROUP	VARIABLES																SIZE				
	A02	A03	A04	A05	A06	A07	W01	W02	W03	W04	W05	W06	W07	W08	W09	W10					
1	0.4089E	02	0.3921E	02	0.5273E	00	0.1468E	02	0.3587E	01	0.1139E	01	0.1021E	01	0.8757E	02	0.1441E	02	0.2934E	02	194
2	0.2297E	02	0.2815E	02	0.1004E	02	0.1457E	02	0.6104E	01	0.4924E	00	0.5424E	00	0.1765E	02	0.1034E	02	0.2442E	02	29
3	0.2563E	02	0.2083E	02	0.7074E	01	0.9264E	01	0.7379E	01	0.9675E	00	0.2978E	00	0.9479E	02	0.6134E	00	0.5266E	01	163
4	0.2260E	02	0.4519E	01	0.4685E	01	0.1253E	02	0.4022E	01	0.7307E	00	0.3152E	01	0.8790E	02	0.1734E	02	0.1233E	02	135
5	0.3516E	02	0.1809E	02	0.1448E	01	0.1241E	02	0.5725E	01	0.1382E	01	0.4530E	01	0.9057E	02	0.7331E	01	0.9198E	01	155
6	0.4061E	01	0.3907E	01	0.2141E	01	0.5195E	01	0.4258E	00	0.1314E	00	0.3225E	01	0.7239E	02	0.5692E	01	0.7471E	01	163
7	0.0000E	02	0.1667E	01	0.0000E	00	0.2500E	01	0.3333E	01	0.2897E	00	0.2760E	02	0.8360E	02	0.1596E	02	0.2575E	02	60
8	0.1299E	02	0.1304E	01	0.3273E	01	0.8149E	01	0.1342E	01	0.3889E	00	0.2273E	01	0.6154E	01	0.3395E	00	0.1025E	02	101
9	0.3953E	02	0.2490E	02	0.6356E	01	0.8383E	01	0.2328E	01	0.1376E	01	0.2960E	01	0.9643E	02	0.1883E	00	0.2404E	01	208
10	0.4011E	02	0.5028E	02	0.1066E	01	0.1734E	02	0.2777E	01	0.1423E	01	0.1781E	01	0.9447E	02	0.9364E	01	0.1747E	02	234
11	0.4583E	01	0.7022E	01	0.1147E	01	0.5083E	02	0.9040E	01	0.1918E	01	0.5238E	01	0.9597E	02	0.5244E	01	0.1027E	02	116
12	0.4753E	02	0.3029E	02	0.4338E	00	0.1511E	02	0.4326E	01	0.1580E	01	0.1817E	01	0.9635E	02	0.1464E	02	0.7227E	01	228
13	0.1885E	02	0.3054E	02	0.7596E	01	0.3051E	01	0.8053E	01	0.3482E	00	0.7524E	00	0.5931E	02	0.1252E	02	0.2043E	02	90
14	0.5926E	02	0.2901E	02	0.8437E	00	0.8081E	01	0.1912E	01	0.1765E	01	0.8968E	00	0.8873E	02	0.1174E	02	0.2460E	02	132
15	0.3664E	02	0.2371E	02	0.5377E	01	0.1201E	02	0.3768E	01	0.1794E	01	0.2513E	01	0.9620E	02	0.2055E	01	0.2584E	02	146
16	0.4580E	01	0.1015E	01	0.4070E	01	0.6832E	02	0.2192E	02	0.2705E	02	0.1568E	02	0.9426E	02	0.1724E	01	0.1264E	02	29
TOTAL	0.3081E	02	0.2426E	02	0.3045E	01	0.1390E	02	0.4218E	01	0.1511E	01	0.3332E	01	0.8487E	02	0.8326E	01	0.1571E	02	2161

GROUP	VARIABLES																SIZE				
	W05	W06	W07	W08	W09	W10	W11	W12	W13	W14	W15	W16	W17	W18	W19	W20					
1	0.1965E	02	0.2993E	02	0.1166E	02	0.9897E	00	0.1433E	00	0.7577E	00	0.6031E	00	0.6608E	00	0.0000E	00	0.0000E	00	174
2	0.1958E	02	0.4158E	02	0.4056E	01	0.9310E	00	0.1724E	00	0.6552E	00	0.5172E	00	0.4483E	00	0.0000E	00	0.0000E	00	29
3	0.4151E	01	0.6493E	01	0.8548E	02	0.1411E	00	0.7362E	01	0.2454E	01	0.5706E	00	0.1840E	01	0.1362E	01	0.6135E	02	163
4	0.1427E	02	0.4896E	02	0.7160E	01	0.4074E	00	0.3778E	00	0.1111E	00	0.7630E	00	0.3704E	01	0.2467E	01	0.2963E	01	135
5	0.2074E	02	0.4296E	02	0.2018E	02	0.1880E	00	0.6767E	01	0.3008E	01	0.6316E	00	0.6774E	01	0.7835E	01	0.0000E	00	135
6	0.2483E	02	0.4806E	02	0.1595E	02	0.2209E	00	0.1943E	00	0.6133E	02	0.4969E	00	0.0000E	00	0.3693E	01	0.4540E	00	165
7	0.1192E	02	0.4049E	02	0.5689E	01	0.1000E	00	0.6000E	00	0.0000E	00	0.3500E	00	0.0000E	00	0.3041E	02	0.3333E	01	60
8	0.1756E	02	0.3405E	02	0.1305E	02	0.2475E	00	0.1287E	00	0.7921E	01	0.5644E	00	0.1188E	00	0.1293E	00	0.1683E	00	101
9	0.3886E	01	0.9035E	02	0.1282E	01	0.1298E	00	0.4808E	01	0.9615E	02	0.6298E	00	0.4808E	01	0.1688E	01	0.4808E	02	208
10	0.3900E	02	0.2489E	02	0.9286E	01	0.7564E	00	0.7245E	01	0.2179E	00	0.9402E	00	0.3974E	00	0.8376E	02	0.4274E	02	234
11	0.2651E	02	0.5187E	02	0.6106E	01	0.3534E	00	0.2414E	00	0.6034E	01	0.8534E	00	0.1724E	01	0.3046E	00	0.6034E	01	116
12	0.1043E	02	0.6105E	02	0.6045E	01	0.7544E	00	0.9649E	01	0.1491E	00	0.8728E	00	0.5570E	00	0.110E	01	0.0000E	00	228
13	0.2034E	02	0.4293E	02	0.3771E	01	0.1000E	01	0.5564E	01	0.7778E	00	0.8778E	00	0.2222E	00	0.0000E	00	0.1111E	01	90
14	0.3655E	02	0.2494E	02	0.4179E	01	0.9015E	00	0.3080E	01	0.8333E	01	0.7879E	00	0.6318E	00	0.0000E	00	0.0000E	00	132
15	0.6438E	02	0.3196E	01	0.4520E	01	0.2192E	00	0.1301E	00	0.2740E	01	0.5068E	00	0.7534E	01	0.6740E	01	0.1370E	01	146
16	0.1351E	02	0.6006E	02	0.1207E	02	0.1034E	00	0.6867E	01	0.0000E	00	0.2414E	00	0.0000E	00	0.9497E	00	0.5448E	01	29
TOTAL	0.2214E	02	0.4078E	02	0.1589E	02	0.4859E	00	0.1356E	00	0.1745E	00	0.6867E	00	0.2772E	00	0.8980E	00	0.5137E	01	2161

CLASS MEANS : CLASSIFICATION I - SAMPLE D



CLUSTER CLASSIFICATION - SAMPLE D

GROUP	VARIABLES																SIZE
	H08	H01	H02	H03	H04	H05	H06	G01	G02	G03							
1	0.1591E 01	0.1000E 01	0.1490E 01	0.0601E 00	0.3003E-01	0.5100E 02	0.1546E-01	0.7190E 02	0.2878E 02	0.6319E 01						194	
2	0.5317E 00	0.6552E 00	0.1793E 01	0.5172E 00	0.1379E 00	0.5276E 02	0.6897E-01	0.6749E 02	0.3128E 02	0.1254E 01						29	
3	0.5670E 01	0.1000F 01	0.1067E 01	0.2693F 00	0.3067E-01	0.7057E 02	0.1288E 00	0.7995E 02	0.2005E 02	0.0000F 00						163	
4	0.2491E 01	0.1000E 01	0.1000E 01	0.9922E 00	0.7407E-02	0.5400E 02	0.4444E-01	0.5235E 02	0.1257E 02	0.5304E 02						135	
5	0.2693E 01	0.0925E 00	0.1023E 01	0.0000E 00	0.9925E 00	0.5584E 02	0.1570E 00	0.6985E 02	0.2839E 02	0.1762E 01						133	
6	0.3078E 01	0.1000E 01	0.1104E 01	0.9881E 00	0.1840E-01	0.5350E 02	0.4601E 00	0.9324E 02	0.6024E 01	0.7432E 00						163	
7	0.1451E 02	0.9835E 00	0.1700E 01	0.9167E 00	0.6667E-01	0.4823E 02	0.1333E 00	0.5839E 02	0.4015E 02	0.1454E 01						60	
8	0.2265E 01	0.1782E 00	0.1198E 01	0.0000E 00	0.1782E 00	0.5241E 02	0.9901E-02	0.7356E 02	0.1021E 02	0.1623E 02						101	
9	0.3092E 01	0.1000F 01	0.1106E 01	0.1000E 00	0.0000E 00	0.5590E 02	0.4231E 00	0.6262E 02	0.3560E 02	0.1785E 01						208	
10	0.1124E 01	0.1000E 01	0.1171E 01	0.9957E 00	0.4274E-02	0.4402E 02	0.1282E 00	0.4945E 02	0.8022E 02	0.3543E 00						234	
11	0.1492E 02	0.1000F 01	0.1441E 01	0.9914E 00	0.8091E-02	0.4937E 02	0.7069E 00	0.7907E 02	0.1868E 02	0.1349E 01						116	
12	0.2936E 01	0.1000F 01	0.1531E 01	0.9868F 00	0.1316E-01	0.5493E 02	0.1570E 00	0.6121E 02	0.1809E 02	0.7037E 00						228	
13	0.1570E 01	0.9667E 00	0.2256E 00	0.9556E 01	0.1111E-01	0.4922E 02	0.8880E-01	0.2374E 02	0.7626E 02	0.0000F 00						90	
14	0.1625E 01	0.1000F 01	0.1712E 01	0.1000E 01	0.0000E 00	0.4380E 02	0.6818E-01	0.2585E 02	0.7283E 02	0.1315E 01						132	
15	0.3004E 01	0.1000E 01	0.1164E 01	0.9932E 00	0.8649E-02	0.3866E 02	0.6370E 00	0.4999E 02	0.4901E 02	0.3995E 00						146	
16	0.3483E 01	0.1000E 01	0.1172E 01	0.8621E 00	0.1379E 00	0.5493E 02	0.6207E 00	0.5696E 02	0.1304E 02	0.0000E 00						29	
TOTAL	0.3819E 01	0.9547E 00	0.1284E 01	0.8695E 00	0.8515E-01	0.5206E 02	0.2318E 00	0.6116E 02	0.3482E 02	0.4021E 01						2161	

GROUP	VARIABLES																SIZE
	G04	G05	G06														
1	0.1280E 00	0.2959E 00	0.9278E-01														194
2	0.4483E 00	0.1483E 01	0.3103E 00														29
3	0.1350E 00	0.1018E 01	0.3681E-01														163
4	0.5185E-01	0.5037E 00	0.1030E 00														135
5	0.8271E-01	0.1235E 01	0.7519E-01														133
6	0.7362E-01	0.6074E 00	0.3681E-01														163
7	0.6167E 00	0.1700F 01	0.3533E-01														60
8	0.1782E 00	0.7129E 00	0.7921E-01														101
9	0.1635E 00	0.1014E 01	0.3565E-01														208
10	0.1154E 00	0.1515E 01	0.1026E 00														234
11	0.1466E 00	0.1664E 01	0.3448E-01														116
12	0.3026E 00	0.2618E 01	0.4025E-01														228
13	0.7667E 00	0.2422E 01	0.5778E 00														90
14	0.6439E 00	0.2227E 01	0.4545E-01														132
15	0.1507E 00	0.1000E 01	0.3425E-01														146
16	0.3448E 00	0.7931E 00	0.1724E 00														29
TOTAL	0.2212E 00	0.1539E 01	0.8191E-01														2161

CLASS MEANS : CLASSIFICATION I - SAMPLE D

CLASSIFICATION II - UNIVARIATE F TESTS

WILKS LAMBDA (U-STATISTIC) AND UNIVARIATE F-RATIO

VARIABLE	WILKS LAMBDA	F
-----	-----	-----
S01	.3943	219.6489
S02	.3694	244.1438
S03	.6045	93.5527
S04	.6145	89.7263
S05	.4015	213.1817
L01	.7174	56.3301
L02	.7472	48.3704
L03	.9584	6.2099
L04	.2673	391.9108
L05	.8394	27.3611
L06	.9598	5.9857
L07	.6369	81.5391
L08	.5323	125.6675
L09	.8645	22.4075
L10	.7828	39.6723
L11	.9656	5.0874
L12	.9258	11.4614
L13	.8093	33.6870
L14	.8499	25.2467
A01	.8760	20.2428
A02	.7007	61.0888
A03	.7965	36.5390
A04	.9666	4.9448
A05	.7617	44.7477
A06	.9570	6.4183
A07	.5606	112.0998
W01	.5699	107.9253
W02	.4366	184.5590
W03	.8966	16.4841
W04	.9009	15.7286
W05	.7877	38.5475
W06	.6419	79.7673
W07	.4879	150.0955
M01	.5622	111.3375
M02	.8851	18.5615
M03	.5737	106.2736
M04	.8673	21.8826
M05	.5044	140.5242
M06	.4721	159.9219
M07	.7013	60.9018
M08	.7136	57.3821
H01	.2803	367.2467
H02	.7574	45.7921
H03	.1616	741.6766
H04	.2848	359.0935
H05	.6538	75.7201
H06	.7340	51.8237
G01	.6863	65.3586
G02	.6294	84.1949
G03	.7781	40.7697
G04	.7826	39.7127
G05	.7334	51.9798
G06	.9327	10.3232

WITH 15 AND 2145 DEGREES OF FREEDOM



CLUSTER CLASSIFICATION - SAMPLE D

GROUP	VARIABLES										SIZE										
	S01	S02	S03	S04	S05	L01	L02	L03	L04	L05											
1	0.3169E	04	0.2731E	04	0.3335E	02	0.2736E	01	0.4283E	01	0.3408E	02	0.6780E	01	0.2771E	00	0.4914E	-01	0.1167E	02	332
2	0.1740E	03	0.5849E	03	0.4495E	01	0.1056E	01	0.1158E	01	0.1762E	02	0.7085E	01	0.3363E	00	0.8841E	00	0.7893E	01	190
3	0.7775E	03	0.6466E	03	0.1497E	01	0.1202E	01	0.1502E	01	0.2559E	02	0.3747E	01	0.1612E	01	0.1520E	01	0.6980E	01	245
4	0.3465E	04	0.2866E	04	0.1174E	02	0.2760E	01	0.2216E	01	0.2320E	01	0.4878E	01	0.1245E	01	0.1485E	01	0.1246E	02	111
5	0.3751E	04	0.5523E	04	0.1154E	02	0.2534E	01	0.5291E	01	0.4624E	02	0.2805E	02	0.6299E	01	0.1433E	01	0.8350E	01	127
6	0.1042E	04	0.1694E	04	0.1474E	02	0.2296E	01	0.2830E	01	0.3909E	02	0.3625E	01	0.6582E	00	0.2708E	00	0.3332E	02	165
7	0.1336E	04	0.1208E	04	0.1517E	02	0.1601E	01	0.2051E	01	0.1808E	02	0.7430E	01	0.2345E	00	0.4806E	00	0.7442E	01	433
8	0.1212E	03	0.1026E	03	0.1031E	00	0.2156E	01	0.1448E	01	0.3992E	00	0.3245E	01	0.1000E	00	0.7903E	02	0.4432E	01	62
9	0.1660E	04	0.1547E	04	0.2137E	02	0.1548E	01	0.2614E	01	0.2330E	02	0.7331E	01	0.1595E	00	0.4151E	00	0.6012E	01	334
10	0.6780E	03	0.6216E	03	0.8746E	01	0.1268E	01	0.1744E	01	0.1952E	02	0.6922E	01	0.3606E	00	0.1225E	01	0.1020E	02	148
11	0.2087E	03	0.1542E	03	0.4791E	02	0.9100E	00	0.6944E	00	0.5623E	01	0.7524E	01	0.0000E	00	0.3049E	01	0.3549E	01	56
TOTAL	0.1757E	04	0.1522E	04	0.1322E	02	0.1905E	01	0.2545E	01	0.2545E	02	0.7543E	01	0.8193E	00	0.2986E	01	0.1019E	02	2101

GROUP	VARIABLES										SIZE										
	L06	L07	L08	L09	L10	L11	L12	L13	L14	A01											
1	0.5071E	00	0.3200E	00	0.4464E	02	0.1133E	01	0.5274E	00	0.0200E	00	0.1002E	02	0.5422E	-01	0.2380E	00	0.6245E	00	332
2	0.2746E	01	0.1106E	01	0.4648E	02	0.3591E	02	0.1225E	01	0.3115E	01	0.1245E	02	0.6474E	-01	0.1263E	00	0.7137E	01	190
3	0.5603E	01	0.1401E	01	0.7781E	01	0.1884E	02	0.2803E	02	0.5637E	01	0.8611E	01	0.2287E	00	0.4933E	-01	0.1447E	02	223
4	0.3786E	01	0.3918E	00	0.2573E	02	0.9534E	01	0.1729E	02	0.3918E	01	0.1227E	02	0.2072E	00	0.9009E	-01	0.3586E	01	111
5	0.6352E	00	0.3800E	00	0.8066E	01	0.6551E	-01	0.4440E	00	0.1023E	00	0.5966E	01	0.1575E	-01	0.4409E	00	0.4930E	01	127
6	0.7973E	00	0.5089E	00	0.1043E	02	0.6550E	01	0.4749E	01	0.2058E	01	0.1016E	02	0.4570E	00	0.2166E	00	0.4930E	01	165
7	0.4254E	00	0.7573E	00	0.6174E	02	0.9070E	00	0.1701E	01	0.1024E	01	0.7040E	01	0.4619E	-01	0.2818E	00	0.3723E	01	433
8	0.2322E	01	0.9984E	00	0.2549E	01	0.0000E	00	0.7012E	01	0.1463E	01	0.1572E	02	0.1613E	-01	0.0000E	00	0.2419E	01	62
9	0.4119E	00	0.4822E	00	0.5940E	02	0.3121E	00	0.2144E	01	0.7262E	00	0.5260E	01	0.5689E	-01	0.2635E	00	0.2654E	01	334
10	0.1152E	01	0.1290E	01	0.4813E	02	0.4263E	01	0.6837E	01	0.1564E	01	0.7607E	01	0.8784E	-01	0.1824E	00	0.2235E	01	148
11	0.0000E	00	0.3158E	02	0.3763E	02	0.4082E	01	0.6945E	01	0.5113E	01	0.2617E	02	0.0000E	00	0.2777E	-01	0.6250E	-01	56
TOTAL	0.1284E	01	0.1243E	01	0.3988E	02	0.6017E	01	0.6884E	01	0.1913E	01	0.8910E	01	0.1143E	00	0.2300E	00	0.4236E	01	2101

GROUP	VARIABLES										SIZE										
	A02	A03	A04	A05	A06	A07	W01	W02	W03	W04											
1	0.4312E	02	0.8451E	02	0.5217E	00	0.1658E	02	0.4316E	01	0.1327E	01	0.1405E	01	0.6076E	02	0.1394E	02	0.2011E	02	332
2	0.2440E	02	0.2070E	02	0.7423E	01	0.9286E	01	0.5904E	01	0.0651E	00	0.3007E	01	0.9309E	02	0.5263E	00	0.6000E	01	190
3	0.4260E	01	0.4523E	01	0.1467E	01	0.1888E	02	0.3016E	01	0.4604E	00	0.3612E	01	0.7976E	02	0.5394E	01	0.9609E	01	223
4	0.1432E	02	0.1522E	02	0.4072E	01	0.1076E	02	0.2685E	01	0.4127E	00	0.1824E	01	0.3990E	01	0.2180E	01	0.1281E	02	111
5	0.1507E	02	0.2401E	02	0.6947E	01	0.7321E	01	0.8648E	01	0.4206E	00	0.1177E	01	0.6950E	02	0.1068E	02	0.1724E	02	127
6	0.2832E	02	0.4265E	02	0.3945E	01	0.1320E	02	0.4544E	01	0.7988E	00	0.3109E	01	0.8623E	02	0.1891E	02	0.1389E	02	165
7	0.4378E	02	0.2751E	02	0.3739E	01	0.1056E	02	0.2833E	01	0.1470E	01	0.2459E	01	0.9468E	02	0.8574E	01	0.4073E	01	433
8	0.0000E	00	0.1613E	01	0.0000E	00	0.2449E	01	0.3226E	01	0.2803E	00	0.2695E	02	0.8287E	02	0.1585E	02	0.2532E	02	62
9	0.4255E	02	0.2806E	02	0.2914E	01	0.1575E	02	0.1882E	01	0.1661E	01	0.1805E	01	0.9474E	02	0.4201E	01	0.2454E	02	334
10	0.3499E	02	0.1904E	02	0.6474E	00	0.1329E	02	0.5475E	01	0.1379E	01	0.4300E	01	0.8838E	02	0.7905E	01	0.113E	02	148
11	0.3973E	01	0.1282E	01	0.3789E	01	0.6431E	02	0.2379E	02	0.2486E	02	0.1415E	02	0.9538E	02	0.2063E	01	0.1643E	02	56
TOTAL	0.3081E	02	0.2426E	02	0.3045E	01	0.1390E	02	0.4218E	01	0.1511E	01	0.3332E	01	0.8487E	02	0.8326E	01	0.1571E	02	2101



CLUSTER CLASSIFICATION - SAMPLE D

GROUP	VARIABLES											SIZE	
	W05	W06	W07	M01	M02	M03	M04	M05	M06	M07			
1	0.2120E	02 0.3310E	02 0.1165E	02 0.9548E	00 0.1245E	00 0.5602E	00 0.7078E	00 0.7771E	00 0.2410E	-03 0.0000E	00 0.0000E	00 0.0000E	332
2	0.5552E	01 0.6582E	01 0.8137E	02 0.1684E	00 0.6872E	-01 0.2105E	-01 0.5895E	00 0.2832E	-01 0.1188E	-01 0.4211E	-01 0.4211E	-01 0.4211E	190
3	0.3022E	02 0.4701E	02 0.7765E	01 0.2735E	00 0.2382E	-01 0.2691E	-01 0.5830E	00 0.0000E	00 0.1244E	00 0.3408E	00 0.3408E	00 0.3408E	223
4	0.1569E	02 0.3666E	02 0.1014E	02 0.3694E	00 0.1582E	00 0.1712E	00 0.5676E	00 0.1822E	00 0.1172E	00 0.1171E	00 0.1171E	00 0.1171E	111
5	0.2167E	02 0.4322E	02 0.7186E	01 0.8661E	00 0.5212E	-01 0.6063E	00 0.8698E	00 0.1654E	00 0.6630E	-01 0.7874E	-02 0.7874E	-02 0.7874E	127
6	0.1545E	02 0.4680E	02 0.4945E	02 0.4945E	00 0.4000E	00 0.1697E	00 0.7455E	00 0.1273E	00 0.2018E	-01 0.2424E	-01 0.2424E	-01 0.2424E	165
7	0.3659E	01 0.8195E	02 0.1742E	01 0.3926E	00 0.5312E	-01 0.3002E	-01 0.7506E	00 0.2794E	00 0.1600E	-01 0.4619E	-02 0.4619E	-02 0.4619E	433
8	0.1194E	02 0.4079E	02 0.6102E	01 0.9677E	-01 0.6129E	00 0.0000E	00 0.3710E	00 0.0000E	00 0.2943E	02 0.3226E	01 0.3226E	01 0.3226E	62
9	0.5921E	02 0.6028E	01 0.6023E	01 0.5689E	00 0.5988E	-01 0.9880E	-01 0.7605E	00 0.5982E	00 0.2991E	-01 0.5988E	-02 0.5988E	-02 0.5988E	334
10	0.2131E	02 0.4209E	02 0.1757E	02 0.2297E	00 0.7482E	-01 0.7432E	-01 0.6284E	00 0.1486E	00 0.7041E	-01 0.1551E	-01 0.1551E	-01 0.1551E	148
11	0.1991E	02 0.5185E	02 0.9722E	01 0.8333E	-01 0.1111E	00 0.0000E	00 0.3611E	00 0.0000E	00 0.9322E	00 0.2778E	-01 0.2778E	-01 0.2778E	36
TOTAL	0.2214E	02 0.4078E	02 0.1589E	02 0.4859E	00 0.1356E	00 0.1745E	00 0.6867E	00 0.2772E	00 0.8950E	00 0.5137E	-01 0.5137E	-01 0.5137E	2161

GROUP	VARIABLES											SIZE	
	M08	M09	M10	M11	M12	M13	M14	M15	M16	M17	M18		
1	0.2245E	01 0.1000E	01 0.1882E	01 0.9970E	00 0.3012E	-02 0.5166E	02 0.6627E	-01 0.7849E	02 0.1887E	02 0.2641E	01 0.2641E	01 0.2641E	352
2	0.3552E	01 0.1000E	01 0.1055E	01 0.9474E	00 0.5243E	-01 0.7012E	02 0.1158E	00 0.7689E	02 0.2059E	02 0.5263E	00 0.5263E	00 0.5263E	190
3	0.6412E	01 0.1000E	01 0.1150E	01 0.9821E	00 0.1764E	-01 0.5009E	02 0.5605E	00 0.9378E	02 0.4996E	01 0.1223E	01 0.1223E	01 0.1223E	223
4	0.2045E	01 0.1441E	00 0.1378E	01 0.9009E	-02 0.1351E	00 0.5234E	02 0.1802E	-01 0.7350E	02 0.1230E	02 0.1426E	02 0.1426E	02 0.1426E	111
5	0.5712E	01 0.1000E	01 0.2000E	01 0.1000E	01 0.0000E	00 0.5066E	02 0.2087E	00 0.2449E	02 0.7551E	02 0.0000E	00 0.0000E	00 0.0000E	127
6	0.2779E	01 0.1000E	01 0.1012E	01 0.1000E	01 0.0000E	00 0.5299E	02 0.4242E	-01 0.4361E	02 0.2806E	02 0.2833E	02 0.2833E	02 0.2833E	165
7	0.5112E	01 0.1000E	01 0.1219E	01 0.1000E	01 0.0000E	00 0.5509E	02 0.3002E	00 0.5973E	02 0.4158E	02 0.1039E	01 0.1039E	01 0.1039E	433
8	0.1445E	02 0.9859E	00 0.1094E	01 0.9194E	00 0.6482E	-01 0.4860E	02 0.1452E	00 0.5738E	02 0.3886E	02 0.1408E	01 0.1408E	01 0.1408E	62
9	0.5058E	01 0.1000E	01 0.1699E	01 0.1000E	01 0.0000E	00 0.3872E	02 0.3413E	00 0.3005E	02 0.6932E	02 0.6275E	00 0.6275E	00 0.6275E	334
10	0.5565E	01 0.9865E	01 0.1034E	01 0.0000E	00 0.9845E	00 0.5551E	02 0.1486E	00 0.6850E	02 0.2845E	02 0.2986E	01 0.2986E	01 0.2986E	148
11	0.5460E	01 0.1000E	01 0.1278E	01 0.8889E	00 0.1111E	00 0.5172E	02 0.6111E	00 0.8336E	02 0.1664E	02 0.0000E	00 0.0000E	00 0.0000E	36
TOTAL	0.3819E	01 0.9547E	00 0.1284E	01 0.8695E	00 0.8515E	-01 0.5206E	02 0.2318E	00 0.6116E	02 0.3482E	02 0.4021E	01 0.4021E	01 0.4021E	2161

GROUP	VARIABLES											SIZE	
	G04	G05	G06	G07	G08	G09	G10	G11	G12	G13	G14		
1	0.2048E	00 0.2982E	01 0.4218E	-01 0.4218E	-01 0.4218E	-01 0.4218E	-01 0.4218E	-01 0.4218E	-01 0.4218E	-01 0.4218E	-01 0.4218E	-01 0.4218E	332
2	0.1158E	00 0.9947E	00 0.3084E	-01 0.3084E	-01 0.3084E	-01 0.3084E	-01 0.3084E	-01 0.3084E	-01 0.3084E	-01 0.3084E	-01 0.3084E	-01 0.3084E	190
3	0.7175E	01 0.9462E	00 0.1794E	-01 0.1794E	-01 0.1794E	-01 0.1794E	-01 0.1794E	-01 0.1794E	-01 0.1794E	-01 0.1794E	-01 0.1794E	-01 0.1794E	223
4	0.2523E	00 0.8829E	00 0.1351E	00 0.1351E	00 0.1351E	00 0.1351E	00 0.1351E	00 0.1351E	00 0.1351E	00 0.1351E	00 0.1351E	00 0.1351E	111
5	0.6614E	00 0.2031E	01 0.2077E	00 0.2077E	00 0.2077E	00 0.2077E	00 0.2077E	00 0.2077E	00 0.2077E	00 0.2077E	00 0.2077E	00 0.2077E	127
6	0.4242E	-01 0.6564E	00 0.2242E	00 0.2242E	00 0.2242E	00 0.2242E	00 0.2242E	00 0.2242E	00 0.2242E	00 0.2242E	00 0.2242E	00 0.2242E	165
7	0.2633E	00 0.1471E	01 0.5312E	-01 0.5312E	-01 0.5312E	-01 0.5312E	-01 0.5312E	-01 0.5312E	-01 0.5312E	-01 0.5312E	-01 0.5312E	-01 0.5312E	433
8	0.6290E	00 0.1758E	01 0.3226E	-01 0.3226E	-01 0.3226E	-01 0.3226E	-01 0.3226E	-01 0.3226E	-01 0.3226E	-01 0.3226E	-01 0.3226E	-01 0.3226E	62
9	0.2150E	00 0.1515E	01 0.5988E	-01 0.5988E	-01 0.5988E	-01 0.5988E	-01 0.5988E	-01 0.5988E	-01 0.5988E	-01 0.5988E	-01 0.5988E	-01 0.5988E	334
10	0.1014E	00 0.1291E	01 0.8108E	-01 0.8108E	-01 0.8108E	-01 0.8108E	-01 0.8108E	-01 0.8108E	-01 0.8108E	-01 0.8108E	-01 0.8108E	-01 0.8108E	148
11	0.3611E	00 0.8889E	00 0.2222E	00 0.2222E	00 0.2222E	00 0.2222E	00 0.2222E	00 0.2222E	00 0.2222E	00 0.2222E	00 0.2222E	00 0.2222E	36
TOTAL	0.2212E	00 0.1539E	01 0.8191E	-01 0.8191E	-01 0.8191E	-01 0.8191E	-01 0.8191E	-01 0.8191E	-01 0.8191E	-01 0.8191E	-01 0.8191E	-01 0.8191E	2161



WILKS LAMBDA (U-STATISTIC) AND UNIVARIATE F-RATIO

VARIABLE	WILKS LAMBDA	F
S01	.8060	51.7572
S02	.7946	55.5656
S03	.7906	56.9416
S04	.7801	60.5975
S05	.6402	120.8068
L01	.8253	45.5114
L02	.7685	64.7534
L03	.9229	17.9660
L04	.2573	620.6626
L05	.8306	43.8369
L06	.9668	7.3732
L07	.6662	107.7089
L08	.6357	123.1860
L09	.8591	35.2614
L10	.8354	42.3471
L11	.9672	7.2932
L12	.9375	14.3442
L13	.8408	40.7040
L14	.9112	20.9641
A01	.9371	14.4266
A02	.7455	73.3932
A03	.8250	45.5931
A04	.9781	4.8183
A05	.8959	24.9777
A06	.9570	9.6656
A07	.5467	178.2923
W01	.5912	148.6594
W02	.5022	213.1286
W03	.9125	20.6162
W04	.9144	20.1140
W05	.7198	83.7047
W06	.5730	160.1983
W07	.4399	273.7749
M01	.7160	85.2614
M02	.8620	34.4326
M03	.6856	98.5747
M04	.9445	12.6382
M05	.6912	96.0528
M06	.4897	224.0786
M07	.7882	57.7811
M08	.8760	30.4366
H01	.1780	993.0384
H02	.8287	44.4325
H03	.0960	2024.2971
H04	.2177	772.6993
H05	.6060	139.7775
H06	.8453	39.3500
G01	.7307	79.2337
G02	.7053	89.8271
G03	.8303	43.9312
G04	.8628	34.2026
G05	.7852	58.8020
G06	.9420	13.2450

WITH 10 AND 2150 DEGREES OF FREEDOM

APPENDIX K

Three Population Classifications



TOTAL NO. OF OBSERVATIONS = 21745

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.2015E 04	0.7427E 04	0.2000E 01	0.7513E 06
S02	0.1655E 04	0.4397E 04	0.1000E 01	0.4131E 06
S03	0.1180E 02	0.9365E 02	0.0000E 00	0.1096E 05
S04	0.1911E 01	0.2164E 01	0.0000E 00	0.1346E 03
S05	0.2517E 01	0.2765E 01	0.0000E 00	0.2400E 02
L01	0.2517E 02	0.2559E 02	0.0000E 00	0.1000E 03
L02	0.7538E 01	0.1123E 02	0.0000E 00	0.1000E 03
L03	0.6142E 00	0.5999E 01	0.0000E 00	0.1000E 03
L04	0.5274E 01	0.1568E 02	0.0000E 00	0.1000E 03
L05	0.6277E 01	0.1519E 02	0.0000E 00	0.1000E 03
L06	0.1125E 01	0.6128E 01	0.0000E 00	0.1000E 03
L07	0.1538E 01	0.5158E 01	0.0000E 00	0.1000E 03
L08	0.4078E 02	0.5477E 02	0.0000E 00	0.1000E 03
L09	0.4254E 01	0.1598E 02	0.0000E 00	0.1000E 03
L10	0.6219E 01	0.1977E 02	0.0000E 00	0.1000E 03
L11	0.2077E 01	0.6762E 01	0.0000E 00	0.5922E 02
L12	0.9423E 01	0.1561E 02	0.0000E 00	0.9472E 02
L13	0.1115E 00	0.5143E 00	0.0000E 00	0.1000E 01
L14	0.2277E 00	0.4519E 00	0.0000E 00	0.1000E 01
A01	0.4376E 01	0.1177E 02	0.0000E 00	0.1000E 03
A02	0.5049E 02	0.2965E 02	0.0000E 00	0.1000E 03
A03	0.6459E 02	0.2652E 02	0.0000E 00	0.1000E 03
A04	0.5177E 01	0.1458E 02	0.0000E 00	0.1000E 03
A05	0.1446E 02	0.2369E 02	0.0000E 00	0.1000E 03
A06	0.6113E 01	0.1581E 02	0.0000E 00	0.9645E 03
A07	0.1956E 01	0.1581E 02	0.0000E 00	0.9645E 03
L01	0.3755E 01	0.1355E 02	0.1422E -03	0.0042E 03
L02	0.6425E 02	0.2222E 02	0.0000E 00	0.1000E 03
L03	0.6525E 01	0.1764E 02	0.0000E 00	0.1000E 03
L04	0.1413E 02	0.2508E 02	0.0000E 00	0.1000E 03
L05	0.2154E 02	0.5338E 02	0.0000E 00	0.1000E 03
L06	0.4169E 02	0.5991E 02	0.0000E 00	0.1000E 03
L07	0.1327E 02	0.2788E 02	0.0000E 00	0.1000E 03
L08	0.4844E 00	0.4494E 00	0.0000E 00	0.1000E 01
L09	0.1377E 00	0.5584E 00	0.0000E 00	0.1000E 01
L10	0.1775E 00	0.5328E 00	0.0000E 00	0.1000E 01
L11	0.6866E 00	0.4539E 00	0.0000E 00	0.1000E 01
L12	0.2819E 00	0.4598E 00	0.0000E 00	0.1000E 01
L13	0.1045E 01	0.8110E 01	0.0000E 00	0.1000E 03
L14	0.4762E -01	0.2137E 00	0.0000E 00	0.1000E 01
L15	0.3977E 01	0.9162E 01	0.0000E 00	0.5000E 03
L16	0.9477E 00	0.2222E 00	0.0000E 00	0.1000E 01
L17	0.1254E 01	0.5945E 00	0.1000E 01	0.4000E 01
L18	0.6722E 00	0.5538E 00	0.0000E 00	0.1000E 01
L19	0.7576E -01	0.2944E 00	0.0000E 00	0.1000E 01
L20	0.5151E 02	0.1244E 00	0.1500E 02	0.9400E 02
L21	0.2170E 00	0.4115E 00	0.0000E 00	0.1000E 01
L22	0.6167E 02	0.5162E 02	0.0000E 00	0.1000E 03
L23	0.4771E 01	0.2027E 02	0.0000E 00	0.1000E 03
L24	0.2200E 00	0.4142E 00	0.0000E 00	0.1000E 01
L25	0.1515E 01	0.1508E 01	0.0000E 00	0.1000E 01
L26	0.6856E -01	0.3179E 00	0.0000E 00	0.5000E 01

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

3346 4240 4411 2671 3093 1982

CLASS NO. OF OBSERVATIONS = 1130

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.2267E 04	0.3053E 04	0.2700E 02	0.5740E 05
S02	0.2100E 04	0.3554E 04	0.2000E 02	0.5190E 05
S03	0.9359E 01	0.2706E 02	0.0000E 00	0.4538E 03
S04	0.1017E 01	0.2034E 01	0.1091E -01	0.2519E 02
S05	0.2657E 01	0.2091E 01	0.0000E 00	0.1900E 02
L01	0.8078E 02	0.1134E 02	0.6662E 02	0.1000E 03
L02	0.5103E 01	0.7916E 01	0.0000E 00	0.3353E 02
L03	0.9165E 00	0.3639E 01	0.0000E 00	0.3260E 02
L04	0.9957E -01	0.1267E 01	0.0000E 00	0.3353E 02
L05	0.4988E 01	0.7896E 01	0.0000E 00	0.3353E 02
L06	0.9093E 00	0.3506E 01	0.0000E 00	0.3353E 02
L07	0.7339E 00	0.2439E 01	0.0000E 00	0.3269E 02
L08	0.4037E 01	0.6930E 01	0.0000E 00	0.3353E 02
L09	0.1344E 01	0.4923E 01	0.0000E 00	0.3353E 02
L10	0.1090E 01	0.4120E 01	0.0000E 00	0.3353E 02
L11	0.1921E 01	0.8915E 01	0.0000E 00	0.8096E 02
L12	0.6183E 01	0.1097E 02	0.0000E 00	0.9500E 02
L13	0.1159E 00	0.3201E 00	0.0000E 00	0.1000E 01
L14	0.1451E 00	0.3522E 00	0.0000E 00	0.1000E 01
A01	0.1252E 02	0.2598E 02	0.0000E 00	0.1000E 03
A02	0.1270E 02	0.2471E 02	0.0000E 00	0.1000E 03
A03	0.1668E 02	0.2795E 02	0.0000E 00	0.1000E 03
A04	0.5988E 01	0.1607E 02	0.0000E 00	0.1000E 03
A05	0.1538E 02	0.2575E 02	0.0000E 00	0.1000E 03
A06	0.8208E 01	0.2389E 02	0.0000E 00	0.1000E 03
A07	0.7386E 00	0.2152E 01	0.0000E 00	0.3250E 02
L01	0.2141E 01	0.5327E 01	0.5141E -01	0.4706E 02
L02	0.7323E 02	0.5360E 02	0.0000E 00	0.1000E 03
L03	0.7229E 01	0.1729E 02	0.0000E 00	0.1000E 03
L04	0.1357E 02	0.2506E 02	0.0000E 00	0.1000E 03
L05	0.2230E 02	0.3425E 02	0.0000E 00	0.1000E 03
L06	0.4003E 02	0.4914E 02	0.0000E 00	0.1000E 03
L07	0.3131E 02	0.2975E 02	0.0000E 00	0.1000E 03
L08	0.4266E 00	0.4981E 00	0.0000E 00	0.1000E 01
L09	0.8230E -01	0.2748E 00	0.0000E 00	0.1000E 01
L10	0.1903E 00	0.3925E 00	0.0000E 00	0.1000E 01
L11	0.7867E 00	0.4096E 00	0.0000E 00	0.1000E 01
L12	0.7168E -01	0.2280E 00	0.0000E 00	0.1000E 01
L13	0.3922E -01	0.7088E 00	0.0000E 00	0.2268E 02
L14	0.1301E 00	0.3364E 00	0.0000E 00	0.1000E 01
L15	0.4154E 01	0.6274E 01	0.0000E 00	0.6667E 02
L16	0.9257E 00	0.2923E 00	0.0000E 00	0.1000E 01
L17	0.1276E 01	0.6281E 00	0.1000E 01	0.4000E 01
L18	0.8687E 00	0.3584E 00	0.0000E 00	0.1000E 01
L19	0.7659E -01	0.2666E 00	0.0000E 00	0.1000E 01
L20	0.3166E 02	0.1244E 02	0.1700E 02	0.9100E 02
L21	0.2451E 00	0.4302E 00	0.0000E 00	0.1000E 01
L22	0.8056E 02	0.4358E 02	0.0000E 00	0.1000E 03
L23	0.5187E 02	0.4103E 02	0.0000E 00	0.1000E 03
L24	0.7579E 01	0.2326E 02	0.0000E 00	0.1000E 03
L25	0.1655E 00	0.5716E 00	0.0000E 00	0.1000E 01
L26	0.9406E 00	0.1398E 01	0.0000E 00	0.2000E 01
L27	0.1071E 00	0.3259E 00	0.0000E 00	0.4000E 01

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

165 123 151 141 535 15

CLASS NO. OF OBSERVATIONS = 390

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.5608E 04	0.5957E 04	0.1000E 02	0.7355E 05
S02	0.2966E 04	0.3199E 04	0.0000E 01	0.4656E 05
S03	0.7495E 01	0.2159E 02	0.0000E 00	0.3542E 03
S04	0.2535E 01	0.4318E 01	0.1220E 00	0.7165E 02
S05	0.2000E 01	0.3784E 01	0.0000E 00	0.3500E 02
L01	0.4636E 02	0.6527E 01	0.0000E 00	0.6517E 02
L02	0.4181E 02	0.6997E 01	0.5535E 02	0.6865E 02
L03	0.1330E 01	0.3460E 01	0.0000E 00	0.1774E 02
L04	0.6600E 00	0.1000E 01	0.0000E 00	0.2500E 02
L05	0.5167E 01	0.6399E 01	0.0000E 00	0.3353E 02
L06	0.5531E -01	0.6746E 00	0.0000E 00	0.7179E 01
L07	0.7439E 00	0.6247E 00	0.0000E 00	0.2174E 02
L08	0.5363E 01	0.6339E 01	0.0000E 00	0.5166E 02
L09	0.5870E 00	0.2688E 01	0.0000E 00	0.5300E 02
L10	0.4833E 00	0.3177E 01	0.0000E 00	0.5335E 02
L11	0.9179E 00	0.2155E 01	0.0000E 00	0.8125E 02
L12	0.7724E 01	0.1181E 02	0.0000E 00	0.8125E 02
L13	0.5759E -01	0.1902E 00	0.0000E 00	0.5166E 02
L14	0.4066E 00	0.5911E 00	0.0000E 00	0.1000E 01
L15	0.4475E 01	0.1741E 02	0.0000E 00	0.1000E 03
L16	0.1665E 02	0.2774E 02	0.0000E 00	0.1000E 03
L17	0.2174E 02	0.5253E 02	0.0000E 00	0.1000E 03
L18	0.4866E 01	0.1978E 02	0.0000E 00	0.1000E 03
L19	0.1550E 02	0.3252E 02	0.0000E 00	0.1000E 03
L20	0.7433E 01	0.5267E 02	0.0000E 00	0.1000E 03
L21	0.7123E 00	0.2345E 01	0.0000E 00	0.2870E 02
L22	0.1918E 00	0.5398E 01	0.6614E -01	0.5600E 02
L23	0.6686E 02	0.3378E 02	0.0000E 00	0.1000E 03
L24	0.9955E 01	0.1637E 02	0.0000E 00	0.1000E 03
L25	0.1584E 02	0.2934E 02	0.0000E 00	0.1000E 03
L26	0.2264E 02	0.3140E 02	0.0000E 00	0.1000E 03
L27	0.4094E 02	0.3978E 02	0.0000E 00	0.1000E 03
L28	0.9621E 01	0.2490E 02	0.0000E 00	0.1000E 01
L29	0.7093E 00	0.4347E 00	0.0000E 00	0.1000E 01
L30	0.7018E -01	0.2554E 00	0.0000E 00	0.1000E 01
L31	0.4712E 00	0.4992E 00	0.0000E 00	0.1000E 01
L32	0.9025E 00	0.2777E 00	0.0000E 00	0.1000E 01
L33	0.1078E 00	0.5103E 00	0.0000E 00	0.1000E 01
L34	0.2565E -01	0.4113E 00	0.0000E 00	0.7652E 01
L35	0.5309E -01	0.1349E 00	0.0000E 00	0.1000E 01
L36	0.5240E 01	0.8488E 01	0.0000E 00	0.7143E 02
L37	0.9323E 00	0.2512E 00	0.0000E 00	0.1000E 01
L38	0.1910E 01	0.8624E 00	0.1000E 01	0.4000E 01
L39	0.8847E 00	0.3194E 00	0.0000E 00	0.1000E 01
L40	0.4762E -01	0.2150E 00	0.0000E 00	0.1000E 01
L41	0.5070E 02	0.1184E 02	0.2200E 02	0.6700E 02
L42	0.1654E 00	0.3716E 00	0.0000E 00	0.1000E 01
L43	0.4310E 02	0.4545E 02	0.0000E 00	0.1000E 03
L44	0.5590E 02	0.4355E 02	0.0000E 00	0.1000E 03
L45	0.1003E 01	0.9968E 01	0.0000E 00	0.1000E 03
L46	0.6566E 00	0.4744E 00	0.0000E 00	0.1000E 01
L47	0.1942E 01	0.1474E 01	0.0000E 00	0.4000E 01
L48	0.1604E 00	0.4055E 00	0.0000E 00	0.5000E 01

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

11 34 261 52 41 0



STANDARD CLASSIFICATION - POPULATION

CLASS 3  
NO. OF OBSERVATIONS = 4733

Table with 7 columns: VARIABLE, MEAN, STA. DEV., MINIMUM, MAXIMUM, and two unlabeled columns. Rows include variables S01 through S66.

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

775 810 626 646 1535 343

CLASS 4  
NO. OF OBSERVATIONS = 556

Table with 7 columns: VARIABLE, MEAN, STA. DEV., MINIMUM, MAXIMUM, and two unlabeled columns. Rows include variables S01 through S66.

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

39 59 340 72 21 25

CLASS 5  
NO. OF OBSERVATIONS = 323

Table with 7 columns: VARIABLE, MEAN, STA. DEV., MINIMUM, MAXIMUM, and two unlabeled columns. Rows include variables S01 through S66.

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

225 0 0 67 167 64



CLASS 6  
NO. OF OBSERVATIONS = 1168

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.8571E-03	0.3212E-04	0.4000E-01	0.8420E-03
S02	0.5944E-03	0.1514E-04	0.45000E-01	0.2160E-03
S03	0.2744E-01	0.2114E-02	0.0000E-01	0.3242E-03
S04	0.1700E-01	0.26740E-01	0.1250E-01	0.6124E-02
S05	0.1041E-01	0.1253E-01	0.0000E-01	0.13500E-02
L01	0.1844E-01	0.5772E-01	0.0000E-01	0.3535E-02
L02	0.5056E-03	0.2463E-01	0.0000E-01	0.3151E-02
L03	0.6843E-01	0.1442E-01	0.0000E-01	0.3333E-02
L04	0.6427E-01	0.3534E-01	0.0000E-01	0.3535E-02
L05	0.1022E-01	0.2329E-01	0.0000E-01	0.3535E-02
L06	0.3244E-01	0.2745E-01	0.0000E-01	0.3535E-02
L07	0.1595E-01	0.4351E-01	0.0000E-01	0.3535E-02
L08	0.1665E-01	0.2153E-02	0.0000E-01	0.3535E-02
L09	0.2656E-01	0.1538E-02	0.0000E-01	0.3535E-02
L10	0.8254E-02	0.2234E-02	0.2041E-01	0.1000E-03
L11	0.5941E-01	0.1427E-02	0.0000E-01	0.9381E-02
L12	0.1145E-02	0.1351E-02	0.0000E-01	0.9941E-02
L13	0.2962E-01	0.1458E-01	0.0000E-01	0.1000E-01
L14	0.1494E-01	0.1513E-01	0.0000E-01	0.1000E-01
A01	0.6744E-01	0.2544E-02	0.0000E-01	0.1000E-03
A02	0.4152E-01	0.1729E-02	0.0000E-01	0.1000E-03
A03	0.4176E-01	0.1553E-02	0.0000E-01	0.1000E-03
A04	0.2654E-01	0.1514E-02	0.0000E-01	0.1000E-03
A05	0.7644E-01	0.2324E-02	0.0000E-01	0.1000E-03
A06	0.4154E-01	0.1514E-02	0.0000E-01	0.1000E-03
A07	0.4744E-01	0.1551E-01	0.0000E-01	0.1085E-03
A08	0.6853E-01	0.1233E-02	0.0474E-01	0.1796E-03
A09	0.5892E-02	0.3524E-02	0.0000E-01	0.1000E-03
A10	0.5504E-01	0.1924E-02	0.0000E-01	0.1000E-03
A11	0.4090E-01	0.2340E-02	0.0000E-01	0.1000E-03
A12	0.1845E-02	0.4554E-02	0.0000E-01	0.1000E-03
A13	0.4544E-02	0.4554E-02	0.0000E-01	0.1000E-03
A14	0.1747E-02	0.3524E-02	0.0000E-01	0.1000E-03
A15	0.1873E-01	0.1923E-01	0.0000E-01	0.1000E-01
A16	0.2444E-01	0.4234E-01	0.0000E-01	0.1000E-01
A17	0.7464E-02	0.8224E-01	0.0000E-01	0.1000E-01
A18	0.5814E-01	0.4552E-01	0.0000E-01	0.1000E-01
A19	0.2543E-03	0.3535E-01	0.0000E-01	0.1000E-01
A20	0.3764E-01	0.1394E-02	0.0000E-01	0.1000E-03
A21	0.1674E-01	0.3535E-02	0.0000E-01	0.1000E-01
A22	0.5015E-01	0.9702E-01	0.0000E-01	0.1055E-03
A23	0.8001E-01	0.3264E-01	0.0000E-01	0.1000E-01
A24	0.1214E-01	0.4570E-01	0.1000E-01	0.4000E-01
A25	0.2502E-01	0.4523E-01	0.0000E-01	0.1000E-01
A26	0.1292E-01	0.3534E-01	0.0000E-01	0.1000E-01
A27	0.5413E-02	0.1225E-02	0.2100E-02	0.6000E-02
A28	0.5361E-02	0.6724E-01	0.0000E-01	0.1000E-01
A29	0.4005E-02	0.2624E-02	0.0000E-01	0.1000E-03
A30	0.1042E-01	0.2624E-02	0.0000E-01	0.1000E-03
A31	0.4944E-01	0.2634E-02	0.0000E-01	0.1000E-03
A32	0.1644E-01	0.3510E-02	0.0000E-01	0.1000E-03
A33	0.3714E-01	0.1114E-01	0.0000E-01	0.4000E-01
A34	0.4963E-01	0.2254E-01	0.0000E-01	0.2000E-01

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

85 130 153 67 618 15

CLASS 7  
NO. OF OBSERVATIONS = 1466

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.1420E-04	0.1510E-04	0.1400E-02	0.1372E-03
S02	0.1253E-04	0.1320E-04	0.4000E-01	0.1105E-03
S03	0.1744E-02	0.1571E-02	0.1000E-01	0.1105E-03
S04	0.1532E-01	0.9390E-01	0.1250E-01	0.1140E-02
S05	0.1893E-01	0.1332E-01	0.0000E-01	0.8000E-01
L01	0.3850E-01	0.7600E-01	0.0000E-01	0.3190E-02
L02	0.2354E-01	0.4720E-01	0.0000E-01	0.3535E-02
L03	0.2174E-01	0.3274E-01	0.0000E-01	0.7166E-01
L04	0.9943E-01	0.9091E-01	0.0000E-01	0.1720E-02
L05	0.1044E-01	0.3544E-01	0.0000E-01	0.3162E-02
L06	0.1044E-01	0.1119E-01	0.0000E-01	0.2632E-02
L07	0.7367E-01	0.1532E-01	0.0000E-01	0.3000E-05
L08	0.9171E-02	0.1354E-02	0.6601E-02	0.1000E-05
L09	0.2260E-01	0.1454E-01	0.0000E-01	0.2090E-02
L10	0.5169E-01	0.2211E-01	0.0000E-01	0.2652E-02
L11	0.1429E-01	0.7247E-01	0.0000E-01	0.8935E-02
L12	0.8972E-01	0.1500E-02	0.0000E-01	0.8692E-02
L13	0.6753E-01	0.2509E-01	0.0000E-01	0.1000E-01
L14	0.1132E-01	0.1639E-01	0.0000E-01	0.1000E-01
A01	0.1394E-01	0.5482E-01	0.3263E-02	0.2632E-02
A02	0.7844E-02	0.1154E-02	0.6607E-02	0.1000E-03
A03	0.1631E-02	0.1074E-02	0.0000E-01	0.3535E-02
A04	0.6924E-03	0.2234E-01	0.0000E-01	0.3105E-02
A05	0.2114E-01	0.5194E-01	0.0000E-01	0.3535E-02
A06	0.6023E-02	0.2983E-01	0.0000E-01	0.3164E-02
A07	0.1427E-01	0.934E-01	0.5428E-01	0.1200E-02
A08	0.2164E-01	0.2259E-01	0.2513E-01	0.2679E-02
A09	0.9141E-02	0.2123E-02	0.0000E-01	0.1000E-03
A10	0.7632E-01	0.1737E-02	0.0000E-01	0.1000E-03
A11	0.1409E-02	0.2754E-02	0.0000E-01	0.1000E-03
A12	0.2293E-02	0.3551E-02	0.0000E-01	0.1000E-03
A13	0.4210E-02	0.3944E-02	0.0000E-01	0.1000E-03
A14	0.1323E-02	0.2814E-02	0.0000E-01	0.1000E-03
A15	0.4464E-01	0.4272E-01	0.0000E-01	0.1000E-01
A16	0.9072E-01	0.2472E-01	0.0000E-01	0.1000E-01
A17	0.5000E-01	0.1704E-01	0.0000E-01	0.1000E-01
A18	0.6504E-01	0.4767E-01	0.0000E-01	0.1000E-01
A19	0.5820E-01	0.4559E-01	0.0000E-01	0.1000E-01
A20	0.9587E-02	0.2125E-01	0.0000E-01	0.6619E-01
A21	0.2044E-02	0.4519E-01	0.0000E-01	0.1000E-01
A22	0.2521E-01	0.1394E-01	0.0000E-01	0.3226E-02
A23	0.9744E-01	0.1564E-01	0.0000E-01	0.1000E-01
A24	0.1504E-01	0.3590E-01	0.1000E-01	0.4000E-01
A25	0.8604E-01	0.3461E-01	0.0000E-01	0.1000E-01
A26	0.1139E-01	0.3172E-01	0.0000E-01	0.1000E-01
A27	0.2184E-02	0.1274E-02	0.1800E-02	0.9100E-02
A28	0.2534E-02	0.4535E-02	0.0000E-01	0.1000E-01
A29	0.4559E-02	0.4535E-02	0.0000E-01	0.1000E-03
A30	0.6125E-01	0.7310E-01	0.0000E-01	0.1000E-03
A31	0.5636E-01	0.4310E-01	0.0000E-01	0.1000E-01
A32	0.1664E-01	0.1355E-01	0.0000E-01	0.4000E-01
A33	0.5956E-01	0.2018E-01	0.0000E-01	0.2000E-01

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

269 323 571 141 153 9

CLASS 8  
NO. OF OBSERVATIONS = 2970

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.2495E-04	0.7500E-04	0.9000E-01	0.2696E-04
S02	0.2027E-04	0.2391E-04	0.4000E-01	0.2391E-04
S03	0.2364E-02	0.4064E-02	0.1000E-01	0.2391E-04
S04	0.1734E-01	0.1142E-01	0.2907E-01	0.1441E-04
S05	0.2174E-01	0.1327E-01	0.0000E-01	0.1000E-02
L01	0.7450E-01	0.5712E-01	0.0000E-01	0.3535E-02
L02	0.2245E-01	0.3769E-01	0.0000E-01	0.3535E-02
L03	0.2333E-01	0.4592E-01	0.0000E-01	0.1792E-02
L04	0.8930E-01	0.1335E-01	0.0000E-01	0.2443E-02
L05	0.1758E-01	0.4164E-01	0.0000E-01	0.3123E-02
L06	0.2107E-01	0.1534E-01	0.0000E-01	0.2032E-02
L07	0.2765E-01	0.1244E-01	0.0000E-01	0.2500E-02
L08	0.6087E-02	0.1172E-02	0.6601E-02	0.1000E-03
L09	0.2541E-01	0.1344E-01	0.0000E-01	0.2712E-02
L10	0.5469E-01	0.2769E-01	0.0000E-01	0.3535E-02
L11	0.1424E-01	0.7259E-01	0.0000E-01	0.8193E-02
L12	0.8542E-01	0.1584E-02	0.0000E-01	0.954E-02
L13	0.7014E-01	0.2552E-01	0.0000E-01	0.1000E-01
L14	0.1574E-01	0.3954E-01	0.0000E-01	0.1000E-01
A01	0.4342E-01	0.1589E-02	0.0000E-01	0.1000E-03
A02	0.5744E-02	0.2375E-02	0.0000E-01	0.6644E-04
A03	0.4029E-02	0.2712E-02	0.0000E-01	0.1000E-03
A04	0.9654E-01	0.2501E-02	0.6000E-01	0.1000E-03
A05	0.6543E-01	0.8774E-01	0.0000E-01	0.3332E-02
A06	0.1654E-01	0.4492E-01	0.0000E-01	0.3535E-02
A07	0.1562E-01	0.5192E-01	0.1727E-03	0.1635E-03
A08	0.1683E-01	0.2094E-01	0.1534E-01	0.375E-02
A09	0.8941E-02	0.2363E-02	0.0000E-01	0.1000E-03
A10	0.8460E-01	0.1764E-02	0.0000E-01	0.1000E-03
A11	0.1541E-02	0.2921E-02	0.0000E-01	0.1000E-03
A12	0.2225E-02	0.3574E-02	0.0000E-01	0.1000E-03
A13	0.4171E-02	0.3954E-02	0.0000E-01	0.1000E-03
A14	0.1404E-02	0.2475E-02	0.0000E-01	0.1000E-03
A15	0.4544E-01	0.4984E-01	0.0000E-01	0.1000E-01
A16	0.8801E-01	0.2533E-01	0.0000E-01	0.1000E-01
A17	0.8240E-01	0.2753E-01	0.0000E-01	0.1000E-01
A18	0.6451E-01	0.4791E-01	0.0000E-01	0.1000E-01
A19	0.5944E-01	0.4381E-01	0.0000E-01	0.1000E-01
A20	0.1147E-01	0.2452E-01	0.0000E-01	0.1031E-02
A21	0.1764E-01	0.1329E-01	0.0000E-01	0.1000E-01
A22	0.1944E-01	0.2559E-01	0.0000E-01	0.1000E-02
A23	0.9082E-01	0.1734E-01	0.0000E-01	0.1000E-01
A24	0.1287E-01	0.5524E-01	0.1000E-01	0.4000E-01
A25	0.9044E-01	0.2444E-01	0.0000E-01	0.1000E-01
A26	0.2267E-02	0.1254E-02	0.1800E-02	0.6700E-02
A27	0.2260E-01	0.4169E-01	0.0000E-01	0.1000E-01
A28	0.5926E-02	0.4744E-02	0.0000E-01	0.1000E-03
A29	0.3851E-02	0.451E-02	0.0000E-01	0.1000E-03
A30	0.2757E-01	0.4444E-01	0.0000E-01	0.1000E-01
A31	0.2757E-01	0.4444E-01	0.0000E-01	0.1000E-01
A32	0.1357E-01	0.1424E-01	0.0000E-01	0.4000E-01
A33	0.5361E-01	0.2524E-01	0.0000E-01	0.5000E-01

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

499 654 751 214 340 224



CLASS 06  
NO. OF OBSERVATIONS = 1079

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.6876	0.3458	0.2000	0.1249
S02	0.7206	0.3938	0.1000	0.1246
S03	0.6538	0.4706	0.1700	0.1096
S04	0.7347	0.1768	0.1250	0.1397
S05	0.1626	0.1154	0.0000	0.1500
L01	0.1452	0.1136	0.0000	0.6557
L02	0.6077	0.3948	0.0000	0.6364
L03	0.2038	0.2537	0.0000	0.5126
L04	0.2111	0.3948	0.0000	0.6604
L05	0.4441	0.3948	0.0000	0.6306
L06	0.1974	0.1809	0.0000	0.1000
L07	0.4964	0.2508	0.0000	0.1000
L08	0.5070	0.3594	0.0000	0.1000
L09	0.5174	0.1154	0.0000	0.6607
L10	0.4958	0.1250	0.0000	0.6608
L11	0.5046	0.1117	0.0000	0.6508
L12	0.1454	0.1198	0.0000	0.9770
L13	0.6434	0.3279	0.0000	0.1000
L14	0.1354	0.3469	0.0000	0.1000
A01	0.4722	0.2262	0.0000	0.3125
A02	0.5927	0.1750	0.0000	0.3500
A03	0.2587	0.3597	0.0000	0.3289
A04	0.7271	0.3518	0.0000	0.3072
A05	0.6248	0.3527	0.0000	0.1000
A06	0.2994	0.3754	0.0000	0.1000
A07	0.1468	0.4770	0.2716	0.9024
A08	0.7347	0.1518	0.1300	0.2187
A09	0.5974	0.2650	0.0000	0.1000
A10	0.5750	0.1150	0.0000	0.1000
A11	0.1236	0.2058	0.0000	0.1000
A12	0.2244	0.3557	0.0000	0.1000
A13	0.4434	0.4202	0.0000	0.1000
A14	0.1452	0.3100	0.0000	0.1000
A15	0.2852	0.4534	0.0000	0.1000
A16	0.1592	0.3598	0.0000	0.1000
A17	0.4554	0.2044	0.0000	0.1000
A18	0.3876	0.4223	0.0000	0.1000
A19	0.6341	0.2768	0.0000	0.1000
A20	0.3258	0.3510	0.0000	0.1000
A21	0.7414	0.3798	0.0000	0.1000
A22	0.4911	0.1753	0.0000	0.9091
A23	0.5641	0.1934	0.0000	0.4000
A24	0.1220	0.5024	0.1000	0.4000
A25	0.6611	0.3662	0.0000	0.1000
A26	0.1010	0.3114	0.0000	0.1000
A27	0.5213	0.1284	0.1500	0.9100
A28	0.5846	0.4568	0.0000	0.1000
A29	0.7627	0.3056	0.0000	0.1000
A30	0.2230	0.1562	0.0000	0.1000
A31	0.1423	0.1111	0.0000	0.1000
A32	0.2549	0.4358	0.0000	0.1000
A33	0.1354	0.1422	0.0000	0.4000
A34	0.1640	0.3969	0.0000	0.2000

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

235 169 309 159 126 77

CLASS 10  
NO. OF OBSERVATIONS = 4054

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.2501	0.2572	0.1400	0.5913
S02	0.2034	0.1973	0.1700	0.2260
S03	0.2507	0.2076	0.1000	0.3036
S04	0.2170	0.1085	0.1250	0.1493
S05	0.5323	0.1743	0.0000	0.1500
L01	0.5148	0.1142	0.0000	0.6354
L02	0.6456	0.0746	0.0000	0.6364
L03	0.2806	0.1820	0.0000	0.4000
L04	0.9815	0.1025	0.0000	0.2133
L05	0.8960	0.1032	0.0000	0.6104
L06	0.4072	0.2097	0.0000	0.3333
L07	0.5614	0.0730	0.0000	0.1552
L08	0.8878	0.0122	0.3500	0.6059
L09	0.3763	0.1469	0.0000	0.2529
L10	0.3100	0.1581	0.0000	0.3252
L11	0.9633	0.0928	0.0000	0.6672
L12	0.6868	0.1197	0.0000	0.9305
L13	0.5044	0.2298	0.0000	0.1000
L14	0.5317	0.0708	0.0000	0.1000
A01	0.2744	0.8111	0.0000	0.1000
A02	0.6625	0.2095	0.0000	0.1000
A03	0.3700	0.2043	0.0000	0.1000
A04	0.1758	0.1028	0.0000	0.1000
A05	0.1001	0.2029	0.0000	0.3322
A06	0.3566	0.3575	0.0000	0.5182
A07	0.1204	0.0580	0.1051	0.9783
A08	0.1844	0.1942	0.0000	0.2272
A09	0.9164	0.2047	0.0000	0.1000
A10	0.1004	0.3091	0.0000	0.1000
A11	0.1335	0.2581	0.0000	0.1000
A12	0.2345	0.3504	0.0000	0.1000
A13	0.5952	0.3537	0.0000	0.1000
A14	0.1159	0.2327	0.0000	0.1000
A15	0.0966	0.4597	0.0000	0.1000
A16	0.1122	0.2372	0.0000	0.1000
A17	0.9364	0.9031	0.0000	0.1000
A18	0.3411	0.4741	0.0000	0.1000
A19	0.7523	0.4317	0.0000	0.1000
A20	0.1118	0.4299	0.0000	0.1000
A21	0.6701	0.2361	0.0000	0.1263
A22	0.9224	0.2676	0.0000	0.1000
A23	0.2746	0.3364	0.0000	0.7143
A24	0.9761	0.1527	0.0000	0.1000
A25	0.7260	0.5588	0.1000	0.4000
A26	0.9224	0.2676	0.0000	0.1000
A27	0.5872	0.1255	0.0000	0.1000
A28	0.5086	0.1171	0.2000	0.9400
A29	0.1516	0.3386	0.0000	0.1000
A30	0.5421	0.3329	0.0000	0.1000
A31	0.4256	0.3322	0.0000	0.1000
A32	0.2834	0.1332	0.0000	0.1000
A33	0.1129	0.3164	0.0000	0.1000
A34	0.1931	0.1354	0.0000	0.4000
A35	0.4731	0.2247	0.0000	0.2000

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

568 1308 342 651 244 945

CLASS 11  
NO. OF OBSERVATIONS = 263

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.1023	0.1376	0.0000	0.1045
S02	0.9281	0.1143	0.0000	0.1045
S03	0.2741	0.2706	0.0000	0.2500
S04	0.1484	0.3948	0.0000	0.2500
S05	0.2176	0.1448	0.0000	0.2500
L01	0.8911	0.1943	0.0000	0.5074
L02	0.5502	0.1487	0.0000	0.2500
L03	0.7977	0.1382	0.0000	0.4474
L04	0.1231	0.1954	0.0000	0.4474
L05	0.1608	0.1607	0.0000	0.3574
L06	0.4564	0.0731	0.0000	0.3574
L07	0.9961	0.2098	0.0000	0.2532
L08	0.8266	0.1424	0.0000	0.1000
L09	0.7016	0.0471	0.0000	0.6000
L10	0.1066	0.1480	0.0000	0.4474
L11	0.4923	0.0971	0.0000	0.4474
L12	0.6157	0.1197	0.0000	0.4474
L13	0.5371	0.1728	0.0000	0.1000
L14	0.2080	0.0441	0.0000	0.6607
A01	0.3140	0.1272	0.0000	0.6574
A02	0.1697	0.1454	0.0000	0.6322
A03	0.2153	0.0881	0.0000	0.6642
A04	0.3660	0.1715	0.0000	0.6642
A05	0.1085	0.1011	0.0000	0.6213
A06	0.5405	0.4584	0.3800	0.6213
A07	0.2643	0.0261	0.1154	0.3252
A08	0.9561	0.1049	0.0000	0.3000
A09	0.6584	0.1364	0.0000	0.3000
A10	0.1538	0.2964	0.0000	0.1000
A11	0.2331	0.3844	0.0000	0.1000
A12	0.6419	0.1011	0.0000	0.1000
A13	0.1351	0.4827	0.0000	0.1000
A14	0.3604	0.2320	0.0000	0.1000
A15	0.5891	0.0264	0.0000	0.1000
A16	0.2631	0.2020	0.0000	0.1000
A17	0.7651	0.4214	0.0000	0.1000
A18	0.5961	0.4021	0.0000	0.1000
A19	0.1401	0.0200	0.0000	0.7000
A20	0.0000	0.0200	0.0000	0.0000
A21	0.3370	0.8274	0.0000	0.2174
A22	0.5822	0.1321	0.0000	0.1000
A23	0.1407	0.5321	0.1000	0.5000
A24	0.9130	0.2319	0.0000	0.1000
A25	0.6927	0.2382	0.0000	0.1000
A26	0.5243	0.1298	0.0000	0.8000
A27	0.2200	0.4156	0.0000	0.1000
A28	0.6548	0.3935	0.0000	0.1000
A29	0.5415	0.3933	0.0000	0.1000
A30	0.3743	0.4367	0.0000	0.6654
A31	0.5275	0.4922	0.0000	0.1000
A32	0.1908	0.1409	0.0000	0.4000
A33	0.9501	0.3120	0.0000	0.2000

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

37 93 324 34 10 57



CLASS 12  
NO. OF OBSERVATIONS = 634

Table with 10 columns: VARIABLE, MEAN, STAI., DEV., MINIMUM, MAXIMUM. Rows 52-666.

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

CLASS 13  
NO. OF OBSERVATIONS = 547

Table with 10 columns: VARIABLE, MEAN, STAI., DEV., MINIMUM, MAXIMUM. Rows 667-812.

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

CLASS 14  
NO. OF OBSERVATIONS = 69

Table with 10 columns: VARIABLE, MEAN, STAI., DEV., MINIMUM, MAXIMUM. Rows 813-881.

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG



STANDARD CLASSIFICATION - POPULATION

CLASS 15  
NO. OF OBSERVATIONS = 666

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.1760	0.4	0.0800	0.2350
S02	0.1402	0.1742	0.0700	0.2326
S03	0.8600	0.1105	0.0000	0.8288
S04	0.1850	0.1597	0.2162	0.2031
S05	0.2146	0.1176	0.0000	0.9000
L01	0.3369	0.2194	0.0000	0.6828
L02	0.7059	0.1192	0.0000	0.6486
L03	0.5838	0.4164	0.0000	0.6181
L04	0.1059	0.4397	0.0000	0.3143
L05	0.1372	0.2105	0.0000	0.6653
L06	0.9076	0.1173	0.0000	0.6667
L07	0.1604	0.4350	0.0000	0.5000
L08	0.3377	0.1597	0.0000	0.5319
L09	0.2455	0.1791	0.0000	0.3518
L10	0.4203	0.1737	0.0000	0.3257
L11	0.1331	0.4172	0.0000	0.8958
L12	0.1018	0.1352	0.0000	0.9741
L13	0.1622	0.3766	0.0000	0.1000
L14	0.1272	0.3780	0.0000	0.1000
A01	0.2324	0.2171	0.0000	0.1000
A02	0.2574	0.1353	0.0000	0.1000
A03	0.2144	0.2110	0.0000	0.1000
A04	0.4971	0.1399	0.0000	0.3257
A05	0.4673	0.1364	0.0000	0.3280
A06	0.1331	0.3212	0.0000	0.3256
A07	0.6342	0.1256	0.0000	0.1000
A08	0.2722	0.3171	0.0000	0.1323
A09	0.9625	0.3107	0.0000	0.1000
A10	0.1715	0.1724	0.0000	0.1000
A11	0.1154	0.2362	0.0000	0.1000
A12	0.1532	0.2317	0.0000	0.1000
A13	0.2414	0.3170	0.0000	0.1000
A14	0.1670	0.3180	0.0000	0.1000
A15	0.3674	0.4372	0.0000	0.1000
A16	0.1652	0.3151	0.0000	0.1000
A17	0.5615	0.2747	0.0000	0.1000
A18	0.2572	0.4101	0.0000	0.1000
A19	0.1160	0.2531	0.0000	0.1000
A20	0.3061	0.2482	0.0000	0.3125
A21	0.1126	0.3161	0.0000	0.1000
A22	0.3715	0.1753	0.0000	0.1250
A23	0.2219	0.2383	0.0000	0.1000
A24	0.1165	0.2460	0.0000	0.1000
A25	0.3766	0.3168	0.0000	0.1000
A26	0.1051	0.3167	0.0000	0.1000
A27	0.3344	0.2136	0.2500	0.8400
A28	0.2122	0.2157	0.0000	0.1000
A29	0.6876	0.2155	0.0000	0.1000
A30	0.2451	0.2484	0.0000	0.1000
A31	0.7632	0.1389	0.0000	0.1000
A32	0.2451	0.2484	0.0000	0.1000
A33	0.2451	0.2484	0.0000	0.1000
A34	0.2451	0.2484	0.0000	0.1000
A35	0.2451	0.2484	0.0000	0.1000
A36	0.2451	0.2484	0.0000	0.1000
A37	0.2451	0.2484	0.0000	0.1000
A38	0.2451	0.2484	0.0000	0.1000
A39	0.2451	0.2484	0.0000	0.1000
A40	0.2451	0.2484	0.0000	0.1000
A41	0.2451	0.2484	0.0000	0.1000
A42	0.2451	0.2484	0.0000	0.1000
A43	0.2451	0.2484	0.0000	0.1000
A44	0.2451	0.2484	0.0000	0.1000
A45	0.2451	0.2484	0.0000	0.1000
A46	0.2451	0.2484	0.0000	0.1000
A47	0.2451	0.2484	0.0000	0.1000
A48	0.2451	0.2484	0.0000	0.1000
A49	0.2451	0.2484	0.0000	0.1000
A50	0.2451	0.2484	0.0000	0.1000
A51	0.2451	0.2484	0.0000	0.1000
A52	0.2451	0.2484	0.0000	0.1000
A53	0.2451	0.2484	0.0000	0.1000
A54	0.2451	0.2484	0.0000	0.1000
A55	0.2451	0.2484	0.0000	0.1000
A56	0.2451	0.2484	0.0000	0.1000
A57	0.2451	0.2484	0.0000	0.1000
A58	0.2451	0.2484	0.0000	0.1000
A59	0.2451	0.2484	0.0000	0.1000
A60	0.2451	0.2484	0.0000	0.1000
A61	0.2451	0.2484	0.0000	0.1000
A62	0.2451	0.2484	0.0000	0.1000
A63	0.2451	0.2484	0.0000	0.1000
A64	0.2451	0.2484	0.0000	0.1000
A65	0.2451	0.2484	0.0000	0.1000
A66	0.2451	0.2484	0.0000	0.1000
A67	0.2451	0.2484	0.0000	0.1000
A68	0.2451	0.2484	0.0000	0.1000
A69	0.2451	0.2484	0.0000	0.1000
A70	0.2451	0.2484	0.0000	0.1000
A71	0.2451	0.2484	0.0000	0.1000
A72	0.2451	0.2484	0.0000	0.1000
A73	0.2451	0.2484	0.0000	0.1000
A74	0.2451	0.2484	0.0000	0.1000
A75	0.2451	0.2484	0.0000	0.1000
A76	0.2451	0.2484	0.0000	0.1000
A77	0.2451	0.2484	0.0000	0.1000
A78	0.2451	0.2484	0.0000	0.1000
A79	0.2451	0.2484	0.0000	0.1000
A80	0.2451	0.2484	0.0000	0.1000
A81	0.2451	0.2484	0.0000	0.1000
A82	0.2451	0.2484	0.0000	0.1000
A83	0.2451	0.2484	0.0000	0.1000
A84	0.2451	0.2484	0.0000	0.1000
A85	0.2451	0.2484	0.0000	0.1000
A86	0.2451	0.2484	0.0000	0.1000
A87	0.2451	0.2484	0.0000	0.1000
A88	0.2451	0.2484	0.0000	0.1000
A89	0.2451	0.2484	0.0000	0.1000
A90	0.2451	0.2484	0.0000	0.1000
A91	0.2451	0.2484	0.0000	0.1000
A92	0.2451	0.2484	0.0000	0.1000
A93	0.2451	0.2484	0.0000	0.1000
A94	0.2451	0.2484	0.0000	0.1000
A95	0.2451	0.2484	0.0000	0.1000
A96	0.2451	0.2484	0.0000	0.1000
A97	0.2451	0.2484	0.0000	0.1000
A98	0.2451	0.2484	0.0000	0.1000
A99	0.2451	0.2484	0.0000	0.1000
A100	0.2451	0.2484	0.0000	0.1000

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

101 106 37 37 309 20

CLASS 16  
NO. OF OBSERVATIONS = 15

VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.1082	0.4	0.2171	0.2000
S02	0.3038	0.3555	0.1000	0.1067
S03	0.3616	0.2302	0.1000	0.1236
S04	0.1722	0.1278	0.1000	0.4000
S05	0.1467	0.1408	0.0000	0.4000
L01	0.1093	0.1142	0.0000	0.3306
L02	0.3479	0.4388	0.0000	0.1579
L03	0.0000	0.3000	0.0000	0.0000
L04	0.2273	0.8304	0.0000	0.3409
L05	0.4243	0.1120	0.0000	0.1705
L06	0.5838	0.1000	0.0000	0.4545
L07	0.2092	0.5781	0.0000	0.1000
L08	0.1471	0.1521	0.0000	0.3168
L09	0.2207	0.2245	0.0000	0.6333
L10	0.1530	0.2391	0.0000	0.6888
L11	0.0000	0.0000	0.0000	0.0000
L12	0.2231	0.3080	0.4702	0.9771
L13	0.2667	0.4522	0.0000	0.1000
L14	0.1333	0.3599	0.0000	0.1000
A01	0.4923	0.1255	0.0000	0.4245
A02	0.2262	0.2313	0.0000	0.5833
A03	0.1354	0.2316	0.0000	0.5841
A04	0.9868	0.1929	0.0000	0.5714
A05	0.3630	0.1769	0.0000	0.6522
A06	0.1275	0.1719	0.0000	0.5833
A07	0.1062	0.2345	0.1538	0.8950
A08	0.2112	0.6152	0.1256	0.2500
A09	0.9622	0.6249	0.7857	0.1000
A10	0.6889	0.1365	0.0000	0.5000
A11	0.7222	0.1517	0.0000	0.5000
A12	0.1778	0.2995	0.0000	0.1000
A13	0.4566	0.4011	0.0000	0.1000
A14	0.2056	0.3544	0.0000	0.1000
A15	0.5333	0.4714	0.0000	0.1000
A16	0.1333	0.3599	0.0000	0.1000
A17	0.1533	0.3599	0.0000	0.1000
A18	0.0000	0.0000	0.0000	0.1000
A19	0.0000	0.0000	0.0000	0.0000
A20	0.0000	0.0000	0.0000	0.0000
A21	0.1973	0.2155	0.0000	0.6270
A22	0.1000	0.0000	0.1000	0.1000
A23	0.1067	0.2494	0.1000	0.2000
A24	0.2333	0.2494	0.0000	0.1000
A25	0.6667	0.2494	0.0000	0.1000
A26	0.2553	0.2528	0.3800	0.6500
A27	0.6000	0.4300	0.0000	0.1000
A28	0.7928	0.2583	0.0000	0.1000
A29	0.2072	0.3583	0.0000	0.1000
A30	0.0000	0.0000	0.0000	0.0000
A31	0.0000	0.0000	0.0000	0.0000
A32	0.1200	0.1141	0.0000	0.4000
A33	0.0000	0.0000	0.0000	0.0000
A34	0.0000	0.0000	0.0000	0.0000
A35	0.0000	0.0000	0.0000	0.0000
A36	0.0000	0.0000	0.0000	0.0000
A37	0.0000	0.0000	0.0000	0.0000
A38	0.0000	0.0000	0.0000	0.0000
A39	0.0000	0.0000	0.0000	0.0000
A40	0.0000	0.0000	0.0000	0.0000
A41	0.0000	0.0000	0.0000	0.0000
A42	0.0000	0.0000	0.0000	0.0000
A43	0.0000	0.0000	0.0000	0.0000
A44	0.0000	0.0000	0.0000	0.0000
A45	0.0000	0.0000	0.0000	0.0000
A46	0.0000	0.0000	0.0000	0.0000
A47	0.0000	0.0000	0.0000	0.0000
A48	0.0000	0.0000	0.0000	0.0000
A49	0.0000	0.0000	0.0000	0.0000
A50	0.0000	0.0000	0.0000	0.0000
A51	0.0000	0.0000	0.0000	0.0000
A52	0.0000	0.0000	0.0000	0.0000
A53	0.0000	0.0000	0.0000	0.0000
A54	0.0000	0.0000	0.0000	0.0000
A55	0.0000	0.0000	0.0000	0.0000
A56	0.0000	0.0000	0.0000	0.0000
A57	0.0000	0.0000	0.0000	0.0000
A58	0.0000	0.0000	0.0000	0.0000
A59	0.0000	0.0000	0.0000	0.0000
A60	0.0000	0.0000	0.0000	0.0000
A61	0.0000	0.0000	0.0000	0.0000
A62	0.0000	0.0000	0.0000	0.0000
A63	0.0000	0.0000	0.0000	0.0000
A64	0.0000	0.0000	0.0000	0.0000
A65	0.0000	0.0000	0.0000	0.0000
A66	0.0000	0.0000	0.0000	0.0000
A67	0.0000	0.0000	0.0000	0.0000
A68	0.0000	0.0000	0.0000	0.0000
A69	0.0000	0.0000	0.0000	0.0000
A70	0.0000	0.0000	0.0000	0.0000
A71	0.0000	0.0000	0.0000	0.0000
A72	0.0000	0.0000	0.0000	0.0000
A73	0.0000	0.0000	0.0000	0.0000
A74	0.0000	0.0000	0.0000	0.0000
A75	0.0000	0.0000	0.0000	0.0000
A76	0.0000	0.0000	0	



POPULATION ASSIGNMENT BY CLASSIFICATION I

TOTAL NO. OF OBSERVATIONS = 21743

Table with 7 columns: VARIABLE, MEAN, STAN. DEV., MINIMUM, MAXIMUM. Rows include variables S01 through S06 and M01 through M06.

CLASS 1 NO. OF OBSERVATIONS = 2260

Table with 7 columns: VARIABLE, MEAN, STAN. DEV., MINIMUM, MAXIMUM. Rows include variables S01 through S06 and M01 through M06.

CLASS 2 NO. OF OBSERVATIONS = 290

Table with 7 columns: VARIABLE, MEAN, STAN. DEV., MINIMUM, MAXIMUM. Rows include variables S01 through S06 and M01 through M06.

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG 5346 4240 4411 2471 5093 1982 225 223 82 601 97 1032 63 24 28 32 136 7



POPULATION ASSIGNMENT BY CLASSIFICATION I

CLASS 3 NO. OF OBSERVATIONS = 1653		CLASS 4 NO. OF OBSERVATIONS = 1248		CLASS 5 NO. OF OBSERVATIONS = 1369										
VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.7209E 03	0.3542E 04	0.5000E 01	0.1402E 06	S01	0.1482E 04	0.1492E 04	0.3700E 04	0.1940E 05	S01	0.8854E 03	0.1307E 04	0.6000E 01	0.1640E 05
S02	0.5263E 03	0.7207E 01	0.4000E 01	0.7400E 04	S02	0.1191E 04	0.1136E 04	0.3600E 02	0.9400E 04	S02	0.7328E 03	0.1104E 04	0.6000E 01	0.2600E 04
S03	0.627E 01	0.8974E 01	0.0000E 00	0.4923E 03	S03	0.7988E 01	0.9085E 01	0.0000E 00	0.1138E 02	S03	0.7352E 01	0.1477E 02	0.0000E 00	0.2042E 02
S04	0.1010E 01	0.7856E 00	0.4250E 00	0.1106E 02	S04	0.2783E 01	0.1849E 01	0.1250E 00	0.3200E 02	S04	0.1253E 01	0.1073E 01	0.1250E 00	0.1000E 02
S05	0.1658E 02	0.1043E 01	0.0000E 00	0.6000E 01	S05	0.2065E 01	0.1312E 01	0.0000E 00	0.1000E 02	S05	0.1594E 01	0.1495E 01	0.0000E 00	0.1200E 02
L01	0.1658E 02	0.2416E 02	0.0000E 00	0.1000E 03	L01	0.3701E 02	0.2174E 02	0.0000E 00	0.1000E 02	L01	0.2166E 02	0.2423E 02	0.0000E 00	0.1000E 03
L02	0.727E 01	0.4203E 02	0.0000E 00	0.4068E 02	L02	0.5234E 01	0.6106E 01	0.0000E 00	0.4793E 02	L02	0.6490E 01	0.1059E 02	0.0000E 00	0.1667E 02
L03	0.1873E 00	0.4927E 01	0.0000E 00	0.5488E 02	L03	0.6546E 00	0.3719E 01	0.0000E 00	0.5882E 02	L03	0.277E 00	0.2935E 01	0.0000E 00	0.7500E 02
L04	0.6819E 00	0.1701E 02	0.0000E 00	0.1000E 03	L04	0.5058E 00	0.2502E 01	0.0000E 00	0.1000E 03	L04	0.6937E 00	0.5441E 01	0.0000E 00	0.7000E 02
L05	0.8088E 01	0.6236E 01	0.0000E 00	0.8584E 02	L05	0.5256E 02	0.2268E 02	0.0000E 00	0.1745E 02	L05	0.1541E 01	0.7776E 01	0.0000E 00	0.9600E 02
L06	0.1060E 01	0.4008E 01	0.0000E 00	0.4000E 02	L06	0.1151E 01	0.4980E 01	0.0000E 00	0.1681E 02	L06	0.1541E 01	0.4126E 01	0.0000E 00	0.5000E 02
L07	0.1766E 01	0.4008E 01	0.0000E 00	0.1000E 03	L07	0.6333E 00	0.1400E 01	0.0000E 00	0.9957E 02	L07	0.1538E 01	0.3750E 02	0.0000E 00	0.1000E 03
L08	0.436E 02	0.5866E 02	0.0000E 00	0.1000E 03	L08	0.1042E 02	0.1755E 02	0.0000E 00	0.1000E 03	L08	0.4362E 02	0.2055E 02	0.0000E 00	0.1000E 03
L09	0.5869E 01	0.1783E 02	0.0000E 00	0.1000E 03	L09	0.7203E 01	0.1793E 02	0.0000E 00	0.8066E 02	L09	0.6963E 01	0.2055E 02	0.0000E 00	0.1000E 03
L10	0.7354E 01	0.2071E 02	0.0000E 00	0.9404E 02	L10	0.2087E 01	0.8225E 01	0.0000E 00	0.8831E 02	L10	0.9438E 01	0.2471E 02	0.0000E 00	0.9557E 02
L11	0.3456E 01	0.1321E 02	0.0000E 00	0.9854E 02	L11	0.1317E 02	0.1672E 02	0.0000E 00	0.1000E 01	L11	0.5361E 01	0.1204E 02	0.0000E 00	0.9249E 02
L12	0.1725E 02	0.1637E 02	0.0000E 00	0.1000E 01	L12	0.6274E 00	0.4835E 00	0.0000E 00	0.1000E 01	L12	0.1924E 02	0.1577E 02	0.0000E 00	0.9000E 01
L13	0.9014E 01	0.3816E 00	0.0000E 00	0.1000E 01	L13	0.5838E 00	0.4863E 00	0.0000E 00	0.1000E 03	L13	0.1096E 00	0.3124E 00	0.0000E 00	0.1000E 01
L14	0.1349E 00	0.3416E 00	0.0000E 00	0.1000E 01	L14	0.5774E 01	0.1212E 02	0.0000E 00	0.1000E 03	L14	0.3453E 01	0.1361E 02	0.0000E 00	0.4000E 03
A01	0.6345E 01	0.1845E 02	0.0000E 00	0.1000E 03	A01	0.2185E 02	0.2965E 02	0.0000E 00	0.1000E 03	A01	0.2866E 02	0.3328E 02	0.0000E 00	0.1000E 03
A02	0.2505E 02	0.3375E 02	0.0000E 00	0.1000E 03	A02	0.4510E 02	0.2828E 02	0.0000E 00	0.1000E 03	A02	0.1690E 02	0.2465E 02	0.0000E 00	0.1000E 03
A03	0.1672E 02	0.2859E 02	0.0000E 00	0.1000E 03	A03	0.5522E 01	0.1202E 02	0.0000E 00	0.1000E 03	A03	0.3497E 01	0.1537E 02	0.0000E 00	0.1000E 03
A04	0.5274E 01	0.1943E 02	0.0000E 00	0.1000E 03	A04	0.1172E 02	0.1657E 02	0.0000E 00	0.1000E 03	A04	0.1326E 02	0.2464E 02	0.0000E 00	0.1000E 03
A05	0.1032E 02	0.2116E 02	0.0000E 00	0.1000E 03	A05	0.4501E 01	0.1358E 02	0.0000E 00	0.1000E 03	A05	0.5052E 01	0.1740E 02	0.0000E 00	0.1000E 03
A06	0.540E 01	0.1722E 02	0.0000E 00	0.1000E 03	A06	0.6891E 00	0.6742E 00	0.0000E 00	0.7778E 03	A06	0.1167E 01	0.2401E 01	0.0000E 00	0.2533E 02
A07	0.1332E 01	0.1908E 01	0.0000E 00	0.2870E 02	A07	0.5416E 01	0.4774E 01	0.1497E 00	0.1728E 03	A07	0.3632E 01	0.5309E 01	0.3066E 01	0.7143E 02
A08	0.3648E 01	0.5330E 01	0.1337E 01	0.8333E 02	A08	0.8839E 02	0.2413E 02	0.1356E 01	0.1000E 03	A08	0.8500E 02	0.2683E 02	0.1466E 01	0.1000E 03
A09	0.931E 02	0.1850E 02	0.3719E 01	0.1000E 03	A09	0.1195E 02	0.1857E 02	0.0000E 00	0.1000E 03	A09	0.0726E 01	0.1717E 02	0.0000E 00	0.1000E 03
A10	0.8409E 00	0.6006E 01	0.0000E 00	0.6667E 02	A10	0.1501E 02	0.2319E 02	0.0000E 00	0.1000E 03	A10	0.1097E 02	0.2327E 02	0.0000E 00	0.1000E 03
A11	0.5133E 01	0.1146E 02	0.0000E 00	0.7500E 02	A11	0.2251E 02	0.3072E 02	0.0000E 00	0.1000E 03	A11	0.1822E 02	0.3218E 02	0.0000E 00	0.1000E 03
A12	0.4572E 01	0.1371E 02	0.0000E 00	0.6667E 02	A12	0.4291E 02	0.3317E 02	0.0000E 00	0.1000E 03	A12	0.4357E 02	0.4095E 02	0.0000E 00	0.1000E 03
A13	0.6944E 01	0.1861E 02	0.0000E 00	0.6667E 02	A13	0.7675E 01	0.1884E 02	0.0000E 00	0.1000E 03	A13	0.2051E 02	0.3450E 02	0.0000E 00	0.1000E 03
A14	0.8733E 02	0.2426E 02	0.2500E 02	0.1000E 03	A14	0.5510E 00	0.4773E 00	0.0000E 00	0.1000E 01	A14	0.2447E 00	0.4399E 00	0.0000E 00	0.1000E 01
A15	0.1725E 02	0.3160E 00	0.0000E 00	0.1000E 01	A15	0.3765E 00	0.4651E 00	0.0000E 00	0.1000E 01	A15	0.7967E 01	0.2708E 00	0.0000E 00	0.1000E 01
A16	0.945E 01	0.2890E 00	0.0000E 00	0.1000E 01	A16	0.5929E 01	0.2362E 00	0.0000E 00	0.1000E 01	A16	0.7266E 01	0.2596E 00	0.0000E 00	0.1000E 01
A17	0.2601E 01	0.1594E 00	0.0000E 00	0.1000E 01	A17	0.7208E 00	0.4203E 00	0.0000E 00	0.1000E 01	A17	0.6349E 00	0.4820E 00	0.0000E 00	0.1000E 01
A18	0.6207E 00	0.4852E 00	0.0000E 00	0.1000E 01	A18	0.2065E 01	0.1696E 00	0.0000E 00	0.1000E 01	A18	0.1922E 00	0.3340E 00	0.0000E 00	0.1000E 01
A19	0.2733E 01	0.1645E 00	0.0000E 00	0.1000E 01	A19	0.6742E 01	0.7391E 00	0.0000E 00	0.1465E 02	A19	0.1331E 00	0.2354E 01	0.0000E 00	0.5744E 02
A20	0.2733E 01	0.1645E 00	0.0000E 00	0.1000E 01	A20	0.2083E 01	0.1428E 00	0.0000E 00	0.1000E 01	A20	0.5947E 01	0.2351E 01	0.0000E 00	0.1000E 01
A21	0.5085E 01	0.3320E 00	0.0000E 00	0.1000E 01	A21	0.2644E 01	0.2983E 01	0.0000E 00	0.2222E 02	A21	0.4475E 01	0.7343E 01	0.0000E 00	0.1000E 01
A22	0.4733E 01	0.6069E 01	0.0000E 00	0.4545E 02	A22	0.1000E 01	0.0000E 00	0.1000E 01	0.1000E 01	A22	0.1010E 01	0.0000E 00	0.1000E 01	0.1000E 01
A23	0.1067E 01	0.0000E 00	0.0000E 00	0.1000E 01	A23	0.1042E 01	0.2337E 00	0.1000E 01	0.4000E 01	A23	0.1639E 01	0.2482E 00	0.1000E 01	0.4000E 01
A24	0.0000E 00	0.0000E 00	0.0000E 00	0.1000E 01	A24	0.0000E 00	0.0000E 00	0.1000E 01	0.1000E 00	A24	0.0000E 00	0.0000E 00	0.1000E 01	0.1000E 01
A25	0.2652E 02	0.5843E 01	0.2800E 02	0.9400E 02	A25	0.5365E 02	0.1179E 02	0.2200E 02	0.9000E 02	A25	0.5569E 02	0.1364E 02	0.2000E 02	0.9100E 02
A26	0.1210E 00	0.3261E 02	0.0000E 00	0.1000E 01	A26	0.8344E 01	0.2835E 00	0.0000E 00	0.1000E 01	A26	0.1377E 00	0.3466E 00	0.0000E 00	0.1000E 01
A27	0.7642E 02	0.4622E 02	0.0000E 00	0.1000E 03	A27	0.4404E 02	0.4792E 02	0.0000E 00	0.1000E 03	A27	0.7314E 02	0.3901E 02	0.0000E 00	0.1000E 03
A28	0.1069E 00	0.3594E 02	0.0000E 00	0.1000E 03	A28	0.6611E 02	0.1249E 02	0.0000E 00	0.1000E 03	A28	0.2377E 02	0.3679E 02	0.0000E 00	0.1000E 03
A29	0.8016E 00	0.3742E 01	0.0000E 00	0.1000E 03	A29	0.4935E 02	0.4972E 02	0.0000E 00	0.1000E 03	A29	0.3550E 01	0.1814E 02	0.0000E 00	0.1000E 03
A30	0.1205E 00	0.3357E 00	0.0000E 00	0.1000E 01	A30	0.9038E 01	0.2991E 00	0.0000E 00	0.1000E 01	A30	0.7011E 01	0.2553E 00	0.0000E 00	0.1000E 01
A31	0.9349E 00	0.1307E 01	0.0000E 00	0.4000E 01	A31	0.5353E 00	0.1039E 01	0.0000E 00	0.4000E 01	A31	0.1632E 01	0.1361E 01	0.0000E 00	0.4600E 01
A32	0.5485E 01	0.1764E 00	0.0000E 00	0.2000E 01	A32	0.1715E 00	0.4469E 00	0.0000E 00	0.4000E 01	A32	0.4277E 01	0.2247E 01	0.0000E 00	0.5000E 01

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POPULATION ASSIGNMENT BY CLASSIFICATION I

CLASS 6 NO. OF OBSERVATIONS = 1295										CLASS 7 NO. OF OBSERVATIONS = 702										CLASS 8 NO. OF OBSERVATIONS = 1004									
VARIABLE	MEAN	STAN.DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN.DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN.DEV.	MINIMUM	MAXIMUM															
S01	0.8516	0.3	0.1215	0.4	0.1300	0.2	0.1200	0.5	0.1200	S01	0.2608	0.4	0.7270	0.4	0.1500	0.2	0.1694	0.6											
S02	0.6956	0.3	0.1158	0.2	0.8000	0.1	0.9000	0.4	0.1368	S02	0.1660	0.4	0.1936	0.4	0.1200	0.2	0.1200	0.5											
S03	0.2667	0.1	0.1158	0.2	0.0000	0.0	0.2400	0.3	0.9672	S03	0.1076	0.2	0.2158	0.2	0.0000	0.0	0.2320	0.3											
S04	0.1575	0.1	0.1177	0.1	0.1250	0.0	0.8000	0.1	0.1400	S04	0.2125	0.1	0.2290	0.1	0.7270	0.2	0.3000	0.2											
S05	0.1744	0.1	0.1177	0.1	0.0000	0.0	0.8000	0.1	0.4600	S05	0.2165	0.1	0.2001	0.1	0.0000	0.0	0.1000	0.2											
L01	0.6722	0.2	0.2578	0.2	0.0000	0.0	1.0000	0.3	0.4440	L01	0.2478	0.2	0.2572	0.2	0.0000	0.0	1.0000	0.3											
L02	0.1466	0.1	0.5487	0.1	0.0000	0.0	0.5070	0.2	0.5000	L02	0.5648	0.1	0.1121	0.2	0.0000	0.0	1.0000	0.3											
L03	0.8133	0.0	0.6781	0.1	0.0000	0.0	1.0000	0.3	0.2273	L03	0.5530	0.1	0.4254	0.1	0.0000	0.0	0.7374	0.2											
L04	0.1390	0.1	0.6192	0.1	0.0000	0.0	0.6254	0.2	0.1000	L04	0.1364	0.1	0.8356	0.1	0.0000	0.0	0.9530	0.2											
L05	0.4366	0.1	0.1195	0.2	0.0000	0.0	1.0000	0.3	0.7553	L05	0.1147	0.2	0.1974	0.2	0.0000	0.0	1.0000	0.3											
L06	0.9437	0.1	0.1365	0.2	0.0000	0.0	1.0000	0.3	0.6279	L06	0.1973	0.1	0.8473	0.1	0.0000	0.0	0.4646	0.2											
L07	0.9440	0.0	0.3235	0.2	0.0000	0.0	0.4495	0.2	0.5714	L07	0.7476	0.0	0.2587	0.1	0.0000	0.0	0.4646	0.2											
L08	0.5351	0.1	0.1977	0.1	0.0000	0.0	1.0000	0.3	0.6923	L08	0.3185	0.2	0.3612	0.2	0.0000	0.0	1.0000	0.3											
L09	0.2566	0.2	0.3522	0.2	0.0000	0.0	1.0000	0.3	0.3283	L09	0.7594	0.1	0.1975	0.2	0.0000	0.0	1.0000	0.3											
L10	0.3272	0.2	0.4055	0.2	0.0000	0.0	1.0000	0.3	0.9202	L10	0.1477	0.2	0.2946	0.2	0.0000	0.0	1.0000	0.3											
L11	0.4432	0.1	0.1594	0.2	0.0000	0.0	0.9844	0.2	0.9972	L11	0.2836	0.1	0.1088	0.2	0.0000	0.0	0.9275	0.2											
L12	0.9433	0.1	0.1475	0.2	0.0000	0.0	0.9660	0.2	0.1000	L12	0.1397	0.2	0.2077	0.2	0.0000	0.0	0.9941	0.2											
L13	0.2370	0.1	0.4210	0.1	0.0000	0.0	1.0000	0.1	0.1000	L13	0.2042	0.0	0.4031	0.2	0.0000	0.0	1.0000	0.1											
L14	0.2052	0.1	0.1459	0.0	0.0000	0.0	1.0000	0.1	0.1000	L14	0.1355	0.0	0.3422	0.0	0.0000	0.0	1.0000	0.1											
A01	0.3942	0.2	0.3841	0.2	0.0000	0.0	1.0000	0.3	0.1000	A01	0.4636	0.1	0.1813	0.2	0.0000	0.0	1.0000	0.3											
A02	0.9411	0.1	0.1642	0.2	0.0000	0.0	1.0000	0.3	0.5455	A02	0.2384	0.2	0.2932	0.2	0.0000	0.0	1.0000	0.3											
A03	0.5371	0.1	0.1981	0.2	0.0000	0.0	1.0000	0.3	0.1000	A03	0.1699	0.2	0.2580	0.2	0.0000	0.0	1.0000	0.3											
A04	0.1623	0.1	0.1132	0.2	0.0000	0.0	1.0000	0.3	0.1000	A04	0.3255	0.1	0.1466	0.2	0.0000	0.0	1.0000	0.3											
A05	0.5350	0.1	0.2011	0.2	0.0000	0.0	1.0000	0.3	0.1000	A05	0.9950	0.1	0.2172	0.2	0.0000	0.0	1.0000	0.3											
A06	0.5650	0.1	0.1656	0.2	0.0000	0.0	1.0000	0.3	0.1000	A06	0.3749	0.1	0.1542	0.2	0.0000	0.0	1.0000	0.3											
A07	0.4338	0.2	0.2041	0.2	0.0000	0.0	0.2507	0.2	0.1000	A07	0.6852	0.0	0.1848	0.1	0.0000	0.0	0.2531	0.2											
M01	0.4166	0.1	0.5091	0.1	0.2100	0.1	0.5270	0.2	0.1000	M01	0.2559	0.1	0.6880	0.1	0.1581	0.2	0.1746	0.3											
M02	0.7146	0.2	0.3244	0.2	0.1488	0.1	1.0000	0.3	0.6042	M02	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.0000	0.0											
M03	0.0744	0.1	0.1683	0.2	0.0000	0.0	1.0000	0.3	0.1000	M03	0.4563	0.1	0.1539	0.2	0.0000	0.0	1.0000	0.3											
M04	0.9300	0.1	0.2288	0.2	0.0000	0.0	1.0000	0.3	0.1000	M04	0.1243	0.2	0.2582	0.2	0.0000	0.0	1.0000	0.3											
M05	0.2190	0.2	0.3465	0.2	0.0000	0.0	1.0000	0.3	0.1000	M05	0.1695	0.2	0.3159	0.2	0.0000	0.0	1.0000	0.3											
M06	0.2080	0.2	0.4172	0.2	0.0000	0.0	1.0000	0.3	0.1000	M06	0.3487	0.2	0.4087	0.2	0.0000	0.0	1.0000	0.3											
M07	0.9311	0.0	0.2316	0.2	0.0000	0.0	1.0000	0.1	0.1000	M07	0.6944	0.1	0.2083	0.2	0.0000	0.0	1.0000	0.3											
M08	0.2270	0.1	0.5091	0.1	0.0000	0.0	1.0000	0.1	0.1000	M08	0.3755	0.0	0.4843	0.0	0.0000	0.0	1.0000	0.1											
M09	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M09	0.1365	0.0	0.3893	0.0	0.0000	0.0	1.0000	0.1											
M10	0.2270	0.1	0.4172	0.1	0.0000	0.0	1.0000	0.1	0.1000	M10	0.1195	0.0	0.3244	0.0	0.0000	0.0	1.0000	0.1											
M11	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M11	0.6116	0.0	0.4876	0.0	0.0000	0.0	1.0000	0.1											
M12	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M12	0.1514	0.0	0.3679	0.0	0.0000	0.0	1.0000	0.1											
M13	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M13	0.1365	0.0	0.3893	0.0	0.0000	0.0	1.0000	0.1											
M14	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M14	0.2516	0.1	0.4038	0.1	0.0000	0.0	0.4615	0.2											
M15	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M15	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.0000	0.0											
M16	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M16	0.1366	0.1	0.7228	0.1	0.0000	0.0	0.4000	0.1											
M17	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M17	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M18	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M18	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M19	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M19	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M20	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M20	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M21	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M21	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M22	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M22	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M23	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M23	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M24	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M24	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M25	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M25	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M26	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M26	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M27	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M27	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M28	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M28	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M29	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M29	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M30	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M30	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M31	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M31	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M32	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M32	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M33	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M33	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M34	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M34	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M35	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M35	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M36	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M36	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M37	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M37	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M38	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M38	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M39	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M39	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M40	0.3361	0.2	0.6202	0.1	0.0000	0.0	1.0000	0.1	0.1000	M40	0.0000	0.0	0.0000	0.0	0.0000	0.0	0.4000	0.1											
M41	0.3361	0.2																											



POPULATION ASSIGNMENT BY CLASSIFICATION I

CLASS 9 NO. OF OBSERVATIONS = 2540											CLASS 10 NO. OF OBSERVATIONS = 2334											CLASS 11 NO. OF OBSERVATIONS = 924										
VARIABLE	MEAN	STAN.DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN.DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN.DEV.	MINIMUM	MAXIMUM																		
S01	0.3503E 03	0.1141E 04	0.7000E 01	0.1184E 05	S01	0.1758E 04	0.1224E 04	0.1200E 04	0.1040E 05	S01	0.2708E 03	0.4148E 03	0.8000E 01	0.6000E 04																		
S02	0.6803E 03	0.1062E 02	0.0000E 01	0.9250E 04	S02	0.1647E 04	0.1103E 04	0.1200E 02	0.7800E 04	S02	0.2328E 01	0.1200E 03	0.7000E 01	0.4195E 04																		
S03	0.7777E 01	0.1062E 02	0.0000E 01	0.1835E 03	S03	0.1925E 02	0.1501E 02	0.0000E 01	0.1590E 03	S03	0.5928E 01	0.1143E 02	0.0000E 01	0.1268E 03																		
S04	0.1100E 01	0.8034E 00	0.1250E 00	0.9216E 01	S04	0.2108E 01	0.9799E 00	0.1250E 00	0.1140E 02	S04	0.9190E 00	0.7904E 00	0.1250E 00	0.7000E 01																		
S05	0.1179E 01	0.9376E 00	0.0000E 00	0.4000E 01	S05	0.3513E 01	0.1436E 01	0.0000E 00	0.1000E 02	S05	0.2051E 01	0.1174E 01	0.0000E 00	0.1300E 02																		
L01	0.7322E 02	0.2104E 02	0.0000E 01	0.1000E 03	L01	0.4081E 02	0.1851E 02	0.0000E 00	0.1000E 03	L01	0.2901E 02	0.2695E 02	0.0000E 00	0.1000E 03																		
L02	0.6399E 01	0.9664E 01	0.0000E 01	0.1000E 03	L02	0.1245E 02	0.1049E 02	0.0000E 00	0.1000E 03	L02	0.1576E 02	0.1938E 02	0.0000E 00	0.1000E 03																		
L03	0.2072E 00	0.2354E 01	0.0000E 00	0.6333E 02	L03	0.1243E 01	0.3381E 01	0.0000E 00	0.3678E 02	L03	0.5467E 01	0.2894E 01	0.0000E 00	0.1476E 02																		
L04	0.3626E 00	0.4065E 01	0.0000E 00	0.6316E 02	L04	0.4140E 01	0.3337E 01	0.0000E 00	0.6028E 02	L04	0.5523E 01	0.1140E 02	0.0000E 00	0.6235E 02																		
L05	0.6201E 01	0.1360E 02	0.0000E 00	0.1000E 03	L05	0.1158E 02	0.1497E 02	0.0000E 00	0.9449E 02	L05	0.8967E 01	0.1778E 02	0.0000E 00	0.1000E 03																		
L06	0.9370E 01	0.4703E 01	0.0000E 00	0.5165E 02	L06	0.5815E 00	0.3163E 01	0.0000E 00	0.4175E 02	L06	0.1752E 01	0.7103E 01	0.0000E 00	0.0566E 02																		
L07	0.1499E 01	0.2677E 01	0.0000E 00	0.4074E 02	L07	0.2951E 00	0.6450E 00	0.0000E 00	0.1316E 02	L07	0.3487E 01	0.6256E 01	0.0000E 00	0.3188E 02																		
L08	0.6387E 02	0.5157E 02	0.0000E 00	0.1000E 03	L08	0.3017E 02	0.2002E 02	0.0000E 00	0.8950E 02	L08	0.1453E 02	0.2199E 02	0.0000E 00	0.1000E 03																		
L09	0.1571E 01	0.6414E 01	0.0000E 00	0.7353E 02	L09	0.9992E 00	0.4340E 01	0.0000E 00	0.5540E 02	L09	0.1297E 02	0.2707E 02	0.0000E 00	0.1000E 03																		
L10	0.4511E 01	0.7334E 01	0.0000E 00	0.6612E 02	L10	0.1471E 01	0.7892E 01	0.0000E 00	0.1000E 03	L10	0.9776E 01	0.2283E 01	0.0000E 00	0.1000E 03																		
L11	0.4303E 01	0.9115E 01	0.0000E 00	0.8935E 02	L11	0.8042E 00	0.4456E 01	0.0000E 00	0.6598E 02	L11	0.1820E 01	0.8455E 01	0.0000E 00	0.9342E 02																		
L12	0.9753E 01	0.1507E 02	0.0000E 00	0.9741E 02	L12	0.4433E 01	0.6571E 01	0.0000E 00	0.9500E 02	L12	0.9100E 01	0.1237E 02	0.0000E 00	0.9909E 02																		
L13	0.5079E-01	0.2196E 00	0.0000E 00	0.1000E 01	L13	0.4799E-01	0.2137E 00	0.0000E 00	0.1000E 01	L13	0.1050E 00	0.3065E 00	0.0000E 00	0.1000E 01																		
L14	0.2205E 00	0.4148E 00	0.0000E 00	0.1000E 01	L14	0.5437E 00	0.4981E 00	0.0000E 00	0.1000E 01	L14	0.1066E 00	0.3009E 00	0.0000E 00	0.1000E 01																		
A01	0.6568E 01	0.1488E 02	0.0000E 00	0.1000E 03	A01	0.2709E 01	0.7583E 01	0.0000E 00	0.1000E 03	A01	0.1401E 01	0.8595E 01	0.0000E 00	0.1000E 03																		
A02	0.5811E 02	0.3380E 02	0.0000E 00	0.1000E 03	A02	0.4048E 02	0.2315E 02	0.0000E 00	0.1000E 03	A02	0.6573E 01	0.1813E 02	0.0000E 00	0.1000E 03																		
A03	0.2762E 02	0.2850E 02	0.0000E 00	0.1000E 03	A03	0.5156E 02	0.2173E 02	0.0000E 00	0.1000E 03	A03	0.4943E 01	0.1619E 02	0.0000E 00	0.1000E 03																		
A04	0.6799E 01	0.2099E 02	0.0000E 00	0.1000E 03	A04	0.1425E 01	0.8990E 01	0.0000E 00	0.1000E 03	A04	0.2107E 01	0.1194E 02	0.0000E 00	0.1000E 03																		
A05	0.1027E 02	0.1819E 02	0.0000E 00	0.1000E 03	A05	0.1566E 02	0.1865E 02	0.0000E 00	0.1000E 03	A05	0.5512E 02	0.4350E 02	0.0000E 00	0.1000E 03																		
A06	0.4701E 01	0.1555E 02	0.0000E 00	0.1000E 03	A06	0.3225E 01	0.1107E 02	0.0000E 00	0.1000E 03	A06	0.5397E 01	0.1178E 02	0.0000E 00	0.1000E 03																		
A07	0.1468E 01	0.2219E 01	0.0000E 00	0.2462E 02	A07	0.1351E 01	0.1191E 01	0.0000E 00	0.2224E 02	A07	0.1738E 01	0.5448E 01	0.0000E 00	0.1000E 03																		
A08	0.2688E 01	0.3294E 01	0.2155E 01	0.5375E 02	A08	0.1828E 01	0.2123E 01	0.5000E -01	0.6250E 02	A08	0.6607E 01	0.8844E 01	0.2102E 00	0.3236E 02																		
A09	0.9414E 02	0.1308E 02	0.1356E 01	0.1000E 03	A09	0.9424E 02	0.1326E 02	0.7301E 01	0.1000E 03	A09	0.9494E 02	0.1288E 02	0.3323E 01	0.1000E 03																		
A10	0.4435E 01	0.1278E 02	0.0000E 00	0.6676E 02	A10	0.1143E 02	0.1973E 02	0.0000E 00	0.1000E 03	A10	0.5406E 01	0.1565E 02	0.0000E 00	0.1000E 03																		
A11	0.2603E 01	0.1012E 02	0.0000E 00	0.6667E 02	A11	0.2179E 02	0.3135E 02	0.0000E 00	0.1000E 03	A11	0.1102E 02	0.2124E 02	0.0000E 00	0.1000E 03																		
A12	0.3666E 01	0.1252E 02	0.0000E 00	0.6667E 02	A12	0.3470E 02	0.3714E 02	0.0000E 00	0.1000E 03	A12	0.2451E 02	0.3644E 02	0.0000E 00	0.1000E 03																		
A13	0.8252E 02	0.2131E 02	0.1429E 02	0.1000E 03	A13	0.2562E 02	0.3058E 02	0.0000E 00	0.1000E 03	A13	0.5194E 02	0.4158E 02	0.0000E 00	0.1000E 03																		
A14	0.1716E 01	0.8181E 01	0.0000E 00	0.5000E 02	A14	0.6401E 01	0.1524E 02	0.0000E 00	0.6647E 02	A14	0.7091E 01	0.1939E 02	0.0000E 00	0.1000E 03																		
A15	0.9046E-01	0.2952E 00	0.0000E 00	0.1000E 01	A15	0.7785E 00	0.4153E 00	0.0000E 00	0.1000E 01	A15	0.3074E 00	0.4641E 00	0.0000E 00	0.1000E 01																		
A16	0.8346E-01	0.2766E 00	0.0000E 00	0.1000E 01	A16	0.1084E 00	0.3109E 00	0.0000E 00	0.1000E 01	A16	0.2684E 00	0.4431E 00	0.0000E 00	0.1000E 01																		
A17	0.1466E-01	0.1275E 00	0.0000E 00	0.1000E 01	A17	0.1654E 00	0.3715E 00	0.0000E 00	0.1000E 01	A17	0.5628E-01	0.2305E 00	0.0000E 00	0.1000E 01																		
A18	0.6164E 00	0.4775E 00	0.0000E 00	0.1000E 01	A18	0.9104E 00	0.2998E 00	0.0000E 00	0.1000E 01	A18	0.7597E 00	0.4272E 00	0.0000E 00	0.1000E 01																		
A19	0.2188E-01	0.1403E 00	0.0000E 00	0.1000E 01	A19	0.3436E 00	0.4749E 00	0.0000E 00	0.1000E 01	A19	0.1082E-01	0.1033E 00	0.0000E 00	0.1000E 01																		
A20	0.5088E-01	0.8269E 00	0.0000E 00	0.2126E 02	A20	0.3631E-01	0.6501E 00	0.0000E 00	0.2246E 02	A20	0.5114E 00	0.1713E 01	0.0000E 00	0.1692E 02																		
A21	0.1244E-01	0.1007E 00	0.0000E 00	0.1000E 01	A21	0.5428E-02	0.5845E-01	0.0000E 00	0.1000E 01	A21	0.7576E-02	0.8671E-01	0.0000E 00	0.1000E 01																		
A22	0.2841E 01	0.3522E 01	0.0000E 00	0.2778E 02	A22	0.2859E 01	0.2178E 01	0.0000E 00	0.2113E 02	A22	0.1719E 02	0.1597E 02	0.0000E 00	0.1250E 03																		
A23	0.1010E 01	0.0000E 00	0.0000E 00	0.1000E 01	A23	0.1000E 01	0.0000E 00	0.1000E 01	0.1000E 01	A23	0.1000E 01	0.0000E 00	0.1000E 01	0.1000E 01																		
A24	0.1165E 01	0.3092E 00	0.1000E 01	0.4000E 01	A24	0.1162E 01	0.4014E 00	0.1000E 01	0.4000E 01	A24	0.1177E 01	0.4444E 00	0.1000E 01	0.6000E 01																		
A25	0.1010E 01	0.0000E 00	0.0000E 00	0.1000E 01	A25	0.1000E 01	0.0000E 00	0.1000E 01	0.1000E 01	A25	0.1000E 01	0.0000E 00	0.1000E 01	0.1000E 01																		
A26	0.5013E 02	0.6882E 01	0.1800E 02	0.8500E 02	A26	0.4442E 02	0.1111E 02	0.1700E 02	0.8100E 02	A26	0.5042E 02	0.1117E 02	0.1900E 02	0.8700E 02																		
A27	0.5606E 00	0.4893E 00	0.0000E 00	0.1000E 01	A27	0.1071E 01	0.3039E 00	0.0000E 00	0.1000E 01	A27	0.6797E 00	0.4666E 00	0.0000E 00	0.1000E 01																		
A28	0.6343E 02	0.3935E 02	0.0000E 00	0.1000E 03	A28	0.2171E 02	0.2862E 02	0.0000E 00	0.1000E 03	A28	0.7574E 02	0.3556E 02	0.0000E 00	0.1000E 03																		
A29	0.3379E 02	0.3907E 02	0.0000E 00	0.1000E 03	A29	0.7812E 02	0.2868E 02	0.0000E 00	0.1000E 03	A29	0.2333E 02	0.3534E 02	0.0000E 00	0.1000E 03																		
A30	0.7747E 00	0.7759E 01	0.0000E 00	0.1000E 03	A30	0.1698E 00	0.2002E 01	0.0000E 00	0.4822E 02	A30	0.9233E 02	0.8062E 01	0.0000E 00	0.1000E 03																		
A31	0.1492E 00	0.3563E 00	0.0000E 00	0.1000E 01	A31	0.9426E-01	0.2922E 00	0.0000E 00	0.1000E 01	A31	0.1280E 00	0.3351E 00	0.0000E 00	0.1000E 01																		
A32	0.9776E 00	0.1265E 01	0.0000E 00	0.4000E 01	A32	0.1322E 01	0.1449E 01	0.0000E 00	0.4000E 01	A32	0.1384E 01	0.1452E 01	0.0000E 00	0.1000E 01																		
A33	0.5016E-01	0.2503E 00	0.0000E 00	0.2000E 01	A33	0.1246E 00	0.3731E 00	0.0000E 00	0.4000E 01	A33	0.1408E-01	0.1961E 00	0.0000E 00	0.1000E 01																		

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG

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POPULATION ASSIGNMENT BY CLASSIFICATION I

CLASS 12  
NO. OF OBSERVATIONS = 2183

Table with 7 columns: VARIABLE, MEAN, STAN.DEV., MINIMUM, MAXIMUM, 320, 101, 386, 592, 250, 525, 42. Rows include variables S01 to S06.

CLASS 13  
NO. OF OBSERVATIONS = 789

Table with 7 columns: VARIABLE, MEAN, STAN.DEV., MINIMUM, MAXIMUM, 34, 38, 607, 65, 42. Rows include variables S01 to S06.

CLASS 14  
NO. OF OBSERVATIONS = 1335

Table with 7 columns: VARIABLE, MEAN, STAN.DEV., MINIMUM, MAXIMUM, 43, 43, 847, 232, 122, 977. Rows include variables S01 to S06.

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POPULATION ASSIGNMENT BY CLASSIFICATION I

CLASS 15  
NO. OF OBSERVATIONS = 1291

VARIABLE	MEAN	STAN.DEV.	MINIMUM	MAXIMUM
S01	0.9567E 03	0.1462E 04	0.8000E 01	0.1800E 05
S02	0.7504E 03	0.1055E 04	0.6000E 01	0.8555E 04
S03	0.9743E 01	0.1316E 02	0.0000E 00	0.1370E 03
S04	0.1171E 01	0.7987E 00	0.1250E 00	0.5884E 01
S05	0.1282E 01	0.9916E 00	0.0000E 00	0.6000E 01
L01	0.1457E 02	0.2074E 02	0.0000E 00	0.1000E 03
L02	0.4869E 01	0.8658E 01	0.0000E 00	0.7683E 02
L03	0.147E 00	0.2526E 01	0.0000E 00	0.7018E 02
L04	0.9587E 00	0.5488E 01	0.0000E 00	0.5902E 03
L05	0.5546E 01	0.132E 02	0.0000E 00	0.1000E 03
L06	0.1433E 01	0.5584E 01	0.0000E 00	0.7315E 02
L07	0.1024E 01	0.2626E 01	0.0000E 00	0.3333E 02
L08	0.6724E 02	0.3194E 02	0.0000E 00	0.1000E 03
L09	0.1511E 01	0.7098E 01	0.0000E 00	0.7761E 02
L10	0.2077E 01	0.1231E 02	0.0000E 00	0.1000E 03
L11	0.1741E 01	0.8083E 01	0.0000E 00	0.8558E 02
L12	0.966E 01	0.1509E 02	0.0000E 00	0.9187E 02
L13	0.7941E 01	0.2698E 00	0.0000E 00	0.1000E 01
L14	0.146E 00	0.3188E 00	0.0000E 00	0.1000E 01
A01	0.4509E 01	0.1483E 02	0.0000E 00	0.1000E 03
A02	0.5626E 02	0.3276E 02	0.0000E 00	0.1000E 03
A03	0.2374E 02	0.2781E 02	0.0000E 00	0.1000E 03
A04	0.660E 01	0.2179E 02	0.0000E 00	0.1000E 03
A05	0.1127E 02	0.197E 02	0.0000E 00	0.1000E 03
A06	0.449E 01	0.1642E 02	0.0000E 00	0.1000E 03
A07	0.1860E 01	0.5081E 01	0.0000E 00	0.2781E 02
A08	0.2041E 01	0.3701E 01	0.641E 01	0.4688E 02
A09	0.9670E 02	0.1290E 02	0.9091E 01	0.1000E 03
A10	0.7249E 01	0.1884E 02	0.0000E 00	0.1000E 03
A11	0.278E 02	0.3815E 02	0.0000E 00	0.1000E 03
A12	0.578E 02	0.411E 02	0.0000E 00	0.1000E 03
A13	0.473E 01	0.131E 02	0.0000E 00	0.6667E 02
A14	0.3509E 01	0.1173E 02	0.0000E 00	0.6667E 02
A15	0.235E 00	0.424E 02	0.0000E 00	0.1000E 01
A16	0.125E 00	0.331E 00	0.0000E 00	0.1000E 01
A17	0.2864E 01	0.1668E 00	0.0000E 00	0.1000E 01
A18	0.378E 00	0.4930E 00	0.0000E 00	0.1000E 01
A19	0.3176E 01	0.1754E 01	0.0000E 00	0.1000E 01
A20	0.2203E 00	0.217E 01	0.0000E 00	0.4815E 02
A21	0.1064E 01	0.1038E 00	0.0000E 00	0.1000E 01
A22	0.316E 01	0.598E 01	0.0000E 00	0.3000E 02
A23	0.100E 01	0.1000E 00	0.1000E 01	0.1000E 01
A24	0.163E 01	0.4207E 00	0.1000E 01	0.4000E 01
A25	0.100E 01	0.0000E 00	0.1000E 01	0.1000E 01
A26	0.000E 00	0.000E 00	0.000E 00	0.000E 00
A27	0.3837E 02	0.7142E 01	0.1700E 02	0.7100E 02
A28	0.6512E 00	0.4765E 00	0.0000E 00	0.1000E 01
A29	0.5458E 02	0.4307E 02	0.000E 00	0.1000E 03
A30	0.451E 02	0.430E 02	0.000E 00	0.1000E 03
A31	0.520E 00	0.3892E 01	0.0000E 00	0.7148E 02
A32	0.1549E 00	0.3618E 01	0.0000E 00	0.1000E 01
A33	0.101E 01	0.1313E 01	0.0000E 00	0.4000E 01
A34	0.6274E 01	0.2754E 00	0.0000E 00	0.5000E 01

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23 377 237 155 255 36

CLASS 16  
NO. OF OBSERVATIONS = 326

VARIABLE	MEAN	STAN.DEV.	MINIMUM	MAXIMUM
S01	0.4633E 03	0.1239E 04	0.2000E 01	0.1463E 05
S02	0.2505E 03	0.6067E 03	0.1000E 01	0.6497E 04
S03	0.1908E 03	0.7427E 03	0.0000E 00	0.1096E 05
S04	0.18549E 00	0.8049E 00	0.1250E 00	0.4375E 01
S05	0.6288E 00	0.9690E 00	0.0000E 00	0.6000E 01
L01	0.4637E 01	0.1458E 02	0.0000E 00	0.1000E 03
L02	0.3550E 01	0.1208E 02	0.0000E 00	0.9615E 02
L03	0.4636E 00	0.3232E 01	0.0000E 00	0.5128E 02
L04	0.1914E 01	0.1019E 02	0.0000E 00	0.1000E 03
L05	0.4368E 01	0.1452E 02	0.0000E 00	0.1000E 03
L06	0.1264E 01	0.7563E 01	0.0000E 00	0.8801E 02
L07	0.4301E 02	0.4600E 02	0.0000E 00	0.1000E 03
L08	0.2831E 02	0.3972E 02	0.0000E 00	0.1000E 03
L09	0.8298E 01	0.2473E 02	0.0000E 00	0.1000E 03
L10	0.4403E 01	0.1670E 02	0.0000E 00	0.1000E 03
L11	0.1032E 02	0.2266E 02	0.0000E 00	0.9962E 02
L12	0.3471E 02	0.2784E 02	0.0000E 00	0.9709E 02
L13	0.2761E 01	0.1638E 00	0.0000E 00	0.1000E 01
L14	0.3988E 01	0.1957E 00	0.0000E 00	0.1000E 01
A01	0.9138E 01	0.6403E 00	0.0000E 00	0.8451E 01
A02	0.2576E 01	0.1237E 02	0.0000E 00	0.1000E 03
A03	0.5724E 01	0.2032E 02	0.0000E 00	0.1000E 03
A04	0.1027E 01	0.9018E 01	0.0000E 00	0.1000E 03
A05	0.5724E 02	0.4464E 02	0.0000E 00	0.1000E 03
A06	0.227E 02	0.3713E 02	0.0000E 00	0.1000E 03
A07	0.3160E 02	0.9709E 02	0.0000E 00	0.9643E 03
A08	0.2243E 02	0.3599E 02	0.9443E 01	0.2500E 03
A09	0.9371E 02	0.1932E 02	0.0000E 00	0.1000E 03
A10	0.4100E 01	0.1395E 02	0.0000E 00	0.1000E 03
A11	0.1329E 02	0.3063E 02	0.0000E 00	0.1000E 03
A12	0.2055E 02	0.3681E 02	0.0000E 00	0.1000E 03
A13	0.4474E 02	0.4600E 02	0.0000E 00	0.1000E 03
A14	0.1732E 02	0.3555E 02	0.0000E 00	0.1000E 03
A15	0.1043E 00	0.3056E 00	0.0000E 00	0.1000E 01
A16	0.1154E 00	0.3243E 00	0.0000E 00	0.1000E 01
A17	0.3067E 02	0.5530E 01	0.0000E 00	0.1000E 01
A18	0.2761E 00	0.4471E 00	0.0000E 00	0.1000E 01
A19	0.1227E 01	0.1101E 00	0.0000E 00	0.1000E 01
A20	0.3379E 00	0.3426E 01	0.0000E 00	0.5000E 02
A21	0.7562E 01	0.2612E 01	0.0000E 00	0.1000E 01
A22	0.5299E 01	0.9646E 01	0.0000E 00	0.9091E 02
A23	0.9724E 00	0.1638E 00	0.0000E 00	0.1000E 01
A24	0.1181E 01	0.4510E 00	0.1000E 01	0.3000E 01
A25	0.8742E 00	0.3316E 00	0.0000E 00	0.1000E 01
A26	0.9816E 01	0.2973E 00	0.0000E 00	0.1000E 01
A27	0.5238E 02	0.1381E 02	0.1500E 02	0.8700E 02
A28	0.3000E 00	0.5000E 00	0.0000E 00	0.1000E 01
A29	0.8448E 02	0.3425E 02	0.0000E 00	0.1000E 03
A30	0.1478E 02	0.3360E 02	0.0000E 00	0.1000E 03
A31	0.7447E 00	0.8149E 01	0.0000E 00	0.1000E 03
A32	0.2488E 00	0.4321E 00	0.0000E 00	0.1000E 01
A33	0.9571E 00	0.1248E 01	0.0000E 00	0.4000E 01
A34	0.2045E 00	0.4521E 00	0.0000E 00	0.2000E 01

FRANCE BELGIUM HOLLAND GERMANY ITALY LUXEMBOURG  
108 03 113 32 6 4



POPULATION ASSIGNMENT BY CLASSIFICATION II

TOTAL NO. OF OBSERVATIONS = 21743		CLASS 1 NO. OF OBSERVATIONS = 3533		CLASS 2 NO. OF OBSERVATIONS = 1821												
VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM		
S01	0.2075E	04	0.7427E	04	0.2000E	01	0.7513E	06	0.8365E	03	0.3534E	04	0.5000E	01	0.1402E	00
S02	0.1659E	04	0.4397E	04	0.1000E	01	0.4131E	06	0.6295E	03	0.1132E	04	0.4000E	01	0.2000E	03
S03	0.1800E	02	0.9663E	02	0.0000E	00	0.1096E	03	0.5017E	01	0.9874E	01	0.0000E	00	0.1923E	03
S04	0.1061E	01	0.4164E	01	0.2733E	02	0.4346E	03	0.7270E	01	0.1072E	01	0.2500E	00	0.2068E	02
S05	0.2586E	01	0.2034E	01	0.0000E	00	0.5400E	03	0.4396E	01	0.1451E	01	0.0000E	00	0.1600E	02
S06	0.2504E	02	0.2358E	02	0.0600E	00	0.1000E	03	0.3670E	02	0.1586E	02	0.0000E	00	0.1000E	03
L01	0.2733E	01	0.1121E	01	0.0000E	00	0.1000E	03	0.7159E	01	0.7095E	01	0.0000E	00	0.4474E	02
L02	0.4774E	01	0.3499E	01	0.0000E	00	0.1000E	03	0.8271E	01	0.1906E	01	0.0000E	00	0.3123E	02
L03	0.3274E	01	0.1586E	01	0.0000E	00	0.1000E	03	0.7231E	01	0.9942E	01	0.0000E	00	0.2860E	02
L04	0.9677E	01	0.1619E	01	0.0000E	00	0.1000E	03	0.1048E	02	0.1202E	02	0.0000E	00	0.7794E	02
L05	0.1185E	01	0.8126E	01	0.0000E	00	0.1000E	03	0.8258E	00	0.7223E	01	0.0000E	00	0.5875E	02
L06	0.1538E	01	0.6156E	01	0.0000E	00	0.1000E	03	0.8269E	00	0.7242E	01	0.0000E	00	0.1872E	02
L07	0.4008E	02	0.3479E	02	0.0000E	00	0.1000E	03	0.8368E	02	0.2296E	02	0.0000E	00	0.1000E	03
L08	0.4574E	01	0.1595E	01	0.0000E	00	0.1000E	03	0.6667E	01	0.5984E	01	0.0000E	00	0.6175E	02
L09	0.6279E	01	0.1677E	01	0.0000E	00	0.1000E	03	0.5344E	00	0.2973E	01	0.0000E	00	0.6588E	02
L10	0.2007E	01	0.8962E	01	0.0000E	00	0.9962E	02	0.8049E	00	0.3519E	01	0.0000E	00	0.7816E	02
L11	0.9473E	01	0.1461E	01	0.0000E	00	0.9972E	02	0.8541E	01	0.1214E	02	0.0000E	00	0.8703E	02
L12	0.1177E	00	0.3141E	00	0.0000E	00	0.1000E	01	0.4982E	01	0.2176E	00	0.0000E	00	0.1000E	01
L13	0.2277E	00	0.4933E	00	0.0000E	00	0.1000E	01	0.2471E	00	0.4281E	00	0.0000E	00	0.1000E	01
L14	0.4378E	01	0.1577E	01	0.0000E	00	0.1000E	03	0.1046E	01	0.3524E	01	0.0000E	00	0.7500E	02
A01	0.2668E	02	0.2965E	02	0.0000E	00	0.1000E	03	0.4080E	02	0.1615E	02	0.0000E	00	0.1000E	03
A02	0.2458E	02	0.2632E	02	0.0000E	00	0.1000E	03	0.4528E	02	0.1823E	02	0.0000E	00	0.1000E	03
A03	0.3167E	01	0.1454E	01	0.0000E	00	0.1000E	03	0.5675E	00	0.4567E	01	0.0000E	00	0.9349E	02
A04	0.1744E	02	0.2360E	02	0.0000E	00	0.1000E	03	0.1807E	02	0.1768E	02	0.0000E	00	0.1000E	03
A05	0.4671E	01	0.1551E	01	0.0000E	00	0.9643E	03	0.4012E	01	0.1092E	02	0.0000E	00	0.1000E	03
A06	0.1056E	01	0.1056E	01	0.0000E	00	0.9643E	03	0.1551E	01	0.1271E	01	0.0000E	00	0.1713E	02
A07	0.3758E	01	0.1056E	01	0.0000E	00	0.6042E	03	0.1349E	01	0.1139E	01	0.7302E	01	0.1698E	02
A08	0.8443E	02	0.8222E	02	0.0000E	00	0.1000E	03	0.9740E	02	0.1686E	02	0.4835E	01	0.1000E	03
A09	0.6523E	01	0.1768E	01	0.0000E	00	0.1000E	03	0.1375E	02	0.2006E	02	0.0000E	00	0.1000E	03
A10	0.1743E	02	0.2605E	02	0.0000E	00	0.1000E	03	0.1929E	02	0.2552E	02	0.0000E	00	0.1000E	03
A11	0.2154E	02	0.3336E	02	0.0000E	00	0.1000E	03	0.3378E	02	0.2844E	02	0.0000E	00	0.1000E	03
A12	0.4409E	02	0.8919E	02	0.0000E	00	0.1000E	03	0.5576E	02	0.2844E	02	0.0000E	00	0.1000E	03
A13	0.1322E	02	0.2786E	02	0.0000E	00	0.1000E	03	0.1001E	02	0.1664E	02	0.0000E	00	0.7500E	02
A14	0.4844E	00	0.4998E	00	0.0000E	00	0.1000E	01	0.9307E	00	0.2540E	00	0.0000E	00	0.1000E	01
A15	0.1367E	00	0.3456E	00	0.0000E	00	0.1000E	01	0.8633E	01	0.2808E	00	0.0000E	00	0.1000E	01
A16	0.1778E	00	0.8233E	00	0.0000E	00	0.1000E	01	0.7010E	00	0.4583E	00	0.0000E	00	0.1000E	01
A17	0.6306E	00	0.8439E	00	0.0000E	00	0.1000E	01	0.6735E	00	0.6671E	00	0.0000E	00	0.1000E	01
A18	0.2814E	00	0.4498E	00	0.0000E	00	0.1000E	01	0.8324E	00	0.3735E	00	0.0000E	00	0.1000E	01
A19	0.1048E	01	0.8110E	01	0.0000E	00	0.1000E	03	0.1700E	01	0.4072E	00	0.0000E	00	0.2266E	02
A20	0.4975E	01	0.2137E	01	0.0000E	00	0.1000E	03	0.1700E	01	0.1682E	01	0.0000E	00	0.1000E	01
A21	0.3078E	01	0.1622E	01	0.0000E	00	0.5000E	03	0.4512E	01	0.2146E	01	0.0000E	00	0.3333E	02
A22	0.4709E	01	0.8222E	01	0.0000E	00	0.4000E	01	0.1000E	01	0.0000E	00	0.1000E	01	0.1000E	01
A23	0.1254E	01	0.5943E	01	0.0000E	00	0.4000E	01	0.1510E	01	0.7124E	00	0.1000E	01	0.4000E	01
A24	0.6707E	00	0.3338E	00	0.0000E	00	0.1000E	01	0.1000E	01	0.0000E	00	0.1000E	01	0.1000E	01
A25	0.7508E	01	0.2644E	01	0.0000E	00	0.1000E	01	0.4098E	02	0.1241E	02	0.1800E	02	0.9100E	02
A26	0.2600E	00	0.4115E	00	0.0000E	00	0.1000E	01	0.8746E	01	0.2825E	00	0.0000E	00	0.1000E	01
A27	0.9177E	02	0.1622E	02	0.0000E	00	0.1000E	03	0.7033E	02	0.3148E	02	0.0000E	00	0.1000E	03
A28	0.8423E	02	0.8222E	02	0.0000E	00	0.1000E	03	0.2689E	02	0.5050E	02	0.0000E	00	0.1000E	03
A29	0.4703E	01	0.8223E	01	0.0000E	00	0.1000E	03	0.2781E	01	0.1103E	02	0.0000E	00	0.1000E	03
A30	0.4200E	00	0.4142E	00	0.0000E	00	0.1000E	01	0.1673E	00	0.3732E	00	0.0000E	00	0.1000E	01
A31	0.1518E	01	0.1506E	01	0.0000E	00	0.4000E	01	0.2910E	01	0.1150E	01	0.0000E	00	0.4000E	01
A32	0.9858E	01	0.3179E	01	0.0000E	00	0.5000E	01	0.8548E	01	0.5166E	00	0.0000E	00	0.4000E	01

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POPULATION ASSIGNMENT BY CLASSIFICATION II

CLASS 5 NO. OF OBSERVATIONS = 1733							CLASS 4 NO. OF OBSERVATIONS = 1117							CLASS 5 NO. OF OBSERVATIONS = 1079						
VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM						
S01	0.7570E 03	0.1239E 04	0.1200E 02	0.1680E 05	S01	0.0341E 04	0.3009E 05	0.1500E 05	0.7513E 06	S01	0.4972E 04	0.6176E 04	0.1200E 02	0.6676E 05						
S02	0.6764E 03	0.9708E 03	0.8000E 01	0.1321E 05	S02	0.4001E 04	0.7656E 05	0.1200E 02	0.4131E 06	S02	0.4632E 04	0.5231E 04	0.8000E 01	0.6387E 05						
S03	0.2769E 01	0.1345E 02	0.0000E 00	0.3242E 03	S03	0.1705E 02	0.4803E 02	0.0000E 00	0.7316E 03	S03	0.1518E 02	0.2250E 02	0.0000E 00	0.2718E 03						
S04	0.1876E 01	0.1309E 01	0.1250E 00	0.1204E 02	S04	0.2828E 01	0.4552E 01	0.7273E-02	0.7163E 02	S04	0.2777E 01	0.1933E 01	0.1250E 00	0.2699E 02						
S05	0.1471E 01	0.1367E 01	0.0000E 00	0.8000E 01	S05	0.2541E 01	0.2875E 01	0.0000E 00	0.3600E 02	S05	0.5617E 01	0.2931E 01	0.0000E 00	0.5400E 02						
L01	0.2003E 02	0.2009E 02	0.0000E 00	0.1000E 03	L01	0.2447E 02	0.2570E 02	0.0000E 00	0.1000E 03	L01	0.4375E 02	0.2033E 02	0.0000E 00	0.2907E 02						
L02	0.2875E 01	0.6587E 01	0.0000E 00	0.5116E 02	L02	0.3775E 01	0.1133E 02	0.0000E 00	0.1000E 03	L02	0.2977E 02	0.2019E 02	0.0000E 00	0.1000E 03						
L03	0.3075E 00	0.2617E 01	0.0000E 00	0.3922E 02	L03	0.2019E 00	0.4279E 01	0.0000E 00	0.7376E 02	L03	0.5667E 01	0.1035E 02	0.0000E 00	0.1000E 03						
L04	0.1843E 01	0.7977E 01	0.0000E 00	0.6000E 02	L04	0.2053E 01	0.1157E 02	0.0000E 00	0.1000E 03	L04	0.1271E 01	0.6970E 01	0.0000E 00	0.1000E 03						
L05	0.3143E 01	0.1305E 02	0.0000E 00	0.1000E 03	L05	0.1133E 02	0.1943E 02	0.0000E 00	0.1000E 03	L05	0.1764E 01	0.1990E 01	0.0000E 00	0.1000E 03						
L06	0.4730E 01	0.1266E 02	0.0000E 00	0.1000E 03	L06	0.1380E 01	0.4112E 01	0.0000E 00	0.8696E 02	L06	0.5941E 00	0.2533E 01	0.0000E 00	0.3899E 02						
L07	0.1427E 01	0.3887E 01	0.0000E 00	0.3636E 02	L07	0.0882E 00	0.2462E 01	0.0000E 00	0.4000E 02	L07	0.3935E 00	0.1711E 01	0.0000E 00	0.2143E 02						
L08	0.5866E 01	0.1442E 02	0.0000E 00	0.1000E 03	L08	0.2222E 02	0.3647E 02	0.0000E 00	0.1000E 03	L08	0.9551E 01	0.1367E 02	0.0000E 00	0.1000E 03						
L09	0.2599E 02	0.3522E 02	0.0000E 00	0.1000E 03	L09	0.2247E 01	0.1932E 02	0.0000E 00	0.1000E 03	L09	0.1679E 00	0.1574E 01	0.0000E 00	0.3642E 02						
L10	0.3622E 02	0.5870E 02	0.0000E 00	0.1000E 03	L10	0.1363E 02	0.2850E 02	0.0000E 00	0.9275E 02	L10	0.1135E 01	0.1592E 01	0.0000E 00	0.6549E 02						
L11	0.4251E 01	0.1360E 02	0.0000E 00	0.9884E 02	L11	0.2737E 01	0.1040E 02	0.0000E 00	0.1000E 03	L11	0.2446E 00	0.2873E 01	0.0000E 00	0.6239E 02						
L12	0.9162E 01	0.1565E 02	0.0000E 00	0.9680E 02	L12	0.1416E 02	0.2041E 02	0.0000E 00	0.9441E 02	L12	0.5578E 01	0.8184E 01	0.0000E 00	0.9997E 02						
L13	0.2135E 00	0.4938E 00	0.0000E 00	0.1000E 01	L13	0.1978E 00	0.5935E 00	0.0000E 00	0.1000E 01	L13	0.2873E-01	0.1670E 00	0.0000E 00	0.9997E 02						
L14	0.3567E-01	0.1555E 00	0.0000E 00	0.1000E 01	L14	0.1397E 00	0.3466E 00	0.0000E 00	0.1000E 01	L14	0.5601E 00	0.4817E 00	0.0000E 00	0.1000E 01						
A01	0.1702E 02	0.3669E 02	0.0000E 00	0.1000E 03	A01	0.4558E 01	0.1807E 02	0.0000E 00	0.1000E 03	A01	0.4327E 01	0.1597E 02	0.0000E 00	0.1000E 03						
A02	0.1953E 01	0.1124E 02	0.0000E 00	0.1000E 03	A02	0.2044E 02	0.2908E 02	0.0000E 00	0.1000E 03	A02	0.1874E 02	0.2660E 02	0.0000E 00	0.1000E 03						
A03	0.3660E 01	0.1407E 02	0.0000E 00	0.1000E 03	A03	0.1744E 02	0.2620E 02	0.0000E 00	0.1000E 03	A03	0.5065E 02	0.3689E 02	0.0000E 00	0.1000E 03						
A04	0.2277E 01	0.1348E 02	0.0000E 00	0.1000E 03	A04	0.3630E 01	0.1524E 02	0.0000E 00	0.1000E 03	A04	0.5043E 01	0.1845E 02	0.0000E 00	0.1000E 03						
A05	0.1733E 02	0.3120E 02	0.0000E 00	0.1000E 03	A05	0.1109E 02	0.2213E 02	0.0000E 00	0.1000E 03	A05	0.7423E 01	0.2068E 02	0.0000E 00	0.1000E 03						
A06	0.4681E 01	0.1892E 02	0.0000E 00	0.1000E 03	A06	0.5846E 01	0.1550E 02	0.0000E 00	0.1000E 03	A06	0.8545E 01	0.2347E 02	0.0000E 00	0.1000E 03						
A07	0.4537E 00	0.1513E 01	0.0000E 00	0.2507E 02	A07	0.6974E 00	0.2019E 01	0.0000E 00	0.2676E 02	A07	0.5070E 00	0.1175E 01	0.0000E 00	0.1000E 03						
M01	0.6468E 01	0.5317E 01	0.6210E-01	0.5919E 02	M01	0.2521E 01	0.6865E 01	0.1452E-03	0.7798E 02	M01	0.1434E 00	0.3501E 01	0.1327E-01	0.6255E 02						
M02	0.7826E 02	0.2512E 02	0.1428E 01	0.1000E 03	M02	0.6953E-01	0.2091E 01	0.0000E 00	0.1000E 03	M02	0.9314E 02	0.2994E 02	0.1056E 01	0.1000E 03						
M03	0.6433E 01	0.1665E 02	0.0000E 00	0.1000E 03	M03	0.4638E 01	0.1504E 02	0.0000E 00	0.1000E 03	M03	0.1747E 02	0.1927E 02	0.0000E 00	0.1000E 03						
M04	0.1146E 02	0.2511E 02	0.0000E 00	0.1000E 03	M04	0.1263E 02	0.2536E 02	0.0000E 00	0.1000E 03	M04	0.1871E 02	0.2716E 02	0.0000E 00	0.1000E 03						
M05	0.2510E 02	0.3651E 02	0.0000E 00	0.1000E 03	M05	0.1759E 02	0.3116E 02	0.0000E 00	0.1000E 03	M05	0.2372E 02	0.2986E 02	0.0000E 00	0.1000E 03						
M06	0.3060E 01	0.1439E 02	0.0000E 00	0.1000E 03	M06	0.3526E 02	0.4023E 02	0.0000E 00	0.1000E 03	M06	0.4769E 02	0.3232E 02	0.0000E 00	0.1000E 03						
M07	0.4266E 00	0.4322E 00	0.0000E 00	0.1000E 01	M07	0.6593E 02	0.2002E 02	0.0000E 00	0.1000E 03	M07	0.4769E 01	0.1366E 02	0.0000E 00	0.1000E 03						
M08	0.6355E 00	0.4405E 00	0.0000E 00	0.1000E 01	M08	0.4011E 00	0.4901E 00	0.0000E 00	0.1000E 01	M08	0.8469E 00	0.5581E 00	0.0000E 00	0.1000E 03						
M09	0.3104E-02	0.7305E-01	0.0000E 00	0.1000E 01	M09	0.1996E 00	0.3997E 00	0.0000E 00	0.1000E 01	M09	0.6302E-01	0.2630E 00	0.0000E 00	0.1000E 01						
M10	0.2253E 00	0.4994E 00	0.0000E 00	0.1000E 01	M10	0.1533E 00	0.5582E 00	0.0000E 00	0.1000E 01	M10	0.5472E 00	0.4833E 00	0.0000E 00	0.1000E 01						
M11	0.2754E-03	0.2368E-01	0.0000E 00	0.1000E 01	M11	0.6034E 00	0.4892E 00	0.0000E 00	0.1000E 01	M11	0.8795E 00	0.5745E 00	0.0000E 00	0.1000E 01						
M12	0.1824E 00	0.1489E 01	0.0000E 00	0.2500E 02	M12	0.1728E 00	0.3781E 00	0.0000E 00	0.1000E 01	M12	0.1687E 00	0.3200E 00	0.0000E 00	0.1000E 01						
M13	0.3403E 00	0.4767E 00	0.0000E 00	0.1000E 01	M13	0.2458E 00	0.2473E 01	0.0000E 00	0.5000E 02	M13	0.3682E-01	0.4439E 00	0.0000E 00	0.8358E 01						
M14	0.6433E 01	0.1025E 02	0.0000E 00	0.1000E 03	M14	0.1038E 00	0.3031E 01	0.0000E 00	0.1000E 01	M14	0.1019E-01	0.1005E 00	0.0000E 00	0.1000E 01						
M15	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M15	0.2369E 01	0.4183E 01	0.0000E 00	0.5000E 02	M15	0.3575E 01	0.1076E 02	0.0000E 00	0.2687E 03						
M16	0.1158E 01	0.4842E 00	0.1000E 01	0.4000E 01	M16	0.8923E-03	0.2991E-01	0.0000E 00	0.1000E 01	M16	0.1902E 01	0.0000E 00	0.1000E 01	0.1000E 01						
M17	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M17	0.1357E 01	0.7958E 00	0.1000E 01	0.4000E 01	M17	0.1902E 01	0.0000E 00	0.1000E 01	0.1000E 01						
M18	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M18	0.8053E-03	0.2991E-01	0.0000E 00	0.1000E 01	M18	0.1902E 01	0.0000E 00	0.1000E 01	0.1000E 01						
M19	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M19	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	M19	0.1902E 01	0.0000E 00	0.1000E 01	0.1000E 01						
M20	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M20	0.5198E 02	0.7776E 00	0.2600E 02	0.5200E 02	M20	0.4903E 02	0.1149E 02	0.2000E 02	0.8700E 02						
M21	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M21	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	M21	0.1659E 00	0.3720E 00	0.0000E 00	0.1000E 01						
M22	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M22	0.7391E 02	0.4033E 02	0.0000E 00	0.1000E 03	M22	0.3672E 02	0.3980E 02	0.0000E 00	0.1000E 03						
M23	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M23	0.1301E 02	0.2984E 02	0.0000E 00	0.1000E 03	M23	0.8543E 02	0.5990E 02	0.0000E 00	0.1000E 03						
M24	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M24	0.1249E 02	0.5269E 02	0.0000E 00	0.1000E 03	M24	0.3665E 00	0.5473E 01	0.0000E 00	0.1000E 03						
M25	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M25	0.2731E 00	0.4455E 00	0.0000E 00	0.1000E 01	M25	0.2312E 00	0.4433E 01	0.0000E 00	0.1000E 03						
M26	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M26	0.1011E 01	0.1583E 01	0.0000E 00	0.4000E 01	M26	0.2767E 01	0.1452E 01	0.0000E 00	0.4000E 01						
M27	0.1100E 01	0.0000E 00	0.1000E 01	0.1000E 01	M27	0.1164E 00	0.3842E 00	0.0000E 00	0.3000E 01	M27	0.2208E 00	0.4667E 00	0.0000E 00	0.3000E 01						

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POPULATION ASSIGNMENT BY CLASSIFICATION II

CLASS 10		CLASS 11							
NO. OF OBSERVATIONS = 3185		NO. OF OBSERVATIONS = 354							
VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.1037E 04	0.1918E 04	0.6000E 01	0.2685E 05	S01	0.4540E 03	0.1193E 04	0.2000F 01	0.1463E 05
S02	0.8513E 03	0.1710E 04	0.6000E 01	0.2685E 05	S02	0.2549E 03	0.5901E 03	0.1000E 01	0.6427E 04
S03	0.7788E 01	0.1568E 02	0.0000E 00	0.2042E 03	S03	0.1796E 03	0.7135E 03	0.0000E 00	0.1096E 05
S04	0.1310E 01	0.1298E 01	0.1250E 00	0.1681E 02	S04	0.8900E 00	0.8624E 00	0.1250E 00	0.5000E 01
S05	0.1658E 01	0.1592E 01	0.0000E 00	0.1300E 02	S05	0.0723E 00	0.9886E 00	0.0000E 00	0.6000E 01
L01	0.2171E 02	0.2425E 02	0.0000E 00	0.1000E 03	L01	0.3141E 01	0.1499E 02	0.0000E 00	0.1000E 03
L02	0.9531E 01	0.1104E 02	0.0000E 00	0.1000E 03	L02	0.5977E 01	0.1226E 02	0.0000E 00	0.9615E 02
L03	0.3006E 00	0.2958E 01	0.0000E 00	0.8647E 02	L03	0.2573E 01	0.3092E 01	0.0000E 00	0.528E 02
L04	0.7145E 00	0.5477E 01	0.0000E 00	0.7500E 02	L04	0.1822E 01	0.9758E 01	0.0000E 00	0.1000E 03
L05	0.8426E 01	0.1771E 02	0.0000E 00	0.1000E 03	L05	0.4679E 01	0.1495E 02	0.0000E 00	0.1000E 03
L06	0.1521E 01	0.7726E 01	0.0000E 00	0.9600E 02	L06	0.1415E 01	0.8959E 01	0.0000E 00	0.1000E 03
L07	0.1549E 01	0.4834E 01	0.0000E 00	0.5000E 02	L07	0.4039E 02	0.4519E 02	0.0000E 00	0.1000E 03
L08	0.4358E 02	0.3705E 02	0.0000E 00	0.1000E 03	L08	0.3091E 02	0.4039E 02	0.0000E 00	0.1000E 03
L09	0.0907E 01	0.2045E 02	0.0000E 00	0.1000E 03	L09	0.7431E 01	0.2364E 02	0.0000E 00	0.1000E 03
L10	0.9506E 01	0.2469E 02	0.0000E 00	0.1000E 03	L10	0.4063E 01	0.1605E 02	0.0000E 00	0.1000E 03
L11	0.5871E 01	0.1204E 02	0.0000E 00	0.957E 02	L11	0.9156E 01	0.2182E 02	0.0000E 00	0.9842E 02
L12	0.1021E 02	0.1573E 02	0.0000E 00	0.9249E 02	L12	0.3332E 02	0.2745E 02	0.0000E 00	0.979E 02
L13	0.1107E 00	0.5138E 00	0.0000E 00	0.1000E 01	L13	0.2542E-01	0.1574E 00	0.0000E 00	0.1000E 01
L14	0.1434E 00	0.3555E 00	0.0000E 00	0.1000E 01	L14	0.4520E-01	0.2077E 00	0.0000E 00	0.1000E 01
A01	0.3423E 01	0.1833E 02	0.0000E 00	0.1000E 03	A01	0.1076E 00	0.6480E 00	0.0000E 00	0.8451E 01
A02	0.2450E 02	0.3318E 02	0.0000E 00	0.1000E 03	A02	0.2429E 01	0.1189E 02	0.0000E 00	0.1000E 03
A03	0.1702E 02	0.2472E 02	0.0000E 00	0.1000E 03	A03	0.5951E 01	0.4025E 02	0.0000E 00	0.1000E 03
A04	0.3572E 01	0.1552E 02	0.0000E 00	0.1000E 03	A04	0.9742E 00	0.6458E 01	0.0000E 00	0.1000E 03
A05	0.1844E 02	0.2468E 02	0.0000E 00	0.1000E 03	A05	0.5757E 02	0.4419E 02	0.0000E 00	0.1000E 03
A06	0.5068E 01	0.1746E 02	0.0000E 00	0.1000E 03	A06	0.2336E 02	0.3731E 02	0.0000E 00	0.1000E 03
A07	0.1164E 01	0.2432E 01	0.0000E 00	0.304E 02	A07	0.4803E 02	0.3667E 02	0.0000E 00	0.9643E 03
M01	0.3607E 01	0.1636E 01	0.3086E-01	0.5937E 02	M01	0.4078E 02	0.3369E 02	0.9445E-01	0.280E 03
M02	0.8452E 02	0.2733E 01	0.1246E 00	0.1000E 03	M02	0.9407E 02	0.1843E 02	0.0000E 00	0.1000E 03
M03	0.6727E 01	0.1716E 02	0.0000E 00	0.1000E 03	M03	0.4369E 01	0.1436E 02	0.0000E 00	0.1000E 03
M04	0.1109E 02	0.2330E 02	0.0000E 00	0.1000E 03	M04	0.1392E 02	0.3117E 02	0.0000E 00	0.1000E 03
M05	0.1046E 02	0.5026E 02	0.0000E 00	0.1000E 03	M05	0.2136E 02	0.3734E 02	0.0000E 00	0.1000E 03
M06	0.4354E 02	0.4052E 02	0.0000E 00	0.1000E 03	M06	0.4403E 02	0.4574E 02	0.0000E 00	0.1000E 03
M07	0.2038E 02	0.5440E 02	0.0000E 00	0.1000E 03	M07	0.1632E 02	0.3472E 02	0.0000E 00	0.1000E 03
M08	0.4503E 00	0.4332E 00	0.0000E 00	0.1000E 01	M08	0.1073E 00	0.3096E 00	0.0000E 00	0.1000E 01
M09	0.8135E-01	0.2730E 00	0.0000E 00	0.1000E 01	M09	0.1213E 00	0.3267E 00	0.0000E 00	0.1000E 01
M10	0.7799E-01	0.2682E 00	0.0000E 00	0.1000E 01	M10	0.2823E-02	0.5307E-01	0.0000E 00	0.1000E 01
M11	0.6877E 00	0.4621E 00	0.0000E 00	0.1000E 01	M11	0.3051E 00	0.4604E 00	0.0000E 00	0.1000E 01
M12	0.1214E 00	0.3266E 00	0.0000E 00	0.1000E 01	M12	0.1452E-01	0.1180E 00	0.0000E 00	0.1000E 01
M13	0.2361E 00	0.5175E 01	0.0000E 00	0.6667E 02	M13	0.5881E 00	0.4016E 00	0.0000E 00	0.5455E 02
M14	0.5912E-01	0.2358E 00	0.0000E 00	0.1000E 01	M14	0.6780E-01	0.2514E 00	0.0000E 00	0.4000E 01
M15	0.4451E 01	0.7349E 01	0.0000E 00	0.1000E 03	M15	0.5653E 01	0.9856E 01	0.0000E 00	0.9691E 02
M16	0.1000E 01	0.7000E 00	0.1000E 01	0.1000E 01	M16	0.9802E 00	0.1392E 00	0.0000E 00	0.5000E 01
M17	0.1042E 01	0.2584E 00	0.1000E 01	0.4000E 01	M17	0.1215E 01	0.4845E 00	0.0000E 00	0.5000E 01
M18	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	M18	0.4903E 00	0.5022E 00	0.0000E 00	0.1000E 01
M19	0.1000E 01	0.0000E 00	0.1000E 01	0.1000E 01	M19	0.6192E-01	0.2742E 00	0.0000E 00	0.1000E 01
M20	0.5571E 02	0.1299E 02	0.2000E 02	0.9100E 02	M20	0.5153E 02	0.1377E 02	0.1500E 02	0.8700E 02
M21	0.1358E 00	0.5626E 00	0.0000E 00	0.1000E 01	M21	0.3068E 00	0.5000E 00	0.0000E 00	0.5000E 01
M22	0.7355E 02	0.3899E 02	0.0000E 00	0.1000E 03	M22	0.8232E 02	0.3508E 02	0.0000E 00	0.1000E 03
M23	0.2324E 02	0.5676E 02	0.0000E 00	0.1000E 03	M23	0.1669E 02	0.3535E 02	0.0000E 00	0.1000E 03
M24	0.2610E 02	0.1818E 02	0.0000E 00	0.1000E 03	M24	0.6858E 00	0.7823E 01	0.0000E 00	0.1000E 03
M25	0.7296E-01	0.2601E 00	0.0000E 00	0.1000E 01	M25	0.2768E 00	0.4474E 00	0.0000E 00	0.1000E 01
M26	0.1036E 01	0.1362E 01	0.0000E 00	0.4000E 01	M26	0.1031E 01	0.1274E 01	0.0000E 00	0.4000E 01
M27	0.4340E-01	0.2299E 00	0.0000E 00	0.3000E 01	M27	0.2175E 00	0.4664E 00	0.0000E 00	0.2000E 01

CLASS 10		CLASS 11							
NO. OF OBSERVATIONS = 1590		NO. OF OBSERVATIONS = 354							
VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.1007E 04	0.1918E 04	0.6000E 01	0.2685E 05	S01	0.4540E 03	0.1193E 04	0.2000F 01	0.1463E 05
S02	0.8513E 03	0.1710E 04	0.6000E 01	0.2685E 05	S02	0.2549E 03	0.5901E 03	0.1000E 01	0.6427E 04
S03	0.7788E 01	0.1568E 02	0.0000E 00	0.2042E 03	S03	0.1796E 03	0.7135E 03	0.0000E 00	0.1096E 05
S04	0.1310E 01	0.1298E 01	0.1250E 00	0.1681E 02	S04	0.8900E 00	0.8624E 00	0.1250E 00	0.5000E 01
S05	0.1658E 01	0.1592E 01	0.0000E 00	0.1300E 02	S05	0.0723E 00	0.9886E 00	0.0000E 00	0.6000E 01
L01	0.2171E 02	0.2425E 02	0.0000E 00	0.1000E 03	L01	0.3141E 01	0.1499E 02	0.0000E 00	0.1000E 03
L02	0.9531E 01	0.1104E 02	0.0000E 00	0.1000E 03	L02	0.5977E 01	0.1226E 02	0.0000E 00	0.9615E 02
L03	0.3006E 00	0.2958E 01	0.0000E 00	0.8647E 02	L03	0.2573E 01	0.3092E 01	0.0000E 00	0.528E 02
L04	0.7145E 00	0.5477E 01	0.0000E 00	0.7500E 02	L04	0.1822E 01	0.9758E 01	0.0000E 00	0.1000E 03
L05	0.8426E 01	0.1771E 02	0.0000E 00	0.1000E 03	L05	0.4679E 01	0.1495E 02	0.0000E 00	0.1000E 03
L06	0.1521E 01	0.7726E 01	0.0000E 00	0.9600E 02	L06	0.1415E 01	0.8959E 01	0.0000E 00	0.1000E 03
L07	0.1549E 01	0.4834E 01	0.0000E 00	0.5000E 02	L07	0.4039E 02	0.4519E 02	0.0000E 00	0.1000E 03
L08	0.4358E 02	0.3705E 02	0.0000E 00	0.1000E 03	L08	0.3091E 02	0.4039E 02	0.0000E 00	0.1000E 03
L09	0.0907E 01	0.2045E 02	0.0000E 00	0.1000E 03	L09	0.7431E 01	0.2364E 02	0.0000E 00	0.1000E 03
L10	0.9506E 01	0.2469E 02	0.0000E 00	0.1000E 03	L10	0.4063E 01	0.1605E 02	0.0000E 00	0.1000E 03
L11	0.5871E 01	0.1204E 02	0.0000E 00	0.957E 02	L11	0.9156E 01	0.2182E 02	0.0000E 00	0.9842E 02
L12	0.1021E 02	0.1573E 02	0.0000E 00	0.9249E 02	L12	0.3332E 02	0.2745E 02	0.0000E 00	0.979E 02
L13	0.1107E 00	0.5138E 00	0.0000E 00	0.1000E 01	L13	0.2542E-01	0.1574E 00	0.0000E 00	0.1000E 01
L14	0.1434E 00	0.3555E 00	0.0000E 00	0.1000E 01	L14	0.4520E-01	0.2077E 00	0.0000E 00	0.1000E 01
A01	0.3423E 01	0.1833E 02	0.0000E 00	0.1000E 03	A01	0.1076E 00	0.6480E 00	0.0000E 00	0.8451E 01
A02	0.2450E 02	0.3318E 02	0.0000E 00	0.1000E 03	A02	0.2429E 01	0.1189E 02	0.0000E 00	0.1000E 03
A03	0.1702E 02	0.2472E 02	0.0000E 00	0.1000E 03	A03	0.5951E 01	0.4025E 02	0.0000E 00	0.1000E 03
A04	0.3572E 01	0.1552E 02	0.0000E 00	0.1000E 03	A04	0.9742E 00	0.6458E 01	0.0000E 00	0.1000E 03
A05	0.1844E 02	0.2468E 02	0.0000E 00	0.1000E 03	A05	0.5757E 02	0.4419E 02	0.0000E 00	0.1000E 03
A06	0.5068E 01	0.1746E 02	0.0000E 00	0.1000E 03	A06	0.2336E 02	0.3731E 02	0.0000E 00	0.1000E 03
A07	0.1164E 01	0.2432E 01	0.0000E 00	0.304E 02	A07	0.4803E 02	0.3667E 02	0.0000E 00	0.9643E 03
M01	0.3607E 01	0.1636E 01	0.3086E-01	0.5937E 02	M01	0.4078E 02	0.3369E 02	0.9445E-01	0.280E 03
M02	0.8452E 02	0.2733E 01	0.1246E 00	0.1000E 03	M02	0.9407E 02	0.1843E 02	0.0000E 00	0.1000E 03
M03	0.6727E 01	0.1716E 02	0.0000E 00	0.1000E 03	M03	0.4369E 01	0.1436E 02	0.0000E 00	0.1000E 03
M04	0.1109E 02	0.2330E 02	0.0000E 00	0.1000E 03	M04	0.1392E 02	0.3117E 02	0.0000E 00	0.1000E 03
M05	0.1046E 02	0.5026E 02	0.0000E 00	0.1000E 03	M05	0.2136E 02	0.3734E 02	0.0000E 00	0.1000E 03
M06	0.4354E 02	0.4052E 02	0.0000E 00	0.1000E 03	M06	0.4403E 02	0.4574E 02	0.0000E 00	0.1000E 03
M07	0.2038E 02	0.5440E 02	0.0000E 00	0					



POPULATION ASSIGNMENT BY CLASSIFICATION II

CLASS 6		CLASS 7		CLASS 8										
NO. OF OBSERVATIONS = 1576		NO. OF OBSERVATIONS = 5048		NO. OF OBSERVATIONS = 702										
VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM	VARIABLE	MEAN	STAN. DEV.	MINIMUM	MAXIMUM
S01	0.2055E 04	0.5243E 04	0.1800E 02	0.5430E 05	S01	0.1412E 04	0.1752E 04	0.7000E 01	0.3000E 05	S01	0.1257E 03	0.1474E 03	0.2000E 01	0.1400E 04
S02	0.1687E 04	0.2833E 04	0.1800E 02	0.4780E 03	S02	0.1264E 04	0.1562E 04	0.5000E 01	0.2143E 05	S02	0.1704E 03	0.1312E 03	0.2000E 01	0.1368E 04
S03	0.1365E 02	0.2928E 02	0.0000E 00	0.5982E 03	S03	0.1544E 04	0.1755E 04	0.0000E 00	0.2146E 05	S03	0.4124E 00	0.4092E 01	0.0000E 00	0.2672E 02
S04	0.3677E 01	0.5227E 01	0.1250E 00	0.1346E 03	S04	0.1505E 01	0.9264E 00	0.1250E 00	0.8739E 01	S04	0.2055E 01	0.1661E 01	0.1250E 00	0.4000E 02
S05	0.6454E 01	0.2041E 01	0.0000E 00	0.2500E 02	S05	0.2056E 01	0.1434E 01	0.0000E 00	0.1000E 02	S05	0.1338E 01	0.1193E 01	0.0000E 00	0.7000E 01
L01	0.374E 02	0.2183E 02	0.0000E 00	0.1000E 03	L01	0.2165E 02	0.2154E 02	0.0000E 00	0.1000E 03	L01	0.4730E 00	0.3558E 01	0.0000E 00	0.6644E 02
L02	0.367E 01	0.6410E 01	0.0000E 00	0.5455E 02	L02	0.7064E 01	0.9014E 01	0.0000E 00	0.2874E 02	L02	0.2928E 01	0.7936E 01	0.0000E 00	0.5000E 02
L03	0.9200E 00	0.3320E 01	0.0000E 00	0.4000E 02	L03	0.2557E 00	0.1846E 01	0.0000E 00	0.5726E 02	L03	0.5976E -01	0.8755E 01	0.0000E 00	0.2273E 02
L04	0.5205E 00	0.3500E 01	0.0000E 00	0.5000E 02	L04	0.4080E 00	0.3252E 01	0.0000E 00	0.5726E 02	L04	0.8095E 02	0.2743E 02	0.0000E 00	0.1000E 03
L05	0.347E 02	0.2310E 02	0.0000E 00	0.1000E 03	L05	0.6897E 01	0.273E 01	0.0000E 00	0.1000E 03	L05	0.1470E 01	0.6937E 01	0.0000E 00	0.6294E 02
L06	0.1082E 00	0.4710E 01	0.0000E 00	0.5000E 02	L06	0.7497E 00	0.4000E 01	0.0000E 00	0.1656E 03	L06	0.2171E 01	0.6603E 01	0.0000E 00	0.635E 02
L07	0.620E 00	0.1760E 01	0.0000E 00	0.3279E 02	L07	0.8672E 00	0.275E 01	0.0000E 00	0.4074E 02	L07	0.1966E 01	0.6664E 01	0.0000E 00	0.8473E 02
L08	0.109E 02	0.1821E 02	0.0000E 00	0.1000E 03	L08	0.937E 02	0.143E 02	0.0000E 00	0.1000E 03	L08	0.2327E 01	0.9434E 01	0.0000E 00	0.4273E 02
L09	0.580E 01	0.1281E 02	0.0000E 00	0.1000E 03	L09	0.1204E 01	0.538E 01	0.0000E 00	0.7533E 02	L09	0.1755E 00	0.1808E 01	0.0000E 00	0.3243E 02
L10	0.616E 01	0.167E 02	0.0000E 00	0.1000E 03	L10	0.1561E 01	0.7126E 01	0.0000E 00	0.1000E 03	L10	0.7498E 01	0.2273E 02	0.0000E 00	0.9972E 02
L11	0.1058E 01	0.7887E 01	0.0000E 00	0.8095E 02	L11	0.1523E 01	0.6841E 01	0.0000E 00	0.8235E 02	L11	0.2239E 01	0.1105E 02	0.0000E 00	0.9272E 02
L12	0.3250E 02	0.162E 02	0.0000E 00	0.9187E 02	L12	0.7894E 01	0.253E 02	0.0000E 00	0.9741E 02	L12	0.1580E 01	0.1484E 02	0.0000E 00	0.9972E 02
L13	0.5152E 00	0.4995E 00	0.0000E 00	0.1000E 01	L13	0.4952E -01	0.2170E 00	0.0000E 00	0.1000E 01	L13	0.1094E -01	0.1390E 00	0.0000E 00	0.1000E 01
L14	0.407E 00	0.4912E 00	0.0000E 00	0.1000E 01	L14	0.2690E 00	0.4434E 00	0.0000E 00	0.1000E 01	L14	0.5561E -01	0.1853E 00	0.0000E 00	0.1000E 01
A01	0.347E 00	0.1146E 02	0.0000E 00	0.1000E 03	A01	0.8100E 02	0.1657E 02	0.0000E 00	0.1000E 03	A01	0.1665E 01	0.1188E 02	0.0000E 00	0.1000E 03
A02	0.464E 02	0.3033E 02	0.0000E 00	0.1000E 03	A02	0.4170E 02	0.2948E 02	0.0000E 00	0.1000E 03	A02	0.1129E 01	0.1006E 02	0.0000E 00	0.5465E 02
A03	0.464E 02	0.3033E 02	0.0000E 00	0.1000E 03	A03	0.2539E 02	0.2893E 02	0.0000E 00	0.1000E 03	A03	0.5898E 00	0.7535E 01	0.0000E 00	0.1000E 03
A04	0.431E 02	0.1171E 02	0.0000E 00	0.1000E 03	A04	0.4245E 01	0.1877E 02	0.0000E 00	0.1000E 03	A04	0.9050E 01	0.1874E 02	0.0000E 00	0.1000E 03
A05	0.362E 01	0.1275E 02	0.0000E 00	0.1000E 03	A05	0.1347E 02	0.2196E 02	0.0000E 00	0.1000E 03	A05	0.2620E 00	0.1554E 02	0.0000E 00	0.1000E 03
A06	0.1054E 02	0.1744E 02	0.0000E 00	0.1000E 03	A06	0.5079E 01	0.1371E 02	0.0000E 00	0.1000E 03	A06	0.2209E 00	0.1713E 01	0.0000E 00	0.3000E 02
A07	0.4255E 01	0.1307E 02	0.0000E 00	0.1000E 03	A07	0.1328E 01	0.1925E 01	0.0000E 00	0.2229E 02	A07	0.3017E 02	0.3876E 02	0.0000E 00	0.642E 03
A08	0.5672E 01	0.4911E 01	0.1464E 00	0.1172E 03	A08	0.2700E 01	0.2789E 01	0.2555E -01	0.537E 02	A08	0.0274E 02	0.2849E 02	0.0000E 00	0.1000E 03
A09	0.644E 02	0.2790E 02	0.135E 00	0.1000E 03	A09	0.9490E 02	0.1433E 02	0.3971E 01	0.1000E 03	A09	0.1214E 02	0.2153E 02	0.0000E 00	0.1000E 03
A10	0.1429E 02	0.2045E 02	0.0000E 00	0.1000E 03	A10	0.638E 01	0.1816E 02	0.0000E 00	0.7500E 02	A10	0.2082E 02	0.333E 02	0.0000E 00	0.1000E 03
A11	0.1597E 02	0.2276E 02	0.0000E 00	0.1000E 03	A11	0.4621E 01	0.1320E 02	0.0000E 00	0.6647E 02	A11	0.2238E 02	0.3526E 02	0.0000E 00	0.1000E 03
A12	0.215E 02	0.2777E 02	0.0000E 00	0.1000E 03	A12	0.5209E 02	0.2777E 02	0.0000E 00	0.6647E 02	A12	0.3510E 02	0.3833E 02	0.0000E 00	0.1000E 03
A13	0.6731E 02	0.1497E 02	0.0000E 00	0.1000E 03	A13	0.7802E 02	0.2777E 02	0.0000E 00	0.1000E 03	A13	0.2394E -01	0.2898E 02	0.0000E 00	0.1000E 03
A14	0.4549E 00	0.4983E 00	0.0000E 00	0.1000E 01	A14	0.2511E 01	0.9699E 01	0.0000E 00	0.5000E 02	A14	0.9259E -01	0.2898E 02	0.0000E 00	0.1000E 03
A15	0.451E 00	0.4976E 00	0.0000E 00	0.1000E 01	A15	0.6434E 01	0.4924E 00	0.0000E 00	0.1000E 01	A15	0.5274E 00	0.4995E 00	0.0000E 00	0.1000E 01
A16	0.4645E -01	0.2952E 00	0.0000E 00	0.1000E 01	A16	0.4388E -01	0.2454E 00	0.0000E 00	0.1000E 01	A16	0.4274E -02	0.6523E -01	0.0000E 00	0.1000E 01
A17	0.7462E 00	0.4352E 00	0.0000E 00	0.1000E 01	A17	0.2595E -01	0.1590E 00	0.0000E 00	0.1000E 01	A17	0.4060E 00	0.4011E 00	0.0000E 00	0.1000E 01
A18	0.9562E -01	0.2790E 00	0.0000E 00	0.1000E 01	A18	0.7480E 00	0.4342E 00	0.0000E 00	0.1000E 01	A18	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00
A19	0.127E 00	0.1225E 01	0.0000E 00	0.2647E 02	A19	0.2355E 00	0.4243E 00	0.0000E 00	0.1000E 01	A19	0.4967E 02	0.3453E 02	0.0000E 00	0.1000E 03
A20	0.1777E -01	0.1321E 00	0.0000E 00	0.1000E 01	A20	0.5217E 01	0.9765E 00	0.0000E 00	0.5128E 02	A20	0.4986E -01	0.2177E 00	0.0000E 00	0.1000E 01
A21	0.2824E 01	0.8800E 01	0.0000E 00	0.6383E 02	A21	0.3764E -02	0.6233E -01	0.0000E 00	0.1000E 01	A21	0.1820E 02	0.3698E 02	0.0000E 00	0.5000E 03
A22	0.1000E 01	0.0000E 00	0.1000E 01	0.4000E 01	A22	0.3100E 01	0.4826E 01	0.0000E 00	0.7692E 02	A22	0.2858E 00	0.1185E 00	0.0000E 00	0.1000E 01
A23	0.1000E 01	0.0000E 00	0.1000E 01	0.4000E 01	A23	0.1192E 01	0.4516E 00	0.1000E 01	0.4000E 01	A23	0.1615E 01	0.6647E 00	0.1000E 01	0.4000E 01
A24	0.1000E 01	0.0000E 00	0.1000E 01	0.4000E 01	A24	0.1000E 01	0.0000E 00	0.1000E 01	0.1000E 01	A24	0.9407E 00	0.4206E 00	0.0000E 00	0.1000E 01
A25	0.2544E 02	0.1165E 02	0.1700E 02	0.9000E 02	A25	0.0000E 00	0.0000E 00	0.0000E 00	0.0000E 00	A25	0.5714E -01	0.1609E 00	0.0000E 00	0.1000E 01
A26	0.4750E -01	0.2750E 00	0.0000E 00	0.1000E 01	A26	0.2551E 02	0.6858E 01	0.1800E 02	0.9400E 02	A26	0.4955E 02	0.3912E 02	0.2300E 02	0.2670E 02
A27	0.4533E 02	0.4710E 02	0.0000E 00	0.1000E 03	A27	0.2892E 00	0.4534E 00	0.0000E 00	0.1000E 01	A27	0.4955E 02	0.3912E 02	0.2300E 02	0.2670E 02
A28	0.1831E 02	0.3555E 02	0.0000E 00	0.1000E 03	A28	0.5819E 02	0.5991E 02	0.0000E 00	0.1000E 03	A28	0.6659E 02	0.4347E 02	0.0000E 00	0.1000E 03
A29	0.3877E 02	0.4837E 02	0.0000E 00	0.1000E 03	A29	0.6938E 00	0.7093E 02	0.0000E 00	0.1000E 03	A29	0.5268E 02	0.427E 02	0.0000E 00	0.1000E 03
A30	0.1060E 00	0.4078E 00	0.0000E 00	0.1000E 01	A30	0.2334E 00	0.4230E 00	0.0000E 00	0.1000E 01	A30	0.7333E 00	0.8269E 01	0.0000E 00	0.1000E 03
A31	0.2641E 00	0.1037E 01	0.0000E 00	0.4000E 01	A31	0.1412E 01	0.1428E 01	0.0000E 00	0.4000E 01	A31	0.6026E 00	0.4894E 00	0.0000E 00	0.4000E 01
A32	0.2367E 00	0.5203E 00	0.0000E 00	0.4000E 01	A32	0.6577E -01	0.2573E 00	0.0000E 00	0.2000E 01	A32	0.2717E -01	0.1708E 00	0.0000E 00	0.2000E 01

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