L SHELL IONISATION AND X-RAY PRODUCTION CROSS SECTION MEASUREMENTS FOR ASYMMETRIC ION-ATOM COLLISIONS

BY

RANJEET SINGH SOKHI

A thesis submitted to The University of Aston in Birmingham for the degree of Doctor of Philosophy

DEPARTMENT OF MATHEMATICS AND PHYSICS MAY 1984

DEDICATED TO THE MEMORY OF MY BELOVED FATHER DALIP SINGH SOKHI

#### THE UNIVERSITY OF ASTON IN BIRMINGHAM

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#### SUMMARY

L shell ionisation and x-ray production cross sections have been measured for Dy, Yb, W, Au, Pb, Bi, Th, and U in the form of carbon backed thin targets. Incident protons, deuterons and alpha particles of energy 1 to 3 MeV were employed to ionise the L shell and the resulting L x-rays were detected with an energy-dispersive Si(Li) x-ray system. The individual  $2_{S_1^1}$ ,  $2_{p_2^1}$  and  $2_{p_3^3}$  state ionisation cross sections were deduced from the measured x-ray production cross sections with the aid of a spectrum fitting programme specifically written for this purpose in Fortran 77. The efficiency of the Si(Li) x-ray detector and the target thicknesses were determined experimentally.

The measured L shell ionisation and x-ray production cross sections, and their ratios, have been compared with the predictions of the plane-wave Born approximation and the ECPSSR theory proposed by Brandt and Lapicki (1981). Comparisons have also been made with the available data of other authors. These comparisons have revealed significant discrepencies between the ECPSSR theory and the measured data for all three subshells. These discrepencies have been found to be particularly large for the  $2p_1^2$  state ionised by incident alpha particles. Possible reasons for theses disagreements are discussed and suggestions are made for future work.

To assess the extent of progress made in this field with regard to proton impact, a comprehensive tabulation of L shell ionisation and x-ray production cross sections, and the pertinent experimental details, has been compiled.

Key words: L shell ionisation, particle induced x-rays, inner-shell x-ray production, cross sections.

### ACKNOWLEDGEMENTS

It is with great respect and admiration that I acknowledge Dr D. Crumpton for his guidance and encouragement throughout the duration of this study. The head of department, Professor E. Neal, and Emeritus Professor S.E. Hunt are thanked for their interest in the present work. The assistance of Dr W. Cox is appreciated regarding some mathematical aspects.

Thanks are due to Mr T. Kennedy and J. Phull for their help and friendship. The assistance offered by the staff at the Physics Workshop and at the Birmingham Radiation Centre is gratefully appreciated. I am much indebted to the members of the applied nuclear physics group for their friendship and for making the research period a very enjoyable one.

The Science and Engineering Research Council is acknowledged for funding this study.

I would like to express my gratitude to Mrs S. Puar for typing the thesis and to Miss E. Taylor and Miss P. Blower for labelling the diagrams.

The encouragement and understanding shown by my family is deeply appreciated. In particular, I am indebted to my mother since it is her patience and her unending sacrifices which have provided me with the opportunity to study for this degree.

> R.S. Sokhi May 1984

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CHAPTER 1

INTRODUCTION

General interest in inner-shell ionisation by light charged particles was initially stimulated by the publication of Merzbacher and Lewis's (1958) review article which provided a comprehensive theoretical description of this phenomenon in terms of the plane-wave Born approximation (PWBA). Comparable theoretical explanations were offered by Bang and Hansteen (1959) and more recently by Garcia et al (1973) who employed the semi-classical (SCA) and the binary-encounter (BEA) approximations respectively. As a direct consequence of these works there was an upsurge of experimental activity in the area of K-shell ionisation by light ions in order to test the above theoretical predictions. The large amount of data that resulted has been tabulated by Gardner and Gray (1978).

Because of the widespread availability of low MeV charged particle accelerators much of the measurements were restricted to particle energies < 4MeV. Comparison of the measured data with the proposed theories revealed large discrepencies, particularly at low impact energies where the theories tended to overpredict the data. Although some improvements have been suggested for the SCA and BEA theories, a much more methodical approach was adopted by Brandt and his colleagues to explain these disagreements by incorporating certain corrections to the first order PWBA model. Over a period of several years their work culminated into the ECPSSR theory (Brandt and Lapiciki 1979 and 1981) to explain K and L shell ionisation by simple projectiles. The ECPSSR theory takes into account the energy loss (E), Coulomb deflection (C), perturbed-stationary-state (PSS) and relativistic (R) effects.

As a result of the developments in the PWBA, SCA and BEA theories there has been considerable recent interest in K shell ionisation (Badica et al 1977, Khan et al 1977, Bauer et al 1978, Badica et al 1979, Benka and Geretschlager 1980, Lopes et al 1980 and Barfoot et al 1980).

Paul (1982) has conducted a detailed comparison of proton-induced K shell ionisation cross sections with the ECPSSR theory and has observed reasonable qualitative and quatitative agreement at intermediate and high impact velocities. At lower proton velocities, however, a modified Coulomb deflection factor has been proposed by Paul (1982) to account for the deviations between theory and experiment.

The amount of L shell x-ray production and ionisation cross section data is not as comprehensive as for the K shell. To estimate the progress achieved in the field of L shell ionisation by proton bombardment of a major compilation containing all the available measured L shell x-ray production and ionisation cross sections, and the associated experimental details, from 1975 to November 1982 has been prepared (Sokhi and Crumpton 1984). This compilation, which is presented in apprendix E, clearly illustrates the need for further data, in particular with regard to ionisation cross sections. In the case of deuteron impact, measurements are very scarce and only a few published values are available for incident alpha particles.

The major purpose of this study is to provide a comprehensive set of L shell data for protons, deuterons and alpha particles incident on medium to high atomic number elements and to perform a detailed comparison with the ECPSSR theory, with the intention of highlighting any significant discrepencies between the data and theory. Measurements have been made between projectile energies of 1 to 3 MeV at steps of 200 keV to establish the energy dependence of the cross sections. To study the dependence of the ionisation cross sections on the target atomic number ( $Z_2$ ), several targets were selected between the range  $66 \le Z_2 \le 92$ . Recently Cohen (1983) has measured L shell ionisation cross sections for 1 to 3 MeV protons and alpha particles incident on some heavy elements. Cohen (1983) has compared his data with the ECPSSR model and has noticed serious disagreements. The present work

provides an independent check on the conclusions reached by Cohen (1983). An additional reason for carrying out this work is to make L shell x-ray production cross sections for experimentalists involved in particle induced x-ray emission analysis (PIXE). This technique has developed over the past decade into a highly versatile analytical tool for solving problems regarding trace elements (Khan and Crumpton 1981). Wherever high Z<sub>2</sub> trace elements are involved L x-rays are employed and thus a reliable data base of particle induced L shell x-ray production cross sections is vital.

Each chapter of this thesis begins with an introduction which explain the underlying philosophy adopted in the chapter. The remaining part of this main introduction outlines the contents of each chapter and discusses the overall philosophy behind this investigation.

The atomic processes which occur once an atom has been ionised by an external purterbation in one of its inner-shells are discussed in chapter 2. For completeness the chapter also discusses processes which are allied to this study. Chapter 3 outlines the principles of nuclear backscattering spectrometery, which is employed in the present work to determine target thicknesses.

The concepts of the ECPSSR theory, and its underlying assumptions, are considered in chapter 4. The SCA and the BEA models are discussed in appendix A for completness. Chapter 5 contains details regarding the apparatus and procedure employed for measuring the L shell ionisation and x-ray production cross sections. This chapter also deals with the method for calculating theoretical cross sections for comparison with the present data.

Detailed comparisons of the measured data in this work with the PWBA and the ECPSSR theories, and with other measured values, are presented in chapter 6. Results of each element are discussed in

order of atomic number before highlighting common trends revealed by the individual comparisons. The final conclusions of the present work are outlined in chapter 7.

## CHAPTER 2

FUNDAMENTALS OF CHARGED PARTICLE

INDUCED X-RAY EMISSION

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### 2.1 INTRODUCTION

Physical concepts necessary for understanding the major features of an x-ray spectrum are reviewed in this chapter. The chapter concentrates on the atomic processes which occur once an inner-shell vacancy has been created, by light positively charged particles in the present case, although processes which are peripheral to this study have been mentioned for completeness. These include phenomena more closely associated with impact by very energetic or heavy charged particles.

The mechanisms by which the projectile produces bremsstrahlung, directly and indirectly, as it traverses matter are also examined. Finally, the main interactions of x-rays with matter, which leads to their attenuation, are mentioned.

Throughout this chapter the underlying philosophy has been to highlight contemporary ideas regarding the relevant atomic processes. Consequently a determined attempt has been made to cite references that are fully representative of the current views held on these areas. Where appropriate, recent noteworthy advances in the fields discussed in this chapter have been indicated.

### 2.2 NOMENCLATURE

The electronic states of an atom are characterised by four basic quantum numbers. These are the principal quantum number, n, the orbital quantum number, &, the total angular quantum number, j, and the magnetic quantum number, m. n can have positive integer values 1, 2, 3 ... or in the x-ray notation K, L, M... and so on. & can taken any integer value from 0 to n -1, m can assume any integral value from -& to +& including zero and j can adopt the values  $\&\pm\frac{1}{2}$  where  $\pm\frac{1}{2}$  represents the two possible values of the electron spin, s.

In the spectroscopic notation different values of l can be denoted by the letters s,p,d.... corresponding numerically to 0, 1, 2, ..., n -1. Derivation of these numbers can be found in any standard text book on

quantum mechanics such as Schiff (1968) and Landau and Liftshitz (1977). The three L subshells can be represented by  $L_1$ ,  $L_2$ ,  $L_3$  in the x-ray notation or equivalently by  $2s_{\frac{1}{2}}$ ,  $2p_{\frac{1}{2}}$  and  $2p_{\frac{3}{2}}$  in the spectroscopic notation. Both of these notations are employed in the present work. 2.3 ATOMIC TRANSITIONS

When an atom experiences a perturbation, such as an encounter with a charged particle, there is a finite probability that an inner-shell electron may be ejected into the continuum or into a higher shell leaving a vacancy in the inner-shell. The excited atom has then several channels open to it through which it may deexcite. These modes of relaxation manifest themselves as characteristic features in an x-ray spectrum.

To understand the mechanisms by which the excited atom deexcites the atom should strictly be treated as a many-body problem. This, however, is extremely difficult even for the simplest atoms. To avoid the complex nature of the many-body problem and to facilitate the discussion the following simplifying assumptions can be made.

- (i) the perturbation experienced by the atom creates a single vacancy in an inner-shell and leaves the other orbitals unaffected or 'frozen' the sudden or the frozen - orbital model (Koopmans 1933),
- (ii) the electrons are considered to be approximately free in relation to the atomic nucleus, and
- (iii)any individual electron is considered to be independent of the position of any other electron at any particular moment (Rooke 1974).

These assumptions, although crude, enable the gross features of an x-ray spectrum to be explained. In light of these assumptions the major relaxation mechanisms relevant to this study are discussed below. A more thorough treatment, however, has been given by Azaroff (1974).

2.3.1 X-Ray Emission

Consider an electron transition from an initial higher atomic state q to a final lower state  $q^1$  where q and  $q^1$  represent sets of quantum numbers

n, &, s, m and n<sup>1</sup>,  $\ell^1$ , s<sup>1</sup>, m<sup>1</sup> respectively. The transition probability per unit time for this transition, resulting in the emission of a photon with energy  $\hbar\omega$  and momentum <u>p</u> =  $\hbar k$ , is proportional to the square of the transition matrix element, M<sub>qq1</sub>, given by (Merzbacher 1970)

$$|M_{qq^1}|^2 = |\langle q| \underline{\epsilon} \cdot \underline{p} \exp((i\underline{k} \cdot \underline{r})) |q^1 \rangle|^2$$
 2.1

where  $\hbar$  is the Planck's constant, h, divided by  $2\pi$ ,  $\omega$  is the angular frequency of the emitted radiation, <u>k</u> is the propagation vector, <u>r</u> is the electron position vector and  $\underline{\varepsilon}$  is the polarisation vector of the emitted photon.

When calculating the transition probability for photon emission it is found that by approximating the exponential term in equation 2.1 by unity much of the emitted radiation can be explained (Rooke 1974). This approximation is referred to as the electric dipole approximation' and the transitions for which the probability can be calculated, by making use of this simplification, are known as 'electric dipole transitions'.

These transitions are governed by certain 'selection rules' which decide whether the transition is allowed or forbidden. These rules originate from the so-called 'recurrence relations' which arise in the quantum mechanical treatment of radiative transition probabilities (Tralli and Pomilla 1969 and Rooke 1974). The selection rules are basically restrictions on the magnitude by which the quantum numbers representing the atomic states can change when a transition takes place from one state to another. These rules ensure that the electric dipole matrix element does not vanish (Schiff 1968). For this to be the case the changes in the quantum numbers, during a transition, must be limited to

 $m - m^{1} = \Delta m = 0, \pm 1; \quad j - j^{1} = \Delta j = 0, \pm 1$ 2.2  $\ell - \ell^{1} = \Delta \ell = \pm 1; \quad s - s^{1} = \Delta s = 0$  The change in the principal quantum number, n, is not restricted.

A large number of observed transitions obey these rules and are called 'allowed' transitions while the relatively few that do not are termed 'forbidden' transitions. Some of these are explained by including the second term in the power series expansion of  $\exp(i\underline{k}.\underline{r})$  in equation 2.1 (electric quadrupole approximation). Such transitions, however, only have a probability of the order of  $10^{-8}$  relative to the dipole transitions (Tralli and Pomilla 1969) which makes them insignificant in relation to the present study.

When a radiative dipole transition takes place in an excited atom the emitted photon has a discrete energy value given by

2.3

 $\hbar\omega = E_f - E_j$ 

where E<sub>i</sub> is the energy of the initial level where the vacancy is created and E<sub>f</sub> the energy of the final level where the vacancy is transferred to as a result of the transition. Figure 2.1 shows schematically the allowed x-ray transitions to the L-shell. Although individual 'diagram' lines are shown in figure 2.1 the resolution of the present-day lithuim drifted silicon detectors, such as the one employed in this study, allow only groups of lines to be observed.  $L_{\alpha}$ ,  $L_{\beta}$  and  $L_{\gamma}$  transitions, occuring as a result of vacancies in the L-shell, are such groups.

### 2.3.2 Non-radiative Processes

In the event of inner-shell ionisation by charged particles electrons are emitted by two successive processes (Stolterfoht 1978). Firstly, electrons which exhibit a continuous energy distribution are ejected as a result of ionisation and secondly, electrons with discrete energies are emitted as a result of Auger transitions which fill the vaciencies (Auger 1925). The latter process, which is another mode of deexcitation and competes with x-ray emission, is treated in terms of a direct interaction between the 'active' atomic electrons (Wentzel 1927). This model is based on the assumption that the electrons taking part in the interaction are



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8.4

non-relativistic. This is a valid assumption for light elements.

The Auger transition is effected by a perturbation arising from the Coulomb interaction between the neighbouring electrons, that is, the ejected and the emitted Auger electron (Burhop 1952). The general theory of the Auger effect is most successfully explained by the Lorentz-covariant theory of quantum electrodynamics discussed by Chattarji (1976). According to this theory the non-radiative Auger transition is caused by the retarded electromagnetic interaction between two bound-state electrons described by Dirac wave functions. The electromagnetic interaction consists of a chargecharge (Coulomb) interaction and a current-current (magnetic) interaction. For non-relativistic cases the interaction reduces to one that is purely Coulombic. A thorough treatment of the Auger effect has also been provided by McGuire (1975).

The energy of the Auger electron,  $E_A$ , is given by (McGuire 1975)

2.4

$$E_A = E_a - E_{b,b}$$

where  $E_a$  is the energy of the subshell, a, with the primary vacancy and  $E_{b_1b_2}$  is the energy associated with subshells  $b_1$  and  $b_2$  in which holes are produced as a result of the Auger transition. Since Auger electrons have discrete energies their study provides a very informative method for investigating inner-shell excitation by charged particles (Stolterfoht 1978). This avenue is being explored not only to understand the collision process (Kojima et al 1979, Schneider and Stolterfoht 1981) but also the mechanism by which Auger electrons are emitted as a consequence of the collision (Schmidt et al 1981, Baragiola et al 1982 and Bastasz and Felter 1982). A recent review article by Weightman (1982) discusses different aspects of x-ray-excited Auger spectroscopy.

If the primary vacancy is created in a shell other than the K, then Coster-Kronig transitions (Coster and Kronig 1935) may compete with the x-ray and the Auger transitions. Essentially these transitions are Auger transitions which occur in the subshells of the shell which initially

suffers the creation of the primary vacancy. Thus a vacancy in the  $2_{S_{\frac{1}{2}}}$ subshell for example, may be filled by an electron from a higher subshell of the same shell, L in this case. The mechanism is similar to that of Auger transitions and is based on a Coulomb interaction of the electrons involved. Via this mechanism a vacancy initially in the 251 may be transferred to a higher subshell  $(2_{p_{\frac{1}{4}}} \text{ or } 2_{p_{\frac{3}{2}}})$  before taking part in a radiative transition. For obvious reasons if a vacancy is created in the highest subshell of any given shell €oster-Kronig transitions are absent. Once the electron redistribution is complete in the subshell an electron in a higher shell may be ejected, again by Coulomb interaction. Coster-Kronig transitions explain why for many elements diagram lines such as  $L_{\beta_3}$  ( $L_1 \rightarrow M_3$ ) and  $L_{\beta_4}$  ( $L_1 \rightarrow M_2$ ) are absent or abnormally weak and transitions originating in  $2p_1$  and  $2p_{3/2}$  subshells appear with considerable intensity (Chattarji 1976). Coster-Kronig transitions are only energetically favourable for certain regions of atomic number  $(Z_2)$  and thus exhibit sharp cut-offs at critical  $Z_2$  values (McGuire 1975 and Doyle and Shafroth 1979).

Transitions in which both the final vacancies occur in the same shell as the initial vacancy but in a different subshell also take place, but with a small probability. These transitions have been termed 'Super Coster-Kronig' transitions by McGuire (1972). There is a small but finite probability that Coster-Kronig transitions may be radiative. This has been confirmed by Karttunen et al (1971) for the  $L_1$  to  $L_3$  transition.

### 2.3.3 Atomic Parameters

When calculating x-ray yields account must be taken of the other relaxation mechanisms discussed in subsection 2.3.2, because of their competitive nature. To do this, information on the atomic yields for each of these processes is required. Definitions of these yields are stated below. Although the definitions are similar for all the shells, the subscripts apply specifically to the L subshells. The fluorescence yield,  $\omega_i$ , ( i = 1, 2, 3) is the number of characteristic L x-ray photons per L<sub>i</sub>

vacancy. The Auger yield,  $a_i$ , is the number of Auger electrons per  $L_i$ vacancy and similarly the Coster-Kronig yield,  $f_{ij}$ , (i < j) is the number of transitions transferring vacancies from the  $L_i$  subshell to the higher  $L_j$  subshell per  $L_i$  vacancy. As mentioned in subsection 2.3.2 Coster-Kronig transitions may be radiative and the total Coster-Kronig yield,  $f_{i,i}^T$ , can be expressed as

2.5

$$f'_{i,j} = f_{i,j} + f'_{i,j}$$

where  $f_{ij}$  and  $f'_{ij}$  denote the radiative and non-radiative parts. For high atomic number elements the radiative transition from L<sub>1</sub> to L<sub>3</sub> subshell becomes important and has to be taken into account. This is illustrated in figure 2.2 which shows the variation of the radiative Coster-Kronig yield ( $f'_{13}$ ) for this transition, expressed as a percentage of its nonradiative counterpart ( $f_{13}$ ), with atomic number. Since the total decay probability for an atom with a vacancy in a shell, L in this case, is unity we can write

$$\omega_{i} + a_{i} + \sum_{j=2,3}^{T} f_{ij} = 1$$
 2.6

The definition of  $\omega_i$ , as stated earlier, is subject to the condition that the primary vacancy distribution of subshell i does not change before the vacancies are filled. However, the presence of the Coster-Kronig transitions between the subshells alter the primary vacancy distribution and to determine the average or the effective fluorescence yields of the subshells the effects of the Coster-Kronig transitions, therefore, have to be incorporated. The average fluorescence yield ( $\nu_i$ ) for the i<sup>th</sup> L subshell can be defined as the number of characteristic L-shell x-rays (not necessarily from transitions to the same subshell L<sub>i</sub>) that are emitted per primary vacancy created in the L<sub>i</sub> subshell (Rao 1975). Thus,  $\nu_i$  is the number of L x-rays emitted including those emitted after rearrangement of vacancies by the Coster-Kronig transitions. The expressions for  $\nu_i$  (i = 1, 2, 3) for





the L subshells interms of  $\omega_i$  and  $f_{i,i}$  are

Only limited work has been performed to determine the atomic parameters experimentally and theoretically despite their considerable importance in x-ray analytical techniques (McGuire 1971 and Bambynek et al 1972). An internally consistent set of values for the atomic yields has been produced by Krause (1979). Values have been supplied by Krause (1979) for K and L-shell yields and in the case of the L-shell atomic number from 12 upwards have been covered. This tabulation has been used to show the variations of the atomic yields with atomic number. Figure 2.3 shows the variation of the Coster-Kronig yields for the L1 subshell with atomic number. It illustrates clearly the regions of atomic number where the L1 Coster-Kronig yields are energetically unfavourable. The three major  $L_1$ subshell atomic yields, that is, the total non-radiative Coster-Kronig yield  $(f_1 = f_{12} + f_{13})$ , the fluorescence yield  $(\omega_1)$  and the Auger yield  $(a_1)$  are shown in figure 2.4. It shows the dominance of the nonradiative processes throughout the relevant range of atomic numbers for the L1 subshell. Another interesting feature highlighted by figure 2.4 is the range of atomic numbers, 50 to 76, where the Coster-Kronig process looses its importance and being competive, the Auger process becomes equally probable. The atomic yields for the L<sub>2</sub> subshell are illustrated in figure 2.5. In this case the Coster-Kronig transitions play a relatively minor role for high atomic number elements. The Auger process dominates the mode of decay for most of the elements and becomes less probable than x-ray emission only for the heaviest elements. The situation is very similar for the  $L_3$  Auger and fluorescence yields as shown in figure 2.6. The Coster-Kronig process is obviously absent for the  $L_3$  shell. Using the expressions 2.7 the average



Variation of the L1 subshell nonradiative Coster-Kronig yields with atomic

number. Values taken from Krause (1979).

Figure 2.3

COSTER-KRONIC YIELD X.01





from Krause (1979).

ATOMIC YIELD X . DI



from Krause (1979).

ATOMIC YIELD X . 01
fluorescence yields were calculated for the L<sub>1</sub> and L<sub>2</sub> subshells and are illustrated in figure 2.7. As shown in this figure  $v_1$  and  $v_2$  have comparable values for all the elements.

For elements of interest in this study Krause (1979) has quoted uncertainties of upto 10% in their  $\omega_i$  values and upto 50% in f<sub>ij</sub>. The small number of measurements, or the lack of them, has been emphasised by Krause (1979) as being one of the major factors contributing to these large uncertainties. Recent measurements by Kodre et al (1981) of  $\omega_i$  for Pb show similar large uncertainties. 25% in  $\omega_1$  and  $\omega_2$  have been quoted, although  $\omega_3$  is much more reliable. The experimental and theoretical values given in the review article by Bambynek (1972) are no more reliable. Comparison of these values and those of Krause (1979) show significant discrepancies between the two, especially for f<sub>ij</sub> and this further casts doubt on the reliability of the available data regarding atomic parameters. In theoretical calculations the precision of these parameters is hampered by the lack or scarity of knowledge of the influence of multiple vacancies and many-body effects (Krause 1979). Experimental problems such as isolating vacancies in the subshells have been discussed by Rao (1975).

A vacancy in a state has a finite life time  $(\tau)$  and is related to the natural width  $(\Gamma)$  of that state by the uncertainty principle, that is,

$$\Gamma = \frac{\pi}{\tau}$$
 2.8

The total width of a state is given by the sum of the radiative (R), Auger (A) and Coster-Kronig (CK) partial widths.

$$\Gamma = \Gamma_{\rm R} + \Gamma_{\rm A} + \Gamma_{\rm CK}$$
 2.9

 $\Gamma_k$  (k = R, A, CK) is proportional to the transition rate (S<sub>k</sub>) of the particular mode of decay (Parratt 1959, McGuire 1970 and Kostrom et al 1971) which is defined as

$$S_k = \frac{\Gamma_k}{tr}$$
 2.10



and as a counterpart to equation 2.9 we have

 $S = S_R + S_A + S_{CK}$ 

Theoretical values for the radiative rates have been reported by McGuire (1971) for selected elements up to an atomic number of 90 and by Scofield (1974a) for atomic numbers upto 94. Scofield (1974b) has presented theoretical values for all elements. Keski-Rahkonen and Krause (1974) have provided a graphically representation of the radiative rates with atomic number up to 120. Theoretical electric dipole x-ray transition rates for all elements have been calculated by Manson and Kennedy (1974). The most probable values for K and L-shell radiative rates have been determined by Salem et al (1974) by fitting a curve to the available experimental data. These authors have presented their values numerically and graphically. A comperhensive list of the atomic parameters, determined experimentally or theoretically between 1972 and 1977 has been provided by Krause (1979).

2.11

Typical uncertainties in radiative rates, determined experimentally, range from about 10-20% (Salem and Lee 1974). These values show systematic discrepencies of the order of 10% from theoretical results (Scofield 1974b). Theoretical calculations may themselves be uncertain by several percent. Scofied (1975) does, however, point out in his theoretical discussion of radiative rates that uncertainties are greatest for low atomic number elements and outer-shell electrons.

2.3.4 Multiple Ionisation Phenomena

Double or multiple vacancies may be produced in an atom by (Nagel and Baun 1974)

- (i) ejection of an electron by non radiative transitions (already discussed in section 2.3.2),
- (ii) the 'shake-off' process (internal ionisation),
- (iii) direct ejection of more than one electron, for example by heavy charge particles.

In the electron 'shake-off' process an outer-shell electron is ejected

as a result of an impulsive perturbation produced by the sudden loss of a core-level electron which partially screens the outer electrons from the nucleus. For charged particle ionisation at very high energies this is the dominant process for producing double vacancies (Nagel and Baun 1974). Ionisation by heavy charged particles can also lead to multiple vacancies (Madison and Merzbacher 1975) by Coulomb interaction with the target atom. Double vacancies can also be produced by light particles such as protons and alpha particles (Knudsen et al 1973, Madison and Merzbacher 1975 and Mokler and Folkmann 1978). Evidence for these effects is seen in x-ray and Auger spectra which reveal the presence of 'satellite' lines with energy higher than the diagram lines (McGuire 1975, Richard 1975, Dyall and Larkins 1982 and Tawara and Richard 1983). Satellite lines on both sides of the main lines due to heavy particle collision have also been studied (Burhop 1979). When multiple vacancies are confined to the inner shells 'hypersatellite' lines originate (Stoller et al 1977).

The radiative counterpart of the radiationless Auger process was discovered by Aberg and Utriainen (1969) giving rise to a simultaneous emission of an electon and a photon with energy lower than that of the main emission line. This effect has been called the 'radiative' or the 'semi-Auger' effect. In this case the Auger electon emitted, when a vacancy is filled, is excited to a higher boundstate by the 'shake-up' processes instead of being ejected into the continuum as in the normal Auger effect (Cooper and La Villa 1970, Burhop and Asaad 1972 and Aberg 1975). Discrete structure as a result of this radiative electon rearrangement has been observerd by Jamison and Richard (1977) for heavy particle impact. Afrosimov et al (1976) observed a variation of this effect where a third electon is emitted instead of a photon for low energy Ar<sup>-</sup> and Cl<sup>+</sup> particles. For highly energetic and highly stripped heavy ions a broad structure on the high energy side of the emission spectrum is observed due to radiation being emitted when target electrons, bound or free, are captured by the projectile (Schnopper et al

1972 and Kienle et al 1973). This 'radiative electron capture' is important at high projectile energies where the particle velocity is comparable to the velocity of the bound target electron (Burhop 1979).

It is clear from above that the degree of inner-shell ionisation will have significant effect on the different modes of decay and consequently makes the mean fluorescence yield dependent on parameters such as the energy and the charge state of the projectile (Burhop 1979). However, with the advent of Synchrotron radiation sources x-rays of specific energies can be used to study x-ray spectra free from the complications of multiple ionisation (Madden 1974 and Chevallier 1978).

#### 2.4 PRODUCTION OF BREMSSTRAHLUNG

In the previous section the mechanism by which characteristic x-rays are produced after the creation of an inner-shell vacancy by an incident charged particle was elucidated in some detail. A major feature of an x-ray spectrum is the background continuum on which these characteristic x-rays are superimposed. The exact nature of this 'bremsstrahlung' is influenced to a large extent by the energy of the projectile and the degree of asymmetry of the ion-atom collision system. Although the term 'bremsstrahlung' refers to the continuum as a whole, in reality several distinct processes, which give rise to this continuum, take place. This section is devoted to the discussion of these processes.

#### 2.4.1 Projectile Bremsstrahlung

In an ion-atom collision as the charged particle approaches an atomic nucleus of a target atom, it will suffer a change of velocity, the extent of which is determined by the proximity of the encounter. This change of velocity is caused by the Coulomb field of the nucleus which also changes the particles direction. This results in the emission of electromagnetic radiation and hence in a decrease in the particles kinetic energy. This contributes to the general stopping of the ions in matter. The electrodynamical theory for this process has been provided by Jackson (1975). The energy of the projectile bremsstrahlung extends from zero upto the projectile

energy (E). Electric dipole radiation is the major contributor to this bremsstrahlung, the cross section of which has been derived by Jakubassa (1975) and Reinhardt et al (1976) in the restraints of the Born approximation. The cross section is approximately proportional to  $Z_1^4 Z_2^2 / M_1^2$ (Alder 1956 and Read 1980), where  $Z_1$  is the projectile atomic number,  $Z_2$ is the target atomic number and  $M_1$  is the mass of the projectile. This process is therefore, most important, for incident particles of small mass. Protons, for example, give rise to bremsstrahlung a factor of 3X106 smaller in intensity than electrons of the same velocity, and thus offer obvious advantages for trace elemental analysis by proton impact (Folkmann et al 1974a and Johansson and Johansson 1976). The bremstrahlung cross section decreases slowly with increasing projectile energy as E<sup>-1</sup> (Folkmann et al 1974a and Mokler and Folkmann 1978), This is illustrated in figure 2.8 which shows the variation of the cross section,  $d\sigma/dE_r$ , with the energy of the radiation E, in relation to the other major source of bremsstralung (subsection 2.4.2). It is clear from this figure that although projectile bremsstrahlung decreases slowly with Er, its contribution to the total background at the higher energy side of the x-ray spectrum gains importance. It is interesting to note that for a collision system consisting of interacting 'partners' with the same chargeto-mass ratio the electric dipole radiation component vanishes (Folkmann et al 1974a). This is due to the fact that the intensity is proportional to the acceleration of the centre of mass of the collision system, which for a symmetrical system moves uniformly (Landau and Liftshitz 1972). For most targets which have a charge-to-mass ratio close to a half bombarded by say, alpha particles  $(Z_1/M_1 = \frac{1}{2})$  the projectile bremsstrahlung is negligible and consists of higher multipolarity contributions. This fact has been experimentally verified by Watson et al (1975). The anisotropy of projectile bremsstrahlung has been pointed out to be insignificant for practical situations (Folkmann et al 1974a).

#### 2.4.2 Secondary Electron Bremsstrahlung

The secondary electrons ejected in ion-atom collisions undergo strong accelerations in the nuclear electric fields of target atoms and radiate bremsstrahlung (Ogier et al 1966) the energy of which may range from zero to the full kinetic energy of the secondary electrons. Intensity of this secondary electron bremsstrahlung (SEB) decreases rapidly at x-rays energies  $(E_x)$  above  $T_m = (4m/M_1)E$  which is the maximum energy transferable to a free electron of mass, m, by a projectile with energy, E, and mass, M1, (Merzbacher and Lewis 1958). SEB is the dominant process by which bremsstrahlung is produced at low x-ray energies  $(E_X < T_m)$ . Detailed calculations regarding this process have been performed by Folkmann et al (1974a) for proton impact. The cross section for this process as a function of the emitted radiation energy  $(E_r)$  is shown in figure 2.8 in comparison with projectile bremsstrahlung. For  $E_x$  upto about 20keV SEB fall's approximately as  $E_r^{-10}$  (Folkmann et al 1974b). For  $E_X < T_m$  Tawara et al (1976) have pointed out that outer-shell electrons play the dominant role in the SEB process where as inner-shell electrons are the major contributors for  $E_x > T_m$ . In experimental situations we must note that for thin targets SEB is less prominant than for thick targets because the secondary electrons will have a greater probability of escaping from the target surface without producing any bremsstrahlung - a meritorious point in favour of thin target measurements (Johansson and Johansson 1976 and Yamadera et al 1981a).

The angular distribution of SEB is peaked at 90° to the incident particle direction and the intensity may change by as much as a factor of two with angle (Folkmann 1976, Ishii et al 1976, Tawara et al 1976 and Kaji et al 1977). Theoretical description of SEB is made difficult by the fact that the electrons may suffer severe deflections before radiating bremsstrahlung. Tawara et al (1976) have, however, compared measured data for protons and helium-3 impact on Al target with theoretical predictions based on the



Figure 2.8 Experimental and theoretical background radiation cross sections for 3MeV protons on thin carbon foil. Detector at 90° to the beam (Folkmann et al 1974a)

binary encounter approximation model of Bonsen and Vriens (1970) and have obtained reasonable qualitative agreement.

Past and future interest in SEB stems from the fact that it is the major source of bremsstrahlung at low x-ray energies, precisely the region which is of fundamental concern to experimenters involved in trace elemental analysis by charged particle impact (Folkmann 1975, Johansson and Johansson 1976, Renan 1980, Khan and Crumpton 1981). It may also be relevant to the understanding of ion-atom collision mechanisms (Tawara et al 1976 and Mokler and Folkmann 1978).

2.4.3 Compton Scattering of Gamma-Rays

If a charged particle has sufficient energy to overcome the Coulomb potential barrier surrounding the target nucleus, it may undergo an inelastic interaction with the nucleaus. At low MeV energies the interaction is most likely with the nucleus as a whole leading to its excitation. The excited nucleus may then deexcite by releasing its excess energy in the form of gamma ( $\gamma$ ) - rays (Lapp and Andrews 1972 and Burcham 1973). These  $\gamma$ -rays Compton scatter (see subsection 2.5.2) from the surroundings and in the detector producing a continuous background in the low keV x-ray region. This form of background is not 'bremsstrahlung' in the strictest sense since bremsstrahlung describes electromagnetic radiation emitted while charged particles are accelerated in an electric field. It is however, discussed in this section because of its direct relevance to the total continuum seen in an x-ray spectrum produced by charged particle impact.

Background due to Compton scattering of  $\gamma$ -rays is only acute for target elements which have high excitation cross sections or exhibit large resonances at low MeV energies. Elements such as <sup>19</sup>F, <sup>23</sup>Na, <sup>27</sup>Al, <sup>12</sup>C and <sup>16</sup>O are particularly prone to this problem causing the background from this source to be comparable, if not more important than the projectile bremmstrahlung at the high energy region of the x-ray spectrum (Folkmann et al 1974a). The discrepency between theory and experiment

in figure 2.8 is explained by the contribution of Compton scattering to the total bremmsstrahlung (Renan 1980).

For the same energy, alpha particles are less susceptible than protons and deuterons to nuclear reactions leading to the emission of  $\gamma$ -rays. Deuterons can undergo 'stipping' and 'pick-up' reactions making them a less attractive choice of bombarding particles for trace-elemental analysis. The significance of Compton scattering to the afore-mentioned analytical technique has been discussed by Folkmann et al (1974b), Folkmann (1975), Johansson and Johansson (1976), Ahlberg and Adams (1978) and Khan and Crumpton (1981).

2.4.4 Quasi-Free Electron Bremsstrahlung

Bremsstrahlung can result from the direct interaction of a charged particle with the orbital electrons of a target atom. This type of bremsstrahlung has been called 'quasi-free electron bremsstrahlung' (QFEB) by Yamadera et al (1981b). It was, however, initially observed by Schnopper et al (1974) who named it 'primary bremsstrahlung'. Jakubassa and Kleber (1975) who developed a theory explaining this phenomenon referred to it as 'radiative ionisation'. In this process when the electric fields of the incident particle and the atomic electron interact, the electron is ejected and experiences an acceleration and thereby emits electromagnetic radiation (Anholt and Saylor 1976). Assuming the projectile velocity (v) is large compared to the orbital electron velocity the electron may be considered to be quasi-free. The resulting bremsstrahlung is characterised by the relative kinetic energy  $(T_r)$  which is equal to  $\frac{1}{2}mv^2$ , where m is the electron mass (Yamadera et al 1981b). QFEB should not be confused with SEB where the radiation is emitted as a result of a two-step process since the electron is first ejected and then suffers a deviation as it interacts with the electric fields of other target atoms. However, like SEB, this process is important for light-ion impact (Chu et al 1981). For heavier targets  $(Z_2 \text{ increasing})$  QFEB depends increasingly on the velocity of the orbital

electrons and the intensity decreases less steeply in the vicinity of the high-energy limit  $T_r$  (Yamadera et al 1981b).

2.4.5 Discharge Electron Bremsstrahlung

Surfaces of targets, which are good insulators, can charge-up to a high voltage (several tens of volts) when bombarded continuously by positively charge particles. The target discharges by attracting free electrons in the vicinity of the target causing their acceleration. As a result an intense bremsstrahlung of energy up to several tens of keV is emitted by the electrons (Ahlberg et al 1975 and Renan 1980). This discharge electron bremsstrahlung (DEB) is particularly severe for thick insulating targets. Several solutions for eliminating this source of background have been proposed. Shabason et al (1973) suggests that the target should be neutralised by placing a hot filament a short distance away from the target. Evaporating a thin layer of carbon on the target to avoid charge build-up has been proposed by Papper et al (1978). Mingay and Barnard (1978) have employed a magnetic field to deflect the secondary electrons onto the target. The tertiary electrons generated as a result discharge the target. Huda (1979) has irradiated his targets in air to eliminate DEB.

2.4.6 Transition Radiation

This name is given to the radiation emitted when a charged particle suddenly crosses a boundary between two media with different dielectric constants. (Ginsburg and Frank 1946 and Garibyan 1958). When the particle passes through the interface its electric field, which is characteristic of its motion and the medium, adapts to the properties of the second medium. As the field reorganises itself transition radiation is emitted (Jackson 1975). The wavelength of this radiation may range from the optical to the x-ray region of the electromagnetic spectrum depending on the energy of the incident particle. Gibb et al (1977) indicated that this radiation, when in the x-ray region, may contribute to the bremsstrahlung normally associated with particle-induced x-ray experiments. Ramsay and Mckee (1978)

have confirmed, however, that the contribution would be negligible even for high energy protons and would not pose any significant problem.

## 2.4.7 Heavy-Ion Effects

Highly stripped heavy ions can capture electrons from target atoms into their vacant states and may directly radiate the excess energy gained through this transition (Mokler and Folkmann 1978 and see subsection 2.3.4). The outer target atomic electrons are normally the participants in this 'radiative electron capture' (REC) and consequently give rise to a peaklike continuum centred above the binding energy of the projectile. The width of this continuum increases with atomic number of the target. Innershell electrons may also be captured by the incoming heavy ion but instead of a distinct peak a continuum ranging to high energies is observed. For light charged particles ( $Z_1 << Z_2$ ) REC is not significantly important in relation to the total bremsstrahlung (Schnopper et al 1974). REC has also been studied by Kleber and Jakubassa (1975), Sohval et al (1976) and Spindler et al (1977).

Another process, which is only significant for heavy ions and gives rise to non-characteristic x-rays is that of quasimolecular x-ray emission (Saris et al 1972). In this case a broad non-characteristic band is observed as well as the individual characteristic x-rays of the projectile and the target. The electron shells of the ion and the target atom interpenetrate and form a transient quasimolecule. The non-characteristic band is due to radiative transitions between the quasimolecular orbital (Kraft et al 1974, Greenberg et al 1974 and Thoe et al 1975). In solid targets x-rays due to one- and two- collisions are emitted and the quasimolecular x-ray yield has been shown to be strongly dependent on the target density and the projectile velocity by Stoller et al (1981).

## 2.5 ATTENUATION OF X-RAYS

The attenuation of a narrow parallel beam of photons with intensity,  $I_0$ , passing through a thin homogeneous absorber of thickness, x, is described by Bouguer-Lambert-Beer exponential absorption law:

$$I = I_0 \exp(-\sigma nx)$$
 2.12

where I is the photon beam intensity after attenuation,  $\sigma$  is the attenuation cross section and n is the number of absorber atoms per unit volume. The term  $\sigma$ n is called the linear attenuation coefficient ( $\mu$ ) and is the attenuation of the photon beam per unit length. That is

$$\mu = \sigma n = \sigma \frac{N_{0}\rho}{A_2}$$
 2.13

where  $N_0$  is the Avogardro's number,  $\rho$  is the absorber density and  $A_2$  is the absorber atomic weight. Since the interaction cross-section ( $\sigma$ ) is dependent on the absorber density, it is more convenient to use the mass attenuation coefficient,  $\mu/\rho$ , which is independent of the mass density. Thus

$$\frac{\mu}{\rho} = \frac{\sigma N_0}{A_2}$$
 2.14

For a mixture or a chemical compound the mass attenuation coefficient,  $(\mu/\rho)_{mix}$ , can be evaluated from the mass attenuation coefficients,  $(\mu/\rho)_i$ , of the constituent elements using the mixute rule

$$\left(\frac{\underline{\mu}}{\rho}\right)_{mix} = \sum_{i} w_{i} \left(\frac{\underline{\mu}}{\rho}\right)_{i}$$
 2.15

where w<sub>i</sub> is the proportion by weight of the i<sup>th</sup> constituent element.

The different interaction mechanisms by which the incoming photon can be completely absorbed or scattered depend on the photon energy and the atomic number of the absorbing material. The major mechanisms pertinent to this study are mentioned below.

#### 2.5.1 Photoelectric Absorption

In this process an incoming photon interacts with an absorber atom as a whole and is completely absorbed. The perturbation on the atom causes a bound electron to be ejected from the atom, as a result of which, the atom recoils. Photoelectric absorption occurs most readily when the energy of the photon ( $E_X$ ) is just larger than the binding energy of the shell from which the electron is ejected. For photons with energy less than 100keV this type of interaction is the most probable. The photoelectric interaction cross section increases rapidly with absorber atomic number ( $Z_2^{4-5}$ )

and decreases with photon energy approximately as  $E_X^{-3.5}$  (Knoll 1979).

The photoelectric effect has been discussed theoretically be Hall (1936), Pratt et al (1964), Rakavy and Ron (1967), Pratt et al (1973) and Park (1974). Experimental measurements of the photoelectric mass absorption coefficient,  $(\mu/\rho)_{PE}$ , have also continued in the past decade (Millar and Greening 1974 a, b, Lawrence 1979, Berry and Lawrence 1979) and more recently measurements have been reported by Sarma et al (1982). A detailed comparison of theoretical and experimental data in the photon energy range 0.1 keV to 1.5 MeV has been given by Hubbell and Veigele (1976). Hubbell (1977a) has presented  $(\mu/\rho)_{PE}$  for light elements and some mixtures deduced from experimental and theoretical data. Parametric expressions for calculating  $(\mu/\rho)_{PE}$  have been derived by Jackson and Hawkes (1981) starting from the fundamental theory of photon-electron interaction. Cross sections for the emission of an inner-shell electron derived using the Born approximation (Bethe and Salpeter 1957) were used and excellent agreement with other published work was acheived (Hawkes and Jackson 1980).

## 2.5.2 Incoherent Scattering

This process involves an incoherent interaction between a photon and an atomic electron assumed to be free. The electron may be excited to a higher\_shell or ejected into the continuum. This effect, named after Compton (1923) causes an increase in the wavelength of the incident photon. Compton scattering occurs impulsively and only when the energy transfer to the atomic electron is greater than its binding energy (Jauncey 1925).

The Compton scattering cross section increases linearly with  $Z_2$  and decreases gradually with increasing  $E_X$  (Knoll 1979). However, for high  $Z_2$ , the cross section looses importance in favour of the photoelectric effect.

The fundamental theory for calculating scattering cross sections is that of Klein and Nishina (1929). The basic assumption of this theory is that the electron involved is free and stationary. This is a reasonable approximation for high energy photons and outer-shell electrons or electrons of light

elements. However, for low energy photons or for inner-shell electrons of medium and heavy atoms relativistic and binding effects have to be allowed for. The binding effects are estimated by the incoherent scattering factor, which is the probability for excitation or ionisation of an atom when it undergoes an incoherent interaction (Raghava Rao et al 1982). The theoretical calculation of this functions has been discussed in detail by Hubbell et al (1975) who have made detailed comparisons with experimental data. Raghava Rao et al (1982) have reported experimental measurements of this factor exclusively for the K-shell which show marked discrepancies when compared with theoretical data of Hubbell et al (1975), highlighting the need for further work in this area. Hawkes and Jackson (1980) have modified the Klein-Nishna cross sections and have formulated parametric expressions for the Compton scattering cross sections. The contribution by Compton scattering to the mass attenuation coefficient of Mg and Ag have been estimated by Lawrence (1979).

Compton scattering has been successfully employed in the study of electron momentum distributions (Cooper 1971) and is thus proving invaluable for studying solid-state properties. Progress in this field, experimental and theoretical, has been surveyed by Williams (1977). Recent work includes that of Pattison and Weyrich (1979), Rindby et al (1982) and Pattison et al (1982).

#### 2.5.3 Coherent Scattering

When bound electrons participate in the photon-atom interaction, there is a finite probability that the electrons will not be transferred to higher atomic states or ejected into the continuum. Scattering in this case is coherent (Rayleigh) and takes place with the atom as a whole, causing the electron to oscillate at the frequency of the incident radiation. The electrons then relax by radiating electromagnetic energy without any change in the frequency, which appears as scattered radiation concentrated in the forward direction. The scattering cross section increases as  $Z_2^{2.5-2.7}$  and

decreases with photon energy as  $E_X^{-2}$  (Dyson 1973). Consequently, this process is important at low photon energies and for heavy absorber elements.

When the interaction takes place with a single electron, assumed to be free, we then have Thomson scattering (Jackson 1975 and Read 1980). Thomson scattering occurs only at low energies where the momentum of the incident photon can be ignored. At higher frequencies the Compton effect comes into operation. Thomson scattering is, therefore, the low frequency limit of the Compton effect (Davisson 1965). Thomson scattering is independent of the photon energy, in the energy region where it takes place, and is approximately proportional to  $Z_2$  (Davisson 1965). A parametrized approach for calculating coherent scattering has been provided by Hawkes and Jackson (1980). The atomic form factors, the square of which gives the probability that the  $Z_2$ electrons of an atom take up a certain recoil momentum without absorbing any energy (Hubbell 1969), required for calculating interaction cross sections for this process have been tabulated by Hubbell (1975). 2.5.4 Tabulations of Mass Attenuation Coefficients

The total mass attenuation coefficient,  $\mu/\rho$ , is obtained by summing the individual contributions. Using equation 2.14 we get,

$$\frac{\mu}{\rho} = (\sigma_{PE} + \sigma_{INC} + \sigma_{COH}) \frac{N_0}{A_2}$$
 2.16

where  $\sigma_{\rm PH}$ ,  $\sigma_{\rm INC}$  and  $\sigma_{\rm COH}$  are the interaction cross sections for the photo-electric absorption, incoherent scattering and coherent scattering respectively.

Considerable activity has been directed to the specific task of compiling an internally consistent and reliable set of data for these quantities. Hubbell (1969) has published tabulated data for mass attenuation coefficients and interaction cross sections for 23 elements and 13 compounds and mixtures, covering a photon energy range of 10keV to 100GeV. For the low energy region uncertainties upto 10% in these quantities are quoted depending on  $Z_2$ , low  $Z_2$  elements having larger uncertainties. The experimental and theoretical data have been comprehensively reviewed by Hubbell (1969, 1971). The very

popular tabulation of theoretical cross section values of Storm and Israel (1970) covers all elements up to  $Z_2 = 100$  and an energy range of 1kev to 100MeV. These authors have quoted uncertainties ranging from 3 to 10% depending on the photon energy, higher uncertainties applying to energies less than 6keV. Storm and Israel (1970) include a comparison of experimental and theoretical values and relative shell contributions to the photo-electric cross section. To facilitate the use of this tabulation Montenegro et al (1978) have fitted logarithmic polynomials to the values of Storm and Israel (1970) and have tabulated mass attentuation coefficients for elements with  $6 \le Z_2 \le 33$  for characteristic K and L x-rays of elements with  $17 \le Z_2 \le 94$ . Semi-experical expressions have been utilised by Gerward (1980) to fit the data of Hubbell et al (1974). An energy range of 5 to 100 keV and elements with  $2 \le Z_2 \le 92$  have been covered. However, the author has admitted in his article that logarithmic expressions, such as those employed by Montenagro et al (1978) would provide better fits. Hubbell (1982) has published theoretical values of the total mass attentuation coefficients for photon energies.1 keV to 20MeV for 40 elements ranging from  $1 \le Z_2 \le 92$  and 45 mixtures and compounds.

From above it is clear that the low x-ray energy region, which is important for most x-ray analytical techniques, photon attenuation coefficients are uncertain by about 10%. At energies around or below 1 keV the uncertainty can be as high as 20% or even greater (Hubbell 1977b). Recognising the necessity of reliable mass attenuation data it was decided at the International Union of Crystallography Congress, held in Warsaw 1978, to set up a committee to organise an evaluation of the experimental techniques adopted for measuring x-ray attenuation coefficients. Further details can be found in the Journal of Applied Crystallography Volume 13 (1980) pp199-200.

# CHAPTER 3 CONCEPTS OF NUCLEAR BACKSCATTERING

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#### 3.1 INTRODUCTION

The atomic processes which reveal themselves through characteristic features in an x-ray spectrum were examined in the preceeding chapter. In the present chapter, concepts which are closely related to a nuclear backscattering spectrum have been addressed. Energy loss and straggling of charged particles passing through matter have been considered qualitatively and contemporary problems in both these areas are highlighted.

Nuclear backscattering spectrometry has been dealt with from the view point of measuring thin film thicknesses and the analytical capabilities of this technique are mentioned only briefly. However, references which consider the analytical aspects in greater detail have been quoted. Fundamental formulae required for determining thin film thicknesses have been stated and corrections to the Coulombic scattering cross section, including recent contributions, are discussed. Throughout this chapter cgs units have been employed in order to be consistent with the published literature on this subject.

# 3.2 ENERGY LOSS AND STRAGGLING OF CHARGED PARTICLES

The study of energy loss and straggling processes of charged particles is important not only for understanding the process mechanisms themselves, but also for the correct interpretation of quantitative information obtained from charged particle based analytical techniques. Two such major techniques are nuclear backscattering spectroscopy (Chu et al 1978) and particle induced x-ray emission analysis (Johansson 1981). The former technique is based on the actual physical laws governing the energy loss of a charged particle as it traverses matter and the latter requires energy loss data for the purpose of applying corrections to quantitative results obtained from thick and semi-thick targets. Although a particle traversing matter loses its energy through collision and radiative processes, only the former is discussed in this section. Radiative losses have been dealt with

in Chapter 2.(section 2.4) in the context of bremsstrahlung emission.
3.2.1 Energy Loss by Collision

As a charged particle travels through a medium it loses its energy to the atomic electrons (electronic stopping) and to the atomic nuclei (nuclear stopping) by electrostatic interaction (Bohr 1913). Nuclear stopping is due to elastic collisions with the target nucleus and predominates when  $v << v_0$ , where v is the particle velocity and  $v_0$  is the Bohr velocity. At particle energies above 200keV/amu it is typically around 1% of the electronic stopping (Ziegler 1980). At higher energies nuclear stopping becomes even more insignificant and the interaction of the projectile with the target nucleus changes from elastic to inelastic. The relative contributions of electronic and nuclear stopping are shown in figure 3.1. At projectile velocities,  $v < v_0 Z_1^{\frac{2}{3}}$ , electronic stopping is proportional to the particle velocity (Linhard and Scharff 1981) where Z is the projectile charge and  $v_0 Z_1^{\frac{2}{3}}$  is the mean velocity of the bound projectile electrons. It reaches a maximum when v approaches  $v_0 Z_1^{\frac{2}{3}}$  beyond which it falls as  $lnv^2/v^2$ .

The proximity of the ion to the atomic electrons determines whether electronic stopping is through excitation or ionisation of the atom. Excitation is predominant for distant collisions and ionisation for close ones. Ionisation contributions to the energy loss of the ion originate in two ways. Firstly, they arise through primary collisions with atomic electrons. The most probable collisions are where the energy transfers in each collision are small, thus resulting in the ejection of low energy secondary electrons (Segre 1953). A small fraction of ionising collisions (close) may produce energetic secondary electrons (delta rays) with a maximum kinetic enegy of  $(4m/M_1)E$ . This is the maximum energy that an ion of mass,  $M_1$ , and energy, E, can transfer to a free electron of mass, m, in a direct collision and corresponds to the electron having a velocity twice that of the incident ion. Secondly, the contribution may come from ionisation by



Comparison of electronic and nuclear stopping of charged particles in

matter (Datz 1978).

Figure 3.1

rewog prigote

indirect interaction with the atomic electrons. This can occur either by the energetic delta rays causing further ionisation or a target atom recoiling as a result of the primary collision and causing ionisation of other atoms (Holmen et al 1979). The direct relationship between secondary electron emission and the electronic stopping of the ion was formulated by Sternglass (1957). The investigation of secondary electron emission as a result of ion impact has been pursued vigorously in recent years, not only for academic interest but also for its direct relevance in stopping power and thermonuclear fusion studies (Stolterfohr 1978, Veje 1982, Svenson and Holmen 1982 and Bell et al 1982).

The behaviour of the rate of energy loss with distances, x, travelled by a fully stripped ion with charge  $Z_1e$  in a medium with atomic number  $Z_2$ , and atomic density, n, is described by the fundamental Bethe formula based on a relativistic quantum mechanical treatment (Bethe and Ashkin 1953 and Fano 1963)

$$-\frac{dE}{dx} = \frac{4\pi (Z_1 e^2)^2 Z_2 n B}{mv^2}$$

$$= \left[ \ln \left( \frac{2mv^2}{I} \right) - \ln (1 - \beta^2) - \beta^2 - \frac{C_1}{Z_2} \right]$$
3.1

and B

where m is the electron rest mass, v is the projectile velocity, e is the electronic charge,  $\beta$  is V/C ratio, c being the velocity of light, I is the mean excitation potential of the stopping medium,  $C_1/Z_2$  is the ith shell correction and B is the stopping number. This equation assumes that there are no radiative energy losses. We should note that the stopping power, dE/dx, shows a simple  $Z_1^2$  dependence assuming that the stopping number is a function of v and  $Z_2$  only. A further important point to note is that this equation is valid only for high energies (>1MeV/amu), that is, beyond the stopping power maximum (figure 3.1). The mean excitation potential, I, is independent of the ion velocity and is defined theoretically, as (Bethe 1930)

$$\ln (I) = \sum_{n} f_n \ln (E_n) \qquad 3.2$$

where  $E_n$  are all possible energy transitions of the target atoms and  $f_n$  are the corresponding dipole oscillator strengths. Except for the simplest atoms the complexity of this equation is overwhelming (Anderson and Ziegler 1977a) and for practical purposes values for I are usually extracted from experimental data (Chu and Powers 1972). For recent progress in this area the reader is referred to Inokuti (1981). The energy dependent shell corrections,  $C_i/Z_2$ , allow for the lack of participation of the inner most electrons in the stopping process (Walske 1956 and Sorensen and Anderson 1973). Without these corrections equation 3.1 is only valid when v is much greater than the orbital velocity of the  $Z_2$  bound electrons. When this is not the case, as for innershell electrons of heavy elements, these corrections are necessary (Walske 1956). Such corrections have been formulated by Walske (1952 and 1956) and Brandt (1975), and Andersen and Ziegler 1977a).

Experimental energy loss data that has accumulated over the past years have revealed the need for high order charge-dependent corrections to Bethe's formula (Andersen et al 1969, Lindhard 1976, Andersen et al 1977 and Anthony and Lanford 1981). A  $Z_1^3$  term takes into account polarisation effects at low velocities. It explains observed differences between stopping powers of particles and their antiparticles, originally noticed by Barkas et al (1963) and thus called the Barkas effect by Lindhard (1976) (Ashley et al 1972, Jackson and McCarthy 1972 and Hill and Merzbacher 1974). Lindhard (1976) obtained a correction twice that of Ashley et al (1972) which was confirmed by Andersen et al (1977). At high energies deviations from the Rutherford formula introduces higher order Z1 terms known as the Mott correction (Morgan and Eby 1973). An expression for this term to order  $Z_1^7$  has been derived by Ahlen (1978). At the two velocity extremes a Bloch's correction of  $Z_1^{2n}$  (n = 2, 3...) is required (Bloch 1933). Recent work on  $Z_1^{3}$  and  $Z_1^{4}$ corrections has been published by Porter and Bryan (1980). Measurements performed by Salaman et al (1981) have revealed a need for a further

correction for relativistic heavy ions. Such a correction has been confirmed and derived by Ahlen (1982).

At low velocities ( $v \sim v_0$ ) the electronic stopping was found to depend in an oscillatory fashion on Z<sub>1</sub> by Bottiger and Bosson (1969). Theoretical explanations for this behaviour has been given by Briggs and Pathak (1974). Also at low velocities stopping power for a given ion (Z<sub>1</sub> fixed) shows similar oscillatory dependence on the stopping medium (Z<sub>2</sub>). This is true for light ions (Ziegler and Chu 1974 and Gertner et al 1980) and for heavy ions (Pietsch et al 1976 and Land et al 1980). Kreussler et al (1981) have shown experimentally that these pronounced target effects diminish with increasing velocity and beyond the stopping power maximum show a smooth Z<sub>2</sub> dependence (Mann and Brandt 1981). At low particle velocities stopping power is determined by the properties of the valance electrons in the medium and not the inner-shell electrons which remain relatively inactive implying that these fluctuations are most likely to be a consequence of the valanceelectron configuration of the elements (Brandt 1981).

The energy loss process for heavy ions is further complicated by the fact that the charge state of the ions changes with penetration. This has been recognised as one of the most fundamental problems in stopping theory (Andersen and Ziegler 1977b). As the ion penetrates matter its charge changes either by electron loss to the medium or by electron capture from the medium. This effect produces discrepencies in the  $Z_1^2$  scaling law unless the effective charge state of the ion is known (Andersen and Ziegler 1977b). At high velocities ( $v > v_0 Z_1$ , where  $v_0 Z_1$  is the velocity of the K-shell electron) the ion can be assumed to be completely stripped of its electrons but if  $v \leq v_0 Z_1^{\frac{2}{3}}$  the ion is only partially stripped (Brandt 1981). Using the Thomas-Fermi model of the atom, Ziegler (1977) has derived an empirical expression for the effective charge of ions. An

based on the work of Northcliffe (1963) and Forster et al (1976) for scaling proton stopping powers to obtain values for heavy ions. This problem has been tackled theoretically by Brandt (1981) and Wietschorke and Soff (1981) and experimentally by Schulz and Brandt (1981) and Anthony and Lanford (1982). Other notable references in the field of energy loss of charged particles include Mayer and Ziegler (1973), Saris and Van der Weg (1976), Andersen et al (1980) and Bird and Clark (1981). Recent measurements have been made by Fukuda (1981) and Santry and Werner (1981) and Ahlen (1980) has recently published a review article on the subject.

Despite the difficulties in explaining the energy loss process theoretically, experimental work on this subject has been unceasing. A comprehensive bibliography has been presented by Andersen (1977) on the subject. Recent tabulations of stopping powers have been published by Andersen and Ziegler (1977a,b) for protons and alpha particles passing through all elements. A more recent tabulation by Ziegler (1980) gives the stopping powers of all ions in all elemental absorbers. The values in these tabulations were obtained by combining experimental and theoretical results. The latter were used to determine stopping powers of ions in elements for which experimental values were unavailable. The projectile energy range covered is 1 - 10<sup>5</sup>keV and empirical formulae fitted to the experimental data are also presented by these authors. These fits are reported to be accurate to 1% and the interpolated values are reliable to 0.5% (Andersen and Ziegler 1977a). 3.2.2 Energy Straggling

The energy loss process mainly involves a large number of independent interactions between the ion and the atomic electrons of the absorber which are subject to statistical fluctuations (Bohr 1915). This stochastic nature of energy loss of ions causes the delta distributions of a mono-energetic ion beam, of identical particles, to broaden considerably after passing through an absorber. The fluctuations in the energy loss of the particles

is known as energy straggling. This is closely related to range straggling (Lewis 1952). The upsurge of interest in this phenomenon in recent years can be attributed to the successful application of ion beam analysis techniques which require a detailed knowledge of energy straggling (Mayer and Ziegler 1973, Saris and Van Der Weg 1976, Andersen et al (1980), and Bird and Clark 1981). In nuclear backscattering spectroscopy, for instance (section 3.3), energy straggling is one of the major factors which limit depth resolution studies (Friedland 1978).and, therefore, it is essential that its effect is quantified.

The original theory formulated by Bohr (1915) predicts that the energy straggling is independent of the particle energy and that the root-mean-square (rms) value of the energy variation increases with the square root of the electron density per unit area (n  $Z_2$ t) in the target, that is,

$$\Omega_{\rm R}^2 = 4\pi (Z_1 e^2)^2 n Z_2 t \qquad 3.3$$

where  $\Omega_B^2$  (keV<sup>2</sup>) is the variance of the energy loss distributions, Z<sub>1</sub> is the projectile atomic number, Z<sub>2</sub> is the targets atomic number, t is the target thickness and n is the number of target atoms per unit volume. The above expression is based on the assumption that the individual energy transfers takes place between a free electron at rest and a fully ionised projectile. Therefore, it is only applicable beyond the stopping power maximum. Lindhard and Scharff (1953) have refined Bohr's theory to extend the range of applicability to below and in the vicinity of the stopping power maximum. Bonderup and Hvelplund (1971) added further improvement to take into account the oscillatory dependence of energy straggling on Z<sub>2</sub>, a situation similar to that found for stopping power. Chu (1976) by incorporating Hartree-Foch-Slater atomic wave functions into the theory of Bonderup and Hvelplund (1971), explained these material dependences. Contrary to Bohr's theory (Bohr 1915), energy straggling measurements reported by Harris and Nicolet (1975) revealed a weak dependence on the

projectile energy which is in qualitative agreement with the other formulations by Lindhard and Scharff (1953), Bonderup and Hvelplund (1971) and Chu (1976). Bohr's theory further predicts a Gaussian energy loss distribution. This, however, has been found to be true only for low velocity projectiles (Wilken and Fritz 1976) and in general is only an approximation. A realistic distribution is asymmetrical and shows significant skewness as shown by Landau (1944), Tschalar (1968) and Bichsel and Saxon (1975). However, in the low MeV energy region for ligh ions the energy resolution of conventional solid-state detectors is not fine enough to show the non-Gaussian shape and the assumption of a Gaussian distribution is acceptable for practical purposes. If the particle has enough energy to completely penetrate through the detector's sensitive volume considerable dispersion is observed in the distribution (Wilken and Fritz 1976).

Experimental investigation of energy straggling has inherent difficulties since the true straggling is hidden within instrumental (Wilken and Fritz 1976) and target inhomogeniety effects (Stoquert et al 1981a). Despite these hindrances interest has continued (Friedland and Kotze 1981 and Molherbe and Alberts 1982).

An important contribution to energy straggling concerns the fluctuations in energy loss caused by charge-exchange effects as the particle passes through matter (Vollmer 1974). This effect is particularly important at the vicinity of the stopping power maximum where the probability of charge exchange is high (Cuevas et al 1964). Sofield et al (1981) has explained discrepencies of upto a factor of two between experimental measurements and theoretical predictions in terms of charge exchange effects. The importance of these effects to the energy loss and straggling processes accompnaying the passage of ions through matter is self-evident from the above discussion and makes the continued pursuance of experimental and theoretical investigations in this area vital.

# 3.3 NUCLEAR BACKSCATTERING SPECTROMETRY

Although the pioneering work of Rutherford (1911) and Geiger and Marsden (1913) gave birth to nuclear backscattering spectrometry it is only in the last two decades that is has established a firm foothold as one of the major surface analystical techniques (Chu et al 1978). This development was primarily a consequence of the advent of fast-response solid-state detectors which offered good resolution and good linearity over a wide range of energies and to the improvements acheived in the electronic systems required for data handling and processing (Chu et al 1978).

The physical concepts of nuclear backscattering spectrometry have been considered only briefly here, simply because as a result of its generally wide acceptance and its high level of development a prodigious amount of literature is now available which covers its concepts and applications in great depth (Mayer and Ziegler 1973, Ziegler 1975, Foti et al 1977, Chu et al 1978, Gyulai 1980, Bird and Clark 1981, Gyulai 1981 and Simons et al 1982). 3.3.1 Kinematic Factor

When a light charged particle of mass,  $M_1$ , impinges on a target there is a finite probability that it will experience a Coulombic interaction with a target nucleus of mass,  $M_2$ . As a result of this interaction the particle transfers momentum to the target nucleus causing it to recoil and is, itself, deflected at an angle,  $\theta$ . A minority of the impinging particles may suffer close 'billiard ball' type encounters with the nucleus and be deflected by obtuse angles as shown in figure 3.2. Provided that the incident projectile energy is below the threshold of nuclear reactions and greater than the binding energy of the target atom (Chu et al 1978) the collision may be considered as an elastic one and using the conservation laws the kinematic factor, K, defined as the ratio of the projectile energy after (E<sub>1</sub>) and before (E) the collision can be calculated. For the non-relativistic case in the laboratory frame and provided  $M_1 < M_2$  we have



$$K = \frac{E_1}{E}$$
 3.4

$$= \left[ \left( \frac{M_2^2 - M_1^2 \sin^2 \theta}{M_2 + M_1} \right)^{\frac{1}{2}} + M_1 \cos \theta}{M_2 + M_1} \right]^2 \qquad 3.5$$

$$= \left[ \frac{(1 - (M_1/M_2)^2 \sin^2\theta)^{\frac{1}{2}} + (M_1/M_2) \cos\theta}{1 + (M_1/M_2)} \right]^2 \qquad 3.6$$

The kinematic factor, therefore, depends on the ratio of  $M_1$  and  $M_2$ and for fixed  $M_1$  and E it facilitates mass discrimination by nuclear backscattering spectrometry.

In practice the mass difference,  $\Delta M_2$ , between two elements of interest in a target must produce as large an energy change,  $\Delta E_1$ , as possible after collision. For fixed  $M_1$  and  $\dot{E}$ ,  $\Delta M_2$  will induce the largest change in K at a scattering angle of  $180^{\circ}$ . Consequently, to achieve the maximum mass resolution  $\theta$  is chosen to be as close as possible to  $180^{\circ}$  as the experimental set-up will allow. Quatitatively  $\Delta E_1$  can be expressed as (Chu et al 1978)

$$\Delta E_1 = E\left(\frac{dK}{dM_2}\right) \Delta M_2 \qquad 3.7$$

 $dK/dM_2$  can be readily obtained from equation 3.5 and

$$\frac{dK}{dM_2} \simeq -\frac{4M_1}{M_2^2} \cos\theta \qquad 3.8$$

If  $\theta$  is different from  $\pi$  by  $\delta$ , where  $\delta$  is small, equation 3.8 can be written as

$$\frac{dK}{dM_2} \simeq (4 - 2\delta^2) \frac{M_1}{M_2^2}$$
 3.9

Substituting 3.9 into 3.7 we arrive at

$$\Delta E_1 = E (4 - 2\delta^2) \frac{M_1}{M_2^2} \Delta M_2 \qquad 3.10$$

From equation 3.10 we can deduce that the mass resolution can be optimised by

- (i) increasing E
- (ii) using heavy ions (increase  $M_1$  provided  $M_1 < M_2$ )
- (iii) measuring at scattering angle as close as possible to  $180^{\circ}$  so that  $\delta \neq 0$ , and
  - (iv) analysing light elements (small M<sub>2</sub>)

The possibility of employing heavy ions for backscattering spectrometry has been explored rigorously by many workers (Peterson et al 1973, Miller and Ischenko 1976, Thomas et al 1976 and Sullins et al 1981). The main disadvantage of adopting heavy ions such as <sup>12</sup>C and <sup>16</sup>O as projectiles instead of <sup>1</sup>H and <sup>4</sup>H<sub>e</sub> is the worsening of the detector resolution that results and which dampens considerably the advantages. However, despte this problem Petersson et al (1973) have attained improvements in the mass resolution of upto a factor of four. Thomas et al (1976) used Lithuim ions of energy upto 3MeV and obtained improvements while still maintaining the detector resolution. Sullins et al (1981) have compared high energy <sup>16</sup>O, <sup>20</sup>Ne and <sup>40</sup>Ar ions and have highlighted the potential capabilities of heavy-ion nuclear backscattering spectrometry for resolving neighbouring masses for elements with 50 < M<sub>2</sub> <100. A mass resolution of better than 1 amu has been achieved by Chevarier et al (1981) with <sup>14</sup>N and <sup>40</sup>Ar ions by using a time-of-flight spectrometer.

The choice of E and the inherent advantage of analysing light elements cannot be discussed in isolation and are subject to compromises imposed by the scattering cross section considered below.

#### 3.3.2 Scattering Cross Section

The concept of the differential scattering cross section,  $d\sigma_R/d\Omega$ , allows quantitative analysis by backscattering spectrometry.  $d\sigma_R/d\Omega$  is a measure of the probability of a scattering event occuring due to a Coulomb interaction. This can be derived classically (Rutherford 1911) or quantum mechanically (Tralli and Pomilla 1969) and in laboratory

co-ordinates is given by

 $\frac{d\sigma_R}{d\Omega} = \left(\frac{Z_1 Z_2 e^2}{4E}\right)^2 \frac{4}{\sin^4\theta} \quad \left[ \left(\frac{1 - (M_1/M_2)^2 \sin^2\theta}{[1 - (M_1/M_2)^2 \sin^2\theta]^{\frac{1}{2}} + \cos\theta} \right]^2 \\ 3.11$ 

This is the Rutherford forumla and gives the differential scattering cross-section with respect to the detector solid angle,  $\Omega$ , for a projectile with incident energy, E, charge, Z<sub>1</sub>e, and atomic mass, M<sub>1</sub>, scattered by a target nucleus of atomic number, Z<sub>2</sub>, and mass, M<sub>2</sub>, at an angle,  $\theta$ . Equation 3.11 assumes that the force between the two nuclei is Coulombic. This is a valid assumption provided that the distance of closest approach is much greater than the nuclear dimensions but smaller than the Bohr radius. For very small solid angles  $\theta$  is well defined and the absolute scattering cross section ( $\sigma_R$ ) can be approximated by  $d\sigma_R/d\Omega$  (Chu et al 1978).

The following points are worth noting, that,  $d\sigma_R/d\Omega$  is

- (i) proportional to  $Z_1^2$  giving an alpha particle backscattered yield four times that of protons or deutrons.
- (ii) proportional to  $Z_2^2$  making nuclear backscattering much more sensitive to heavy elements than to light ions,
- (iii) proportional to E<sup>-2</sup> and, therefore, the backscattering yield increases rapidly with diminishing projectile energy,
  - (iv) a function of  $\theta$  and, therefore, is axially symmetrical with respect to the axis of the incident beam, and
    - (v) approximately proportional to cosec<sup>4</sup>θ and as a result the backscattering yield decreases rapidly with increasing θ.

Although the mass resolution is improved by increasing E, the fact that the scattered yield diminishes as  $E^{-2}$  for a given projectile has to be taken into account. Using light charged particles such as alpha particles, at about 2MeV is usually a good compromise. The inherent advantage of high mass resolution for light elements, mentioned in subsection 3.3.1, has to be weighed with the disadvantage of the backscattering

yield being less sensitive to light elements. These points illustrate that the exact experimental conditions depend on the nature of the analytic problem.

3.3.3 Corrections to the Scattering Cross Section

As the incoming projectile approaches a target nucleus it experiences and responds to the Coulomb potential of this nucleus which is itself screened by its atomic electrons. When scattering takes place in the vicinity of the atomic electron 'cloud' significant deviations from the Rutherford formula (equation 3.15) arise, as pointed out by Wenzel and Whaling (1952). This is because the Rutherford formula corresponds to the case where the target nucleus is unscreened. These deviations remain significant even when the scattering takes place close to the nucleus, that is within the K-shell radius, since in a screened atomic nucleus the particle is affected by the repulsive nuclear force only after it has penetrated the electron 'cloud' unlike the Rutherford case where the repulsive force is present even at large distances (L'Ecuyer et al 1979). Deviation of up to 4% for 1MeV He ion incident on a Bi target have been observed by L'Ecuyer et al (1979).

While determining stopping powers of low energy protons and deuterons in D2O ice Wenzel and Whaling (1952) formulated a correction to the Rutherford cross section,  $\sigma_R$ , that is,

$$\frac{\sigma - \sigma_{\rm R}}{\sigma_{\rm R}} = \frac{-\Delta}{E_{\rm CM}} \qquad 3.12$$
$$\sigma = \left(1 - \frac{\Delta}{E_{\rm CM}}\right) \sigma_{\rm R} \qquad 3.13$$

3.13

or

Where  $\sigma$  is the corrected cross section,  $E_{CM}$  is the projectile energy (keV) in the centre-of-mass frame, given by  $E_{CM} = EM_2/(M_1 + M_2)$ , assuming  $M_2$  is initially at rest, and  $\triangle$  is the absolute value of the electrostatic potential at the atomic nucleus. A has been derived by Foldy (1951) using a Hartree model of the atom and employed by Wenzel and Whaling (1952),

where

$$\Delta = \frac{12}{5} R_{\infty} Z_1 Z_2^{7/5}$$
 3.14

and since the Rydberg  $(R_{\infty})$  has the value 13.6eV,

$$\Delta = 0.0326 Z_1 Z_2^{\frac{7}{5}} \text{ keV} \qquad 3.15$$

By substituting equation 3.15 into 3.13, we arrive at the correction factor, F, used by Wenzel and Whaling (1952),

$$F = 1 - \frac{0.0326Z_1Z_2^{75}}{E_{CM}}$$
 3.16

L'Ecuyer et al (1979) utilised a classical approach by assuming that the distance of closest approach is greater than the de Broglie wavelength (Bohr 1948) and have derived F where

$$F = 1 - \frac{0.049Z_1Z_2^{4/3}}{E_{CM}}$$
 3.17

From equations 3.16 and 3.17 the increasing importance of the correction at low incident energies and for heavy targets is clearly apparant. L'Ecuyer et al (1979) have achieved good agreement with experimental results.

Hautala and Luomajarvi (1980) have given a more accurate treatment using Dirac-Fock electron distributions (Desclaux 1975). They, like L'Ecuyer et al (1979), have found the correction factor to be a function of  $Z_1 Z_2^{\frac{1}{7}}$ /E<sub>CM</sub>. However, the older correction given by Wenzel and Whaling (1952) have yielded closer agreement with their calculated results, except at high  $Z_2$  where good agreement was found by applying the correction derived by L'Ecuyer et al (1979). Hautala and Luomajarvi (1980) have also investigated the angular dependence of the correction factor and have noticed a weak dependence at backward angles in accordance with the above correction formulae.

From the foregoing discussion it is clear that the calculated scattering cross section may be employed reliably in quatitative work provided that the appropriate correction is made.

## 3.3.4 Determination of Thin Film Thicknesses

A target in the form of a film is considered to be 'thin' when the energy loss suffered by a projectile passing through it produces no significant variation in the interaction cross section. This criterion is discussed further in Chapter 5 while considering the choice of target thickness employed in the present study. It is shown that if a target is thin in relation to inner-shell ionisation cross section then it is also thin in relation to the Rutherford scattering cross section.

Unlike thick targets, both the front and the back surface features of thin targets are identifiable in a backscattering spectrum. Ideally, this spectrum would be rectangular in shape with a constant width,  $\Delta E$ , which is the sum of the energy loss suffered by the ingoing particle and the outgoing particle scattered from the back surface. In reality, however, this shape is superimposed by instrumental and energy straggling effects (Stoquert 1981b). Whereas the former effect contributes to both sides of the spectrum the latter appears only on the low energy side giving the spectrum a slightly skewed-Gaussian appearance, but as mentioned in subsection 3.2.2, for thin targets the skewness is minimal and is not noticed significantly by the present-day surfacebarrier detectors. The experimental measurement of the full-width-athalf maximum (FWHM) or  $\Delta E$  , affords a means by which the target thickness. can be determined (Chu et al 1978). Although ∆E decreases as the target thickness decreases, for a given set of experimental conditions a natural delimitation is imposed on the FWHM of the Gaussian peak by the instrumental effects, namely the detector resolution and the noise of the electronics. This fact makes the use of  $\Delta E$  for calculating very thin target thickness unreliable. For such targets the thickness may be determined from their backscattering yield, YB, which is related to the thickness, t, of the target by the expression

$$Y_{\rm B} = N_{\rm p} \sigma \Omega nt$$

3.18

where  $N_p$  is the total number of particles to which the target has been exposed,  $\sigma$  is the nuclear elastic scattering cross section at a particular scattering angle,  $\Omega$  is the detector solid angle and n is the number of target atoms per unit volume. Expression 3.18 relies on the assumptions that the projectile energy loss in the target is negligible. Furthermore, the thin film density is assumed to be equivalent to the bulk density.

In the cases where the energy loss of the projectile in the target, although small, is not negligible a correction is required to account for the variation of the nuclear scattering cross section in the target. A simple correction can be derived by assuming that the energy loss varies linearly with projectile energy and can be incorporated in equation 3.18 giving (Foti et al 1977 and Chu et al 1978)

$$Y_{\rm B} = N_{\rm D}\sigma\Omega nt C_{\rm F}$$
 3.19

and

$$F = \left(1 - \frac{\operatorname{nte}(\bar{E}_{in})}{E}\right)^{-1} \qquad 3.20$$

where  $C_F$  is the correction factor,  $\varepsilon(\overline{E}_{in})$  is the stopping power of the projectile in the film and is defined as

C

$$z(\bar{E}_{in}) = \frac{-1}{n} \frac{dE}{dx} \Big|_{\bar{E}_{in}}$$
 3.21

 $\bar{E}_{in}$  is the mean energy in the target of the incident projectile of energy E and can be estimated by E - ( $\Delta E$  /4) or simply by E (Chu 1975 and Chu et al 1978).  $\varepsilon(\bar{E}_{in})$  may be obtained from the tables of Andersen and Ziegler (1977a,b). It is worthwhile remarking that  $\varepsilon(\bar{E}_{in})$  appears only as a correction in the yield equation (3.19) and the uncertainty in  $\varepsilon(\bar{E}_{in})$ , therefore, does not play a major part in the thickness measurement. t can be isolated from equations 3.19 and 3.20 to give

$$z = \frac{Y_B}{n \left( N_P \sigma \Omega + Y_B \varepsilon \left( \frac{E_{in}}{E} \right) \right)}$$
 3.22
The above approach has been used to determine target thicknesses in the present study. The uncertainties in the experimentally measured quantities,  $Y_B$ ,  $N_p$  and  $\Omega$  determine the precision of t and are discussed in Chapter 5 along with the experimental procedure. The reliability of the calculated elastic nuclear scattering cross section  $\sigma$ , via equations 3.11 and 3.17, has already been referred to in subsection 3.3.3. The stopping power  $\varepsilon(\vec{E}_{in})$  was determined at  $\vec{E}_{in} = E$  since the energy lost by the charge particles in thin elemental targets of interest in this work is only a few keV at an incident energy of IMeV and less at higher energies.

## CHAPTER 4

# THEORETICAL DESCRIPTION OF INNER-SHELL IONISATION BY LIGHT CHARGED PARTICLES

4.

4.

4.

4.

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#### 4.1 INTRODUCTION

The plane-wave Born approximation (PWBA) and its recent improvements by Brandt and Lapicki (1979, 1981), known as the ECPSSR theory, are discussed in this chapter. The other major theoretical models for describing inner-shell ionisation are the semi-classical approximation (SCA) and the binary-encounter approximation (BEA). The ECPSSR theory has been chosen for comparison with the measured L-shell ionisation and x-ray production cross sections in this study (Chapter 6) instead of the SCA and the BEA. This approach has been followed because the ECPSSR model has been developed to a sufficient degree to allow detailed quantitative as well as qualitative comparison with the experimental data. The formulation of this theory by Brandt and Lapicki (1981) permits the major corrections to be included in the PWBA. In the case of the SCA and the BEA an equivalent readily accessible formulation to improve the calculated cross sections does not exist. However, both of these theories are reviewed in appendix A, not only for completeness but also because they can be closely related to the PWBA (Madison and Merzbacher 1975).

For the sake of brevity emphasis is placed on the discussion of the underlying assumptions on which the PWBA is based and the mathematical details have been omitted. References are, however, quoted which deal with the latter in great depth.

To explain exactly the mechanism of inelastic collisions between charged particles and atoms is a formidable task even for the simplest case and consequently the above-mentioned theories were introduced, which rely on substantial simplifications. The following two assumptions are common to these theoretical descriptions.

(i) The dynamics of the inner-shell ionisation process can be adequately treated in terms of an independent-electron model. The projectile and an independent inner-shell electron experience a Coulombic

interaction, the result of which is to cause a transition to the continuum. This inner-shell electron, therefore, plays the 'active' role with the projectile, while the other electrons of the target atom are mere 'spectators' of the collision. This assumption is consistent with most of the x-ray phenomena discussed in Chapter 2.

(ii) The collision which creates the single inner-shell vacancy is assumed to take place in a short time compared with the time taken for the occurrence of the subsequent atomic transition ( $\simeq 10^{-8}$ s) (Madison and Merzbacher 1975).

Protons, deuterons and alpha particles as projectiles with velocities less than the velocity of the inner-shell electron are considered in the present work.. In this collision regime, effects such as electron capture by the projectile and target-orbital contractions can be neglected (Brandt and Lapicki 1981 and McDaniel 1983).

In order to maintain consistency with the published literature cgs and atomic units are used throughout this chapter.

# 4.2 PLANE-WAVE BORN APPROXIMATION

The first quantum mechanical treatment of inner-shell ionisation by charged particles was based on the Born approximation (Born 1926). The interaction between the projectile and an inner-shell electron, which causes the electron to be ejected into the continuum, is Coulombic in nature and is treated in terms of the first order time-independent perturbation theory. The validity of such an approach is only ensured when the perturbing potential is small and since the magnitude of this potential depends on the charge of the projectile ( $Z_1$ ), incident particles with low atomic numbers such as protons and alpha particles are the most suitable for testing the predictions of this theory (Sarkadi 1983). The theory, therefore, holds for  $Z_1 << Z_2$  where  $Z_2$  is the atomic number of the target atom. This is the region of direct Coulomb ionisation (Madison and

Merzbacher 1975).

In the Born approximation the distortion of the wave function of the incoming particle by the inner-shell electron involved in the inelastic collision is assumed to be negligible and is, therefore, ignored. This is the primary assumption in the Born approximation (Madison and Merzbacher 1975). For an asymmetric collision between an incident partice of charge  $Z_1e$  and velocity  $v_1$  and a target atom with a nuclear charge of  $Z_2e$  the validity condition for the Born approximation is given by (Williams 1945 and Bohr 1948).

$$\frac{Z_1 Z_2 e^2}{R v_1} << 1$$
 4.1

This condition can be interpreted as the de Broglie wavelength being larger than the dimensions of the scattering field (Williams 1945).

The ionisation of the K-shell by light charged particle impact was treated non-relativistically by Henneberg (1933) who based his theoretical approach on the Born approximation. Henneberg (1933) replaced the initial and final wave functions of the incident particle by the product of two plane waves, that is

$$\exp\left(i\left(\underline{k_{i}} - \underline{k_{f}}\right), \underline{R}\right) \qquad 4.2$$

and  $\underline{k} = \frac{2\pi}{\lambda}$ 

where  $\hbar \underline{k}_i$  and  $\hbar \underline{k}_f$  are the initial and final momenta of the incident particle with a position vector  $\underline{R}$  and a wavelength  $\lambda$ . The momentum change suffered by the particle is then  $\hbar(\underline{k}_i - \underline{k}_f)$  or  $\hbar \underline{q}$  where  $\underline{q} = \underline{k}_i - \underline{k}_f$ . Plane waves can be used provided that the radii of the inner-shell electron orbits are large compared to the classical distance of closest approach for the projectile (Henneberg 1933). This approximation is known as the plane-wave Born approximation (PWBA) (Merzbacher and Lewis 1958 and Inokuti 1971). The assumption that the plane wave is not distorted by the inner-shell electron during the collision is justified if the inequality 4.1 is satisfied (Merzbacher and Lewis 1958).

During an inelastic collision between a charged particle and an heavy target atom an inner-shell vacancy can be created even at very low incident energies. However, atomic transitions caused by the collision are not detectable unless the relative energy of the collision partners is much greater than the electronic binding energies of the inner-shells involved. (Madison and Merzbacher 1975). A lower limit to the velocity of the incident particle is set by the inequality 4.1. For direct collisions in the region of a few MeV the velocity of the projectile is less than or comparable to the velocity of the inner-shell orbital electron (Madison and Merzbacher 1975). The present work deals with collisions in this 'near-adiabatic' region. It is convenient to employ the maximum energy transferrable (T<sub>m</sub>) to a free electron of mass, m, by a projectile of mass, M<sub>1</sub>, and energy, E, that is

$$T_m \simeq \frac{4m}{M_1} E$$
 4.3

to compare with the binding energy of the inner-shell electron (I)(Merz-bacher and Lewis 1958). As the collision becomes less adiabatic and  $T_m$  approaches I, inner-shell ionisation becomes increasingly probable and reaches a maximum when  $T_m$  is comparable to I.

The problem of representing the inner-shell electron, involved in the collision, by a suitable wave function is considered below. Initially this electron is in its ground state, 2s or 2p in the present context. The electron may undergo a transition into one of the continuum states if the inner-shell is ionised. The final state, therefore, represents the vacancy in the inner-shell and the electron emitted into the continuum. Provided that  $Z_1 \ll Z_2$  and that the charge on the incident particle is comparable to the value of the electronic charge (e) the inner-shell orbits are not polarised to any great extent, allowing the use of atomic wave functions of the unperturbed atom for the 'active' electron (Mott 1931 and Merzbacher and Lewis 1958).

Most of the calculations of inner-shell ionisation by charged particles have employed non-relativistic hydrogenic wave functions (Mott and Massey 1965) for the electron in its initial and final states (Henneberg 1933, Merzbacher and Lewis 1958, Khandelwal et al 1969, Choi et al 1973. Rice et al 1977, Benka and Kropf 1978 and Johnson et al 1979). These wave functions approximate the more realistic atomic wave functions such as the Hartree-Fock type (Madison and Merzbacher 1975). This approximation may be applied successfully provided that the 'screening' effects of the target atomic electrons are accounted for (Taulbjerg 1976). In multielectron atoms, the nuclear charge experienced by the active electron is reduced by the presence of other inner-shell electrons. A further effect of screening is the reduction of the binding energy of the inner-shell electrons caused by the presence of the less-tightly bound outer electrons. These two effects can be taken into account approximately by introducing simple modifications (Livingston and Bethe 1937). The 'inner' screening of the full nuclear charge  $(Z_2e)$  may be accounted for by reducing  $Z_2$ by an appropriate amount calculated by Slater (1930). For the complete L-shell the Slater value is 4.15, giving the effective nuclear charge  $(Z_{2L})$  felt by an L-shell electron as

$$Z_{21} = Z_2 - 4.15$$
 4.4

The 'outer' screening shifts the binding energy of the inner-shell without changing the wave function significantly in the vicinity of the inner-shell. This is taken into account by introducing a dimensionless quantity  $\theta_{L_1}$ (i = 1, 2, 3 and refers to the three L-subshells) known as the 'screening number' or the 'scaled binding energy'. It expresses the actual binding energy  $I_{L_1}$ , in terms of the hydrogenic binding energy,  $E_{L_1}$ , which is free from the effects of outer screening, that is,

$$\theta_{L\hat{1}} = \frac{I_{L\hat{1}}}{E_{L\hat{1}}}$$

$$4.5$$

Since

$$E_{2L} = Z_{2L}^{2} R_{\infty} / n_{L}^{2}$$
  

$$\theta_{Li} = \frac{n_{L}^{2} I_{Li}}{Z_{2L}^{2} R_{\infty}}$$
4.6

where  $n_L = 2$  is the principal quantum number for the L-shell and  $R_{\infty}$  is the K-shell ionisation energy of hydrogen (Rydberg) and has the value 13.6eV.  $\theta_{Li}$ , therefore, is a measure of the nonhydrogenic aspect of  $I_{Li}$ . Figure 4.1 shows the variation of  $\theta_{Li}$  with  $Z_2$ .  $\theta_{Li}$  was calculated from equation 4.6 and employing  $I_{Li}$  from Storm and Israel (1971). For the elements of interest in this study  $\theta_{Li}$  lies between 0.4 - 0.8.

The use of the PWBA, based on the above assumptions, for evaluating inner-shell ionisation cross sections for light positively charged particles has been discussed comprehensively by Merzbacher and Lewis (1958), Madison and Merzbacher (1975) and Briggs and Taulbjerg (1978). Here only the final results are quoted.

The L-shell ionisation cross section is expressed in terms of the dimensionless quantities, W, k and Q defined by

$$W = \frac{\varepsilon}{Z_{2L}^{2}R_{\infty}}$$
;  $k = a_{2}K$ ;  $Q = a_{2}^{2}q^{2}$  4.7

where  $\varepsilon$  is the energy transferred to the target atom as a result of the inelastic collision,  $a_2 = a_0/Z_{2L}$  is the K-shell radius of the target atom,  $a_0$  being the Bohr radius of hydrogen, K is the wave number of the hydrogenic wave function and q is the momentum transferred to the atom in units of  $\hbar$ . The energy transferred to the atom is

$$\varepsilon = T + I_{Li}$$

where T is the kinetic energy of the electron of mass, m, at infinity and equals  $\hbar^2 K^2/2m + V_{Li}$ . The potential,  $V_{Li}$ , represents the reduction in the binding energy of the L-shell electron due to the effects of outer screening and is given by



$$=\frac{Z_{2L}^{2}R_{\infty}}{n^{2}L}-I_{Li}$$

Substituting equation 4.9 into 4.8 gives

$$\varepsilon = \frac{\hbar^2 K^2}{2m} + \frac{Z_2^2 L R_{\infty}}{n_{\perp}^2}$$
 4.10

Using equation 4.7 W can be expressed as

$$W = k^2 + \frac{1}{n^2}$$
 4.11

In terms of the quantities defined by equation 4.7 the PWBA L<sub>i</sub>-subshell ionisation cross section,  $\sigma_{Li}$ , in the centre-of-mass system, for an electronic transition from an initially filled Li-subshell to a final state with an energy transfer  $\varepsilon$  can be expressed as (Merzbacher and Lewis 1958).

$$\sigma_{\text{Li}} = 8\pi Z_1^2 \left(\frac{e^2}{\hbar v}\right)^2 \frac{a_0^2}{Z_2^2 L} \int_{\text{Wmin}}^{\text{Wmax}} dW \int_{\text{Qmin}}^{\text{Qmax}} \frac{dQ}{Q^2} |Fw_{\text{Li}}(Q)|^2$$
4.12

where v is the relative velocity of incidence and  $F_{WLi}(Q)$  is known as the inelastic form factor for the collision. Expressions for  $F_{W_{Li}}(Q)$  can be found in Merzbacher and Lewis (1958), Choi et al (1973) and Benka and Kropf (1978). The velocity of the projectile (v<sub>1</sub>) can be expressed in terms of the velocity of the inner-shell electron (v<sub>2L</sub>) through the reduced or the scaled energy parameters, n<sub>L</sub>,

$$n_{L} = \left(\frac{v_{1}}{n_{L}v_{2L}}\right)^{2} = \frac{1}{Z_{2L}^{2}} \left(\frac{\hbar v_{1}}{e^{2}}\right)^{2}$$
 4.13

since  $v_{2L} = Z_{2L}e^2/n_L\hbar$ . Through  $n_L$ , sometimes referred to as the adiabaticity parameter, the energy of the projectile (E) in the laboratory frame enters the cross section calculations, that is,

$$n_{L} = \frac{m E}{M_1 Z_{2L}^2 R_{\infty}}$$

$$4.14$$

using  $v_1^2 = 2E/M_1$  and  $R_{\infty} = e^4m/2\hbar^2$ , where m is the mass of the electron. Employing  $n_L$  the ionisation cross section can be stated as (Choi et al 1973),

$$\sigma_{Li} = \frac{8\pi Z_1^2 a_0^2}{Z_{2L}^4 \eta_L} f_{Li} (\eta_L, \theta_{Li})$$
4.15

where

$$f_{Li} (n_L, \theta_{Li}) = \int_{W_{min}}^{W_{max}} dW \int_{Q_{min}}^{Q_{max}} |F_{W_{Li}} (Q)|^2 \frac{dQ}{Q^2}$$

$$4.16$$

The L<sub>i</sub>-subshell cross section can be obtained by evaluating the interals in equation 4.16 over the variables W and Q. These calculations have been performed for the L-shell by Choi et al (1973) and Benka and Kropf (1978). Choi et al (1973) have tabulated  $f_{Li}$  ( $n_L$ ,  $\theta_{Li}$ ) for bare charged particles such as protons and alpha particles and have restricted their calculations to 0.0018 <  $n_L$  < 7.0 and 0.24 <  $\theta_{Li}$  < 0.78. Benka and Kropf (1978), on the other hand, have concentrated on proton impact only and have extended their calculations to cover a larger range of proton energies and target elements. Their format is, however, slightly different to that of Choi et al (1973) and they have tabulated the 'reduced universal cross section',  $F_{Li}$  ( $n_L/\theta_{Li}^2$ ,  $\theta_{Li}$ ), defined by

$$\sigma_{Li} = \frac{8\pi Z_{1}^{2} a_{0}^{2}}{Z_{2L}^{4} \theta_{Li}} F_{Li} (n_{L}/\theta_{Li}^{2}, \theta_{Li})$$
 4.17

where

boly

$$F_{Li} = \begin{pmatrix} \frac{\theta_{Li}}{\eta_{L}} \end{pmatrix} f_{Li} (\eta_{L}, \theta_{Li})$$
4.18

Their calculations cover  $10^{-4} \le n_L/\theta^2_{Li} < 10^2$  and  $0.2 \le \theta_{Li} < 2.7$ . In terms of  $Z_2$  and E their tabulation covers all values with  $Z_2 \ge 10$  and proton energies of the order of  $10^{-6}$  to  $10^{4}$ MeV.

The more pronounced difference between the two tabulations concerns the integration limits of equation 4.16. These limits are obtained from the conservation of energy and momentum relations (Merbacher and Lewis 1958). Both the tabulations have used

$$V_{\min} = \frac{\theta_{Li}}{n_{L^2}}$$
 4.19

which is arrived at by substituting the minimum energy transfer  $\varepsilon_{min} = I_{Li}$ , obtained by setting T = 0 in equation 4.8, into equation 4.7. Choi et al

(1973) have approximated  $W_{max}$ , which corresponds to the maximum energy transferrable to the atom, by

$$W_{max} = \infty$$
 4.20

Benka and Kropf (1978) have replaced this by the exact integration limit

$$M_{\text{max}} = \frac{M_1}{m} \eta_L$$
 4.21

Limit 4.21 is obtained by setting  $\varepsilon_{max}$  equal to the maximum energy available for transfer to the target atom, which simply is the projectile energy before collision, E. This makes  $W_{max}$  dependent on the projectile mass,  $M_1$ , unlike the approximation used by Choi et al (1973) which clearly is independent of  $M_1$  (equation 4.20). The expression for  $Q_{min}$  can be derived from

$$\begin{split} &\hbar q_{\min} = \hbar k_{i} - \hbar k_{f} = \left[ 2M_{1}E \right]^{\frac{1}{2}} - \left[ 2M_{1}(E - \varepsilon) \right]^{\frac{1}{2}} \\ &\hbar^{2}q^{2}min = 2M_{1} \left[ E^{\frac{1}{2}} - (E - \varepsilon)^{\frac{1}{2}} \right]^{2} \\ &= 2M_{1}E \left[ 1 - \left( 1 - \frac{\varepsilon}{E} \right)^{\frac{1}{2}} \right]^{2} \\ \end{split}$$

$$\begin{aligned} &4.22 \\ &4.23 \end{aligned}$$

Using the binomial theorem 4.23 can be written as

$$\hbar^2 q^2 \min \simeq \frac{M_1 \varepsilon^2}{2E} \left(1 + \frac{\varepsilon}{2E}\right)$$

and if the energy loss,  $\varepsilon$ , of the projectile is smaller than the projectile energy, E, that is,  $\varepsilon \ll E$ ,

$$\hbar^2 q^2 \min \simeq \frac{M_1 \varepsilon^2}{2E} = \frac{\varepsilon^2}{V_1^2}$$
 4.24

In terms of the dimensionless quantities Q, W, and  $n_L$  the minimum momentum transfer may be expressed as

$$Q_{\min} = \frac{W^2}{4n_L}$$
 4.25

This expression for  $Q_{min}$  has been employed by Choi et al (1973) for their calculations. Benka and Kropf (1978) have retained the exact expression 4.23 in their calculations, which can be rearranged to

$$Q_{\min} = \left(\frac{M_1}{m}\right)^2 n_L \left[1 - \left(1 - \frac{m W}{M_1 n_L}\right)\right]^2$$
4.26

For the maximum momentum transfer we have

$$\hbar q_{max} = \hbar k_i + \hbar k_f$$

$$= [2M_1E]^{\frac{1}{2}} + [2M_1(E - \varepsilon)]^{\frac{1}{2}}$$
 4.27

$$\hbar^2 q^2 max = 2M_1 E \left[1 + \left(1 - \frac{\varepsilon}{E}\right)^{\frac{1}{2}}\right]^2$$
 4.28

Expanding the bracket term and since  $\varepsilon \ll E$  equation 4.28 can be approximated to

$$\hbar^2 q^2_{\text{max}} \simeq 8M_1 E \qquad 4.29$$

Merzbacher and Lewis (1958) have approximated  $q_{max} \simeq \infty$ , which they point out introduces no serious errors. Choi et al (1973) have also used this limit for  $Q_{max}$ , that is

$$Q_{\text{max}} = \infty$$
 4.30

Benka and Kropf (1978), however, have used the exact expression 4.28 for the maximum momentum transfer leading to

$$Q_{max} = \left(\frac{M_1}{m}\right)^2 \eta_L \left[1 + \left(1 - \frac{m}{M_1} \frac{W}{M_1}\right)^{\frac{1}{2}}\right]^2$$
 4.31

As a result of using the exact integration limits the cross section values for incident protons at low energies calculated by Benka and Kropf (1978) are considerably smaller than those of Choi et al (1973). For intermediate and high energies,  $\eta_L > 0.1$ , the cross sections agree to within 1% for all targets (Benka and Kropf 1978). In the present study, however,  $\eta_L$  is typically  $10^{-2}$  for protons and significant differences between the two tabulations exist at these energies. In the case of Au ( $Z_2 = 79$ ), for example, bombarded by 1.6MeV protons ( $\eta_L = 0.011$ ) the L<sub>1</sub> ionisation cross sections differ by about 7%.

Benka and Kropf (1978) have used the exact integration limits and as a result their tabulation has been employed in the present study to generate the cross sections for proton impact in preference to that of Choi et al (1973). For deutrons and alpha particles on the other hand, the latter tabulation was adopted since the values of Benka and Kropf (1978) are valid only for proton impact.

In pertinance to the expression 4.17 for the PWBA L-shell ionisation cross section several notable points can be made.

(i) The form factor  $Fw_{Li}$  (Q) is explicitly independent of the target charge  $Z_2$  (Madison and Merzbacher 1975) and consequently the cross section exhibits a universal behaviour for all targets and projectiles when expressed in the form

$$\frac{\theta_{\text{Li}}}{8\pi} \left( \frac{Z_{2\text{L}}^2}{Z_1} \right)^2 \frac{\sigma_{\text{Li}}}{a_0^2} = F_{\text{Li}} \left( n_{\text{L}} / \theta_{\text{Li}}^2, \theta_{\text{Li}} \right)$$
4.32

The form factor, for a given atomic transition, has large values for  $Q \simeq 1$  and then decreases rapidly as Q increases(Inokuti 1971). According to equation 4.25 Q<sub>min</sub> is large at low projectile velocities, and the dominant contribution to the cross section arises, therefore, from the lowest momentum transfers. The universal behaviour observed by plotting  $(\theta_{Li} Z_{2L}^4 \sigma_{Li})/(8\pi Z_1^2 a_0^2)$  versus  $n_L/\theta_{Li}^2$  is thus limited to the low velocity region where the projectile velocity is smaller than the inner-shell electron velocity,  $v_1 < v_{2L}$ . Expression 4.32 also exhibits  $Z_1^2$  scaling and thus permits cross sections to be determined for different projectiles ( $Z_1$ ) for given  $Z_2$  and E provided that  $\sigma_{Li}$  is known for a certain projectile. The validity of the universal property and that of  $Z_1^2$  scaling has attracted considerable experimental scrutiny (Madison and Merzbacher 1975, Chaturvedi et al 1975, Khan 1975, Button et al 1979 and Bhattacharya et al 1980) and reasonable qualitative agreement has been established.

- (ii) The inner-shell ionisation cross section for charged particles rises to a broad maximum at around  $\eta_L/\theta_{Li}^2 \approx 1$  or  $v_1 \approx v_{2L}$  for the L-shell. Beyond this 'velocity matching' peak the cross section falls off.
- (iii) Any divergence from the universal behaviour may be indicative of the inadequacies of the PWBA model. These might include the unsuitability of the unperturbed hydrogenic wave functions, the single-independent

electron assumption or more seriously the approximate nature of the Born model itself (Madison and Merzbacher 1975, McGuire and Macdonald 1975 and Chen et al 1982). Improvements of the PWBA theory are discussed in the next section.

- At low projectile velocities the contribution to the ionisation cross (iv) section is predominantly from collisions which transfer energies close to zero to the electron. The cross section is sensitive to the high-momentum tail of the momentum distribution of the initial-state wave functions. In other words, the ionisation of the inner-shell occurs most probably when the particle penetrates deep inside the shell (Madison and Merzbacher 1975 and Montenegro and de Pinho 1982a). At low projectile velocities, therefore, the ionisation cross section for the 2p states rises smoothly with increasing collision energy in qualitative agreement with the momentum wave functions associated with these states. The ionisation cross section for the 2s state on the other hand displays a pronounced 'knee' in the neighbourhood of  $n_{L}/\theta_{2Li}^{2} \simeq 0.01$ , a feature which is a consequence of the radial node in the wave function of this state, either in the coordinate or the momentum representation.
- (v) Provided that the target atoms are not light or highly ionised before collision, the contribution of the excitation of inner-shell electrons to unoccupied discrete bound levels, as a result of a heavy charged particle impact, to the total vacancy production cross section.is negligible and may be ignored (Madison and Merzbacher 1975).
- (vi) The validity condition for the PWBA, expressed in the form of the inequality 4.1, has been recognised to be over-restrictive for many ion-atom collisions (Merzbacher and Lewis 1958 and Briggs and Taulbjerg 1978), particularly in the case of total ionisation cross section. The Born approximation applied to the inner electron-

projectile interaction may still be valid in certain regions where 4.1 is violated. This arises in slow collisions but provided  $Z_1 << Z_2$  the effect of the incident particle may be treated as a small perturbation, authenticating the use of the plane-wave Born approximation. The validity of the perturbation theory, therefore, critically depends on the magnitudes of the nuclear charges of the projectile and of the target atom (Briggs and Taulbjerg 1978). CORRECTIONS TO THE PLANE-WAVE BORN APPROXIMATION - THE ECPSSR THEORY

4.3

The plane-wave Born approximation has been exceedingly successful in describing the qualitative behaviour of inner-shell ionisation cross sections with respect to the incident particle energy. As far as predicting the numerical values of the cross sections or the projectile velocity dependence of the cross sections the PWBA model falls far short and consistently over estimates in the  $v_1 < v_{21}$  region (Brandt and Lapicki 1974). This has been substantiated by the significant amount of experimental cross section measurements performed at various laboratores (Busch et al 1973, Datz et al 1974, Gray et al 1975, Chen 1977, Khan et al 1978, Button et al 1979, Bhattacharya et al 1980, Sokhi and Crumpton 1981, Cohen 1981 and Bhattacharya 1982). However, it is not surprising that this is the case since the PWBA is only the first step of a perturbation expansion using plane waves and unperturbed initial-state hydrogenic wave functions to describe the projectile and the inner-shell electron respectively. The obvious improvement of expanding the Born series to the second order term is usually avoided because of the mathematical complexity (Madison and Merabacher 1975). Some work has been done using more sophisticated atomic wave functions such as the Dirac -Hartree-Slater wave functions and agreement with experimental data has been improved (Chen et al 1982). Brandt and his co-workers have followed a phenomenological approach to the collision problem and have developed the ECPSSR theory in an attempt to

explain the large descrepenceis between the PWBA predictions and experiment.

The ECPSSR theory is a result of many noteworthy contributions made to the theory of inner-shell ionisation by charged particles by Brandt and his collaborators over the past decade (Brandt et al 1966, Basbas et al 1973a, Basbas et al 1973b, Brandt and Lapicki 1974, Basbas et al 1978, Brandt and Lapicki 1979 and Brandt and Lapicki 1981). The theory accounts for the effects of the kinetic energy loss (E) of the incident particle in the ionisation process, the Coulomb deflection (C) of the projectile in the field of the target nucleus, the influence of the projectile on the innershell electron orbits (the binding energy and polarisation effects) in terms of the perturbed stationary states (PSS) and the relativistic effects (R) of the inner-shell electrons of high  $Z_2$  elements on the probability of inner-shell ionisation by non-relativistic charged particles. Each of these effects and the expressions derived by Brandt and Lapicki (1979) for including these effects in the PWBA are now considered.

4.3.1 Relativistic Effect

A relativistic description of the inner-shell electrons of heavy elements is required instead of the simple hydrogenic picture because (Choi 1971)

- (i) in the vicinity of the atomic nucleus the relativistic bound-state wave functions are larger in magnitude than the non-relativistics, and
- (ii) the spin-orbit slitting of the inner electronic states, such as the splitting of the 2p state into  $2p_{1/2}$  and  $2p_{3/2}$ , becomes significantly large for heavy elements, and the difference in the binding energies of these subshells has a non-trivial affect on the calculations of inner-shell ionisation cross sections.

Qualitatively this effect may be understood by recognising that at

relativistic velocities the electron mass increases and as a result the maximum energy transfer to an electron increases making ionisation more probable (Paul 1980).

Jamnik and Zupancic (1957) applied hydrogenic Dirac wave functions for K-shell ionisation in the Born approximation. Similar calculations were carried out by Choi (1971) for the L-shell and highlighted the necessity of relativistic corrections for medium-heavy and heavy target elements. Mukoyama and Sarkadi (1981, 1982a) have employed an analogous relativistic procedure to that adopted by Choi (1981) for L-shell ionisation by slow protons (Mukoyama and Sarkadi 1983a) and alpha particles (Mukoyama and Sarkadi 1983b) and in addition have applied Coulomb and binding energy correction as developed by Brandt and Lapicki (1974). After comparison with experimental data they emphasise the need of relativistic corrections for low-energy projectiles ionising heavy target elements. Such calculations are complicated however, and other methods have been proposed which are less involved numerically. Merzbacher and Lewis (1958), for instance, followed the method of Honl (1933) and proposed that non-relativistic screened hydrogenic wave functions may still be used for calculating the cross section but taking into account the fact that the relativistic ideal ionisation potential without outer screening (Eli for the L-shell) is larger than the non-relativistic potential, thus reducing  $\theta_{1,i}$  (equation 4.5 and 4.6). Hardt and Watson (1973) have suggested that the velocity of the inner-shell electron should be reduced and Berinde et al (1978) studying K-shell ionisation by protons have modified the K-shell radius to correct for the relativistic effects. Brandt and Lapicki (1979) have, however, pointed out that these approaches only explain experimental measurements when the incident projectile and the electron velocity are comparable. These approaches and that of Brandt and Lapicki (1979), which will be discussed below, entail using either relativistic wave functions or

modifying parameters used in the PWBA and as a consequence yield cross sections which do not exhibit the scaling behaviour predicted by the nonrelativistic treatement (Madison and Merzbacher 1975 and Mukoyama and Sarkadi 1982b). For low energy charged particles (below 1MeV for protons) Mukoyama and Sarkadi (1982b) have derived an approximate relativistic correction for L-shell ionisation following a method developed by Amundsen et al (1976) for K-shell ionisation. The relativistic cross section is simply obtained by multiplying this correction factor to the non-relativistic PWBA cross section and as a result the scaling behaviour is retained.

Before discussing Brandt and Lapicki's (1979) approach the central parameters in their theory are first defined. Consider an inelastic collision in which a target atom of mass,  $M_2$ , is ionised in its L-shell by a projectile of mass,  $M_1$ , and velocity,  $v_1$ . The minimum momentum transfer hqmin is given by equation 4.24. For collisions where the projectile energy E is much larger than the binding energy  $\hbar \omega_{21}$  then

$$q_{\min} \simeq \frac{\omega_{21}}{v_1}$$
 4.3

Impact parameters which contribute most to the ionisation have values  $\simeq q_{\min}^{-1}$  (or  $v_1/\omega_{2L}$ ) (Bang and Hansteen 1959). The condition for deep penetration of the inner-shell (L-shell in this case) is

$$q_{min}^{-1} << a_{2L}$$
  
 $v_{1} << \omega_{21} a_{21}$ 
  
4.34

or in terms of  $\theta_{Li}$  and using atomic units,

or

$$v_1 << \frac{1}{2} \theta_{1,j} v_{2,j}$$
 4.35

A useful way of distinguishing slow and fast collisions is to compare the time it takes for the projectile to transverse the target L-shell (characteristic collision time)  $\simeq a_{2L}/v_1$  with the characteristic time of the target L-shell electron  $n_L/\omega_{2L}$ . The condition  $a_{2L}/v_1 >> n_L/\omega_{2L}$  or  $q_{min}^{-1} << a_{2L}/n_L$  defines slow collisions and leads to the central dimension-

less parameter of the theory,  $\xi_{Li}$ , known as the 'reduced velocity parameter' (Brandt and Lapicki 1979)

$$F_{Li} = \frac{n_L}{q_{min}a_{2L}}$$
4.36

Since, in atomic units  $a_{2L} = n_L^2/Z_{2L}$  and the velocity of the L-shell electron  $v_{2L} = Z_{2L}/n_L$ , then  $q_{min} \approx \frac{\theta_{Li} v_{2L}}{2v_1}$  4.37

and  $\xi_{l,i}$  can be written as

$$\xi_{Li} = \frac{v_i}{\frac{1}{2}\Theta_{Li}v_{2L}}$$
4.38

This variable differentiates between slow collisions, where  $\xi_{Li} < 1$ and fast collisions, where  $\xi_{Li} > 1$ . The velocity of the projectile  $v_1$  can be expressed as

$$v_1 = (Z_2 n_L)^{\frac{1}{2}}$$
 4.39

In the low velocity region,  $\xi_{Li} << 1$ , the ionisation cross section is proportional to the fourth power of

$$T_{\rm m} = 2mv_1^2 = m\theta_{\rm Li}\omega_{\rm 2L}\xi_{\rm Li}^2 \qquad 4.40$$

(using equation 4.38 and substituting for  $v_{2L} = Z_{2L}/n_L$ )(Huus et al 1956). Instead of setting m to unity, Brandt and Lapicki (1979) have introduced a relativistic electron mass,  $m_{Li}^R$  ( $\xi_{Li}$ ), using the virial theorem (Rose and Welton 1952) for a relativistic electron in a central potential of the form  $Z_{2L}/r$  at a distance r from the target nucleus and is given by

$$m_{Li}^{R}(\xi_{Li}) \simeq (1 + 1.1y_{Li}^{2})^{\frac{1}{2}} + y_{Li}$$
 4.41

where

 $y_{L_1} = \frac{0.40(Z_{2L}/c)^2}{n_L \xi_{L_1}}$ 

4.42

and

$$y_{L_{2,3}} = \frac{0.15 (Z_{2L}/c)^2}{\xi_{L_{2,3}}}$$

In accordance with equation 4.40  $\xi_{Li}$  has to be transformed to  $\left[m_{Li}^{R}\left[\xi_{Li}\right]\right]^{\frac{1}{2}}\xi_{Li}$ .  $n_{L}$  may be expressed in terms of  $\theta_{Li}$  and  $\xi_{Li}$  $n_{L} = \left(\frac{\theta_{Li}\xi_{Li}}{2n_{L}}\right)^{2}$ 4.43

and substituting the relativistic  $\xi_{Li}$  into 4,43 allows  $n_L/\theta_{Li}^2$  to be transformed to its relativistic counterpart,

$$(n_{L}/\theta_{Li}^{2})^{R} = \left[ \left( \frac{(M_{Li}^{R}(\xi_{Li}))^{\frac{1}{2}} \xi_{Li}}{2n_{L}} \right]^{2} + 4.44 \right]$$

where  $n_L = 2$  (for the L-shell). The relativistic PWBA L-subshell ionisation cross section,  $\sigma_{Li}^{PWBAR}$ , can now be calculated from

$$\sigma_{Li}^{PWBAR} = \sigma_{Li}^{PWBAR} \left( \left( \frac{\eta_L}{\theta_L^2 i} \right)^R, \theta_{Li} \right)$$
 4.45

using equation 4.17 or from

$$\sigma_{Li}^{PWBAR} = \sigma_{Li}^{PWBA} (\eta_{L}^{R}, \theta_{Li})$$
 4.46

where

$$n_{L}^{R} = m_{Li}^{R} (\xi_{Li}) n_{L}$$
4.47

and using equation 4.15. Cross sections calculated from these expressions agree closely with those obtained by using relativistic wave functions (Choi 1971).

The effect of the relativistic correction may be illustrated by plotting  $\sigma_{Li}^{PWBAR}/\sigma_{Li}^{PWBA}$  ratio versus the projectile energy. This has been done for proton impact on gold and is shown in figure 4.2. The ionisation cross sections were calculated for expressions 4.17 and 4.45 and using the tables of Benka and Kropf (1978). The relativistic correction affects the L<sub>1</sub> subshell more than the L<sub>2</sub> and L<sub>3</sub>. This is because for heavy elements (Z<sub>2</sub>) the relativistic bound-state wave functions are larger near the atomic nucleus than the non-relativistic ones and consequently the  $2S_{\frac{1}{2}}$ state is influenced much more than the  $2p_{\frac{1}{2}}$  and the  $2p_{\frac{3}{2}}$  (Justiniano et al 1980). In the low velocity region the presence of the radial node in the 2s wave functions increases the L<sub>1</sub> ionisation cross section and thus



Relativistic effect for gold  $(Z_2 = 79)$  bombarded by protons. The L<sub>i</sub> subshell ionisation cross sections were calculated using equations 4.17 and 4.45 and tables of Benka and Kropf (1978). Figure 4.2

complicates the shape of the ratio (figure 4.2).

4.3.2 Polarisation and Binding Energy Effects

The inner-electron states experience perturbations caused by the presence of the charged particle. These perturbations affect the ionisation probability in a manner which depends on whether the impact parameter is less or greater than the inner-shell radius ( $a_{2L}$  for the L-shell). In the regime where  $v_1 \ll v_{2L}$ , at impact parameters less than  $a_{2L}$ , the ionisation cross section is reduced since the binding energy of the target electron is increased. At intermediate and high particle velocities impact parameters larger than the inner-shell radius contribute the most to the ionisation cross section. When the projectile is traversing 'outside' the shell, it polarises the shell, thus, reducing the binding energy of the electron (Brandt and Lapicki 1979). Both these effects have been accounted for in terms of the perturbed-stationary-state (PSS) theory (Basbas et al 1973b and Brandt and Lapicki 1979). The polarisation factor for the L-shell, calculated by Brandt and Lapicki (1979), is given by

$$P_{Li} = 1 - \left(\frac{2Z_1}{Z_2 L^{\theta} L_i}\right) h_{Li} (\xi_{Li}, C_{Li})$$
 4.48

with

an

$$h_{Li}(\xi_{Li}; C_{Li}) = \left(\frac{2n_L}{\theta_{Li}\xi_{Li}^3}\right) I \left(\frac{C_{Li}n_L}{\xi_{Li}}\right)$$
 4.49

where  $C_{L_1} = 3/2$  and  $C_{L_{2,3}} = 5/4$  and the polarisation function  $I(C_{L_1}n_L/\xi_{L_1})$  is given by (Basbas et al 1978)

$$I(x) = \frac{3\pi}{4} (\ln \frac{1}{x^2} - 1) \text{ for } 0 < x \le 0.035$$
  
d 
$$I(x) = e^{-2x} (0.031 + 0.210x^{\frac{1}{2}} + 0.005x - 0.069x^{\frac{3}{2}} + 0.324x^2)^{-1}$$
 4.50

for 
$$0.035 < x \le 3.1$$

where  $x = C_{Li}n_L/\xi_{Li}$ . For x > 3.1 the polarisation function may be neglected. The binding energy factor, accounting for the increased binding energy of the inner-shell electron is given by

$$\varepsilon_{Li}^{B} = 1 + \left(\frac{2Z_{1}}{Z_{2}L^{\theta}L_{i}}\right) g_{Li} (\xi_{Li}; C_{Li})$$

$$4.51$$

The rather lengthy expressions for  $g_{Li}$  ( $\xi_{Li}$ ;  $C_{Li}$ ) have been stated by Brandt and Lapicki (1979). The polarisation and the binding energy factors may be combined to give a perturbed-stationary-state factor  $\zeta_{Li}$  for  $\theta_{Li}$ which takes into account the polarisation and the binding energy effects on the ionisation cross section, that is,

$$\xi_{Li} = 1 + \left(\frac{2Z_{1}}{Z_{2L}\theta_{Li}}\right) \left[g_{Li} (\xi_{Li}; C_{Li}) - h_{Li} (\xi_{Li}; C_{Li})\right]$$
4.52

The PSS cross section for direct ionisation in terms of the PWBA can be obtained by transforming  $\theta_{Li}$  to  $\zeta_{Li}\theta_{Li}$  and  $\eta_L/\theta_{Li}^2$  to  $(\xi_{Li}/2n_L\zeta_{Li})^2$ , thus,  $\sigma_{Li}^{PSS} = \sigma_{Li}^{PWBA} ((\xi_{Li}/2n_L\zeta_{Li})^2, \zeta_{Li}\theta_{Li})$  4.53

In the collision regimes under study in this work the polarisation effect does not play a significant role and the PSS factor is dominated by the contribution of the binding energy effect.

The PSS effect is very similar for the L<sub>2</sub> and L<sub>3</sub> subshells and is demonstrated in figure 4.3 which shows the ratio,  $\sigma_{Li}^{PSS}/\sigma_{Li}^{PWBA}$ , as a function of proton energy for gold. The  $\sigma_{Li}^{PSS}$  cross sections were evaluated using equation 4.53 and the tabulation of Benka and Kropf (1978). The L<sub>1</sub> ionisation cross sections for protons increases in the low velocity region exhibiting a 'knee' as mentioned in section 4.2, and is less sensitive to the PSS effect. This behaviour is analogous to that shown in figure 4.2 which illustrated the relativistic effect.

The relativistic correction can be incorporated by introducing  $\xi_{Li}/\xi_{Li}$ into equation 4.41 and 4.42 to yield the relativistic reduced velocity, that is,

$$\xi_{Li}^{R} = \left[ m_{Li}^{R} \left( \xi_{Li} / \zeta_{Li} \right) \right]^{\frac{1}{2}} \xi_{Li}$$
 4.54

To obtain the PSS cross section with relativistic correction  $(\sigma_{Li}^{PSSR})$  $n_{L}/\theta_{Li}^{2}$  in equation 4.17 has to be replaced by  $(\xi_{Li}^{R}/2n_{L}\zeta_{Li})^{2}$ , thus,



The  $L_1$  subshell ionisation cross sections were calculated using equations 4.17 The perturbed stationary-state effect for proton impact on gold  $(Z_2 = 79)$ . and 4.53 and tables of Benka and Kropf (1978). Figure 4.3

$\sigma_{Li}^{PSSR} = \sigma_{Li}^{PWBA} ((\xi_{Li}^{R}/2n_{L}\zeta_{Li})^{2}, \zeta_{Li} \theta_{Li})$	4.55
or $\eta_L$ in equation 4.15 has to be replaced by $\eta_L^R/\zeta_{Li}^2$ , thus	
$\sigma_{Li}^{PSSR} = \sigma_{Li}^{PWBA} (n_L^R / {\zeta_{Li}}^2, {\zeta_{Li}}^{\theta} L_i)$	4.56

#### 4.3.3 Coulomb Deflection Effect

The PWBA description neglects the effects of the Coulomb field of the target nucleus on the incoming bare nucleus. The projectile suffers a deviation from its incident path and retardation because of the internuclear repulsion. Both of these effects are collectively referred to as the Coulomb deflection effect (Brandt and Lapicki 1979) and reduce the ionisation cross section. The PWBA predicts that the inner-shell ionisation cross section for incident isotopes, such as protons and deutrons, of the same velocity are numerically equal. Brandt et al (1966) and Shima et al (1971) have, however, demonstrated experimentally to the contrary that the cross sections infact disagree markedly, especially at low projectile velocities. This 'isotope effect' arises because of the Coulomb deflection of the projectile and is explained by the fact that the degree of deflection is dependent on the projectile mass. (Bang and Hansteen 1959 and Brandt et al 1966). A simple multiplicative Coulomb factor has been derived by Brandt et al (1974, 1979), which, in terms of the half-distance of closest approach in a head-on collision,

d =  $Z_1Z_2/Mv_1^2$  with the reduced mass M =  $(M_1^{-1} + M_2^{-1})^{-1}$ ,  $q_{min}$  and  $\zeta_{Li}$  is given by

$$C_{Li} (dq_{min}\zeta_{Li}) = \frac{exp(-\pi dq_{min}\zeta_{Li})}{1 + \pi dq_{min}\zeta_{Li}/(9 + 2\ell)}$$

$$4.57$$

where  $M_1$  and  $M_2$  are the masses of the projectile and the target nucleus respectively,  $q_{min}$  is evaluated using equations 4.37 and 4.39, the PSS factor  $\zeta_{Li}$  is determined from equation 4.52 and  $\ell$  is the orbital quantum number and has the values,  $\ell = 0$  for  $L_1$  and  $\ell = 1$  for  $L_2$  and  $L_3$  subshells. This Coulomb factor has been extracted from the formulae of Bang and Hansteen (1959), who employed the semi-classical approximation (see Appendix A) with straight-line and hyperbolic trajectories, by Brandt and his co-workers following the analytical approach of Amundsen (1977a). A fully quantum-mechanical treatment using Coulomb wave functions in the frame-work of the Born approximation has been given by Lapicki and Losonsky (1979). The Coulomb factor is defined as the ratio of the Coulomb to plane-wave Born cross sections and is derived for any inelastic collision in which the particle moves with a low velocity and suffers relatively small loss of its incident energy. Lapicki and Losonsky (1979) have, however, indicated that for slow collisions which occur at impact parameters comparable to dequation 4.57 is adequate for determining the correction factor. The L-subshell ionisation cross section corrected for Coulomb deflection, PSS, and relativistic effects,  $\sigma_{\rm Li}^{\rm CPSSR}$  is given by

$$\sigma_{Li}^{CPSSR} = C_{Li}(dq_{min}\xi_{Li})\sigma_{Li}^{PSSR}$$
 4.58

 $\sigma_{Li}^{PSSR}$  may be evaluated using equation 4.55 or 4.56. 4.3.4 Energy Loss Effect

A comparison of the CPSSR theory with the published K and L-shell experimental data for protons and deuterons was performed by Brandt and Lapicki (1979) who found that on average the agreement was to within 30% which is comparable to the uncertainties associated with experiment measurements. Further analysis by the same authors showed a statistically significant disagreement between the theory and experiment at low projectile velocities ( $\xi < 1$ ). The extent to which this discrepency may be explained by the finite energy loss suffered by the projectiles in the event of innershell ionisation has been investigated analytically by Brandt and Lapicki (1981). These authors have incorporated the minimum fractional energy loss of the projectile during inner-shell ionisation, L-shell in the present case

and denoted by  $\Delta_{Li}$ , in the minimum and the maximum momentum transfers (see expressions 4.23 and 4.28 where the energy loss is denoted by  $\varepsilon$ ). A multiplicative factor  $f_{li}(Z_{li})$  defined by

$$\sigma_{Li}^{EPWBA} = f_{Li}(Z_{Li})\sigma_{Li}^{PWBA}$$
4.59

has been derived by Brandt and Lapicki (1981) where  $\sigma_{Li}^{EPWBA}$  is the PWBA cross section corrected for the projectile energy loss. The energy loss correction is given by

$$f_{Li}(Z_{Li}) = 2^{-\nu}(\nu - 1)^{-1} \left[ (\nu Z_{Li} - 1)(1 + Z_{Li})^{\nu} + (\nu Z_{Li} + 1)(1 - Z_{Li})^{\nu} \right]$$

$$4.60$$

where the argument  $Z_{Li}$  is

$$Z_{Li} = (1 - \Delta_{Li})^{\frac{1}{2}}$$
 4.61

and v = 9 for L<sub>1</sub> and v = 11 for L<sub>2</sub> and L<sub>3</sub> subshells.

The energy loss correction varies smoothly with increasing projectile energy and ranges from about 5% at low energies to less than 2% at high energies for the collision systems under study.

The argument of the Coulomb deflection factor (equation 4.57) in the presence of projectile energy loss must be modified to take into account the energy loss effect. The Coulomb deflection factor is now given by

$$C_{Li}(x_{Li}) = \frac{\exp(-\pi x_{Li})}{1 + \pi x_{Li}/(9 + 2\ell)}$$
 4.62

with 
$$x_{Li} = \frac{2dq_{min}\zeta_{Li}}{Z_{Li}(1+Z_{Li})}$$
 4.63

The Coulomb deflection factor,  $C_{Li}(x_{Li})$ , is illustrated in figure 4.4 for protons, deutrons and alpha particle impact on gold.  $C_{Li}(x_{Li})$  was calculated using equation 4.62. The figure shows the deflection factor for the L<sub>1</sub> and L<sub>3</sub> subshells. The behaviour of  $C_{Li}(x_{Li})$  for the L<sub>2</sub> subshell is very similar to that of L<sub>3</sub> and thus has been omitted from figure 4.4 for clarity. The importance of this correction at low impact energies and for





heavier charged particles is clearly evident from this figure.

Incorporating the PSS factor  $\zeta_{Li}$  into the argument of the energy loss function,  $Z_{li}$  can now be defined as

$$Z_{Li}^{2} = 1 - \zeta_{Li} \Delta_{Li}$$
$$= 1 - \frac{4}{M\zeta_{Li} \theta_{Li}} \left(\frac{\zeta_{Li}}{\zeta_{Li}}\right)^{2}$$
4.64

where M is the reduced mass. The ionisation cross section predicted by the ECPSSR theory (E denoting the energy loss effect) is calculated from  $\sigma_{Li}^{ECPSSR} = C_{Li} \left[ \frac{2dq_{min}\zeta_{Li}}{Z_{Li}(1 + Z_{Li})} \right] f_{Li} (Z_{Li}) \sigma_{Li}^{PSSR} 4.65$ 

The L<sub>2</sub> and L<sub>3</sub> subshells are affected the most by incorporating the total ECPSSR effect into the PWBA cross sections. This is demonstrated in figure 4.5 which shows a plot of  $\sigma_{Li}^{ECPSSR}/\sigma_{Li}^{PWBA}$  ratio for proton impact on gold. The ECPSSR ionisation cross sections were calculated using equation 4.65 and tables of Benka and Kropf (1978). In the case of the L<sub>1</sub> state the relativistic effect compensates to a certain extent the PSS and the Coulomb deflection effects and as a result the total ECPSSR affect on L<sub>1</sub> is somewhat reduced.

A systematic comparison between the predictions of the ECPSSR theory and experimental K-shell ionisation cross sections for proton impact has been made by Brandt and Lapicki (1981). An agreement to within 10% has been achieved between the theory and experiment. A detailed comparison with L-shell data, however, has yet to be performed in any substantial way. Nevertheless, at these levels of correlation it would now be possible to detect inadequacies of the atomic wave functions employed in the theoretical treatment and whether significant improvements can be achieved by using more realistic atomic wave functions (Brandt and Lapicki 1981). One of the aims of this study is to make a detailed comparison of experimentally determined Li-subshell ionisation and x-ray production cross sections for protons, deutrons and alpha particles incident on medium and high Z<sub>2</sub> elements with





the ECPSSR predictions.

## 4.4 INNER-SHELL ALIGNMENT BY CHARGED PARTICLE IMPACT

Emission of collisionally induced inner-shell x-rays have been shown to be non-isotropic for transitions to subshells with total angular momentum  $j > \frac{1}{2}$  (Mehlhorn 1968). In the case of L-shell ionisations the anisotropy of x-rays resulting from transitions to the  $L_3$  (2p  $_{3/2}$ ) subshell has been demonstrated by Jitschin et al (1979) for proton impact on heavy atoms. This is due to the alignment of inner-shell vacancies created when an unpolarised beam of charged particles impinges upon unpolarised target atoms. The vacancies retain information regarding the incident direction of the beam and consequently the x-rays are emitted at an angle which reflects the degree of alignment of the inner-subshell. The alignment effect is understood in terms of the magnetic substates associated with the inner-shells. Alignment of an inner-subshell such as the L3, reflects the different vacancy population of the magnetic substates (Jitschin et al 1979). Experimental measurement of inner-shell ionisation cross sections, however, involve an incoherent sum of magnetic substate populations (Rosel et al 1982). Study of alignment effects, therefore, provides complementary information to the cross section measurements for testing inner-shell theories (Sarkadi 1983). This fact has instigated the considerable work being done in this area (Jitschin et al 1979, Palinkas et al 1981, Barros Leite et al 1982, Jitschin et al 1982Land Rosel et al 1982). Cleff (1982) has provided a comprehensive review of the subject.

The anisotropy of the emitted x-rays can be studied by measuring the x-ray yield at different angles from the incident beam axis. From these measurements the degree of polarisation (P) of the x-rays can be determined. P is defined by the expression (Berezhko and Kabachnik 1977)

 $I(\theta) = I(90^{\circ}) (1 - P\cos^2\theta)$  4.66

where  $I(\theta)$  is the intensity of the dipole characteristic radiation at angle

 $\theta$  to the direction of the beam. Energy dependence of the polarisation of emitted x-rays, resulting from vacancies in the L<sub>3</sub> subshell, has been established by Jitschin et al (1979) for proton impact and by Palinkas et al (1980) for helium impact.

Of all the transitions to the L<sub>3</sub> subshell the LL x-rays exhibit the most anisotropy, P = +7% for IMeV protons impact on  $Dy(Z_2 = 66)$ (Jitschin et al 1979). The other major x-ray transitions, the L $\alpha_1$ , 2 and L $\beta_2$ , 15 show relatively small anisotropy (Jitschin et al 1979 and 1982a). This alignment phenomenon explains why some experimentalists have obtained x-ray production cross section ratios of L $\alpha$  and L $\ell$  transitions for charged particle impact which are energy-dependent (Busch et al 1973, Tawara et al 1974, Tawara et al 1975 and Kamiya et al 1979). This is in contradiction to the prediction of the PWBA dicussed in section 4.2 which does not take into account the alignment of the subshells and, therefore, predicts a constant value of the ratio.

# CHAPTER 5 EXPERIMENTAL APPARATUS AND PROCEDURE

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#### 5.1 INTRODUCTION

The various aspects of the aparatus and the measuring techniques, employed for determining L shell x-ray production and ionisation cross sections, are explained in this chapter. Major features of the experimental arrangement for L x-ray yield measurements are described. Further details are, however, contained in Khan (1975) and Saied (1981). Procedure and results of the x-ray detector efficiency and target thickness measurements are presented. The chapter also discusses the experimental precision of the measured cross section values. The final section is addressed to the method employed for calculating theoretical ECPSSR cross sections required for comparison with the experimental data.

#### 5.2 EXPERIMENTAL APPARATUS

The main components of the experimental arrangement employed in this study, are described in this section in such a way so as to trace the path of the particle beam from the accelerator right down into the scattering chamber where it encounters a fixed target. With this in mind the experimental apparatus may be broadly classified into the following:

- (i) The Dynamitron.
- (ii) Beam transport and experimental line.
- (iii) Scattering chamber.
- (iv) Target assembly.

Important features of each of these, pertinent to the experimental work, are highlighted in the forthcoming sub-sections.

5.2.1 The Dynamitron

The charged particles under study were accelerated to energies in the range 1-3 MeV using the Dynamitron accelerator situated at the Radiation Centre, University of Birmingham. The accelerator is a

variable-energy potential-drop machine capable of terminal potentials from about 0.6 to 3MV. It is powered by a radiofrequency oscillator operating at 130 kHz. Sixty-four rectifier modules, arranged in a vertical chain from the base of the machine to the terminal, rectify the radiofrequency and produce the d.c. potential at the terminal.

The Dynamitron can be operated in a negative mode to accelerate electrons or in a positive mode to accelerate singly charged positive light ions, as in the present case. In the positive mode beam currents from about lnA to 2mA are available.

The positive ions, employed in the collision experiments, are produced in a duoplasmatron ion source (Radiation Dynamics, Inc, 1967). Hydrogen, deuteruim and helium gases are used for producing protons, deuterons and helium (He<sup>+</sup>) particles respectively. Ions of mass-one, two and three (protons only) are available and particles of the required mass may be selected by adjusting the potential needed to extract the ion from the source. Mass one ions were employed in the present investigation. With regard to the He<sup>+</sup> particle the single remaining electron can be assumed to be stripped off the ion and lost to the target medium immediately after striking the target. This assumption is valid provided that the velocity of the projectile is greater than the mean velocity of its bound electrons (Brandt 1981 and see section 3.2). In the impact energy range of interest this assumption holds true and the incident He<sup>+</sup> ion may be treated as an alpha (He<sup>2+</sup>) particle in the context of inner-shell ionisation. As a result the helium ion is simply referred to as an alpha particle in this thesis.

The output voltage at the terminal is measured on a digital voltmeter (DVM) by drawing d.c. current through a high voltage potential divider resistor board with a total resistance of  $10^{10}\Omega$ . The output
voltage is stabilised by an auto-regulator which compares the potential divider output with a variable reference voltage and compensates for any change in the terminal voltage (Radiation Dynamics, Inc 1967). The DVM readings can be translated into beam energy by calibrating the DVM with well-known nuclear reactions (Weaver 1976). A polynomial of the form

$$I = \frac{3}{100} a_i E^i$$
 5.1

where V is the DVM reading,  $a_i$  are constants and E is the particle energy, is fitted to the measured data. The precision of the measurements range from 0.7% at IMeV to 0.3% at 3MeV. Since the inner-shell ionisation cross sections are approximately proportional to E<sup>4</sup> (Merzbacher and Lewis 1958) the effect of these uncertainties is to make the measured ionisation cross sections uncertain by about 1.2% to 2.8%. Duration of x-ray yield measurements at a particular beam energy lasted upto 30 minutes. Variation of the beam energy during this time was less than lkeV producing only a nominal change in the ionisation cross section. Machine calibrations are performed regularly to ensure the reliability of the beam energy (Weaver 1976).

The accelerator has to be 'conditioned' before using beams of high energies inorder to ensure stability of the beam energy. Conditioning was performed each time prior to conducting the experiments. The 'conditioning point' tends to fall with time and to avoid any adverse affects on the beam energy, measurements were performed from 3MeV down to 1MeV, reducing the energy in steps of 200keV to establish the energy dependence of the x-ray production and ionisation cross sections.

5.2.2. Beam Transport and Experimental Line

The extracted mass one ions were subjected to a magnetic field in the top terminal causing them to be deflected into the line of the

accelerator. After acceleration the particle beam can be directed into five experimental beam lines, each of which is based in an individual scattering room. For the present experimental work the ion beam was bent twice through 45° in succession by two magnets and transported into a horizonatal line, constructed of stainless steel components, leading to the scattering chamber. Beam focussing was achieved by means of a pair of quadrupole electromagnets.

A schematic diagram of the essential components of the experimental beam line and the scattering chamber employed in the collision experiments is shown in figure 5.1. Before the beam enters the scattering chamber the size of the beam is defined by two tantalum collimators,  $C_1$  and  $C_2$ , 30cm apart and with diameters 2mm and 1.5mm respectively.  $C_2$  defines the final beam diameter as it enters the scattering chamber. The collimators were tapered to reduce scattering of the charged particles and insulated from the rest of the line and the chamber with polytetrafluorethylene (PTFE) rings, which allows the current to be monitored on  $C_1$  and  $C_2$  as the beam travels down the line. This aided the machine operators considerably to direct the ion beam into the target chamber.

Alignment of the experimental line was achieved by passing a fine horizontal laser beam through the line after removing the target assembly and the Faraday cup (figure 5.1). The individual components of the line were adjusted until the laser beam passed through the collimators without hindrance and produced an intense spot on a reference mark,  $R_1$ , on the wall beyond the scattering chamber (figure 5.1). By placing a plane mirror at  $45^{\circ}$  to the beam axis inside the chamber and in the path of the laser, it was ensured that the reflected laser beam also produced an intense spot on a second reference mark,  $R_2$ , on the adjacent wall, as shown figure 5.1. The lithuim drifted silicon



(Si(Li)) detector, employed for the x-ray measurements, was positioned at  $90^{\circ}$  to the beam axis using the reflected laser beam. The position of the silicon surface barrier (SSB) detector, required for detecting backscattered particles, was similarly checked. Positions of both of these detectors were verified each time before beginning the measurements. With the aid of R<sub>1</sub> and R<sub>2</sub> the positions of the target holders were adjusted until the laser beam created a spot on the centre of the targets when placed at  $45^{\circ}$  to the beam line.

A rotary pump was used to evacuate the experimental line and the scattering chamber to an initial pressure of  $10^{-1}$  torr and then a diffusion pump to attain a working pressure of less than  $10^{-5}$  torr. A clean system was maintained throughout the duration of the experiments by means of an ion pump and a liquid nitrogen trap illustrated in figure 5.1.

#### 5.2.3. Scattering Chamber

After being collimated by aperatures  $C_1$  and  $C_2$  the particle beam enters a rectangular scattering chamber constructed of 1 cm stainless steel plates (figure 5.1). The inside dimensions of the chamber are approximately 12 x 15 cm. The chamber was electrically insulated from the beam line by teflon and PTFE insulating couplings. One of the sides of the chamber, parallel to the beam line, incorporates a viewing port made of 1.25 cm thick glass plate. The opposite side houses a 50  $\mu$  m melinex window of about 5 cm diameter. The x-rays produced by the particles impinging on the target pass through this window before being measured by the Si(Li) detector.

An aluminium aperature,  $C_3$ , of 1.5 cm in diameter was placed in the entrance port of the chamber (figure 5.1). The purpose of  $C_3$  was to 'catch' the energetic secondary electrons emitted from the target when bombarded by charged particles and thus prevents the electrons from

reaching C2 and vitiating the beam current measurements.

To measure the backscattered particles a silicon surfact barrier (SSB) detector was mounted from the 1.25 cm thick stainless steel coverplate. The backscattering angle was defined by two tantalum apertures (T in figure 5.1) attached to the front of the SSB and placed 5 mm apart. Both of the aperatures were reamed to avoid any scattering at the edges. The diameters of the aperatures were measured with a 'Universal Measuring Machine' (model MU214B) and were determined to be  $2.531 \pm 0.003$ mm. The aperatures also ensured that the collimated backscattered beam struck the centre of the active area of the SSB detector and avoided any 'edge' effects.

A Faraday cup constructed of a 40 cm long stainless steel tube was attached to the end of the chamber (figure 5.1) to collect the charged particles after interacting with the thin targets. The Faraday cup was insulated from the chamber by PTFE and teflon couplings. A tantalum aperature (C<sub>4</sub>) of 1.5 cm diameter, attached to the entrance of the Faraday cup, prevented secondary electrons escaping from the cup into the chamber and causing 'leakage' of current. The opening of the Faraday cup was about 15 cm from the target position.

5.2.4 Target Assembly

The target assembly consisted of four aluminium mounts fixed vertically to the outer edges of a horizontal disc, also made of aluminium. The whole assembly was suspended from the chamber coverplate by a stainless steel shaft. The target mounts were simply two columns with groves which held the targets securely in place.

Targets backed by nuclepore  $(1mg/cm^2)$  and carbon  $(40\mu g/cm^2)$ were employed in this work. Both types of targets were commercially obtained from MicroMatter and Co. The carbon backed targets were obtained ready-mounted on pieces of aluminium 1.5 x 1.5 cm and 0.5 mm

thick with a 1 cm circular aperture. Targets backed by nuclepore were fixed onto aluminium frames 1.5 x 2.0 cm and 2 mm thick with a 1.5 cm diameter hole by means of an aluminium ring pressed into the hole. These targets were simply slotted into the mountings and the carbon backed targets were secured into the mounts with the aid of aluminiun circlips. The target assembly as a whole could be moved vertically and the target mcuntings laterally, permitting precise alignment with the laser (section 5.2.2).

The position of the targets was controlled remotely by means of a high resolution stepping motor attached to the shaft suspending the target assembly and connected to a remote control unit. This has been described in details by Saied (1981). Targets could be positioned at the required angle in increments of  $0.9^{\circ}$  without breaking the vacuum. A T.V. camera was used to monitor the target assembly throughout the experiments.

## 5.3 CHOICE OF TARGETS

To study the dependence of L shell x-ray production and ionisation cross sections on target atomic number  $(Z_2)$ , 10 solid targets spanning  $46 \le Z_2 \le 92$  were employed for the L shell cross section measurements. Table 5.1 lists the targets, together with the form of the target, type of backing, the projectiles incident on the target and type of cross section measured. Targets of sufficiently high melting points were chosen to avoid any possibility of evaporation during bombardment by the charged particles.

All the experimental cross section measurements in this study were performed with thin targets. The criterion usually adopted to decide whether a target is 'thin' is that the interaction cross section must not be affected significantly by the energy loss suffered by the projectile as it passes through the target. In the present context

														cross sections cross sections
Cross sections <sup>(b)</sup> measured	X	X	X	Х, І	Х, І	Х, І	X	X, I	X	X, I	X; I	X, I	Х, І	<pre>X = L x ray production I = L shell ionisation</pre>
Projectiles <sup>(a)</sup>	b	d	p	p, d	p, d, α	p, d, α	d	p, d, α	p	p, d, α	p, d, α	b	b	oha particles. (b)
Type of backing	Nuclepore	Nuclepore	Nuclepore	Carbon	Carbon	Carbon	Nuclepore	Carbon	Nuclepore	Carbon	Carbon	Carbon	Carbon	erons, $\alpha = Alp$
Target form	Elemental	Elemental	Elemental	DyF <sub>3</sub>	YbF3	MO3	Elemental		Elemental		Elemental	ThF 4	UF,	ons, d = Deute
Target (Z <sub>2</sub> )	Pd (46)	Te (52)	Dy (66)		Yb (70)	W (74)	Au (79)		Pb (82)		Bi (83)	Th (90)	U (92)	(a) p = Proto

Table 5.1. Targets employed for cross section measurements.

the affect on the elastic scattering and x-ray production cross sections must be minimal. The former varies with projectile energy as  $E^{-2}$ (equation 3.11) and the latter as  $E^{+}$  (Merzbacher and Lewis 1958). X-ray production cross section is, therefore, more sensitive to the projectile energy loss and if this effect is small then it is also small for the nuclear elastic scattering cross section. Targets with typical thicknesses of about 50µg/cm were used for the experimental work and to estimate the effect on the x-ray production cross section. of the projectile energy loss in such a target a multiplicative correction,  $C_{\chi}$ , to the x-ray production cross section was derived and is given by

$$C_{X} = \left[1 - \frac{\operatorname{at} \operatorname{ne}(E)}{2E}\right]^{-1}$$
 5.2

where t is the target thickness and n is the target atomic density. Equation 5.2 assumes that the stopping,  $\varepsilon(E)$ , varies linearly with projectile energy and that the x-ray production cross section varies as  $E^a$ . a was determined by fitting a function of the form  $\sigma = \sigma_0 E^a$ to the ECPSSR cross sections in the vicinity of the incident particle energy, where  $\sigma_0$  is a constant.  $\varepsilon(E)$  was extracted from the tables of Andersen and Ziegler (1977b). Using equation 5.2 corrections were found to be negligible for proton and deuteron impact, even at low energies. In the case of alpha particles a correction of about 3% was necessary at low incident energies.

Since the stopping power appears only in the correction it does not introduce any significant uncertainties in the measured cross sections. In comparison, for thick target measurements  $\varepsilon(E)$  enters directly into the cross section calculations. As a consequence the precision of the cross sections obtained from thick target data is determined to a large extent by the precision of  $\varepsilon(E)$ . Furthermore the derivative

of the yield excitation function is required when using thick targets. This is usually obtained by fitting polynomials to the yield curves or simply by graphical means (Khan and Crumpton 1978). Apart from introducing futher uncertainties in the cross sections this procedure obviously entails complications. Corrections must also be made for the self-absorption suffered by the particle induced x-rays in the thick targets. This leads to an additional criterion for characterising the thickness of a target. If self-absorption can be ignored then the target is considered 'thin'. In relation to metallic targets if the x-ray production cross section criterion is fulfilled then the target is sufficiently thin to make self-absorption insignificant.

In the case of thin target measurements the calculation procedure is relatively straightforward. The problem of determining precisely the target thickness, however, does arise and is discussed in section 5.6. This difficulty is clearly absent for thick target experiments.

Thin and thick target techniques for obtaining x-ray production cross sections by light charged particle bombardment have been compared by McKnight et al (1975) and more recently by Khan and Crumpton (1978) and Barfoot et al (1980). There is a general concensus that although the uncertainties of the cross sections obtained from the two techniques are comparable, the thin target method is slightly more precise. For the aforementioned reasons present measurements were performed with thin targets only.

As mentioned in subsection 5.4.2 targets on lmg/cm<sup>2</sup> nuclepore and 40µg/cm<sup>2</sup> backings were studied. Initial measurements of proton induced L shell x-ray production cross sections were conducted with nuclepore backed targets because they can be handled without difficulty and their thicknesses are known to within 5% (MicroMatter and Co.). A severe limitation of this type of target, however, is that it cannot

withstand high beam currents because of the non-conducting backing material and beam currents of only a few nanoamperes can be used. As a direct consequence counting statistics, although adequate for x-ray production measurements, were poor for the purposes of deducing ionisation cross sections. To overcome this difficult targets baked by  $40\mu g/cm^2$  carbon were adopted for ionisation cross section measurements. These targets can sustain beam currents of several hundred nanoamperes for a few hours without undergoing any serious deterioration. Currents of upto 100nA were employed in the measurements reported in this thesis while keeping count-rates below  $500s^{-1}$  to avoid pulse pileup. An inherent disadvantage with this type of backing is their fragile nature and its primarily because of this fact that backings of  $40\mu g/cm^2$ .

#### 5.4 DATA AQUISITION

L x-ray production cross sections were deduced from the measured x-ray yields and the appropriate target charge. The procedures adopted for determining both of these fundamental experimental quantities are described in this section. Details are also given of the calibration of the x-ray detection system.

# 5.4.1 Determination of Target Charge

The total charge to which the target is exposed during irradiation by charged particles was determined by feeding the charge collected in the Faraday cup to a Keithly electrometer (model 600B), shown in figure 5.2. The electrometer integrates the beam current and outputs a voltage signal whose level is proportional to the meter deflection. By varying the input resistence the electrometer supplies a 1V signal for a fullscale-deflection (FSD). The precision of the Keithley electrometer at FSD is around 1%. The output voltage signal is fed



into a voltage-to-frequency converter (VFC) which outputs a chain of pulses with frequency proportional to the input. For an input of IV the frequency is 10<sup>5</sup>Hz. The pulse chain is fed into a decade divider unit which scales the pulses for counting with a scalar/timer device. Counting for a fixed number of these pulses is equivalent to counting for a fixed target charge. An automatic stop unit, linked to the scalar/timer, ceases the accumulation of data once a preset count on the scalar has been achieved. X-ray spectra of sufficient statistical precision were obtained for a specific total charge. The number of charged particles to which the target is exposed is simply obtained by dividing the integrated charge by the electronic charge (e).

Under this experimental arrangement reproducibility of K x-ray yields of low to medium  $Z_2$  nuclepore backed targets bombarded by 2.5MeV protons was investigated in collaboration with Saied (1981). The yields were found to be irreproducible when measurements were performed at different times. This was attributed to

- (i) charge leakage caused by secondary electrons escaping from the Faraday cup into the chamber and
- (ii) since the Keithley electrometer is a high impedence instrument there is the possibility of direct leakage of current between the chamber and the Faraday cup.

To eliminate these causes the chamber, which was initially earthed, was electrically connected to the Faraday tube thus combining the two into one Faraday cup. With this new arrangement reproducible x-ray yields were obtained within statistical deviations. The results of these investigations have been discussed extensively by Saied (1981). During the L shell x-ray measurements reprocibility of the system was checked everytime an experiment was performed by repeating a few measurements on a target which had been studied previously.

As an alternative to utilising a current integrator the number of incident particles can also be determined by measuring the backscattered yield, accumulated over the duration of the x-ray experiment, and employing equation 3.19. This would then avoid the difficulties associated with charge collections discussed above. An additional advantage is that the target thickness, common to backscattered and x-ray yields, may be eliminated in the cross section calculations. This method was initially adopted but since the nuclear scattering cross section varies as  $E^{-2}$ , at low impact energies the enormous backscattered yield caused pulse pile-up problems. By using low beam currents this difficulty can be reduced but then the x-ray yield diminishes and accumulation times can become impracticable. An alternative is to use variable aperatures for the SSB detector, however, the present experimental set-up made this unfeasible. As a consequence the backscattering system was employed solely for measuring target thickness.

### 5.4.2 X-Ray Detection System

After passing through a 50 $\mu$ m melinex window the charged particle induced x-rays travel through 2.5 cm of air before being measured by a Si(Li) detector placed at 90<sup>°</sup> to the beam axis. To ensure that the x-rays impinge only on the central area of the silicon crystal and thus avoid any complications of 'edge' effects (section 5.5) a lead aperture, denoted in figure 5.1 by L, of 3.97 mm and 4.18 mm thick was attached to the front of the detector. The solid angle subtended by the Si(Li) detector was measured with an aid of vernier calipers and value of (1.67 ± 0.03) x 10<sup>-3</sup> steradians was obtained.

A Kevex-ray Si(Li) detector (model number 3201) with a crystal of area 30  $mm^2$  and thickness 3 mm, cooled with liquid nitrogen, was employed for the cross section measurements. A Si(Li) detector is

commonly used for such measurements because it offers good resolution,  $164 \pm 7eV$  at 5.898keV for the above detector, and high efficiency at the x-ray energies of interest. Another common photon detector is the lithuim drifted germanium, Ge(Li), detector. Although it has superior resolution to that of the Si(Li), it suffers from markedly lower detection efficiencies and would increase greatly data accumulation times. A further advantage over the Ge(Li) detector is that the Si(Li) requires less frequent replenishment of liquid nitrogen for a given dewer size, and can even be temperature cycled many times without damaging the crystal. Economically Si(Li) is also favoured to the Ge(Li) detector. Thallium activated sodium iodide, NaI(TI), detectors are also employed for detecting photons but their poor resolution (50% at 5.898keV) makes their use in the present context inappropriate.

The operation of the Si(Li) detector is covered extensively in the literature (Gedcke 1972 and Knoll 1979) and only brief details are presented below.

The silicon crystal has an approximately 200Å thick gold layer on both sides which acts as electrical contacts. The photons also have to pass through approximately 0.1µm of silicon deadlayer before reaching the active region of the crystal. Electron-hole pairs are produced in this region by the photons interacting primarily through the photoelectric effect (section 2.5). The number of charge carriers produced are directly proportional to the x-ray energy since the average energy required to create an electron-hole pair in silicon, cooled to liquid nitrogen temperature, is a constant value of 3.8eV. The charges were collected by applying a voltage of 1kV across the crystal and converted into voltage pulses by a charge-sensitive pulse optical feedback preamplifier (model 2002) while retaining the chargeenergy proportionality. The electronics adopted for the x-ray

measurements are schematically shown in figure 5.2. The Si crystal and the field effect transistor, which forms the first stage of the preamplifier, are cooled by liquid nitrogen to prevent lithium diffusing through the crystal and to minimise electrical noise caused by thermally excited charge carriers in the crystal. The crystal is housed in a vacuum protected by 13µm thick berylluim window, which also acts as an optical shield.

The pulses from the preamplifier were processed and amplified by a Kevex spectroscopy amplifier (model 4500P) to make them compalible with the requirements of a 200MHz analogue-to-digital converter (ADC) forming a part of the multichannel analyser (MCA). The x-ray spectrum was displayed over 2048 channels and the pulses from the amplifier were monitored on a cathode ray oscilloscope (figure 5.2).

Deterioration of the Si(Li) detector resolution by external environmental noise, known as microphonics, has been demonstrated by Khan et al (1979). In view of this care was exercised to avoid all unnecessary mechanical noise and vibration while conducting the x-ray measurements and effects of microphonics, as a result, were not noticable.

A Hewlett-Packard 5406B computer system was available for fast storage and retrieval of data (Weaver 1976). The several ADC's offered by the sytem may be used in combination for multi-parameter or multiplex experiments. The feasibility experiments regarding the determination of the total target charge by measuring the backscattered yield, mentioned in subsection 5.4.1 were performed with two ADC's in multiplex mode. In the subsequent work one ADC was used. The MCA is directly linked to the computer allowing storage of the accumulated x-ray spectra onto a magnetic hard disc for immediate and on magnetic tape for future analysis. Various software packages are available for

spectral analysis and may be initiated via a terminal. Typical L shell x-ray spectra, obtained with the aforementioned x-ray system, are shown in figure 5.3 and 5.4 for ytterbuim ( $Z_2 = 70$ ) bombarded by 3MeV alpha particles and bismuth ( $Z_2 = 83$ ) bombarded by 3MeV protons respectively. During the x-ray measurements LL transition yield was monitored and x-ray spectra were accumulated until the LL yield was greater than 500 counts to obtain reasonable counting statistics for the other peaks. Continuous monitoring of the LL peak also allowed any significant variations in the beam current or damage to the target to be detected. Typical accumulation times ranged from about 5 to 30 minutes.

## 5.4.3. X-Ray Energy Calibration

The direct proportionality between x-ray energy and the number of electron-hole pairs produced in the Si crystal, referred to in the previous subsection, may be checked by performing an energy calibration of the Si(Li) detector. This may be achieved by measuring the pulse heights or the x-ray peak centroids at different energies. Such a detector response is also necessary for identifying x-ray peaks of interest.

A variable x-ray energy source, consisting of a  $10mCi^{2+1}Am$ primary source and six fluorescent targets, in the range  $29 \le Z_2 \le 65$ , together with the targets used for reproducibility studies, were employed to calibrate the x-ray detection system. A software package, available on the computer system for fitting a single Gaussian distribution to an x-ray peak, was used to determine the peak centroids and the standard deviations. The package assumes a linear background on which the x-ray peak is superimposed. A linear relationship between x-ray energy and peak centroid was obtained, validating the chargeenergy proportionality. The following equation was obtained by fitting



Figure 5.3. L x-ray spectrum for ytterbuim ( $Z_{A}$  = 70) obtained by 3 MeV alpha particle impact.





a linear model to the data with the least square method

 $E_{\chi}(keV) = -0.5846 + 0.0408c$  5.3 where  $E_{\chi}$  is the x-ray energy and c is the centroid of the x-ray peak. The correlation coefficient, R, which measures the proportion of total variation about the mean  $\bar{Y}$  explained by the regression (Draper and Smith 1981), may be calculated to estimate the goodness of fit.  $R^2$  is defined as

5.4

5.6

$$x^{2} = \frac{\prod_{i=1}^{n} (\hat{Y}_{i} - \bar{Y})^{2}}{\prod_{i=1}^{n} (Y_{i} - \bar{Y})^{2}}$$

R

where  $Y_i$  is the observed value, x-ray energy in the above context,  $\hat{Y}_i$  is the least square predictions of  $Y_i$  and n is the number of data values. A value of 0.9999 was obtained for equation 5.3. A perfect fit would yield a value of 1.0. The resolution response of the Si(Li) detector varies according to the relation

 $\sigma^2 = \sigma_{\text{noise}}^2 + \varepsilon F E_x \qquad 5.5$ 

where  $\sigma^2$  is resultant variance of the measured x-ray peak,  $\sigma_{noise}^2$  is the contribution from the preamplifier noise,  $\varepsilon FE_x$  is the contribution from the Si(Li) diode due to the ionisation statistics,  $\varepsilon$  is the energy required to create a single electron-hole pair ( $\varepsilon = 3.8eV$  for cooled Si) and F is the Fano factor. The variation of  $\sigma^2$  with  $E_x$  has been studied by Saied (1981) for the detector employed in this work. A linear relationship between  $\sigma^2$  and  $E_x$ , as predicted by equation 5.5, was demonstrated. A least square equation

 $\sigma^2 = 1.5339 + 0.4446E_{v}$ 

was fitted to the data and a value of 0.99 for  $R^2$  was calculated. The gradient of equation 5.6 offers a convenient method for evaluating F for the detector. A value of F = 0.117 ± 0.003 was obtained by Saied (1981). From the intercept  $\sigma_{noise}$  was determined to be 50.5eV.

### 5.5 Si(Li) DETECTOR EFFICIENCY

The reliability of the measured cross section values depends, among other factors (see subsection 5.7.4), on the precision of the x-ray detector efficiency. Much evidence has been brought to light that suggests that the detector efficiency should be determined experimentally (Gallagher and Cipolla 1974). This section is addressed to this problem.

For a well collimated and parrallel x-ray beam striking normally on the silicon crystal the efficiency of the Si(Li) detector,  $\varepsilon$ , may be calculated from

$$s = C_{Be} \left[ 1 - exp(-\mu_{si}x_{si}) \right]$$
 5.7

where  $C_{Be}$  represents the absorption correction for the beryllium detector window,  $\mu_{si}$  is the linear absorption coefficient for Si and  $x_{si}$  is the thickness of the crystal. In practice, however, the situation is not so straightforward. Complications arise due to the possibility of the detector specifications, quoted by the manufacturers, being erroneous (Gallagher and Cipolla 1974). The main factors which are required to calculate the efficiency reliably are

(i) beryllium window thickness (12µm),

- (ii) dimensions of the Si crystal (3mm x 30mm<sup>2</sup>),
- (iii) Si dead layer thickness (0.1µm),
- (iv) gold contact layer thickness (0.02μm),
- (v) depletion layer thickness, and
- (vi) charge collection efficiency.

The values in parenthesis refer to the manufactuer specifications for the Si(Li) detector employed in this study. Although some of these factors are quantified by the manufactors they may be unreliable or may even alter with time deteriorating the efficiency. Cohen (1982) has highlighted the deteriorating effects of ice build-up on the front face of the Si crystal at low x-ray energies. Consequently the necessity for determining the detector efficiency experimentally has been stressed by many workers. (Routti and Prussin 1969, Hansen et al 1973, Gallagher and Cipolla 1974 and Johnson et al 1978).

5.5.1 Measuring Techniques

Two basic techniques are usually employed for measuring x-ray detector efficiencies. These are the 'absolute' and the 'comparison' techniques (Johnson et al 1978). The first method relies on calibrated radioactive sources with known activities, to which the x-ray detector is exposed. The efficiency is simply given by the ratio of the observed and the calculated photon fluxes. This method has been adopted recently by Dias and Renner (1982). There are, however, several drawbacks to this technique. Apart from the economic costs of obtaining the several sources that would be required to measure the efficiency at different x-ray energies, serious difficulties are encountered in determining accurate activities and acquiring knowledge of decay schemes (Hansen et al 1973 and Cipolla and Hewitt 1976). Considerable self-absorption in the radioactive source causes further complications (Johnson et al 1978 and Palinkas and Schlank 1980). Also there are relatively few sources avaiable that have convenient half lives in the x-ray region of interest (Johnson et al 1978).

These difficulties may be avoided by adopting the 'comparison' technqiue. This involves the comparison of the Si(Li) detector response with that of another detector whose efficiency is predetermined. The main advantage of this method is that the incident flux does not have to be known absolutely. The extent of the advantages depends on the way the incident fluxes are produced. Different methods for generating the test photon flux have been discussed by Johnson et al (1978). Basically the test photons may be emitted directly by

radionuclides or indirectly by fluorescing a series of appropriate targets. The first method suffers from the disadvantages listed for the 'absolute' method. Johnson et al (1978) have used the second method and utilise the x-rays emitted when targets are fluoresced by a mono-energetic source. Shima (1979) and more recently Tolson and Spyrou (1982) have generated the test flux by bombarding selected targets by energetic protons and have used a proportional counter to compare the response of their Si(Li) detector. Cohen (1982) has compared the ratio of the M to L shell x-rays, produced by He<sup>+</sup> impact of high  $Z_2$  elements, with the ratios predicted by the plane-wave Born approximation to calculate the Si(Li) detector efficiency.

In the present work a variation of the method used by Johnson et al (1978) is adopted for measuring the detector efficiency, while retaining the advantages of the 'comparison' technique.

# 5.5.2 Procedure and Results

A standard variable x-ray energy souce, consisting of Cu, Rb, Mo, Ag, Ba and Tb targets fluoresced by 60 keV  $\gamma$ -rays from a 10m Ci<sup>2+1</sup>Am source, was used to provide the test photons. A 0.1mCi<sup>55</sup>Fe source encased in lead for safety, was also used to extend the energy range down to 5.959keV. In addition, Ag x-rays from the variable x-ray energy source were employed to fluoresce thick targets of Ni and Zn. The efficiency was thus determined over the energy range 5.959 -45.5keV. The sources employed here are inexpensive and readily available and thus makes the method particularly attractive. Table 5.2 lists the sources and the energies of the characteristic x-rays. The energies quoted are the weighted K x-ray energies from Storm and Israel (1970) instead of the individual K<sub>ac</sub> and K<sub>β</sub> energies. The reason for this is that all the fluorescent targets are thick and self absorption is obviously considerable. Furthermore, self-absorption

Table	5.2.	List	of	sources	and	x-ray	energies
	empl	oyed	for	Si(Li)	deteo	ctor	
		effic	iend	cy measu	remer	nts.	

Sources	Weighted K x-ray
	energy* (keV)
<sup>55</sup> Fe	5.959
Ni <sup>(a)</sup>	7.558
Cu <sup>(b)</sup>	8.136
Zn <sup>(a)</sup>	8.735
<sub>Rb</sub> (b)	13.596
Mo <sup>(b)</sup>	17.781
Ag <sup>(b)</sup>	22.581
Ba <sup>(b)</sup>	32.89
Tb <sup>(b)</sup>	45.469

\* Storm and Israel (1970).
(a) Fluoresced by Ag K x-rays.
(b) Variable x-ray energy source.

of  $K_{\alpha}$  and  $K_{\beta}$  x-rays is different and as a result the  $K_{\alpha}/K_{\beta}$  ratio of the emergent x-rays is unknown.

A thallium activated sodium iodide, NaI(T1), detector (Harshaw 6SHA 6M/2A) with a 6 mm thick and 4 cm diameter crystal was used for the comparison. NaI(T1) was used as the reference detector because its efficiency is 100% for the energies of interest. To avoid correcting for absorption in the 25.4µm thick aluminium window, of the NaI(T1) detector an identical window was obtained from the manufacturers and placed in front of the Si(Li) detector while performing the measurements. This was done to eliminate any doubt in the manufacturers specification of the aluminium window thickness.

The geometrical arrangement and the electronics are shown in figure 5.5 for the variable x-ray energy and <sup>55</sup>Fe sources. Both of the detectors were exposed to the sources for a sufficient time to obtain satisfactory counting statistics. To eliminate pulse pile-up countrates were restricted to less than 500s<sup>-1</sup>. The Si(Li) detector was apertured with the same lead collimator as used in the cross section measurements. The NaI(T1) detector was apertured by 1 cm thick lead with a 0.5 cm diameter hole to ensure that the photons avoid the edges and strike the crystal normally. The scintillation pulses from the NaI(T1) detector, powered by a 1.1kV bias, were processed and amplified by a Harshaw MB11 preamplifier and a 472A Ortec amplifier. These pulses and those from the Si(Li) detector were monitored on a cathode ray oscilliscope and fed into a Canberra (series 35) multichannel analyser (figure 5.5). The data aquisition system allows storage of spectra on magnetic tape and offers plotting and printing facilities.

Thick Ni and Zn targets were placed at  $45^{\circ}$  to the detector axis and fluoresced by Ag K x-rays from the variable x-ray energy source placed at  $90^{\circ}$  to the detector (figure 5.5iii). Although Rb and Mo



Lead aperature



absorber

• •

(ii)



### (iii)

Figure 5.5. Schematic representation of the electronics for Si(Li) detector efficiency measurements.

K x-rays were also available and have energies closer to the K absorption edge of Ni and Zn and thus would ideally be chosen for fluorescing these elements, their intensities were low and consequently were not used. Source to detector distances were typically 1.5 cm.

Figures 5.6 and 5.7(i) show Mo K x-rays detected by Si(Li) and NaI(T2) detectors respectively. As the figures show the NaI(T1) spectrum is complicated compared to the Si(Li) spectrum. In the letter case the detected number of x-rays for a given collection time were simply obtained by summing the counts under the characteristic peaks and subtracting the appropriate background, assumed linear.

The procedure is somewhat more complicated in the case of NaI(T1) spectrum. The  $K_{\alpha}$  and  $K_{\beta}$  components of the Mo K x-rays are not resolved by the NaI(T1) detector, as shown in figure 5.7(i). The characteristic K x-ray peak rests on a prominent continuum which originates from different physical processes. The high energy distribution consists of a 60 keV gamma-ray peak from the 241 Am variable x-ray energy source which also undergoes Compton scattering in the source and produces a peak of approximately 50 keV energy. The continuum is enhanced further by Compton scattering in the source and the detector. Both these peaks produce their associated iodine escape peaks at about 21 keV and 11 kev respectively which lie under the Mo k x-ray peak. These escape peaks make it difficult to obtain the area under the Mo x-ray peak in the same manner as described for the Si(Li) spectrum. For this reason the escape peak contributions have to be extracted before the area can be found. The following method was adopted for achieving this. A background spectrum was generated for each of the test photons from the variable x-ray energy source and for Ni and Zn which were fluoresced by this source. The characteristic x-rays of elements Ni and Mo were absorbed with Al of thickness upto 6 mm and of Ag and Ba with Ti



Figure 5.6. Molybdenum K x-rays detected with a Si(Li) detector.



of thickness upto 5 mm. The resulting background spectrum was accumulated until the area under the Compton + 60 keV distribution was equal to the area under the same distribution in the initial composite spectrum. Subtracting the background spectrum from the composite spectrum gives the characteristic peak and the area can be obtained readily by summing the counts. Figure 5.7(i), (ii) shows the total and the background spectrum for Mo x-rays and figure 5.8 shows the resultant x-ray peak obtained after subtraction. The Compton + 60 keV  $\gamma$ -ray distribution becomes less important as the target element atomic number  $(Z_2)$  increases. This is because the 60 keV  $\gamma$ -rays increasingly undergo photoelectric interactions (section 2.5) producing characteristic x-rays as  $Z_2$  increases. This is clearly demonstrated by figures 5.9 and 5.10 which show  $Cu(Z_2 = 29)$  and  $Ag(Z_2 = 47)$  spectra. For  $Tb(Z_2 = 65)$  this distribution was negligible and the iodine escape peaks produced by the Tb x-rays do not interfere with the characteristic peak (figure 5.11). As a result the peak area was determined directly from the spectrum. The x-rays from the 55Fe source lie on a flat distribution and do not pose any problems.

Counting times of upto 30 minutes were adequate to ensure that the statistical uncertainties for x-rays emitted from the variable energy source were insignificant for both detectors. For the <sup>55</sup>Fe source times upto 2.5 hours were necessary. In the case of Ni and Zn statistical uncertainties of less than 1.5% were achieved after accumulation times of upto 4 hours. It is difficult to quantify exactly the uncertainties caused by the stripping procedure adopted for NaI(T $\ell$ ) spectra. This is because the A $\ell$  and Ti absorbers differentially attenuate the 50keV Compton and 60keV  $\gamma$  - ray peaks. This alters the relative intensities of their associated iodine escape peaks. Consequently the contribution of these escape peaks, approximately







Figure 5.9. Copper K x-rays detected with a NaI(T1) detector.



Figure 5.10. Silver K x-rays detected with a NaI(T1) detector.



upto 20% of the photopeak, cannot be removed completely from the observed spectra. However, it is expected that most of the contribution is removed and the remaining should be negligible. This situation only applies in the case of Mo where the photopeak rests on top of the escape peaks (figure 5.7). In the case of the other elements the photopeaks either only partially or completely separated from the iodine escape peaks. Changing the region of interest, over which the Compton + 60keV distribution was normalised, caused a variation of less than 2% in the photopeaks of Ni and Zn and less than 1% in the case of other elements. The uncertainties in the detector solid angles were typically 1.5%.

The efficiency of the Si(Li) detector,  $\boldsymbol{\varepsilon}_{\mathrm{si}}$ , can be determined from the expression

$$\varepsilon_{si} = \frac{\gamma_{si} \exp\left(-\frac{\mu}{\rho}(\rho t)\right)_{air}^{NaI} \Omega_{NaI}}{\gamma_{NaI} \exp\left(-\frac{\mu}{\rho}(\rho t)\right)_{air}^{Si} \Omega_{Si}} 5.8$$

where  $Y_{si}$  and  $Y_{NaI}$  are the photon fluxes detected by the Si(Li) and the NaI(T2) detectors respectively, the exponential terms represent the air correction for both the detectors, t is the air gap and  $\Omega_{Si}$  and  $\Omega_{NaI}$ are the solid angles subtended by the two detectors. To evaluate the air absorption correction, mass absorption coefficients were extracted from Storm and Israel (1970). Polynomials were fitted to this data (subsection 5.7.1) and employed to facilitate the calculations for the individual target elements. The uncertainties quoted by Storm and Israel (1970) in their mass absorption coefficient data are 10% for x-ray energies less than 6 keV and 3% for energies greater than 6 keV. For the elements. The air gap, t, was measured precisely using vernier calipers to an uncertainty of less than 0.5%. The total uncertainty in the efficiency calculations were in the range 2 to 3.5%.

Table 5.3 shows the numerical values of  $\varepsilon_{Si}$  for the elements. A logarithmic polynomial to power 5 was fitted to the experimental data, that is

$$\varepsilon_{Si} = \exp(-15.5404 + 32.077 \ln E_{\chi} - 26.4129(\ln E_{\chi})^{2} + 10.5938(\ln E_{\chi})^{3}$$
  
- 2.0478  $(\ln E_{\chi})^{4} + 0.15(\ln E_{\chi})^{5}$  5.9

Correlation coefficient for the fit is  $R^2 = 0.9998$ . The fit is shown in figure 5.12 together with the experimental data and the calculated efficiency using expression 5.7 and the manufacturers specifications for the Be window. The discrepencies between experimental data and calculated efficiences is striking. It is only at the higher energies where the two curves tend to converge. The experimental values differ by up to 35% from the calculated values. In the x-ray energy range of interest the absorption in the 200Å gold layer is at most 2% and in the 0.1 µm silicon dead layer it can be ignored. However, as pointed out by Gallagher and Cipolla (1974) the depth of the dead layer may increase with time and may explain some of the discrepencies. An accumulation of dust particles was noticed on the Be window. This will absorb the low energy x-rays reducing the detector efficiency. Cohen (1982) has shown that ice build-up on the front face of the Si crystal reduces considerably the detection efficiency of low energy x-rays. The detector in question is nearly 13 years old and all the above effects are likely to be important and collectively may explain the large differences between theory and experimental data.

Preliminary measurements of L-shell x-ray production cross sections, employing nuclepore backed targets, were corrected only by the calculated detector efficiency (Appendix E). The cross section measurements using carbon backed targets, on which this thesis is mainly base, have been corrected by the experimentally determined efficiency and figure 5.12 highlights the need for doing so. The time difference between the two

Table 5.3. Measured Si(Li) detector efficiency.

X-ray energy * (KeV)	Efficiency
5.959	0.767 ± 0.027
7.558	0.771 ± 0.023
8.136	0.793 ± 0.016
8.735	0.769 ± 0.027
13.596	0.779 ± 0.016
17.781	0.707 ± 0.014
22.581	0.591 ± 0.012
32.89	0.322 ± 0.006
45.469	0.141 ± 0.003

\* Weighted x-ray energies from Storm and Israel (1970).


Figure 5.12. Si(Li) detector efficiency as a function of x-ray energy.

sets of cross section measurements was nearly 2.5 years and some deterioration of the detection efficiency would be expected. The efficiency measurements reported in this section were conducted immediately after the x-ray yield experiments for the carbon backed targets had been performed. This avoided the possibility of any further degeneration of the efficiency.

The energy of the Dy LL x-rays (5.744 keV) lie just outside the lower energy limit of the efficiency measurements (5.959 keV), see table 5.3). The limited time available for performing the efficiency experiments made it impracticable to extend the measurements to lower x-ray energies. Consequently the efficiency for detecting the Dy LL x-rays was obtained by extrapolating equation 5.9.

5.6 TARGET AREAL DENSITY MEASUREMENTS

The uncertainties in the areal densities of the carbon backed targets, quoted by MicroMatter Co, are greater than 25%. Since the precision of the target areal densities will also influence the uncertainty of the cross sections the areal densities have to be determined as reliably as possible. To measure this quantity the nuclear backscattering technique was adopted. The physical concepts on which this method is based were discussed in chapter 3 and this section deals with the procedure and the results of the experiments.

A schematic representation of the electronics employed for measuring target and areal densities is illustrated in figure 5.13. The backscattered particles were measured with a silicon surface barrier (SSB) detector with an active area of 75 mm and thickness of 190  $\mu$ m and required a 12V power supply. The detector was placed at a backward angle as close as possible to 180<sup>°</sup> to the beam axis as the experimental arrangement allowed. The angle was measured geometrically with an aid of a variable height gauge and checked with a Nikon 1354 type shadow



Figure 5.13. Schematic representation of the target thickness measurement system.

graph projector. A value of  $144.92^{\circ} \pm 0.02^{\circ}$  was obtained. The effect of the uncertainty in the angle on the elastic scattering cross section in minimal and can be neglected. The SSB was aperatured by two tantalum collimators, 5 mm apart and 2.5 mm in diameter, to ensure that a collimated backscattered beam strikes the centre of the active region of the detector. Pulses from the SSB were processed by a preamplifier and a 472A Ortec main amplifier and then fed into an MCA of the HP5406B data aquisition system (subsection 5.4.2). The charge collection procedure is identical to that described in subsection 5.4.1. To eliminate pulse pile-up counting rates were kept below 500s<sup>-1</sup> while maintaining good statistics (< 3%). In many cases the statistical uncertainties were negligible. Performance of the electron system was monitored by feeding test pulses of the same characteristics as the pulses due to the scattered particles into the preamplifier. Employing equation 3.22 the areal densities of the thin targets can be determined from the measured backscattered yield. Expression 3.22 however, has to be modified since the target were positioned at 45° to the beam axis, that is,

$$(pt) = \frac{A_2 Y_B}{N_0 \sqrt{2} \left( N_p \Omega \sigma + Y_B \frac{\varepsilon(E)}{E} \right)}$$
 5.10

where ( $\rho$ t) denotes the target areal density,  $\rho$  is the mass density of the target with atomic mass A<sub>2</sub>, Y<sub>B</sub> is the experimentally measured backscattered yield,  $\Omega$  is the SSB solid angle, N<sub>p</sub> is the number of incident particles with energy E,  $\sigma$  is the Rutherford scattering cross section,  $\varepsilon$ (E) is the stopping power of the particles at energy E in the target and N<sub>0</sub> is the Avogadro's number.

X-ray fluorescence calibration targets, backed on nucelpore  $(1mg/cm^2)$ , and used for the initial L x-ray production cross sections

(Appendix E), were utilised to verify the integrity of the thickness measuring system. Thicknesses of these thin targets were quoted by the manufactureres to within 5% and thus are ideally suited for testing the system. Thicknesses of Pd, Te, Dy, Au and Pb targets were measured with incident proton and alpha particles at selected impact energies. Backscatter spectra for 2.5 MeV protons and alpha particles impiring on Au are illustrated in figures 5.14 and 5.15. The figures show the carbon and oxygen 'edges', due to the polycarbonate backing, as well as the Au and pulser peaks. The position of the Te peak centroid, or more strickly the high energy edge of the peak, corresponds to a particle energy (E1) of KE, where K is the kinematic factor for the collision system and E is the incident projectile energy (see section 3.3). Energy calibration of the system was performed by noting the peak positions and a linear relationship, as expected, between the peak positions and incident particle energy was established. Calibration was checked everytime prior to conducting each experiment. A typical least square fit to the calibration data for incident alpha particles is

 $E_1 = 0.160 + 0.01212c$ 

5.11

where c is the channel number corresponding to the high energy edge of the peak. The corresponding correlation coefficient is  $R^2 = 0.9996$ . Although energy calibration of the system is not of primary importance in the context of target thickness measurement, it does, however, serve the purpose of testing the system response and give confidence in the measuring technique.

Low beam currents of about 3nA were used to reduce the possibility of target damage and as a result count rates were low enough to exclude the problem of pulse pile-up. Accumulation times of the order of a few minutes sufficed to reduce counting statistics to less than 3% for



Figure 5.14. A backscattering spectrum of Au(lmg/cm<sup>2</sup> nuclepore backing) bombarded by 2.5 MeV protons.



proton impact and make them unimportant for alpha particle impact. An interactive software routine, which formed a part of the Hewlett-Packard data manipulation package, was used to determine the peak areas. The routine employs a linear model for the background over a region of interest defined by the user. Relatively small changes in the region of interest have only a minimal affect on the peak areas. Corrections for the variation of the Rutherford scattering cross section in the target was insignificant for protons and less than 2% for alpha particles.

In the case of carbon backed targets beam currents of up to 100 nA were employed which allowed yields of considerable precision to be accumulated within a few minutes while exercising due care to avoid problems of pulse pile-up. Since the target and the backing are thin the backscattering spectrum consists of peaks, as is clearly illustrated in figures 5.16 and 5.17 for Au bombarded by 2.4 MeV protons and alpha particles respectively. Comparison of the figures demonstrate how the relative intensities of low and high Z<sub>2</sub> elements change with projectile atomic number. For DyF3, YbF3, ThF4 and UF4 targets proton impact was avoided and measurements were performed only with alpha particles in order to minimise the possibility of nuclear reactions which would complicate backscattering spectra. To determine the stopping power of the alpha particles in these targets and WO3, individual  $\varepsilon(E)$ , weighted according to their atomic masses, were summed. Effect of variation of  $\sigma$  in the target for incident alpha particles on the areal densities was about 2% at low energies and decreases as E increases.

The main factors which determine the precision of the measured areal densities are



Figure 5.16. A backscattering spectrum of  $Au(40\mu g/cm^2$  carbon backing) bombarded by 2.4MeV protons.





(i)	counting statistics	<3%
(ii)	beam current measurement	1%
(111)	SSB solid angle	1.5%
(iv)	Rutherford scattering cross section	<1.4%

The uncertainty in the Rutherford scattering cross section, which is proportional to  $E^{-2}$ , is due to E being uncertain by up to 0.7% (subsection 5.2.1). Uncertainties of the experimentally determined stopping powers range typically 5 - 10% in the literature. However, since  $\varepsilon$  (E) appers only in the correction (equation 5.10) the uncertainty in  $\varepsilon$  (E) has a negligible affect on the final precision of (pt). The total uncertainty in (pt) is obtained by combining the individual percentage errors quadratically and ranges from 2 - 4%.

The measured areal densities, and their values quoted by Micro-Matter and Co., are tabulated in tables 5.4 and 5.5. Values for all targets backed by nuclepore (table 5.4) agree within the precision quoted by the manufacturers ( $\pm$  5%). Agreement is very good not only between the values at different energies but also between the proton and alpha particle data. In the case of targets backed by carbon the internal consistency of the data is very good(table 5.5). Although the measured areal densities differ markedly from those quoted by the manufacturers for some elements they do however, agree within the uncertainty specified by MicroMatter and Co (25%). Weighted means of the areal densities, measured by proton and alpha particle impact, were used in the calculations of experimental cross sections and are listed in table 5.5. The uncertainties in the means were less than 1.5%. 5.7 DETERMINATION OF EXPERIMENTAL CROSS SECTIONS

The procedure adopted for evaluating L shell x-ray production and ionisation cross sections from the measured x-ray yield is outlined in this section.

Table 5.4. Measured areal densities for nuclepore backed targets.

(pt) <sup>M</sup> µg/cm <sup>2</sup>	49.0 ± 2.5	50.0' ± 2.5	<b>52.0 ± 2.6</b>	35.0 ± 1.8	39.0 ± 2.0
(ρt) <sup>E</sup> μg/cm	49.3 ± 1.0 49.0 ± 1.0	$\begin{array}{c} 48.6 \pm 1.0 \\ 50.3 \pm 1.0 \end{array}$	$\begin{array}{c} 48.6 \pm 1.0 \\ 49.0 \pm 1.0 \\ 50.0 \pm 1.0 \end{array}$	$\begin{array}{c} 36.1 \pm 0.7 \\ 34.9 \pm 0.7 \\ 35.2 \pm 0.7 \end{array}$	$39.9 \pm 0.8$ $40.1 \pm 0.8$
Alpha particle energy MeV	1.5 2.0	2.0 2.5	1.5 2.0 2.5	1.5 2.0 2.5	2.0 2.5
(ρt) <sup>E</sup> µg/am	$\begin{array}{c} 50.7 \pm 1.5 \\ 51.4 \pm 1.5 \\ 49 \pm 2 \end{array}$	$\begin{array}{c} 50.1 \pm 1.5 \\ 49 \pm 2 \end{array}$	$\begin{array}{c} 49.7 \pm 1.3 \\ 48.5 \pm 2.0 \\ 50 \pm 2 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$40.9 \pm 1.2$ $41.8 \pm 1.7$
Proton energy MeV	2.0 2.5 3.0	2.5 3.0	2.0 2.5 3.0	2.0 2.5 3.0	2.6 3.0
arget	Pd	Te	Dy	Au	Pb

M = Values quoted by MicroMatter and Co. E = Experimental values

(pt) <sup>M</sup> (μg/cm <sup>2</sup> )	28 ± 7	35 ± 9	37 ± 9	52 ± 13	57 ± 14	50 ± 13	30 ± 8	42 ± 11	
Mean (ρt) <sup>E</sup> (μg/cm <sup>2</sup> )	32.8 ± 0.5	<b>36.5 ± 0.4</b>	$45.5 \pm 0.4$	$56.9 \pm 0.5$	$61.9 \pm 0.7$	60.0 ± 0.6	<b>34.3 ± 0. 5</b>	41.3 ± 0.6	
$(\rho t)^{E}$ $(\mu g/cm^{2})$	$\begin{array}{c} 32.4 \pm 0.6 \\ 33.3 \pm 0.7 \end{array}$	$36.7 \pm 0.7$ $35.9 \pm 0.7$ $36.8 \pm 0.7$	$\begin{array}{c} 44.9 \pm 0.9 \\ 45.1 \pm 0.9 \\ 45.7 \pm 0.9 \end{array}$	55.4 ± 1.1 57.3 ± 1.1 55.2 ± 1.1	$61.6 \pm 1.2$ $62.4 \pm 1.2$	59.1 ± 1.2 60.3 ± 1.2 59.8 ± 1.2	$\begin{array}{c} 33.7 \pm 0.7 \\ 34.8 \pm 0.7 \end{array}$	$\begin{array}{c} 41.0 \pm 0.8 \\ 41.5 \pm 0.8 \end{array}$	
Alpha particle energy (MeV)	2.4 3.0	2.0 2.4 3.0	2.0 2.4 2.9	2.0 2.4 2.9	2.6 3.0	2.2 2.6 3.0	2.0 2.6	2.4 3.0	ter and Co.
$(\rho t)^{E}_{2}$ $(\mu g/cm^{2})$	1	1	$\begin{array}{c} 45.7 \pm 1.1 \\ 46.9 \pm 1.2 \\ 44.9 \pm 1.8 \end{array}$	$57.5 \pm 1.2 \\ 56.9 \pm 1.1 \\ 56 \pm 2$	$\begin{array}{c} 62.1 \pm 1.9 \\ 60.8 \pm 1.8 \\ 63.1 \pm 25 \end{array}$	$\begin{array}{c} 60.2 \pm 1.8 \\ 61.5 \pm 1.8 \\ 60 \pm 2 \end{array}$	1	1	ted by MicroMat
roton energy (MeV)	1	1	2.0 2.4 3.0	2.0 2.4 3.0	2.0 2.6 3.0	2.0 2.6 3.0	1	1	s M = Values quo
Element of P interest	Dy	Υb	м	Au	Pb	Bi	Th	Ŋ	perimental values
Target	DyF <sub>3</sub>	YbF <sub>3</sub>	W0 <sub>3</sub>	Au	Pb	Bi	ThF 4	UF 4	E = Ex

141

Table 5.5. Measured areal densities of carbon backed targets.

## 5.7.1 L shell X-Ray Production Cross Sections

For a thin elemental target  $(Z_2)$  of thickness, t, and atomic density, n, the L x-ray yield,  $Y_{L_j}$  produced by N<sub>p</sub> charged particles  $(Z_1)$  impinging normally on the target at a given energy (E), is related to the appropriate L<sub>j</sub> x-ray production cross section,  $\sigma_{L_j}^{x}$ , and is given by

$$Y_{Lj} = N_p n t \sigma_{Lj}^{X}$$
 5.12

where j represents an L x-ray group transition,  $\alpha$ ,  $\beta$  or  $\gamma$ , or an individual transition such as  $\ell$ . Expression 5.12 assumes that the x-rays are emitted isotropically and the target is thin enough to ensure that self-absorption of the x-rays and variation of  $\sigma_{Lj}$  in the target is negligible. In the present experimental arrangement the target is at 45° to the beam axis (subsection 5.2.4) and the number of x-rays detected are limited by the detector solid angle,  $\Omega$ , and thus equation 5.12 becomes

$$Y_{Lj} = N_p n t \sigma_{Lj}^{X} \frac{\Omega}{4\pi} \sqrt{2}$$
 5.13

Since  $n = N_0 \rho / A_2$ 

$$Y_{Lj} = \frac{N_p N_o \rho t \sigma_{Lj} \Omega \sqrt{2}}{A_2 4\pi} 5.14$$

where  $N_0$  is the Avogadro's number and  $A_2$  is the target atomic mass. The term  $\rho t$  is usually referred to as the areal density of the target.

Euqation 5.14 has to be corrected for the attenuation suffered by the x-rays in the 50  $\mu$ m melinex chamber exit window and 2.5 cm of air before reaching the Si(Li) detector and for the Si(Li) detector efficiency, thus

$$Y_{Lj} = \frac{N_p N_0 \rho t \sigma_{Lj}^X \Omega}{A_2 4 \pi} \sqrt{2} \epsilon_j C_{Lj}$$
 5.15

where  $\boldsymbol{\epsilon}_{L_j}$  and  $\boldsymbol{C}_{L_j}$  are the detector efficiency and the total absorption

correction for the L<sub>j</sub> x-rays. By rearranging 5.15  $\sigma_{Lj}^{X}$  can be isolated,  $\sigma_{Lj}^{X} = \frac{Y_{Lj} A_2 4\pi}{N_p N_0 \rho t \Omega \sqrt{2} \epsilon_{Lj} c_{Lj}}$ 5.16

The importance of correcting for the variation of the x-ray production cross section in the target for low energy  $\alpha$ -particles was indicated in section 5.3. Applying this correction given by equations 5.2 to 5.16 we arrive at

$$\sigma_{L_j}^{X} = \frac{Y_{L_j} A_2 4\pi}{N_p N_0 (\rho t) \Omega \sqrt{2} \varepsilon_{L_j} C_{L_j}} \left[1 - \frac{a t n \varepsilon(E)}{2E}\right]^{-1} 5.17$$

L shell x-ray production cross section were evaluated from the above equation.  $Y_{Lj}$  were determined with the aid of a spectrum fitting programme, discussed in subsection 5.7.3. The determination of N<sub>p</sub>, pt and  $\varepsilon_{Lj}$  has already been addressed in sections 5.4, 5.6, and 5.5 respectively and the measurement of  $\Omega$  and the airpath in subsection 5.4.2. The atomic parameters, A<sub>2</sub> and N<sub>0</sub> and the mass densities,  $\rho$ , were obtained from Tennet (1978). The total x-ray absorption correction, CL<sub>j</sub>, is given by

$$C_{L_{j}} = \exp \left[-\left(\frac{\mu}{\rho}\right)_{air} (\rho t)_{air} - \left(\frac{\mu}{\rho}\right)_{M} (\rho t)_{M}\right]$$
 5.18

where M represents the melinex window. The mass absorption coefficients,  $\mu/\rho$ , for melinex and air were calculated using the mixture rule (equation 2.15).  $\mu/\rho$  values for the individual constituents of air and melinex were extracted from Storm and Israel (1970). To facilitate calculation of  $\sigma_{L_j}^{\chi}$  logarithmic polynomials of the form  $\ln \left(\frac{\mu}{\rho}\right) = i \sum_{i=0}^{5} a_i \left[\ln(E_{\chi})\right]^i$ 5.19

were fitted to the values of  $\mu/\rho$  for x-ray energies (E<sub>X</sub>) between 3 - 30keV employing the linear least square method.  $a_i$  represents the least square coefficients and are listed in table 5.6 for melinex and air along with the values of the regression correlation coefficient R<sup>2</sup>

Table 5.6. Least square coefficents, a<sub>i</sub>, for polynominal fits to mass absorption coefficients of melinex and air (equation 5.19).

Coefficients	Melinex	Air	
a <sub>0</sub>	13.1642	5.2206	
a <sub>1</sub>	-16.7939	3.7207	
a <sub>2</sub>	14.4835	-5.3016	
a <sub>3</sub>	-7.2330	2.0064	
a4	1.7124	-0.3713	
a <sub>5</sub>	-0.1551	0.0268	
R <sup>2(+)</sup>	0.9999	0.9999	

+  $R^2$  = Coefficient of regression (equation 5.4).

(equation 5.4). The fact that the values of  $R^2$  are very nearly unity indicates the excellent correlation between the regression model (equation 5.19) and the mass absorption coefficient data. Discussion of experimental x-ray production cross sections and their comparison with the ECPSSR theory is contained in chapter 6. The x-ray transitions, for which the cross sections were measured, for each target will also be indicated in that chapter. The uncertainties in  $\sigma_{Li}^{X}$  are discussed in subsection 5.7.4.

5.7.2 L shell Ionisation Cross Sections

L-shell x-ray production cross sections can be related to the individual L subshell ionisation cross sections,  $\sigma_{Li}$  (i = 1, 2, 3), in terms of the atomic parameters discussed in chapter 2. Relationships for the major L shell x-ray transitions are

$$\sigma_{L\ell}^{X} = \omega_{3} \left[ \sigma_{L_{1}} (f_{12} f_{23} + f_{13} + f_{13}') + \sigma_{L_{2}} f_{23} + \sigma_{L_{3}} \right] \frac{S_{3\ell}}{S_{3}}$$
 5.20

$$\sigma_{L_{\alpha}}^{X} = \omega_{3} \left[ \sigma_{L_{1}} (f_{12}f_{23} + f_{13} + f_{13}') + \sigma_{L_{2}}f_{23} + \sigma_{L_{3}} \right] \frac{S_{3\alpha}}{S_{3}}$$
 5.21

$$\sigma_{L\beta}^{X} = \omega_{1} \quad \sigma_{L1} \frac{S_{1}\beta}{S_{1}} + \omega_{2} \left[ \sigma_{L_{1}}f_{12} + \sigma_{L_{2}} \right] \frac{S_{2}\beta}{S_{2}} + \omega_{3} \left[ \sigma_{L_{1}} \left( f_{12}f_{23} + f_{13} + f_{13}^{\prime} \right) + \sigma_{L_{2}} f_{23} + \sigma_{L_{3}} \right] \frac{S_{3}\beta}{S_{3}} \qquad 5.22 \sigma_{L\gamma}^{X} = \omega_{1}\sigma_{L_{1}} \frac{S_{1}\gamma}{S_{1}} + \omega_{2} \left[ \sigma_{L_{1}}f_{12} + \sigma_{L_{2}} \right] \frac{S_{2}\gamma}{S_{2}} \qquad 5.23$$

where  $\omega_i$  (i = 1, 2, 3) is the fluorescence yield for subshell L<sub>i</sub>, f<sub>ik</sub> are the Coster-Kronig nonradiative transitions, f'<sub>13</sub> is the radiative Coster-Kronig transition, S<sub>i</sub> is the total emission rate for subshell L<sub>i</sub> and S<sub>ij</sub> is the emission rate for x-ray transition or group of transitions, denoted by j, to subshell L<sub>i</sub>. The major L shell x-ray transitions pertinent to the ongoing discussion, previously shown schematically in figure 2.1, are illustrated again in figure 5.18. It would appear that by substituting the experimental L<sub>j</sub> x-ray production



(Gray 1974).

cross sections,  $\sigma_{L_1}^{x}$ , into the above relations  $\sigma_{L_1}$  may be determined by solving them. These equations, however, are not linearly independent and thus are illconditioned. Depending on the degree of illconditioning relatively small changes in  $\sigma_{Li}^{X}$  can yield disproportionately different values of  $\sigma_{Li}$  and may even lead to unphysical solutions (Madison et al 1974, Cohen 1980 and Sokhi and Crumpton 1982). In order to evaluate  $\sigma_{Li}$ , therefore, expressions have to be developed which are well conditioned and yield stable soltuions. Cohen (1980) has used expressions, involving L subshell x-ray production cross sections in terms of the effective fluorescence yield for the L shell and the total ionisation cross section, to determine  $\sigma_{Li}$ . His approach entails the use of the  $L_{\rm n}$  and  $L_{\rm g}$  x-ray yields which are relatively weak, the former being the weaker transition, and thus involve large statistical uncertainties. An alternative is to extract from the partially resolved Ly group the Ly1 and Ly23 components with the aid of a spectrum fitting program. Since the  $L_{\gamma_{2,3}}$  transitions are to the  $L_1$ subshell contributions from the other subshells, through Coster-Kronig transitions, obviously do not arise and thus  $\sigma_{L\gamma_{2\,3}}$  can be directly related to  $\sigma_{L_1}$  through the simple relation

$$\sigma_{L\gamma_{23}} = \omega_1 \sigma_{L_1} \frac{S_1\gamma_2}{S_1}$$

5.24

Employing tabulated values for the fluorescent yields (Krause 1979) and emission rates (Scofied 1974b)  $\sigma_{L_1}$  can be determined from 5.24. The  $L_{\gamma_1}$  yield can now be used to evaluate  $\sigma_{L_2}$ .  $L_{\gamma_1}$  is contaminated on the low energy side by the  $L_{\gamma_1}$  transition, also to the  $L_{\gamma_5}$  subshell. The  $L_{\gamma_5}/L_{\gamma_1}$  ratio is typically around 3.5% (Scofield 1974b) and has to be accounted for. The expression for  $L_{\gamma_{15}}$  in terms of  $\sigma_{L_1}$  and  $\sigma_{L_2}$  is

$$\sigma_{L_{\gamma_{15}}}^{X} = \omega_{2} \left( \sigma_{L_{1}} f_{12} + \sigma_{L_{2}} \right) \frac{S_{2\gamma_{15}}}{S_{2}} 5.25$$

These values for  $\sigma_{L_1}$  and  $\sigma_{L_2}$  can then be substituted into equation 5.21 to extract  $\sigma_{L_2}$ .

Experimental L subshell ionisation cross sections reported in this thesis have been evaluated with this approach. This approach, however, requires some qualifying remarks. Firstly,  $L_{\gamma_{23}}$  and  $L_{\gamma_1}$ transitions are relatively weak transitions and counting times have to be sufficiently long to ensure reasonable statistical precision. It is for this reason that carbon backed targets, which can sustain high beam currents for relatively long periods, were employed. These targets yielded precisions of better than 5% for  $L_{\gamma_{23}}$  group even at low particle energies. The statistics are slightly improved by including the yield of the  $L_{\gamma_{44}}$ , transitions, also to the L<sub>1</sub> subshell. Secondly,

a complication arises in that the  $L_{\gamma_{23}}$  is contaminated by contributions from the  $L_{\gamma_8}$  transition and, for  $Z_2 \ge 71$ , by the  $L_{\gamma_6}$  transition. The importance of these transitions is made clear by considering, for example, Au bombarded by 3 MeV protons where  $\sigma_{L\gamma_6}^{\text{ECPSSR}} / \sigma_{L\gamma_{23}}^{\text{ECPSSR}} = 50\%$  and  $\sigma_{L\gamma_8}^{\text{ECPSSR}} / \sigma_{L\gamma_{23}}^{\text{ECPSSR}} = 3.7\%$ . These contributions may be estimated by comparing it with the  $L_{\gamma_{15}}$  group and employing theoretical radiative rates. The  $L_{\gamma_{23}}$  contribution is thus obtained from

$$L\gamma_{23} = L\gamma_{2368} - L\gamma_{15} \frac{S_2\gamma_{68}}{S_2\gamma_{15}}$$
 5.26

Datz et al (1974) considered only the  $L\gamma_6$  contribution to the  $L\gamma_{23}$ peak and obtained it magnitude from the  $L\gamma_1$  transition. The obtained an experimental value of  $0.125 \pm 0.01$  for the ratio  $S_2\gamma_6/S_2\gamma_1$  for proton impact on Au by comparing the response of  $L\gamma_{236}/L\gamma_1$  and  $L\gamma_{44}/L\gamma_1$  at different proton energies. This was not possible in the present study since the  $L\gamma_{44}$  statistics were poor. Instead the theoretical values for the ratio from Scofield 1974b were employed. In the case of Au Scofield's value of  $S_2\gamma_6/S_2\gamma_1$  is 0.094 which compares favourable with the value obtained by Datz et al (1974). Taking into

account  $L\gamma_8$  and  $L\gamma_5$  transition the value of the ratio  $S_{2\gamma_{68}}/S_{2\gamma_{15}}$ becomes 0.098. The expressions employed for determining the experimental values of  $\sigma_{Li}$  are summarised below:

$$\sigma_{L_{1}} = \frac{S_{1}}{S_{1}\gamma_{2344}}, \frac{\sigma_{L}\gamma_{2344}}{\omega_{1}}$$
 5.27

$$\sigma_{L_2} = \frac{S_2}{S_2 \gamma_{15}} \frac{\sigma_{L \gamma_{15}}}{\omega_2} - f_{12} \sigma_{L_1}$$
 5.28

$$\sigma_{L_3} = \frac{S_3}{S_{3\alpha}} \frac{\sigma_{L\alpha}}{\omega_3} - (f_{13} + f_{13}' + f_{12}f_{23})\sigma_{L_1} - f_{23}\sigma_{L_2}$$
 5.29

The method adopted for extracting the semi-resolved components of the Ly group is described in detail in subsection 5.7.3. The values of  $\sigma_{\text{Li}}$ , obtained from the above relations, for the target - projectile combinations of interest are discussed in chapter 6 and the uncertainties are dealt with in subsection 5.7.4.

## 5.7.3. Spectrum Fitting

Contemporary Si(Li) x-ray detectors are unable to resolve all the individual x-ray transitions to the L-shell. The energy resolution is typically 170eV at 5.898 keV and consequently, groups of several x-ray lines are observed in spectra obtained with these detectors. Figures 5.3 and 5.4 illustrate the  $L_{\alpha}$ ,  $L_{\beta}$  and  $L_{\gamma}$  groups for Yb and Bi obtained with 3 MeV alpha and proton impact respectively. In the  $L_{\alpha}$  peak the individual components,  $L_{\alpha_1}$  and  $L_{\alpha_2}$ , cannot be resolved whereas the components of the  $L_{\beta}$  and  $L_{\gamma}$  group may be partially resolved depending on the atomic number of the target. The importance of the individual  $L_{\gamma}$  components, required for determining L subshell ionisation cross sections was highlighted in subsection 5.7.2. These components may be resolved sufficiently by adopting a wavelength dispersive detection system which employs a crystal spectrometer. A severe limitation with this approach is the very low detection efficiency relative to the Si(Li) detector. The comparatively high

cost further outweighs the advantages offered by such a system.

The usual procedure for extracting the required components of a partially resolved x-ray group is to mathematically 'fit' suitable functions which approximate the Si(Li) detector response. Ideally, the response of a Si(Li) detector to a monoenergetic x-ray would be a delta function. In practice the effects of incomplete charge collection, bulk trapping and detector resolution produces an output which can be described approximately by a Gaussian distribution with a certain amount of skewness (Jenkins et al 1981). In the case of inner-shell x-rays the peak is further broadened by the fact that these x-rays may consist of bi or polyenergetic lines of similar energies, however, the essentially Gaussian profile still applies. The x-ray peak rests on a background which can be adequately described by a straight line function in the x-ray energy range of interest.

Detail studies of fitting non-linear mathematical functions to the response of energy dispersive detectors have been conducted by Gunnink and Niday (1971), Gunnink (1975), McNelles and Campbell (1975), Phillips and Marlow (1976), Horch and Campbell (1977) and Campbell and Jorch (1979). Exponential tailing and stepping functions are usually adopted to simulate the low energy electronic distortions of the main Gaussion. Such a description can be extended to L x-ray spectra containing several fully or partially resolved peaks from which areas of individual peaks can be extracted. As an alternative to the Gaussian description Ingamells and Fox (1979) have utilised Poisson probability functions to determine individual components of composite peaks. With regard to the present study corrections for the distortion of the L x-ray peaks were not found to be necessary. The L x-ray spectra are, therefore, approximated solely by Gaussian distributions super-imposed essentially on a linear bremsstrahlung. The remaining part of this subsection

deals with the fitting procedure adopted in this work and based on the nonlinear least square method. Mathematical principles, on which this method relies, are well established and thus have been omitted. The reader interested in the theory of nonlinear regression, however, is referred to Bevington (1969) and Draper and Smith (1981).

An x-ray spectrum of m channels consisting of q Gaussian peaks, resting on a linear background, may be described by the nonlinear analystic function  $f(\underline{x}_i, \underline{b})$ ,

$$f(\underline{x}_{j}, \underline{b}) = b_{1} + b_{2}x_{j} + \sum_{i=1}^{q} b_{2+i} \exp\left[-(\underline{x}_{j} - b_{3+i})^{2}\right]$$

$$(j = 1, 2, ..., m)$$
5.30

where the independent variable, x<sub>j</sub>, represents the j<sup>th</sup> channel number and b<sub>u</sub> (u = 1, 2, ..., p where p = 3q + 2) are the regression parameters. Thus  $f(\underline{x}_j, \underline{b})$  is the fitted value of the actual number of x-ray counts in channel x<sub>j</sub> denoted by Y<sub>j</sub>. In the exponential term in equation 5.30 b<sub>2+i</sub> represents the amplitude of the peak, b<sub>3+i</sub> denotes the peak centroid and b<sub>4+i</sub> equals  $2\sigma_i^2$  where  $\sigma_i$  is the standard deviation of peak i. The regression problem entails computing estimates of the parameters b<sub>u</sub> which will minimise the weighted sum of the squares of residuals, known as 'chi square',

$$\chi^{2} = \prod_{j=1}^{m} \left[ \frac{Y_{j} - f(\underline{x}_{jm} \underline{b})}{\sigma_{j}^{2}} \right]^{2}$$
5.31

where the residuals are weighted by the variances,  $\sigma_j^2$ , associated with each data point. Since x-ray counting experiments follow a Poisson distribution  $\sigma_j^2$  can be estimated simply by the counts in channel j, denoted by Y<sub>j</sub>. Normalising 5.31 by the number of degrees of freedom v, gives the reduced chi-square,  $\chi_r^2$ 

$$\chi_{r}^{2} = \frac{\chi^{2}}{\nabla}$$
 5.32

 $\nu$  is obtained by subtracting the number of free parameters from the

number of data channels (m). Since the height, H<sub>i</sub>, of a Gaussian distribution depends on its standard deviation,  $\sigma_i$ , through the relation

$$A_i = \frac{A_i}{\sigma_i (2\pi)^2}$$
 5.33

where A<sub>j</sub> is the i<sup>th</sup> peak area and is equivalent to Y<sub>Lj</sub> in equation 5.17, there are 2 free parameters per Gaussian peak (Bevington 1969). The total number of free parameters is, therefore, 2(background) + 2q (q = number of Gaussian peaks) and thus v = m - 2 - 2q. If the regression function,  $f(\underline{x_j}, \underline{b})$ , is a good approximation to the measured data then  $\chi_r^2$  has a vlaue of unity or near unity. The larger the value of  $\chi_r^2$  the less appropriate is the fitting function. A  $\chi_r^2$  value of less than one does not indicate an improvement of the fit, it is merely a consequence of the finite uncertainty in the determination of the variance of the fit (Bevington 1969).

To find the least square estimate of <u>b</u> equation 5.30 needs to be differentiated and set to zero, giving the minimum value of  $\chi^2$ ,

$$\frac{\partial \chi^2}{\partial \underline{b}} = \int_{j=1}^{\underline{m}} \left[ \frac{\gamma \mathbf{j} - \mathbf{f}(\underline{x}\mathbf{j}, \underline{b})}{\sigma_{\mathbf{j}}^2} \right] \left[ \frac{\partial \mathbf{f}(\underline{x}\mathbf{j}, \underline{b})}{\partial \mathbf{b}_{\mathbf{u}}} \right] = 0$$
5.34

Equation 5.34 provides p nonlinear normal equations which have to be solved for <u>b</u>. This, however, is complicated and it is very difficult to obtain the solution directly. Instead, iterative techniques have to be employed, either to 'search' for the minimum value of  $\chi^2$  or to solve the equations analytically.

Chi-square is considered a continuous function of the nonlinear parameters  $b_u$  and describes a hypersurface in q-dimensional space (Bevington 1969).  $\chi^2$  is minimum at the point defined by the least square estimates. For a linear model the contours of  $\chi^2$  in parameter - space, <u>b</u>-space, consist of concentric ellipses, where as for a non linear model, such as described by equation 5.30, the contours may

become distorted and often highly elongated (Draper and Smith 1981). There are several methods with varying degrees of sophistication which can be used for searching for the minimum value of  $\chi^2$  in parameter space. Details of these methods can be found in Draper and Smith (1981), Bevington (1969) and Schamber (1981). The main disadvantage of these methods is that the solution converges very slowly when the search approaches the  $\chi^2$  minimum particularly when  $\chi^2$  contours are attenuated (Draper and Smith 1981).

As an alternative to the 'search' method analytical techniques may be employed to compute the least square parameters. A major technique, known as the 'linearisation' or 'Taylor series' method improves initial estimates of the parameters, denoted by  $\underline{b}_0 = (b_{10}, b_{20}, \ldots, bp_0)$ ', in successive iterations by using the results of linear least squares. This method has been found to be superior to those which involve searching for the minimum value of  $\chi^2$  regarding speed of convergence and reliability of the final solutions (Draper and Smith 1981, Bevington 1969 and Schamber 1981). Consequently this method has been adopted for the fitting of L shell x-ray spectra in this study.

In order to determine the least square values of the nonlinear parameters <u>b</u>, initial estimtes, <u>b</u><sub>0</sub>, for these parameters are required. Initial values for the peak centroids and variances were estimated from equation 5.3 and 5.6. Inputing these values into the regression function (equation 5.30) transforms it into a linear form. The remaining unknown parameters, namely those for the background and the peak heights, were determined with the normal linear least square method.

Expanding  $f(\underline{x}_j, \underline{b})$  in terms of a Taylor series to first order about the point  $b_0$ , when b is close to  $\underline{b}_0$ , we have

$$f(\underline{x}_{j}, \underline{b}) = f(\underline{x}_{j}, \underline{b}_{0}) + \sum_{u=1}^{p} \left[\frac{\partial f(\underline{x}_{j}, \underline{b})}{\partial b_{u}}\right] (b_{u} - b_{u_{0}})$$

$$5.35$$

Adopting the following notation

$$f_{j}^{0} = f(x_{j}, b_{0})$$

$$\delta b_{u}^{0} = b_{u} - b_{u_{0}}$$

$$Z_{uj}^{0} = \left[\frac{\partial f(x_{j}, b)}{\partial b_{u}}\right]_{b} = b_{0}$$
5.36

the regression model may be written approximately as

$$Y_{j} - f_{j}^{o} = u_{\Xi_{1}}^{P} \delta b_{u}^{o} Z_{uj}^{o} + e_{j}$$
 5.37

where  $e_j$  is the 'error' and is the deviation of  $Y_j$  from the regression curve. It is noted that the model is of a linear form in  $\delta b_u^0$ , the validity of which is true only for the selected first order approximation. Chi-square for the model is given by

$$\chi^{2} = \sum_{j=1}^{m} \frac{1}{\sigma_{j}^{2}} \left[ Y_{j} - f_{j}^{0} - \sum_{u=1}^{p} Z_{uj}^{0} \delta b_{u}^{0} \right]^{2}$$
 5.38

Applying linear least square theory  $\chi^2$  is minimised with respect to  $\delta b^{\hat{u}}$  and the p normal equations required for determining  $\delta \underline{b}^0$  in matrix notation are

$$\underline{C}^{\circ}\delta\underline{b}^{\circ}=\underline{B}^{\circ}$$
5.39

where

$$C^{\circ} = \begin{bmatrix} m \\ j \stackrel{n}{\leq}_{1} \frac{1}{\sigma_{j}^{2}} Z^{\circ}_{uj} Z^{\circ}_{uj} \end{bmatrix} \delta b^{\circ}_{u}, \text{ and}$$

$$B^{\circ} = \prod_{j \stackrel{n}{\leq}_{1}} \frac{1}{\sigma_{j}^{2}} Z^{\circ}_{uj} (Y_{j} - f_{j}^{\circ}) \qquad 5.40$$

where prime denote the transpose and u = 1, 2, ..., p.  $\underline{C}^{0}$  is known as the 'curvature' matrix. The partial derivatives were evaluated using the 'centred difference' approximation (Himmelblau 1972),

$$\left[\frac{\partial f(x_j, \underline{b})}{\partial b_u}\right]_{b = b_0} = \frac{f(x_j, b_u + \Delta b_u) - f(x_j, b_u - \Delta b_u)}{2\Delta b_u}$$
 5.41

where  $\Delta b_{\rm u}$  is a small increment. A value of  $0.002b_{\rm u}$  yields derivatives of sufficient precision and was adopted in the calculations. The improvements,  $\delta b_{\rm u}^0$ , of the initial parameters are arrived at by solving the normal equations. The revised estimates after s iterations are given by

$$b_{usth} = b_{us} + \delta b_{u}^{S} \qquad 5.42$$

where s = o for the initial parameters. From the revised estimates, bu<sub>1</sub> (s = o for the first iteration),  $f_j^1$  and  $Z_{uj}^1$  are generated and substituted into equation 5.39 to determine  $\delta b_u^1$  lead to the next revised estimates  $b_{u2}$  and so on. Chi-square is calculated for each set of parameters at the end of every iteration. The improvements of the least square estimates after each iteration is indicated by the convergence of  $\chi^2$ ; eventually to its minimum value.

Provided that the initial estimates and the subsequent value after each iteration lie inside a region where the  $\chi^2$  hypersurface is approximately parabolic the linearisation method coverges quite rapidly to the minimum  $\chi^2$  value. On the other hand if the estimates lie far from the least square values the method may not converge at all, indeed, it may even diverge (Draper and Smith 1981, Bevington 1969) implying that the  $\chi^2$  surface is so poorly approximated that the linear approximation breaks down (Schamber 1981). However, it is not always possible to arrive at good initial estimates and to reduce the possibility of divergence two modification have to be introduced into the iterative procedure.

(i) The improvements,  $\delta b_{u}^{s}$ , calculated after each iterations are 'damped' by an appropriate amount (Marquardt et al 1961), that is,  $\delta b_{u}^{2}$  is multiplied by a factor  $\kappa^{2} \leq 1$  from which the new estimates are determined.

 $b_{us+1} = b_{us} + \kappa^{S} \delta b_{u}^{S}$ 

A numerical value for  $\kappa^{S}$  is chosen which ensures covergence, that is,

$$\chi^2(s+1) < \chi^2(s)$$
 5.44

and as convergence is approached,  $\kappa^{S}$  is increased until  $\kappa^{S} \approx 1$ , expediting the iterative procedure. An initial value of 0.4 has been suggested by Schamber (1981). In the present work, however, this value was found to be too large to initiated convergence and a much smaller value of 0.001 was adopted for the first iteration. The value is increased by this amount for successive iterations until convergence seems assured. 10 iterations seemed sufficient for the problems encounted in this study. Byond this iteration  $\kappa^{S}$  is increased by larger amounts determined from the simple empirical expression

 $\kappa^{S+1} = \kappa^{S} + 0.01(s - 10)$  5.45

until  $\kappa^{S} = 1$ .

(ii) In practice failure to converge is not completely eliminated by introducing 'damping' into the fitting technique (Marquardt 1963). To reduce futher the likelihood of divergence Marquardt (1963) proposed an algorithm which greatly enlarges the number of problems that can be successfully solved by nonlinear estimation (Draper and Smith 1981). Marquardt (1963) formulated the required algorithm by combining the properties of the gradient-search and the linearisation methods. In the first method all the parameters in the proposed model are simultaneously incremented by an amount that is adjusted to ensure that the method travels along a 'direction of steepest desent'. Although this method does not converge rapidly when in the immediate vicinity of the  $\chi^2$  minimum it is, however, able to approach the minimum when the estimates are far from their least square values. The linearisation

method on the other hand, coverges quite rapidly but only when the parameters are not distant from their least square estimates. Marquardt(1963) was able to reach a compromise between the two methods in his algorithm. The algorithm causes the convergence of the iterative procedure by increasing the magnitude of the diagonal terms of the curvature matrix by an amount  $\lambda^{S}$ ,

$$(C^{S} + \lambda^{S}I)\delta b^{S} = B^{S}$$
 5.46

here I is the identity matrix. Solving for  $\delta \underline{b}^{S}$  and using equation 5.43 the improved estimates are determined.  $\lambda^{S}$  is selected so as to ensure the validity of the inequality 5.44. The magnitude of  $\lambda^{S}$  should be small enough to allow rapid convergence when in the neighbourhood of  $\chi^{2}$  minimum and large enough to initiate converge successfully even when distant from the least square values. The algorithm consists of several logical statements that compare the sum of residual,  $\Phi$ , defined by

$$\Phi = \sum_{j=1}^{m} \left[ Y_j - f(\underline{x}_j, \underline{b}) \right]^2$$
 5.47

for iteration s and s+1. In the present study the fitting procedure is weighted according to the variance  $\sigma_j^2$  and as a result  $\chi^2$  are incorporated into Marquardt's (1963) algorithm. A modification of the algorithm concerns the initial value of  $\lambda^0$  (s =  $\circ$ ). A value of  $10^{-2}$ has been suggested by Marquardt (1963). This value was found to be unnecessarily large and was reduced to  $10^{-5}$ . The algorithm as applied to this work is stated below:

1. Let 
$$\lambda^{\circ} = 10^{-3}$$

2. Compute  $\chi_1^2(s)$  for  $\lambda^{S-1}$  and  $\chi_2^2(s)$  for  $\lambda^{S-1}/10$  with corresponding <u>b</u> and <u>b</u>' respectively.

3. If  $\chi_2^2(s) \le \chi^2(s-1)$  let  $\lambda^s = \lambda^{s-1}/10$  with b' as the improved estimates where  $\chi^2(s-1)$  is chi-square of the previous iteration

4. If  $\chi_2^2(s) > \chi^2(s-1)$  and  $\chi_1^2(s) \le \chi^2(s-1)$  let  $\lambda^s = \lambda^{s-1}$  with <u>b</u> as the improved estimates.

5. If  $\chi_2^2(s) > \chi^2(s-1)$  and  $\chi_1^2(s) > \chi^2(s-1)$  increase  $\lambda^{S-1}$  by succesive multiplication by  $10^{\omega}$  with  $\omega = 2$  (Marquardt (1963) suggests  $\omega = 1$ ) and  $\kappa = \kappa/10$  until  $\chi_3^2(s) \le \chi^2(s-1)$  where  $\chi_3^2$  is chi-square for increased  $\lambda^{S-1}$  and decreased  $\kappa$  adopting improved estimates for the smallest  $\omega$ . 6. Let  $\lambda^S = \lambda^{S-1}$ .  $10^{\omega}$ .

Condition 5 was seldom encountered and only at the final stages of the iterative procedure. Iterations were terminated when

 $\chi^2(s+1) - \chi^2(s) \le \psi$  5.48 A value for  $\psi = 0.0001$  was adequate to stabilise the least square

estimates.

A software package was written in Fortran 77 as a part of this study using the University's Harris 800 mainframe computer for fitting the accumulated L shell x-ray spectra. The package entitled 'SPECTRUM' is based on the damped linearisation technique described above and incorporates Marquardt's algorithm. Two routines, entitled 'GAUSS' and 'REFINE' are included in the package and are utilised by SPECTRUM to solve the least square normal equations. GAUSS initially solves the equations using Gaussian elimination with pivotal condensation and REFINE corrects these solutions for rounding-off errors by iterative refinement (Buckingham 1962 and Gerald 1978). A hard copy of the package is presented in appendix D. SPECTRUM is capable of fitting simultaneously 20 Gaussian peaks, superimposed on a linear or a higher order background, contained in a region of 300 channels. The number of peaks and the spectra region were restricted by the allocated computer memory. Complete L x-ray spectra were fitted in one execution of the program. Figure 5.19 illustrates a typical fit to W L x-ray spectrum obtained by 2.9MeV alpha impact. Less than 30 iterations



were required to obtain the least square values of the regression parameters. Chi square values of around and often less than 1.5 were achieved. Peak areas obtained by fitting composite spectra using equation 5.33 were checked by fitting individual L x-ray groups and agreement of less than 1%, even for the relatively weak  $L_{g}$  and  $L_{\gamma}$ transitions, was attained. A fit to the  $L_{\gamma}$  group of Pb bombarded by 3.0 MeV protons, presented in figure 5.20 shows the individual  $L_{\gamma}$  components. As mentioned previously in subsection 5.7.2. statistics for  $L_{\gamma_{5}}$  and  $L_{\gamma_{4+1}}$ , are poor making their yields, obtained by fitting the  $L_{\gamma}$  group, unreliable. Consequently the  $L_{\gamma_{5}}$  and  $L_{\gamma_{4+1}}$ , were appropriate, were summed with the  $L_{\gamma_{1}}$  and  $L_{\gamma_{23}}$  components respectively.

The performance of SPECTRUM is demonstrated by figures 5.21 and 5.22 which show the improvement of the peak parameters and the reduction of  $\chi^2_r$  with iteration for the Bi L<sub>l</sub> peak obtained by impact of 3MeV deuterons. Figure 5.23 shows the fit obtained with the initial estimates of <u>b</u>, its improvement at an itermediate stage of the iterative procedure and the final fit obtained at  $\chi^2_r$  minimum for the L<sub>l</sub> peak.

Uncertainty in the actual area, A<sub>i</sub>, of the ith peak is simply given by  $\sigma_i$  which can be estimated by Ai<sup> $\frac{1}{2}$ </sup>.  $\sigma_i$ , however, reflects the uncertainty of the measured data as a sample of the parent distribution and does not include the additional uncertainty in A<sub>i</sub> introduced by the regression procedure. For  $\chi_r^2 \leq 1$ , as was invariably the case, the uncertainty in A<sub>i</sub> is essentially that of the parent distribution since the effect of the fit on  $\sigma_i$  is minimal (Bevington 1969). On the other hand, for cases where  $\chi_r^2 > 1$  the uncertainty due to the fitting procedure is not negligibel and has to be included in  $\sigma_i$ . The uncertainty introduced by the regression is of the order of  $\chi_r^2$  and the total uncertain in Ai can be estimated, according to Bevington (1969), by



161

the dashed curve indicates the individual components.
















$\sigma_i \chi_r^2$ .  $\chi_r^2$  in the present work was seldom greater than 1.5 and so at worst, the uncertainty in A<sub>i</sub> is increased by a factor between 1.5 - 2.0. 5.7.4 Uncertainties in the Measured Cross Sections

The major sources of uncertainties in the cross section measurements employing carbon backed targets are quantified and summarised below:

(i)	Projectile energy (E)	1.2 - 2.8%
(ii)	Charge collection (Mp)	1%
(iii)	Target areal density (pt)	≤1.5%
(iv)	Si(Li) detector efficiency $(E_{Lj})$	2 - 3.5%
(v)	X-ray absorption correction $(C_{Lj})$	1 - 5%
(vi)	Si(Li) detector solid angle $(\Omega)$	1.8%

(vii) Counting statistics including the effects of

fitting (YLi)

≤10%

The effect of the uncertainties in the stopping power,  $\varepsilon(E)$ , is negligible on the measured x-ray production cross sections,  $\sigma_{Lj}$ , since it appears only in the correction factor (equation 5.17). The uncertainty in  $C_{Lj}$  depends on the x-ray energy. The values of the mass absorption coefficients in the tabulation of Storm and Israel (1970), which were used to evaluate  $C_{Lj}$ , are uncertain by 10% when the x-ray energy is less than 6keV and by 3% for higher energies. To determine the resultant uncertainty in  $\sigma_{Lj}^{X}$  the individual uncertainties, listed above, were combined quadratically. This yields uncertainties in  $\sigma_{Lj}^{X}$  in the range of 4 - 12%. Uncertainty of each value of  $\sigma_{Lj}^{X}$  are listed together with the absolute cross section values in appendix B.

Uncertainties, (i) - (iii) and (iv), which appear systematically in the  $\sigma_{Lj}^{x}$  calculations, disappear when considering ratios of x-ray production cross sections. Since the ratios are free from the systematic uncertainties their comparison with theory is usually

more informative than the comparison with absolute cross sections. Uncertainties in the ratios range from about 7% to 16% depending on the x-ray transitions and particle energy.

In the case of L subshell ionisation cross sections,  $\sigma_{Li}$ , the situation is complicated by the presence of  $\omega_i$ ,  $S_{ij}$  and  $f_{ik}$  (subsection 5.7.2). These parameters introduce systematic uncertainties in  $\sigma_{Li}$ . For the targets under consideration, uncertainty in  $\omega_i$ ,  $f_{ik}$  and  $S_{ij}$  may be up to 20%, 50% (Krause 1979) and 10% (Scofield 1974b) respectively. The philosophy adopted in this work is to recognise the existence of these uncertainties but to consider only those uncertainties which arise from the adopted experimental technique. Thus the uncertainties in  $\sigma_{Li}$  reflect purely the experimental precision of the measurements. This philosophy is also usually adopted in the literature relevant to this work. The final uncertainties in  $\sigma_{Li}$  range up to 12% for  $\sigma_{Li}$ , 10% for  $\sigma_2$  and 9% for  $\sigma_{L3}$ . These result in uncertainties are quoted for each  $\sigma_{Li}$  value in appendix B. 5.8. CALCULATION OF THEORETICAL CROSS SECTIONS

Tabulations compiled by Choi et al (1973) and Benka and Kropf (1978) have been employed in the present work to calculate L shell ionisation cross sections. Benka and Kropf (1978) have provided an interpolation formula to evalute the cross section value for any  $\theta_{Li}$  and  $n_L/\theta_{Li}^2$ , which lie inside the range of the tables. However, despite this, it is very tedious to calculate the cross sections since a large amount of interaction is required on the part of the user. The situation is worse in the case of the tables by Choi et al (1973) since an appropriate method for interpolation has not been suggested by the authors.

For these reasons polynomials were fitted to the data contained in both the tables. In the case of the tabulation of Benk and Kropf (1978) the data was transformed from the  $f(n_L/\theta_{Li}, \theta_{Li})$  format to the  $f(n_L/\theta_{Li}, \theta_{Li})$  form. This was necessary to obtain fits of adquate accuracy. A multiple regression polynomial of the form

$$\ln[f(n_{L}, \theta_{Li})] = a_{0} + \frac{n}{i\sum_{i=1}^{m}} a_{i} [\ln(n_{L})]' + \frac{m}{j\sum_{i=1}^{m}} a_{j+n} [\ln \theta_{Li}]^{j}$$
5.49

was fitted to  $f(n_L, \theta_{Li})$ . Several fits had to be performed to the data in order to deduce the ionisation cross section for the collision regimes under study. Typically n = m = 3 and agreement to within 0.1% was attained with the values of Benka and Kropf (1978). Values for R were practically unity for the fits. The agreement obviously compares well with the interpolation formula quoted by Benka and Kropf (1978) which reproduced their data to within 2%. Cross sections obtained by their interpolation formula and by fits of the form 5.49 were compared for proton impact of Dy and agreement to within 2.5% was observed. The situation was more complicated in the case of the tables by Choi et al (1973). Fits of the form 5.49 were inadequate and the strategy adopted was as follows. Polynomials of the form

$$\ln [f(n_1)] = \sum_{i=0}^{n} a_i [\ln(n_1)]^1$$
 5.50

were fitted to the tabulated data for several  $\theta_{Li}$  values. n depended on the number of data points and ranged between 2 - 5. Agreement with the tabulated values to less than 0.5% was achieved and typically  $R^2 = 0.9999$ . These fits were incorporated into the computer programme written in basic for calculating the ECPSSR cross sections. The programme substitutes the appropriate  $n_L$  value into the polynomials and calculates  $f(n_L)$  for the fixed  $\theta_{Li}$  values. A least square regression routine was

appended to the main programme which fitted a polynomial of the same form as 5.50, except that  $n_L$  is replaced by  $\theta_{Li}$ , to the  $f(\theta_{Li})$  values,  $n_L$  being fixed in this instance. The required  $f(n_L, \theta_{Li})$  was calculated from this resulting polynomial.

Wherever possible the compilation of Choi et al (1973) was used to evaluate cross sections for deuteron and alpha impact. For elements heavier than Au, however, the main parameters,  $\eta_{L}$  and  $\theta_{L\,i}$  , fall outside the ranges addressed by those authors for alpha impact. At this stage the choice available is either to omit comparison with theory or to somehow estimate the ECPSSR cross sections. In order to gain some insight at least into the theoretical descriptions of ionisation by alpha particles for heavy elements an attempt was made to determine approximate ECPSSR cross section values. To do this the tables of Benka and Kropf (1978) were employed. Although these authors caution against the use of their tables for any other projectile except protons, as noted in chapter 4 (section 4.2), it is hoped that the cross section values will approximate the 'true' ECPSSR values to a degree comparable to that of the experimental uncertainties. Values derived by this procedure for alpha particle bombardment of elements for which this problem does not arise, were compared with the values calculated from the tables of Choi et al (1973). The values obtained from the tables of Benka and Kropf (1978) were found to be smaller than those of Choi et al (1973) by about 10% at 1MeV and by about 3% at energies approximately 3MeV. These difference are indeed comparable to experimental uncertainties and imply that these value may be used to estimate the ECPSSR cross sections. It should be noted that the values of Benk and Kropf (1978) for proton impact are generally less than those of Choi et al (1973) by two percent especially at lower impact energies. This fact was highlighted in chapter 4(Section 4.2)

and may explain some of the observed differences for alpha particle impact.

This approach has also been adopted by Braziewicz et al (1984) who have encounted the same difficulties. Cohen (1981) has also extracted the ionisation cross sections for alpha particle bombardment of heavy elements from the tables of Benka and Kropf. (1978) but has not justified this approach.

The L x-ray production cross sections were obtained by substituting the ionisation cross sections for the appropriate collison regime into equations 5.20 - 5.23 stated previously in subsection 5.7.2. Theoretical L shell x-ray production and ionisation cross sections for the targets and projectiles under investigation are tabulated in appendix C.

## CHAPTER 6

# RESULTS AND DISCUSSION

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#### 6.1 INTRODUCTION

This chapter discusses the L shell x-ray production and ionisation cross sections measured in the present study. The measured cross sections are compared with the PWBA and the ECPSSR theories (Brandt and Lapicki 1981 and see chapter 4). Comparison is also made with recent measurements reported by other authors. It must be noted, however, that there appears to be a complete lack of published deuteron impact data peritent to this study. Consequently comparison of the present deuteron measurements is made only with the theories. With regard to incident alpha particles there are a few published measurements for the elements of interest and comparison has been made whenever the data was available in tabular form. Sokhi and Crumpton (1984)(appendix E) have published a tabulation of recent experimental L shell x-ray production and ionisation cross sections for proton impact with allows comparison to be made conveniently. However, even for protons there is a significant lack of relevant data.

The cross sections measured in the present work are presented graphically in this chapter while tabulated values are contained in appendix B. To facilitate the discussion ionisation cross section are considered before proceeding with the x-ray production cross sections. This approach is adopted because the latter may be understood in terms of the Li subshell ionisation cross sections. Finally, common features highlighted by measurements for the individual elements are discussed. 6.2 DYSPROSIUM ( $Z_2 = 66$ )

For dysprosium (Dy) LL, L  $_{\alpha+\eta}$ , L $_{\beta_{1346}}$ , L $_{\beta_{2715}}$ , L $_{\gamma_{15}}$  and L $_{\gamma^{23844}}$ ' transitions were measured for proton and deuteron impact. The Li subshell ionisation cross sections were deduced from L $_{\alpha+\eta}$ , L $_{\gamma_{15}}$  and L $_{\gamma_{23844}}$ ' x-ray transitions as outlined in section 5.7.2. It should be noted here that the L $_{\alpha}$  and L $_{\eta}$  transitions could not be resolved with

the experimental set-up employed in this study and consequently the Ln contribution had to be accounted for in expression 5.29.

### 6.2.1 Proton Impact Measurements

Total and individual Li subshell ionisation cross section,  $\sigma_{\mbox{Lt}}$  and  $\sigma_{li}$  respectively, are illustrated in figure 6.1 with the PWBA and ECPSSR predictions. For both the  $L_2$  and  $L_3$  subshells the data and the ECPSSR theory shows reasonable agreement only at high energies. As the proton enegy  $(E_p)$  decreases discrepencies increase upto 35%, which is about five times the experimental uncertainties in the measured cross sections, and the data converges towards the PWBA predictions. Figure 6.1 clearly demonstrates that the variation of  $\sigma_{\text{L}_2}$  and  $\sigma_{\text{L}_3}$  with decreasing collision energy is less sharp than predicted by the ECPSSR model. Experimental values of 2s1 state ionisation cross sections, although lying 5-10% above the ECPSSR values, exhibit a measure of agreement both with the ECPSSR and the PWBA theories. The energy dependence of  $\sigma_{L_1}$ , established experimentally, is reproduced quite accurately by the ECPSSR theory. The pronounced decrease of  $\sigma_L$  at  $n_L \le 0.01$  (Ep  $\le$  1MeV,  $n_{L}$  = scaled energy), the origin of which was discussed in section 4.2, is verified by the experimental data. The disagreement between the ECPSSR values and experimental  $\sigma_{L_2}$  and  $\sigma_{L_3}$  is reflected in the total L shell ionisation cross sections ( $\sigma_{Lt}$ ). Agreement with the ECPSSR theory is good for Ep > 2.2MeV.

The theoretical predictions can be tested further by comparing them with the ratios of experimental Li subhsell ionisation cross sections. These ratios are particular sensitive to the shape of the excitation function and highlight regions of disagreement not obvious from comparison with absolute values. Ionisation cross section ratios for proton impact on Dy are illustrated in figures 6.2 and 6.3 with increasing impact energy together with the values obtained by Jitschin

et al (1982) in the energy range of interest. Theoretical predictions of  $\sigma_{L_1}/\sigma_{L_2}$  agree with the present values for proton energies greater than 1.8MeV. At lower energies the experimental values lie below the theoretical curve. The  $\sigma_{L_2}/\sigma_{L_3}$  ratios (figure 6.3) at lower proton energies lie above the values predicted by the theories. Assuming that any existing systematic discrepencies cancel the theory still deviates from the  $\sigma_{L_2}/\sigma_{L_3}$  ratios by about 15% at lower Ep. These comparisons suggest that the ECPSSR significantly underestimate the L2 subshell ionisation cross sections, particularly at lower proton energies. Better agreement is observed for the  $\sigma_{L_1}/\sigma_{L_3}$  ratios implying that the theories reproduces  $\sigma_{L1}$  and  $\sigma_{L3}$  more closely than  $\sigma_{L2}$  . The data of Jitschin et al (1982) follow the general trend exhibited by the present values and also agree quantitatively within the experimental uncertainties of 20%. Since the wave functions of  $2p_{\frac{1}{2}}$  and  $2p_{\frac{3}{2}}$  electrons are similar the ratio  $\sigma_{L_2}/\sigma_{L_3}$  shows only slight variation with proton energy. The more distinct energy dependence for the  $\sigma_{L_1}/\sigma_{L_2}$  and  $\sigma_{L_1}/\sigma_{L_3}$  ratios is a direct consequency of the nodal structure in the 2s radial wave function. It is worthwhile noting that the PWBA and ECPSSR yield comparable values of the ratio since the corrections to the PWBA largely cancel out.

The measured L<sub>g</sub>, L<sub> $\alpha+\eta$ </sub>, L<sub> $\beta_{13+6}$ </sub>, L<sub> $\beta_{2715}$ </sub>, L<sub> $\gamma_{15}$ </sub> and L<sub> $\gamma_{238+4+1}$ </sub> x-ray production cross sections are shown in figures 6.4 - 6.7. Present values are compared with PWBA and ECPSSR theories and with the data of Khan and Crumpton (1978) and the more recent data of Sokhi and Crumpton (1982) which formed a part of the preliminary measurements performed prior to the experiments described in this thesis. The present L<sub>j</sub> x-ray production cross section,  $\sigma_{Lj}^X$ , in general lie systematically above the values of Khan and Crumpton (1978) by  $\simeq$  20%. Measurements by these authors were made on thick targets and this fact most probably explains much of these descrepencies since the precision

of  $\sigma_{l,i}^{X}$  derived from thick target x-ray yields depends directly on the accuracy of energy loss values for protons and on the mass absorption coefficients. Typically uncertainties in the former are around 10% (Andersen and Zeigler 1977) and 3-10% in the latter (Storm and Israel 1970). The values of Sokhi and Crumpton (1982) are also systematically lower than the present values. The deviations are about 25% for  $\sigma_{L\,\varrho}^X$ and about 5-10% for the other cross sections. There was a time difference of about 2 years between the present and the preliminary measurements reported by Sokhi and Crumpton (1982). These initial measurements assumed the validity of theoretically calculated Si(Li) detector efficiency whereas the present values were corrected by experimentally determined Si(Li) efficiency (section 5.5). However, as pointed out in section 5.5 calculated efficiencies may not be reliable and may overestimate the true efficiency. Therefore the most likely explanation of the discrepencies is the further deterioration of the Si(Li) efficiency over the 2 years. As reported in section 5.5 differences of about 20% were noted between the measured and calculated efficiencies. Futhermore the initial experiments were conducted with nuclepore targets and thus low beam currents ( $\simeq$  3nA) had to be employed. In order to avoid long counting times data was accumulated for less charge compared to the present measurements which were made with carbon backed targets. Consequently the initial measurements were subject to relatively larger statistical uncertainties. This may also be regarded as a contributory cause of the observed differences in the two sets of measurements.

The  $\sigma_{Lj}^{X}$  values follow the trend exhibited by the relevant Li subshell ionisation cross sections.  $\sigma_{L\ell}^{X}$ ,  $\sigma_{L\alpha+\eta}^{X}$  and  $\sigma_{L\beta_{2715}}^{X}$ , which represent cross sections for L<sub>j</sub> transitions to the L<sub>3</sub> subshell, are underestimated by the ECPSSR theory (figures 6.4 and 6.5) as was the case with  $\sigma_{L_3}$ 

(figure 6.1). The contribution of the Ln x-rays to  $\sigma_{L,\alpha+n}^{x}$  is only about 1-2% and thus can be ignored for comparison purposes.  $\sigma_{L\beta_{13+6}}^{x}$ and  $\sigma_{L\gamma_{15}}^{x}$ , figures 6.5 and 6.6 respectively, mimic the response of  $\sigma_{L_2}$  since these x-ray transition are to the L<sub>2</sub> subshell. The major contribution to  $\sigma_{L\gamma_{23844}}^{x}$  comes from L<sub>1</sub> ionisation and is directly proportional to  $\sigma_{L_1}$ , through expression 5.27, and thus exhibits analogous behaviour to  $\sigma_{L_1}$ . The significant deviations in the partial  $L_{\beta_j}$  and  $L_{\gamma_{15}}$  cross sections are reflected in the total L<sub>β</sub> and L<sub>γ</sub> x-ray production cross sections, as shown in figures 6.5 and 6.6 respectively. The underprediction of  $\sigma_{L_2}$  and  $\sigma_{L_3}$  by the ECPSSR theory is also evident in the total x-ray production cross sections ( $\sigma_{L_1}^{x}$ ), shown in figure 6.7. The experimental values of Khan and Crumpton (1978) and Sokhi and Crumpton (1982) lie below the present data for reasons discussed earlier.

Figures 6.8 - 6.10 illustrate the variation of Lj x-ray production cross section ratios with proton energy. A major advantage of comparing these ratio with theoretical predictions is that the systematic uncertainties in the experimental procedure (subsection 5.7.4) are eliminated. Experimental values of  $\sigma_{L\alpha+\eta}^X/\sigma_{L\lambda}^X$  indicate an energy dependence in contrast to the constant value predicted by the ECESSR theory. Such a marked energy dependence has also been noticed by Busch et al (1973), Tawara et al (1975) and Kamiya et al (1979) for light ion impact a high  $Z_2$  elements. This dependence on the projectile energy may be explained in terms of  $2p_{\frac{3}{Z}}$  alignment effect as addressed in section 4.4. Kamiya et al (1979) have incorporated this effect into the PWBA theory and have obtained good agreement with measured data. The preliminary measurements (Sokhi and Crumpton 1982) indicate a trend opposite to that predicted by the present values. However, the L $\lambda$  x-ray measurement were subject to high statistical deviations and

since the ratios are very sensitive to the shape of the excitation functions large scatter in the ratio is not unexpected and thus cannot be relied upon to yield precise information.  $\sigma_{LL}^{X}$  values reported in this work were measured with counting statistics of  $\leq$  5% and usually < 3% and hence are likely to be more trustworthy.

 $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\beta}^{X}$  ratios show reasonable qualitative agreement with the ECPSSR predictions (figure 6.9) and with measurements of Sokhi and Crumpton (1982). The values of Khan and Crumpton (1978), performed on thick targets, deviate considerably from the present measurements Similar behaviour was noticed in the case of  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\gamma}^{X}$  and  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratios, illustrated in figure 6.10.

6.2.2 Deuteron impact measurements

Li subshell ionisation cross sections for deuteron impact on Dy are shown in figure 6.11. The measured values are compared with the PWBA and ECPSSR theories. The structure in  $\sigma_{L_1}$  at deuteron energies (Ed)  $\simeq$  1MeV, due to the radial node in the  $2_{s\frac{1}{2}}$  wavefunctions, is clearly indicated by the measurements. The ECPSSR theory predicts the data well at  $E_d$  < 2.2MeV. At higher  $E_d$  the experimental values rise more steeply than the ECPSSR curve and converges towards the PWBA predictions. Unlike proton measurements where some agreement was observed at higher proton energies with ECPSSR theory, the experimental values of  $\sigma_{L_2}$  for deuter impact lie above the ECPSSR predictions by more than 30% throughout the energy range. The PWBA theory appears to reproduce the data well within experimental uncertainties. Disagreement is less for  $\sigma_{1,3}$  where the data deviates by about 12% from the ECPSSR curve. These descrepencies are transfered into the total L shell ionisation cross section,  $\sigma_{Lt}$ , also shown in figure 6.11.

Li subshell ionisation cross section ratios are illustrated in

figure 6.12. The structure in the  $\sigma_{L_1}$  causes a minimum in  $\sigma_{L_1}/\sigma_{L_2}$ and  $\sigma_{L_1}/\sigma_{L_3}$  ratios. Experimental values of  $\sigma_{L_1}/\sigma_{L_2}$  are overestimated by the theories for  $E_d \leq 2.2 \text{MeV}$  although the trend is reproduced quite well. Furthermore, the theories predicts a minimum at  $\eta \approx 0.01$  ( $E_d = 2 \text{MeV}$ ) whereas the data indicate a minimum at  $\eta_L \approx 0.008$ ( $E_d = 1.6 \text{MeV}$ ). Similar behaviour is exhibited by the  $\sigma_{L_1'}\sigma_{L_3}$  ratio. This shift in the minimum implies that the plateau predicted by the PWBA in  $\sigma_{L_1}$  at  $\eta_L \approx 0.01$  occurs inreality at a lower  $\eta_L$  value. This was also noticed by Change et al (1975) and it suggests that the radial node in the  $2_{s\frac{1}{2}}$  wave function occurs at a higher momentum value than predicted by hydrogenic nonrelativistic wave functions (Chang et al 1975). The failure of the ECPSSR to predict  $\sigma_{L_2}$  data is also highlighted in the comparison of  $\sigma_2/\sigma_{L_3}$  with theory (figure 6.12). The measured ratio follow the same pattern as  $\sigma_{L_2}$ , in that they lie above the predicted values.

The measured absolute  $\sigma_{Lj}^{X}$  are shown in figures 6.13 - 6.16. Since the L<sub>a</sub> and L<sub>k</sub> transitions are to the L<sub>3</sub> subshell  $\sigma_{Lk}^{X}$  and  $\sigma_{L\alpha+\eta}^{X}$ (figure 6.13) follow the trend of  $\sigma_{L_3}$  and numerically are underestimated by the ECPSSR theory.  $\sigma_{Lk}^{X}$ , however, shows a larger deviation from the ECPSSR curve (~30%) than  $\sigma_{L\alpha+\eta}^{X}$  (~14%). Partial  $\sigma_{L\beta_j}^{X}$  and total  $\sigma_{L\beta}^{X}$ (figure 6.14) exhibit agreement with the uncorrected PWBA theory. Similar behaviour is also expressed by the L<sub>Y</sub> x-ray cross sections, shown in figure 6.15. Since L<sub>Y2344</sub>, transitions occur to the 2<sub>S<sup>1</sup>/2</sub> state  $\sigma_{L_{Y23844}}^{X}$  data also reveals the structure of  $\sigma_{L_1}$ (figure 6.11) The total L x-ray production cross section,  $\sigma_{Lt}^{X}$ , illustrated in figure 6.16, depicts analogous behaviour to its individual components,  $\sigma_{L_1}^{X}$ , and differs from the ECPSSR values by as much as 18%.

The evidence for energy dependence of  $\sigma_{L\alpha}^{X}/\sigma_{Ll}^{X}$  provided by proton data (figure 6.8) is further reinforced by the measurements made with

incident deuterons, and is shown in figure 6.17. With regard to the other ratios, illustrated in figures 6.18 and 6.19, agreement is noticed only with  $\sigma_{L\beta}^{\ X}/\sigma_{L\gamma}^{\ X}$  whereas  $\sigma_{L\alpha+\eta}^{\ X}/\sigma_{L\beta}^{\ X}$  and  $\sigma_{L\alpha+\eta}^{\ X}/\sigma_{L\gamma}^{\ X}$  are overestimated by the theories. Since major components of L<sub>β</sub> and L<sub>γ</sub> x-rays arise from electronic transitions to the L<sub>2</sub> subshell this implies that much of the discrepencies noticed with  $\sigma_{L_2}$  values cancel when considering  $\sigma_{L_\beta}/\sigma_{L_\gamma}$  ratios.

### 6.3 YTTERBUM $(Z_2 = 70)$

From the L x-ray spectra of ytterbium (Yb), obtained by proton, deuteron and alpha particle bombardment, L<sub>ℓ</sub>, L<sub>α+η</sub>, L<sub>β1346</sub>, L<sub>γ15</sub> and L<sub>γ23844</sub>, x-ray transitions were analysed. As with Dy, contribution of the L<sub>η</sub> x-rays to the L<sub>α</sub> peak was taken into account when deriving  $\sigma_{L_3}$  cross sections from equation 5.29.

#### 6.3.1 Proton Impact Measurements

The ECPSSR theory reproduces  $\sigma_{L_1}$  quite well and is illustrated in figure 6.20. At proton energies, E<sub>p</sub>, less than 2 MeV the ECPSSR predictions deviate by about 20% below the measured value of  $\sigma_{L_2}$ (figure 6.20), describing similar behaviour to that noticed with proton bombardment of Dy (section 6.2.1). The experimental  $\sigma_{L_3}$  values lie below the ECPSSR prediction by 5-10%, just outside the experimental uncertainties of 4-6% in  $\sigma_{L_3}$ . Agreement of ECPSSR predictions with the total L shell ionisation cross section,  $\sigma_{L_t}$ , is remarkably good throughout the energy range of interest.

Experimental  $\sigma_{L_1}/\sigma_{L_2}$  ratios, figure 6.21, are predicted by the theories qualitatively and quatitatively within experimental uncertainties. Data values, however, lie below the theoretical curves for  $E_p < 2$  MeV and above the curves for higher  $E_p$  implying that the  $\sigma_{L_1}$  contribution relative to  $\sigma_{L_2}$  increases more sharply than indicated theoretically. The minimum at  $E_p \approx 1.2$  MeV predicted by theory is

substantiated by the experimental measurements. The trend described by the measured  $\sigma_{L_1}/\sigma_{L_2}$  is supported by  $\sigma_{L_1}/\sigma_{L_3}$  ratios, shown in figure 6.22 where the experimental values depend more sharply on increasing Ep than the theoretical values. For the  $\sigma_{L_2}/\sigma_{L_3}$  ratio the agreement with theory is poor at lower impact energies and also the data indicate a nearly constant value for the ratio, incontrast to theory, which predicts a slow increase in the  $\sigma_{L_2}$  contribution with increasing Ep relative to  $\sigma_{L_3}$ .

 $\sigma_{L_{j}}^{X}$  for the appropriate  $L_{j}$  x-ray transition are illustrated in figures 6.23 - 6.26.  $\sigma_{L\alpha+\eta}^{X}$  and  $\sigma_{L\ell}^{X}$  follow the trend of  $\sigma_{L3}$  and show reasonable correlation with ECPSSR predictions (figure 6.23).  $\sigma_{L\beta_{2715}}^{X}$ describes similar behaviour since its main contributor is the  $L_{\beta_{2}}$ transition which occurs to the  $2p_{\frac{3}{2}}$  state (figure 6.24). Since  $L_{\beta_{1}}$ x-rays originate from electronic transitions to the  $L_{2}$  subshell,  $\sigma_{L\beta_{1346}}^{X}$  describes a similar energy dependence to that of  $\sigma_{L_{2}}$ . The measured total  $L_{\beta}$  x-ray production cross sections,  $\sigma_{L\beta}^{X}$ , (figure 6.24) illustrate reasonable agreement with the ECPSSR values but lie above the theory by a few percent.  $\sigma_{L\gamma_{j}}$  are shown in figure 6.25. Agreement of  $\sigma_{L\gamma_{23844}}$ , is good with ECPSSR values unlike  $\sigma_{L\gamma_{15}}$  which deviate from theory at low Ep by upto 23%. This discrepency is also visible in the total  $L_{\gamma}$  cross section,  $\sigma_{L\gamma}^{X}$ , illustrated in figure 6.25. The total L x-ray cross section,  $\sigma_{L\gamma}^{X}$ , shows very good agreement with the ECPSSR theory at all Ep values (figure 6.26).

Evidence for the energy dependence of  $\sigma_{L\alpha}^{X}/\sigma_{L\lambda}^{X}$  ratio is substantiated by the measurements, shown in figure 6.27.  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratio, figure 6.28, shows reasonable correlation with theory but deviations become significant at lower impact energies. The  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\beta}^{X}$  ratio show only qualitative agreement with theory, except at intermediate energies (figure 6.28). The situation is similar in the case of  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\gamma}^{X}$ ,

shown in figure 6.29, but the data values depict a significantly less pronounced energy dependence than described by the theories. This is because the measured  $\sigma_{L1}/\sigma_{L_3}$  and  $\sigma_{L2}/\sigma_{L_3}$  ratio, presented in figure 6.22, suggests that the  $\sigma_{L_1}$  and  $\sigma_{L_2}$  contribute more to the total L shell ionisation relative to  $\sigma_{L_3}$  than is theoretically predicted. Consequently the ratio  $\sigma_{L_{\alpha+\eta}}^X/\sigma_{L_{\gamma}}^X$  is smaller numerically than the predicted values. The less pronounced energy dependence at low Ep is explained by the experimental evidence, that  $\sigma_{L_2}$  is more important relative to  $\sigma_{L_3}$  at lower energies.than is accounted for theoretically (figure 6.22).

#### 6.3.2. Deuteron Impact Measurements

The measured  $\sigma_L$ , values for deuteron impact on Yb show a more marked dependence on deuteron energy (Ed) than implied by both the theories (figure 6.30). The experimental  $\sigma_{L_1}$  values cross over the theoretical curves at  $E_d \simeq 2.1 \text{MeV}$ . Such a behaviour was also noticed when considering Dy  $\sigma_{L1}$  for incident deuterons and was shown in figure 6.11. The  $\sigma_{\text{L}_2}$  data repeat the trend demonstrated by the previously discussed measurements and exhibit closer agreement with the PWBA theory, as shown in figure 6.30. As with proton bombardment of Yb,  $\sigma_{L_2}$  for deuteron impact show reasonable agreement with the EPSSR theory although the latter does tend to overpredict the measured values. The total L shell ionisation cross sections,  $\sigma_{Lt}$ , illustrated in figure 6.30, are well reproduced by the ECPSSR theory. Figure 6.31 shows the variation of  $\sigma_{L_1}/\sigma_{L_2}$  with  $E_d$  and highlights the large discrepencies between experimental data and theory for Ed < 2MeV. In this region the theory predicts values nearly twice the measured values. The shape of the experimental  $\sigma_{L_1}/\sigma_{L_2}$  values also differs from that of the theories. This is due to the measured  $\sigma_{L_1}$  rising more steeply with Ed than the corresponding theoretical values whereas the energy

depedence of the experimental and theoretical  $\sigma_{L_2}$  is very similar. This affect can again be observed for  $\sigma_{L_1}/\sigma_{L_3}$  ratios, demonstrated in figure 6.32, where the data values show considerable deviations from the ECPSSR predictions at Ed > 2 MeV. The under-estimation of  $\sigma_{L_2}$  by the ECPSSR theory is strikingly obvious from the comparison of  $\sigma_{L_2}/\sigma_{L_3}$  with theory, also shown in figure 6.32.

 $\sigma_{L\alpha+\eta}^{X}$  and  $\sigma_{L\lambda}^{X}$ , seen in figure 6.33 follow the behaviour of  $\sigma_{L_3}^{X}$ and exhibit close correlation with the predictions of the ECPSSR theory The case is similar for  $\sigma_{L\beta_{2715}}^{X}$  shown in figure 6.34. On the other hand  $\sigma_{L\beta_{13+6}}^{X}$ , and hence  $\sigma_{L\beta}^{X}$ , lie systematically above the ECPSSR curve but show some quantitative similarities within experimental uncertainties (figure 6.34).  $\sigma_{L\gamma_{23844}}^{X}$ , exhibit analogous characteristics to that of  $\sigma_{L_3}$  since they are directly realted and  $\sigma_{L\gamma_{15}}^{X}$  follows the trend of  $\sigma_{L_2}^{X}$ . Since at Ed > 2 MeV  $\sigma_{L\gamma_{22844}}^{X}$ , as well as  $\sigma_{L\gamma_{15}}^{X}$ , is under predicted by theory  $\sigma_{L\gamma}^{X}$  shows larger disagreement in this energy region with both the PWBA and ECPSSR predictions. The total x-ray production cross section, figure 6.36, is reproduced extremely well by the ECPSSR model.

The energy dependence of  $\sigma_{L\alpha}^{X}/\sigma_{L\lambda}^{X}$ , not predicted by the theories, is again clearly reaffirmed by the measurements shown in figure 6.37. Smaller values of  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\beta}^{X}$  than those calculated with the ECPSSR model were obtained experimentally (figure 6.38). This also implies that the mechanism of  $2p_{\frac{1}{2}}$  state ionisation by incident low energy charged particles is not fully accounted for by the ECPSSR model. Since  $L_{\gamma}$  x-rays contain a large component of  $L_{\gamma_{15}}$  x-rays, a consequence of transitions to L<sub>2</sub> subshell, similar behaviour is demonstrated by  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\gamma}^{X}$  ratio and is shown in figure 6.39. Some of the  $\sigma_{L_2}$ discrepencies are eliminated in the  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratio and as a result the disagreement between theory and experiment is markedly reduced (figure 6.39)

## 6.3.3 Alpha particle Impact

In contrast to proton and deuteron impact measurements the experimental  $\sigma_{L1}$ , (figure 6.40) for alpha particles incident on Yb are overestimated by the ECPSSR theory by upto 30%.  $\sigma_{L_2}$  follows the trend encountered with the previously discussed measurements and lies systematically above the predictions of the ECPSSR model (figure 6.40). However, the discrepencies are much more serious and the values may disagree by a factor of 2. The ECPSSR theory is only able to explain  $\sigma_{L_3}$  and the total L shell ionisation cross section ( $\sigma_{L1}$ ) as shown in figure 6.41. The gross discrepencies observed for  $\sigma_{L_1}$  and  $\sigma_{L_2}$  are strikingly apparent when comparing  $\sigma_{L_1}/\sigma_{L_2}$  ratio with the theories (figure 6.42). Disagreement by factors of 1.5 - 2.5 were noticed. Discrepencies are somewhat reduced for  $\sigma_{L_1}/\sigma_{L_3}$  ratios (figure 6.43) but still is reproduced only by PWBA model. The highly inadequate explanation of the measured  $\sigma_{L_2}$  data by the ECPSSR theory is also sharply expressed by the  $\sigma_{L_2}/\sigma_{L_3}$  ratios shown in 6.44.

 $σ_{L\alpha+\eta}^{X}$ , illustrated in figure 6.45, is reasonably explained by the ECPSSR model. The theory, however, deviates significantly from the  $σ_{L\ell}^{X}$  data, also shown in figure 6.45. These deivations are probably caused by the anisotropy of L<sup>ℓ</sup> x-rays, an effect not taken into account by the theories. The total L<sub>β</sub> and the partial L<sub>βj</sub> x-ray production cross sections are shown in figure 6.46. Close agreement with the predictions of the ECPSSR model is shown by the total and the partial cross sections. Figure 6.47 illustrates the x-ray production cross sections for the L<sub>γ</sub> group.  $σ_{L_{γ_{15}}}^{X}$  and  $σ_{L_{γ_{23844}}}^{X}$  exhibit similar behaviour to  $σ_{L_2}$  and  $σ_{L_1}$  respectively. Discrepencies between  $σ_{L_γ}^{X}$  and the ECPSSR theory tend to increase with alpha particle energy to about 25%. The total L shell x-ray production cross section, shown in figure 6.48, on the other hand is explained by the ECPSSR model extremely well.

The anisotropy of L2 x-rays, mentioned above, is also apparent in the  $\sigma_{L\alpha+\eta}^{\ x}/\sigma_L^{\ x}$  ratios (figure 6.49) which expresses an energy dependence not explained by theory.  $\sigma_{L\alpha+\eta}^{\ x}/\sigma_{L\beta}^{\ x}$  ratios shown in figure 6.50, disagree significantly (7-15%) at the extremities of the energy range. Futhermore the energy dependence of the measured ratio at higher impact energies is less pronounced than indicated by theory. The ECPSSR model overestimates the experimental  $\sigma_{L\alpha+\eta}^{\ x}/\sigma_{L\gamma}^{\ x}$  data (figure 6.51) by 20-35% with deviations increasing with increasing alpha particle energy.  $\sigma_{L\beta}^{\ x}/\sigma_{L\gamma}^{\ x}$  data exhibits a similar qualitative behaviour to that of  $\sigma_{L\alpha+\eta}^{\ x}/\sigma_{L\gamma}^{\ x}$  with deviations of 5-20% from the theory, as demonstrated in figure 6.51.

6.4 TUNGSTEN  $(Z_2 = 74)$ 

L2,  $L_{\alpha+\eta}$ ,  $L_{\beta_{146}}$ ,  $L_{\beta_{25715}}$ ,  $L_{\gamma_{15}}$  and  $L_{\gamma_{236844'}}$  x-ray lines were studied for proton, deuteron and alpha particle impact on tungsten (W). The Li subshell ionisation cross sections were obtained from  $\sigma_{L_{\alpha+\eta}}^{X}$ ,  $\sigma_{L_{\gamma_{15}}}^{X}$ and  $\sigma_{L_{\gamma_{236844'}}}^{X}$ .

6.4.1 Proton Impact Measurements

The individual Li subshell ( $\sigma_{Li}$ ) and total L shell ( $\sigma_{Lt}$ ) ionisation cross section for proton impact on W are illustrated in figures 6.52 and 6.53 respectively. Comparison of the present data is made with the cross sections reported by Justiniano et al (1980) as well as with the PWBA and the ECPSSR theories.  $\sigma_{L1}$  data generally lies a few percent above the ECPSSR curve but reporduces the predicted energy dependence. The values of Justiniano et al (1980), however, are markedly larger than the present values by nearly a factor of 2. The present  $\sigma_{L_2}$  values show close agreement with the PWBA theory and the data of Justiniano et al (1980). The ECPSSR theory predicts  $\sigma_{L_3}$  extremely well throughout the energy range of interest. Significant deviations of about 17%, however, occur from the values of Justiniano et al(1980) at lower Ep.  $\sigma_{Lt}$ , shown in figure 6.53, exhibits close correlation with the ECPSSR theory except at intermediate Ep values. The data of Justiniano et al (1980) systematically lies above the present  $\sigma_{Lt}$  values by about 10%.

Experimental  $\sigma_{L_1}/\sigma_{L_2}$  ratios, illustrated in figure 6.54, show good agreement with the theories except at Ep < 1.4 MeV. The measured values of Justiniano et al (1980), however, show considerable deviations from the present values and the theories, caused by their markedly larger  $\sigma_{L_1}$  values (figure 6.53). The same effect is observed with regard to the  $\sigma_{L_1}/\sigma_{L_3}$  ratio shown in figure 6.55. The theoretical predictions exhibit a less sharp energy dependent than indicated by the present values. The underestimation of  $\sigma_{L_2}$  by the ECPSSR theory is also apparent in the case of  $\sigma_{L_2}/\sigma_{L_3}$  ratios, figure 6.55, where the data consistently lies above the predicted values. The values of Justiniano et al (1980) closely follow the trend shown by the present measurements.

The Lj x-ray production cross section for incident protons on W are shown in figure 6.56 - 6.59.  $\sigma_{L\alpha^+\eta}^X$  and  $\sigma_{L\ell}^X$  follow the trend of  $\sigma_{L_3}$  and show reasonable agreement with the ECPSSR predictions. The  $\sigma_{L\alpha^+\eta}^X$  values of Justiniano et al (1980) are higher than the present values by about 20%.  $\sigma_{L\beta}^X$  and  $\sigma_{L\beta j}^X$ , shown in figure 6.57, are underestimated by the ECPSSR theory and the deviations increase with decreasing Ep. Similar behaviour is observed in the cases of  $\sigma_{L\gamma}^X$  and  $\sigma_{L\gamma_{15}}^X$  whereas closer agreement with the ECPSSR model is seen for  $\sigma_{L\gamma_{23563441}}^X$ , figure 6.58. The ECPSSR model is also quite successful in explaining qualitatively and quatitatively the total L shell x-ray production cross section (figure 6.59).

In contrast to the ECPSSR predictions the present  $\sigma_{L\alpha+\eta}/\sigma_{L\lambda}^{\chi}$  values, shown in figure 6.60, clearly exhibit a dependence on energy, in line with observations noted for Dy and Yb, discussed earlier. In the case of  $\sigma_{L\alpha+\eta}^{\chi}/\sigma_{L\beta}^{\chi}$  ratios (figure 6.61) the theories and data agree

reasonably although the latter is systematically overestimated by the theories. The situation is very similar for  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\gamma}^{X}$  and  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratios.shown in figure 6.62 where the theories overpredict the experimental values significantly.

6.4.2 Deuteron Impact Measurements

For deuteron energies,  $E_d$ , greater than 2 MeV the ECPSSR model explains the  $\sigma_{L_1}$  data, illustrated in figure 6.63, within the experimental uncertainties. At low  $E_d$  values the present  $\sigma_{L_1}$  values deviate below the ECPSSR curve indicating a more pronounced plateau than predicted theoretically. The ECPSSR model reporduces the energy dependence of  $\sigma_{L_2}$ , figures 6.63, but falls short by about 20-80%. In contrast  $\sigma_{L_3}$  and  $\sigma_{Lt}$  are explained by the ECPSSR model extremely well, figure 6.64. The deviations observed for  $\sigma_{L_2}$  are stikingly apparent in the case of  $\sigma_{L_1}/\sigma_{L_2}$  ratio, shown in figure 6.65, where discrepencies of upto 50% exist between experimental data and theory. The  $\sigma_{L_2}$  deviations are also observed for  $\sigma_{L_2}/\sigma_{L_3}$  ratio, figure 6.66, where the data lies above the theories throughout the energy range.  $\sigma_{L_1}/\sigma_{L_3}$  figure 6.66, however, is explained well for  $E_d > 2.0$  MeV but agreement decreases for  $E_d < 2.0$  MeV.

Very good agreement between experimental  $\sigma_{L_{\alpha}+\eta}^{X}$  and  $\sigma_{L_{z}}^{X}$  values and the ECPSSR model is observed, figure 6.67.  $\sigma_{L_{\beta}}^{X}$  and  $\sigma_{L_{\beta}j}^{X}$  (figure 6.68) are reproduced reasonably well by the ECPSSR model although the measured values lie above the ECPSSR predictions. The behaviour of  $\sigma_{L_{\gamma_{236844}}}^{X}$  is analogous to that of  $\sigma_{L_{1}}$  and deviates from the ECPSSR curve only for E<sub>d</sub> < 2.0 MeV. The present  $\sigma_{L_{\gamma_{15}}}^{X}$  values lie about 20% above the ECPSSR model. Agreement between experimental  $\sigma_{L_{\gamma}}^{X}$  and ECPSSR values deteriorates as E<sub>d</sub> increases and disagreements of upto 16% are noticed, figure 6.69. Excellent agreement between  $\sigma_{L_{t}}^{X}$  and the ECPSSR theory is observed and is demonstrated in figure 6.70. The energy dependence of  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\ell}^{X}$  is indicated clearly by the experimental data, figure 6.71. Present  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\beta}^{X}$  ratios lie below the ECPSSR curve, figure 6.72, but show a measure of agreement within the experimental uncertainties.  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratios, figure 6.73, exhibit similar behaviour whereas the discrepencies between the ECPSSR theory and  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\gamma}^{X}$  are considerable at  $E_d > 1.6$  MeV, figure 6.73. 6.4.3. Alpha Particle Impact Measurements

The ECPSSR model significantly overestimates the experimental  $\sigma_{L_1}$  values whereas  $\sigma_{L_2}$  is grossly underpredicted by upto 80%, figure 6.74. Discrepencies for  $\sigma_{L_3}$  and  $\sigma_{Lt}$  are much less but still nontrivial as illustrated in figure 6.75. Experimental  $\sigma_{L_1}/\sigma_{L_2}$  ratio at low alpha particle energies ( $E_{\alpha}$ ) are overpredicted by the ECPSSR values by a factor of 2, although discrepenceis decrease as  $E_{\alpha}$  increases (figure 6.76).  $\sigma_{L_1}/\sigma_{L_3}$  exhibits closer agreement with the PWBA theory and differs by more than 35% at low  $E_{\alpha}$  from the ECPSSR values. In the case of  $\sigma_{L_2}/\sigma_{L_3}$  not only do the experimental and ECPSSR values differ numerically by as much as 50%, the energy dependence indicated by the data values is contradictory to that followed by the theory, in that the experimental  $\sigma_{L_2}/\sigma_{L_3}$  ratios decrease and ECPSSR values increase with increasing  $E_{\alpha}$  (figure 6.78). Similar behaviour was encountered for alpha particle impact on Yb (figure 6.44).

Very good agreement between the ECPSSR values and  $\sigma_{L_{\alpha+\eta}}^{X}$  (figure 6.79) is observed. The two values of Braziewicz et al (1984) lie significantly below the present data. For  $\sigma_{L_{\alpha}}^{X}$  shown in figure 6.79, the experimental values are in general larger than the ECPSSR values by 10-20%. Discrepencies of nearly 50% are noticed between experimental  $\sigma_{L_{\beta_{1}+6}}^{X}$  and ECPSSR values (figure 6.80).  $\sigma_{L_{\beta_{2}5715}}^{X}$  shows close agreement with the ECPSSR model for  $E_{\alpha} > 2$  MeV. Below this energy the data and theory disagree by 50%.  $\sigma_{L_{\beta}}^{X}$  (figure 6.80) is predicted by the

ECPSSR theory quite well but differences of upto 18% exist. The data of Braziewicz et al (1984) are lower 'than the present  $\sigma_{L_{\beta}}^{X}$  values by about 10-15%.  $\sigma_{L_{\gamma_{236844}}!}^{X}$ , shown in figure 6.81, follows the same trend as  $\sigma_{L_{1}}$  (figure 6.74).  $\sigma_{L_{\gamma_{15}}}^{X}$  data deviates from the ECPSSR predictions by as much as 50% where  $\sigma_{L_{\gamma}}^{X}$  shows reasonable agreement with the ECPSSR model except at  $E_{\alpha} > 2.6$  MeV where the theory yields lower values. (figure 6.81). The measured  $\sigma_{L_{\gamma}}^{X}$  values of Braziewicz et al (1984) lie significantly below the present data.  $\sigma_{L_{t}}^{X}$  is reproduced well by the ECPSSR approximation where as the data of Braziewicz et al (1984) disagree considerably (figure 6.82).

 $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\alpha}^{X}$  data describes a less sharp variation with energy than observed for proton and deuteron impact data (figures 6.60 and 6.71 respectively) and is demonstrated in figure 6.83. The ECPSSR theory predicts  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\beta}^{X}$  ratio quite well and agreement is also noticed with the values of Braziewicz et al (1984). The theory also explains reasonably well the  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\gamma}^{X}$  ratio although the data lies below the theoretical curves (figure 6.85). Better agreement is observed with  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratio shown in figure 6.85. 6.5 GOLD( $Z_{1}$  = 79)

Ll, La, LB, LY, LY<sub>15</sub> and LY<sub>236844</sub>, x-ray production cross sections have been measured for protons, deuterons and alpha particles incident on gold (Au). L<sub>i</sub> subshell ionisation cross section were determined from  $\sigma_{L\alpha}^{X}$ ,  $\sigma_{L\gamma_{15}}^{X}$  and  $\sigma_{L\gamma_{236844}}^{X}$ . 6.5.1 Proton Impact Measurements

 $L_i$  subshell ionisation cross sections,  $\sigma_{Li}$ , for proton impact on Au are compared with the thin target measured values of Cohen (1980) and de Pinho (1982) as well as with the theories and are illustrated in figure 6.86. The present  $\sigma_{L_1}$  values show good agreement with the ECPSSR model for  $E_p > 2.0$  MeV below which the data shows reasonable correlation with the PWBA theory.  $\sigma_{L_1}$  values of Cohen (1980) and de Pinho (1982) disagree markedly from the present data. Furthermore the measured values of Cohen (1980) do not indicate the presence of the plateau in  $\sigma_{L_1}$  at  $E_p \simeq 1.1$  MeV unlike the present work. For  $\sigma_{L_2}$ , figure 6.86, values reported in this work are predicted better by the PWBA model and also exhibit very good agreement with the data of de Pinho (1982). The values of Cohen (1980) lie below the present data by about 10-20% but agree with in the experimental uncertainties of 20% quoted by Cohen (1980). In the case of  $\sigma_{L_3}$  the values measured in this study in general show close agreement with the vlaues of Cohen (1980) and de Pinho (1982) and with the ECPSSR theory, as demonstrated in figure 6.86. The discrepencies noticed for  $\sigma_{L_2}$  show themselves in  $\sigma_{Lt}$ , illustrated in figure 6.87, and the present data disagrees by upto 19% from the ECPSSR theory. The values of de Pihno (1982) are in closer agreement with the present data than the values of Cohen (1980) which lie below the measured data.

The minimum in  $\sigma_{L_1}/\sigma_{L_2}$ , caused by the plateau in  $\sigma_{L_1}$ , is reproduced well by the measured values and is shown in figure 6.88. The data of Jitschin et al (1982) also predicts the minimum reasonably well whereas the values of de Pinho (1982), and in particular the values of Cohen (1980), show large deviations at intermediate E<sub>p</sub> values. The situation is very similar for  $\sigma_{L_1}/\sigma_{L_3}$  ratios shown in figure 6.89. In the case of  $\sigma_{L_2}/\sigma_{L_3}$  better agreement is observed with other measured values, figure 6.89, although all values lie significantly above the predicted curves.

Present values of  $\sigma_{L\ell}^{X}$ , figure 6.90, are predicted well by the ECPSSR model. The data of Tawara et al (1975) deviates by upto 30% at low E<sub>p</sub> and converges with the values of Bhattacharya et al (1980). The preliminary measurements of  $\sigma_{L\ell}^{X}$  on nuclepore targets (Sokhi and

Crumpton 1981) deviate significantly only at  $E_p > 2.6$  MeV.  $\sigma_{L\alpha}^{X}$  and  $\sigma_{L\beta}^{X}$ , shown in figure 6.91, exhibit good correlation with the other measured values except for those reported by Khan and Crumpton (1978) which lie systematically below the present values. The reasons for these deviations were considered in section 6.2.1. The PWBA theory tends to predict the  $\sigma_{L\beta}^{X}$  values better than the ECPSSR model, as was the case with  $\sigma_{L_2}$  (figure 6.86).  $\sigma_{L\gamma}^{X}$ , figure 6.92, follows a very similar trend to that observed with  $\sigma_{L\beta}$ .  $\sigma_{L\gamma_{15}}^{X}$  and  $\sigma_{L\gamma_{236844}}^{X}$ , also illustrated in figure 6.92, show the same behaviour demonstrated by  $\sigma_{L_2}$  and  $\sigma_{L_1}$  respectively (figure 6.86). The present  $\sigma_{Lt}^{X}$  values and those reported by other authors, except by Khan and Crumpton (1978), agree reasonably well and are explained better by the PWBA model, figure 6.93.

The energy dependence of  $\sigma_{L\alpha}^{X}/\sigma_{L\lambda}^{X}$  ratio, figure 6.94, is observed to be much less than for targets discussed earlier. The present values show a measure of agreement with the values of Sokhi and Crumpton (1981), whereas the data of Tawara et al (1975) and Bhattacharya et al (1980) deviate considerably at low Ep.  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  ratios reported in this thesis and those of other workers, illustrated in figure 6.95, are overpredicted significantly by the theories and disagreement tends to increase to about 15% with decreasing Ep.  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratios, figure 6.96, also show similar behaviour. However, the present values in contrast to the other measurements converge towards the predicted values. In the case of  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$ , also shown in figure 6.96, a very close agreement is observed with the theoretical approximations. The data reported by other authors, however, lie significantly below the present values.

### 6.5.2 Deuteron Impact Measurements

The energy dependence of the measured  $\sigma_{L_1}$  is reproduced well by the ECPSSR theory, as shown in figure 6.97, although quantitatively

the data lies above the predictions by approximately 11%.  $\sigma_{L_2}$ , figure 6.97, is also reproduced qualitatively by the ECPSSR whereas numerically the PWBA model shows closer agreement.  $\sigma_{L_3}$  and  $\sigma_{L_t}$ , illustrated in figure 6.98, are explained quite well by the ECPSSR theory.

The theoretical predictions reproduce closely the measured  $\sigma_{L_1^{-}}/\sigma_{L_2}$  ratios, figure 6.99.  $\sigma_{L_1}/\sigma_{L_3}$ , however, deviates increasingly from the theoretical values with decreasing E<sub>d</sub> by upto 40% and  $\sigma_{L_2^{-}}/\sigma_{L_3}$  ratios lie considerably above the ECPSSR curve, shown in figure 6.100.

 $\sigma_{L\ell}^{X}$ ,  $\sigma_{L\alpha}^{X}$  and  $\sigma_{L\beta}^{X}$  are illustrated in figure 6.101. At  $E_d > 2 \text{ MeV}$   $\sigma_{L\ell}^{X}$  data agrees very well with the ECPSSR values and tends towards the PWBA curve at lower energies. The ECPSSR predictions of  $\sigma_{L\alpha}^{X}$  show very good correlation with the measured values.  $\sigma_{L\beta}^{X}$ , however, is systematically underestimated by the ECPSSR model by 10-20%. These deviations are in line with those observed for  $\sigma_{L_2}$ , figure 6.97. Similar discrepencies are noticed for  $\sigma_{L\gamma}^{X}$  and  $\sigma_{L\gamma_j}^{X}$ , shown in figure 6.102, although the energy dependence is explained well by the theories.  $\sigma_{L\tau}^{X}$ , figure 6.103, is reproduced very successfully by the ECPSSR approximation.

Energy dependence of the measured  $\sigma_{L\alpha}^{X}/\sigma_{L\ell}^{X}$  ratios, figure 6.104, is more apparent than observed for proton impact measurements (figure 6.94) and the data converges towards the predicted value as E<sub>d</sub> increases.  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  ratios are grossly overpredicted by the ECPSSR predictions, particularly at lower E<sub>d</sub> values, shown in figure 6.105. Analogous behaviour is observed for  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$ , figure 6.106.  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratios, also shown in figure 6.106, describe a much better agreement with the theories.

6.5.3 Alpha Particle Impact Measurements

Figure 6.107 illustrates the measured  $\sigma_{L_1}$  and  $\sigma_{L_2}$ , together with the values of Cohen (1981) and those predicted by the PWBA and ECPSSR approximations.  $\sigma_{L_1}$  values increasingly deviate from the ECPSSR

model by about 46% as  $E_{\alpha}$  decreases. The values reported by Cohen (1981) lie below the present data although agreement is observed within the experimental uncertainties of Cohen's (1981) values.  $\sigma_{L_2}$  exhibits much closer correlation with the PWBA model and the values of Cohen (1981) differ from the ECPSSR predictions even more, especially at lower impact energies. Agreement with the values predicted by the ECPSSR theory is much better for  $\sigma_{L_3}$  and  $\sigma_{Lt}$ , illustrated in figure 6.108. With regard to the values reported by Cohen (1981) correlation with the present data is seen only at intermediate energies.

Reasonable agreement is observed for  $\sigma_{L_1}/\sigma_{L_2}$  with the theoretical predictions, figure 6.109. The data of Cohen (1981) deviates significantly below the present values by as much as 80%. Better agreement is observed for  $\sigma_{L_1}/\sigma_{L_3}$  ratio with the theories and the values of Cohen (1981) except at  $E_{\alpha} < 1.8$  MeV where the present data predict much higher values, figure 6.110. The measured  $\sigma_{L_2}/\sigma_{L_3}$  ratios, figure 6.111, decrease with increasing  $E_{\alpha}$ , in contrast to the theoretical models, and converge towards the theories at  $E_{\alpha} > 2.6$  MeV. This circumstance is supported by the values of Cohen (1981) although these values show a less sharpe variation with  $E_{\alpha}$  than indicated by the present data.

The  $\sigma_{\text{Li}}$  data of Bhattacharya et al (1982), for 0.9 - 1.8 MeV alpha particle impact on Au, came to the authors attention after the analysis of the data had been performed and, thus, was not included in figures 6.107 - 6.111. However, within the energy range of interest, the present values are larger than those of Bhattacharya et al (1982) by 25-50% for  $\sigma_{\text{L}_1}$ , 4-12% for  $\sigma_{\text{L}_2}$  and 30-180% for  $\sigma_{\text{L}_3}$ . In the case of  $\sigma_{\text{Lt}}$  the values differ by about a factor of 1.5. With regard to the ratios the data of Bhattacharya et al (1982) indicate similar trends to that of the present values, figure 6.109 - 6.111, but deviate

numerically by 25-60%,  $\sigma_{L_2}/\sigma_{L_3}$  showing the worst disagreement.

The ECPSSR theory predicts closely the  $\sigma_{L_{L}}^{X}$  data, figure 6.112, except at  $E_{\alpha} < 2.0$  MeV. For  $\sigma_{L_{\alpha}}^{X}$  deviations arise at  $E_{\alpha} > 2.6$  MeV, below which agreement with the ECPSSR theory is good, figure 6.112. Discrepencies are more pronounced for  $\sigma_{L_{\beta}}^{X}$  and increase with decreasing  $E_{\alpha}$  to about 35%, also demonstrated in figure 6.112.  $\sigma_{L_{Y_{236844}}}^{X}$  and  $\sigma_{L_{Y_{15}}}^{X}$ , figure 6.113, exhibit similar behaviour to that of  $\sigma_{L_{1}}$  and  $\sigma_{L_{2}}$ . respectively shown in figure 6.107. The large disagreements observed for  $\sigma_{L_{Y_{j}}}^{X}$  are reflected in  $\sigma_{L_{Y}}^{X}$ , illustrated in figure 6.113, and are increasingly under-estimated by the ECPSSR theory as  $E_{\alpha}$  decreases.  $\sigma_{L_{T}}^{X}$ , measured in this work, follow the general trend of the ECPSSR model but lie above the theory by 20%.

The measured  $\sigma_{L\alpha}^{X}/\sigma_{L\ell}^{X}$  ratios show much more striking dependence on impact energy, figure 6.115, than was indicated by proton and deuteron measurements (figures 6.94 and 6.104 respectively). The measured values crossover the ECPSSR prediction at  $E_{\alpha} \approx 2.4$  MeV. Large disagreement is noticed at  $E_{\alpha} < 2.6$  MeV for  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$ , as shown in figures 6.116. This behaviour is reprodued by  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$ , figure 6.117. Agreement with the theories is in general quite good for  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratio, since the large  $\sigma_{L_{2}}$  discrepencies cancel to a certain extent.

6.6 LEAD  $(Z_2 = 82)$ 

 $L_{\ell}$ ,  $L_{\alpha}$ ,  $L_{\beta}$ ,  $L_{\gamma}$ ,  $L_{\gamma_{15}}$  and  $L_{\gamma_{236844}}$ , x-ray production cross sections were determined for protons, deuterons and alpha particles incident on lead (Pb).  $L_{i}$  subshell ionisation cross sections were deduced from  $\sigma_{L_{\alpha}}^{x}$ ,  $\sigma_{L_{\gamma_{15}}}^{x}$  and  $\sigma_{L_{\gamma_{236844}}}^{x}$ .

#### 6.6.1 Proton Impact Measurements

Figures 6.118 and 6.119 illustrate  $L_1$  subshell and total L shell ionisation cross sections for proton impact on Pb. At  $E_p$  > 1.4 MeV

ECPSSR predictions and measured  $\sigma_{L_1}$  differ by upto 60% and much larger deviations are observed for the data Leite et al (1977) and Cohen (1980) from the theory. The thin target  $\sigma_{L_1}$  values of Cohen (1980) are larger than the present ones by nearly a factor of 2 in the region of the plateay at E<sub>p</sub>  $\approx$  1.2 MeV. Agreement between the present  $\sigma_{L_2}$  values and those of Leite et al (1977) and Cohen (1980) is very good and all measured values exhibit better correlation with the PWBA model than the ECPSSR. With regard to  $\sigma_{L_3}$  and  $\sigma_{Lt}$  the present values in general show reasonable agreement with the ECPSSR model but differ significantly from the other measured data at E<sub>p</sub> < 2.0 MeV.

The minimum in  $\sigma_{L_1}/\sigma_{L_2}$  ratio, shown in figure 6.120, is reproduced well by the present data and that of Leite et al (1977) while the values of Cohen (1980) indicate a much less pronounced minimum. The underprediction of  $\sigma_{L_1}$  and  $\sigma_{L_2}$  by the ECPSSR model is stikingly evident in  $\sigma_{L_2}/\sigma_{L_3}$  and  $\sigma_{L_2}/\sigma_{L_3}$  ratios, shown in figure 6.121, where the data consistently lies above the theoretical estimates. In the case of  $\sigma_{L_2}/\sigma_{L_3}$  the present data indicate considerably larger discrepencies from the theories than implied by the other measured values.

The ECPSSR theory overpredicts the measured  $\sigma_{LL}^{X}$  values at  $E_p > 2.0$ MeV and this is supported by the data of Tawara et al (1974), figure 6.122. The initial measurements of  $\sigma_{LL}^{X}$  (Sokhi and Crumpton 1982) show some disagreement with the present values at the extremities of the energy range (~18%). However, these differences are comparable to the uncertainties in the initial values. Furthermore the preliminary measurements were performed with low beam currents, typically 3 - 10nA, and consequently the problem of leakage current, discussed in subsection 5.4.1, can become significant. The present values of  $\sigma_{L\alpha}^{X}$ , and the other measured data of Tawara et al (1974), Leite et al (1977) and Sokhi and Crumpton (1982), describe very good agreement with the ECPSSR

predictions whereas the  $\sigma_{L\beta}^{X}$  values, although agreeing with each other, lie significantly above the theory, figure 6.123.  $\sigma_{L\gamma_{15}}^{X}$  and  $\sigma_{L\gamma_{236844}}^{X}$ , shown in figure 6.124, display large disagreement with the theories and these are reflected in  $\sigma_{L\gamma}^{X}$  values, which are larger than the ECPSSR estimates by upto 35%. The other measured values of  $\sigma_{L\gamma}^{X}$ , figure 6.124, in general provide very close agreement with the present data. In the case of  $\sigma_{Lt}^{X}$ , figure 6.125, good agreement is found with the ECPSSR theory and with the values of other authors.

 $\sigma_{L\alpha}^{X}/\sigma_{L\lambda}^{X}$  data of Tawara et al (1974) support the energy dependence indicated by ratios measured in this study, figure 6.126. There is also a measure of agreement with the values of Sokhi and Crumpton (1982) except at higher energies. Since the experimental  $\sigma_{L\beta}^{X}$  values are larger then predicted the  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  ratio yields values considerably smaller than those of the ECPSSR model, as demonstrated in figure 6.127. The other measured values exhibit similar trends. This effect is also apparent in the case of  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratio and to a lesser extend in  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$ shown in figure 6.128.

# 6.6.2 Deuteron Impact Measurements

Although the ECPSSR model describes the energydependence of  $\sigma_{L_1}$ quite well it underestimates the measured values by upto 40% as illustrated in figure 6.129. A similar disagreement is observed for  $\sigma_{L_2}$ , also shown in figure 6.129. Measured values of  $\sigma_{L_3}$  show adequate correlation with the ECPSSR predictions and the agreement with theory is even better for  $\sigma_{Lt}$ , figure 6.130. The deviations encountered for  $\sigma_{L_1}$  and  $\sigma_{L_2}$ , figure 6.129, partly cancel in  $\sigma_{L_1}/\sigma_{L_2}$  ratio and as a result the experimental data follows the ECPSSR curve quite well, figure 6.131. Underestimation of  $\sigma_{L_1}$  by the ECPSSR approximation is highlighted in  $\sigma_{L_1}/\sigma_{L_3}$ , shown in figure 6.132, where the data lies above the theory by about 25-50%. Disagreement with theory is even more striking in the case of  $\sigma_{L_2}/\sigma_{L_3}$  ratio, figure 6.133. In line with the trend of  $\sigma_{L_3}$ , figure 6.130,  $\sigma_{L\ell}^X$  and  $\sigma_{L\alpha}^X$  describe good agreement with the ECPSSR estimates, demonstrated in figure 6.134. The PWBA theory provides a better description of the measured  $\sigma_{L\beta}^X$ values, figure 6.134. Energy variation of  $\sigma_{L\gamma}^X$  and  $\sigma_{L\gamma_j}^X$  is reproduced well by the ECPSSR model, figure 6.135, but the theory significantly underestimates the numerical values, unlike the case of  $\sigma_{L\tau}^X$ , figure 6.136, where the theory provides an extremely good agreement.

The energy dependence of  $\sigma_{L\alpha}^{X}/\sigma_{L\lambda}^{X}$  observed for proton measurements figure 6.126, is supported by deuteron impact values, shown in figure 6.137. The theories grossly overpredict the  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  ratio, figure 6.138, although the energy variation is similar to that described by the data. The situation is analogous for  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$ , figure 6.139. Overprediction of  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  by the theories, figure 6.139, is less marked but gains importance as E<sub>d</sub> increases.

### 6.6.3 Alpha Particle Impact Measurements

The ECPSSR theory describes the  $\sigma_{L1}$  data well at  $E_{\alpha} > 2.0$  MeV, figure 6.140, below which the data deviates by upto 24%. Devaitions of upto a factor of 3.5 are observed for  $\sigma_{L2}$ , figure 6.140, in comparison with the ECPSSR theory. The measured values of Cohen (1981) disagree with the present  $\sigma_{L1}$  values only at  $E_{\alpha} < 1.8$  MeV and with  $\sigma_{L2}$  at  $E_{\alpha} > 2.2$  MeV. The present  $\sigma_{L3}$  and  $\sigma_{L1}$  values and those of Cohen (1981) show very good correlation with each other but deviate by upto 30% at low  $E_{\alpha}$  from theory, figure 6.141.

 $\sigma_{L_1}/\sigma_{L_2}$  ratio describe very large disagreements with the theories at lower energies. The measured values show a maximim at  $E_{\alpha} \approx 1.8$  MeV in stark contrast to the models. This appears to be verified by the thin target measurements of Cohen (1981), figure 6.142. In contrast  $\sigma_{L_1}/\sigma_{L_3}$  ratios in general show good agreement with the ECPSSR theory. The data of Cohen (1981), however, disagrees with the presnt values considerably at  $E_{\alpha} < 2.2$  MeV, as illustrated in figure 6.143. The present  $\sigma_{L_2}/\sigma_{L_3}$  data and that a Cohen (1981) describe an energy dependence that is contradictory to the theoretically predicted variations and decreases with increases  $E_{\alpha}$ , figure 6.144.

 $\sigma_{L\alpha}^{\ X}$  and  $\sigma_{L\ell}^{\ X}$  increasingly deviate from the ECPSSR curve as  $E_{\alpha}$  decreases, as shown in figure 6.145,  $\sigma_{L\ell}^{\ X}$ , however, shows larger discrepencies than  $\sigma_{L\alpha}^{\ X}$ . Deviations of 15-65% are observed for  $\sigma_{L\beta}^{\ X}$ , figure 6.145, with larger deviations ocurring at low energies.  $\sigma_{L\gamma_{236844}}^{\ X}$  disagrees with the ECPSSR model significantly on at  $E_{\alpha} < 2.0$  MeV. The large discrepencies noticed for  $\sigma_{L2}$ , figure 6.140, are reflected in  $\sigma_{L\gamma_{15}}^{\ X}$ , and hence in  $\sigma_{L\beta}^{\ X}$  cause  $\sigma_{Lt}^{\ X}$  to disagree with the ECPSSR predictions by as much as 40% at low impact energies, figure 6.147.

Measured values of  $\sigma_{L\alpha}^{X}/\sigma_{L\lambda}^{X}$  for incident alpha particles provide further evidence for the ratio being energy dependent, demonstrated in figure 6.148. The gross  $\sigma_{L_2}$  discrepencies cause  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  ratio, figure 6.149, to be overestimated considerably by the ECPSSR model. The same is true for  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratio shown in figure 6.150.  $\sigma_{L_2}$  deviations particularly cancel in the  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratios and consequently the experimental data provides a much better agreement with the ECPSSR theory, figure 6.151.

6.7 BISMUTH  $(Z_2 = 83)$ 

Cross sections for LL, L $\alpha$ , L $\beta$ , L $\gamma$ , L $\gamma_{15}$  and L $\gamma_{236844}$ ' (L $\gamma_{2368}$  in the case of deuteron and alpha particle impact) have been measured for the three projectiles incident on Bi.  $\sigma_{Li}$ 's were determined from  $\sigma_{L\gamma j}^{X}$  and  $\sigma_{L\gamma}^{X}$ .

6.7.1 Proton Impact Measurements

 $\sigma_{Li}$  and  $\sigma_{Lt}$  for incident protons are illustrated in figure 6.152. The structure in  $\sigma_{L_1}$ , as predicted by the theories at Ep  $\simeq$  1.8 MeV, is not indicated by the present measured values. In this E<sub>p</sub> region the data and the ECPSSR theory differ by upto 45%, below which the data converges towards the theory and may imply that the  $\sigma_{L_1}$  structure occurs at a lower E<sub>p</sub> value than predicted by the theory. The sparse values of Leite et al (1977) are much larger than the present data but show agreement at lower energies. The measured  $\sigma_{L_2}$  values lie above the ECPSSR theory by about 20-50%. The values of Leite et al (1977) deviate from the present data only at high impact energies and show close correlation with the ECPSSR model. In general the present  $\sigma_{L_3}$  and  $\sigma_{Lt}$  are in good agreement with the ECPSSR theory and with the data of Leite et al (1977).

The ECPSSR model explains the present  $\sigma_{L_1}/\sigma_{L_2}$  data at intermediate energies but deviates significantly at the extremities of the energy range, figure 6.153. Values measured by Leite et al (1977) show marked disagreement from the theories and from the present values. In the case of  $\sigma_{L_1}/\sigma_{L_2}$ , figure 6.154, the ECPSSR theory and the present values show good correlation only at low energies. As was the situation for  $\sigma_{L_1}/\sigma_{L_2}$ ,  $\sigma_{L_1}/\sigma_{L_3}$  values of Leite et al (1977) increasingly deviate from the results of this work as Ep increases. The  $\sigma_{L_2}/\sigma_{L_3}$  ratios are consistently underestimated by the theoretical models by upto 50% in the case of the present values and by upto 27% for the values of Leite et al (1977), figure 6.154.

 $\sigma_{LL}^{X}$  and  $\sigma_{L\alpha}^{X}$ , measured in this work and shown in figure 6.155, agree well with the ECPSSR model and with the measured data of Tawara et al (1975) and Leite et al (1977). The data of Bhattacharya et al (1980), however, lie significantly above the other values. With regard to the other experimental results the situation is similar for  $\sigma_{L\beta}^{X}$ , the ECPSSR model however, considerably underpredicts the measured data, figure 6.155. Large discrepencies between present  $\sigma_{L\gamma}^{X}$  and  $\sigma_{L\gamma_{15}}^{X}$  and the ECPSSR theory are also observed, figure 6.156. The other measured

values of  $\sigma_{L\gamma}^{X}$  describe larger deviations from the theory.  $\sigma_{L\gamma_{236844}}^{X}$ , figure 6.156, is also considerably underestimated by the ECPSSR theory and displays better agreement with the PWBA theory at low Ep. Agreement, however, is good between the present  $\sigma_{Lt}^{X}$  and the other measured data, except that of Bhattacharya et al (1980) which lie above the other values, figure 6.157. The ECPSSR model also offers a good description of the experimental values.

The present  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratios and those of Tawara et al (1975) show very good agreement with each other and with thoretical predictions figure 6.158. The present data, however, suggests a slow variation with Ep. Values of Bhattacharya et al (1980) lie significantly below the values of this study. All the measured  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  ratios agree with each other quite well but lie considerably below the thories, as shown in figure 6.159. The situation is very similar for  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratio, illustrated in figure 6.160. Comparison between the present  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$ values, and of other authors, show a reasonable agreement with the theories, figure 6.160.

### 6.7.2 Deuteron Impact Measurements

Figure 6.161 shows  $\sigma_{L_1}$  and  $\sigma_{Lt}$  for deuteron impact on Bi. At Ep < 1.8 MeV the  $\sigma_{L_1}$  data is explained well by the ECPSSR model and at higher energies the data converges towards the PWBA theory. The  $\sigma_{L_2}$  data lies above the ECPSSR theory by as much as 60%. Agreement with the ECPSSR theory is very good for  $\sigma_{L_3}$  and  $\sigma_{Lt}$  except at low energies.

The  $\sigma_{L_2}$  discrepencies are clearly apparent in figure 6.162, which shows  $\sigma_{L_1}/\sigma_{L_2}$ , particularly at low impact energies. Agreement is much better for  $\sigma_{L_1}/\sigma_{L_3}$ , figure 6.163, throughout the energy range. The measured  $\sigma_{L_2}/\sigma_{L_3}$  ratio lies systematically above the theory by about 40%, as shown in figure 6.164.

 $\sigma_{L_{x}}^{X}$  and  $\sigma_{L_{\alpha}}^{X}$ , shown in figure 6.165, follow the trend of  $\sigma_{L_{3}}^{X}$ and deviate from the ECPSSR only at Ep < 1.8 MeV. The  $\sigma_{L_{2}}^{X}$  deviations, figure 6.161, are reflected in  $\sigma_{L_{\beta}}^{X}$  which lie considerably above the theories, figure 6.165. The ECPSSR model underestimates  $\sigma_{L_{Y_{2368}}}^{X}$  by upto 40% and  $\sigma_{L_{Y}}^{X}$  and  $\sigma_{L_{Y_{15}}}^{X}$  by upto 50%, figure 6.166.  $\sigma_{L_{t}}^{X}$ , shown in figure 6.167, is in general explained better by the PWBA model than the ECPSSR.

The energy variation described by the measured  $\sigma_{L\alpha}^{X}/\sigma_{L\lambda}^{X}$  ratio for deuteron impact, figure 6.168, is much more marked than was noticed for incident protons, figure 6.158. The  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  and  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratios, measured in this study, are considerably overestimated by the theories, as demonstrated in figures 6.169 and 6.170 respectively. The  $\sigma_{L2}$  deviations cancel to a certain extent in  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratio and consequently the ratio shows reasonable agreement with ECPSSR predictions.

The present  $\sigma_{L_1}$  values for alpha particles incident on Bi, figure 6.171, exhibit good agreement with the ECPSSR model at intermediate energies. Values of Bhattacharya et al (1982) show reasonable agreement with the present data within the experimental uncertainties quoted by the author (15%). The present  $\sigma_{L_2}$  data, and that of Bhattacharya et al (1982), show much closer correlation with the PWBA theory than with the ECPSSR model, figure 6.171. In the case of  $\sigma_{L_3}$ and  $\sigma_{Lt}$ , shown in figure 6.172, they are explained well by the ECPSSR theory except at  $E_{\alpha} < 2$  MeV. Measurements of Bhattacharya et al (1982) show large deviations from the present data, particularly for  $\sigma_{L_3}$  where the deviations of upto a factor of 2.5 are observed.

 $\sigma_{L_1}/\sigma_{L_2}$  ratio, measured in this work, lies considerably below the theories and show increasing disagreement as  $E_{\alpha}$  decreases, figure 6.173. This is supported by the data of Bhattacharya et al (1982). Agreement with the theories is much better for the present  $\sigma_{L_1}/\sigma_{L_3}$  values
figure 6.174. Data of Bhattacharya et al (1982), however, depict very large discrepencies from the values of this study, particularly at lower impact energies. The situation is very similar for  $\sigma_{L_2}/\sigma_{L_3}$ , figure 6.175, with regard to the measured values of Bhattacharya et al (1982). The models underestimate the  $\sigma_{L_2}/\sigma_{L_3}$  ratio considerably at all energies.

 $σ_{L_{\alpha}}^{X} \text{ and } σ_{L_{\alpha}}^{X}, \text{ illustrated in figures 6.176 and 6.177, follow the} trend of σ_{L_{3}}^{X} and show good correlation with the ECPSSR model for <math display="block">E_{\alpha} > 2 \text{ MeV}. \quad \sigma_{L_{\beta}}^{X}, \text{ figure 6.177, disagree increasingly from the ECPSSR approximation as } E_{\alpha} \text{ decreases. } \sigma_{L_{\alpha}}^{X} \text{ and } \sigma_{L_{\beta}}^{X} \text{ values of Braziewicz et al} (1984) lie significantly below the present values and disagree by as much as 80% at high E_{\alpha}. The present <math>\sigma_{L_{Y2368}}^{X}$  values agree with the ECPSSR model at high energies but tend towards the PWBA curve as  $E_{\alpha}$  decreases figure 6.178.  $\sigma_{L_{Y15}}^{X}$  and  $\sigma_{L_{\gamma}}^{X}$ , shown also in figure 6.178, are explained well by the uncorrected PWBA theory. The  $\sigma_{L_{\gamma}}^{X}$  values of Braziewicz et al (1984) lie below the present data. The same is true for  $\sigma_{L_{\tau}}^{X}$ , illustrated in figure 6.179. The ECPSSR model, however, reproduces  $\sigma_{L_{\tau}}^{X}$  quite well at  $E_{\alpha} > 2.4$  MeV below which it underpredicts the data considerably.

The  $\sigma_{L\alpha}^{X}/\sigma_{L\ell}^{X}$  ratio is observed to depend on  $E_{\alpha}$ , in contrast to the ECPSSR theory, figure 6.180. The present  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  values, and those of Braziewicz et al (1984), shown in figure 6.181, are underpredicted by the ECPSSR model by upto 30%. Similar discrepencies are noticed for  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratio, illustrated in figure 6.182. In the case of  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratio reasonable agreement with the ECPSSR theory is established only at low energies, figure 6.183. The data of Braziewicz et al (1984) agrees well with the present values.

6.8 THORIUM  $(Z_2 = 90)$ 

Ll, La, LB, LB135, LB24615, LY, LY15 and LY2368 x-ray production cross sections have been determined for proton impact on Th.  $\sigma_{Li}$ 

were deduced from  $\sigma_{L\gamma_{i}}^{X}$  and  $\sigma_{L\alpha}^{X}$ .

The measured  $\sigma_{L_1}$  values, shown in figure 6.184 describe reasonable agreement with the ECPSSR theory except at  $E_p < 1.8$  MeV. The data of Leite et al (1977) are considerably higher than the present data. Only qualitative agreement with the ECPSSR model is observed for  $\sigma_{L_2}$ , figure 6.184, and the present data and that of Leite et al (1977) are underestimates markedly by the theory. In contrast,  $\sigma_{L_3}$  is explained well by the ECPSSR approximation and also shows good agreement with the values of Leite et al (1977) figure 6.185.  $\sigma_{Lt}$ , however, deviates significantly from the data of Leite et al (1977) and from the ECPSSR prediction at Ep > 2 MeV, also shown in figure 6.185.

The  $\sigma_{L_2}$  discrepencies are strikingly apparent in the case of  $\sigma_{L_1}/\sigma_{L_2}$ ratio, illustrated in figure 6.186, where the data and the ECPSSR theory differ by upto a factor of 2. The data of Leite et al (1977) disagrees only at 3 MeV with the measurements of this study. Correlation between the present  $\sigma_{L_1}/\sigma_{L_3}$  values and the ECPSSR theory is reasonable except at energies around 2.2 MeV, figure 6.187. Values of Leite et al exhibit large disagreements with the present data. The  $\sigma_{L_2}/\sigma_{L_3}$  ratio is underestimated by the theories by about 70% and differs from the values of Leite et al (1977) at high Ep, as demonstrated in figure 6.188.

The present  $\sigma_{LL}^{X}$  measurements show very good correlation with the ECPSSR model and the situation is similar for  $\sigma_{L\alpha}^{X}$ , figure 6.189. Agreement for  $\sigma_{L\alpha}^{X}$  with the values of Leite et al (1977) is reasonable but rather poor with regard to the data of Bearse et al (1973) which are considerably below the present measurements. The nontrivial deviations observed for  $\sigma_{L_2}$ , figure 6.184, are reflected in  $\sigma_{L\beta_{135}}^{X}$  and hence in  $\sigma_{L\beta}^{X}$ , shown in figure 6.190. The values of  $\sigma_{L\beta_{24615}}^{X}$ , figure 6.190, follow the behaviour of  $\sigma_{L_3}$  and describe satisfactory agreement

with the ECPSSR model.  $\sigma_{L\gamma}^{X}$  and  $\sigma_{L\gamma_{15}}^{X}$ , although agreeing qualitatively with the ECPSSR theory, are significantly underestimated by the theory, figure 6.191. Deviations between  $\sigma_{L\gamma_{2368}}^{X}$  and the ECPSSR predictions increase with increasing Ep to about 45%, figure 6.191. The description of the measured  $\sigma_{Lt}^{X}$  data is quite good by the ECPSSR model except at Ep > 2 MeV, as shown in figure 6.192. Measurements of Leite et al (1977) disagree with the present data as Ep decreases.

 $\sigma_{L\alpha}^{X}/\sigma_{L\ell}^{X}$  ratio, shown in figure 6.193, decreases at Ep < 2 Mev, unlike the theory which remains constant. Large differences between theory and present data are noticed for  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  and  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratios, illustrated in figure 6.194 and 6.195 respectively. Much smaller deviations although still significant, are observed for  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratio, as shown in figure 6.196.

6.9 URANIUM  $(Z_2 = 92)$ 

Proton induced L<sub>l</sub>, L<sub>a</sub>, L<sub>β</sub>, L<sub>β135</sub>, L<sub>β24615</sub>, L<sub>Y</sub>, L<sub>Y15</sub> and L<sub>Y2368</sub> x-ray production cross sections have been measured for U.  $\sigma_{\text{Li}}$  were determined from  $\sigma_{\text{LY}_{i}}^{X}$  and  $\sigma_{\text{La}}^{X}$ .

Figure 6.197 shows  $\sigma_{L_1}$  and  $\sigma_{L_2}$  measured in the present study. Disagreement for  $\sigma_{L_1}$  is observed from the ECPSSR values only at Ep around 2.2 MeV. The data of Leite et al (1977) shows good correlation with the present  $\sigma_{L_1}$  values except at 3 MeV. The present  $\sigma_{L_2}$  values, and those of Leite et al (1977), are underpredicted by the theories significantly. However,  $\sigma_{L_3}$  and  $\sigma_{Lt}$ , illustrated in figure 6.198, describe good agreement with the data of Leite et al (1977) and with the ECPSSR model.

The theories deviate increasingly from the present  $\sigma_{L_1}/\sigma_{L_2}$  ratio at Ep < 2.2 MeV while the data of Leite et al (1977) show good correlation, figure 6.199. In the case of  $\sigma_{L_1}/\sigma_{L_3}$ , shown in figure 6.200, the theories underestimate the ratio at Ep > 2 MeV. The values of

Leite et al (1977) disagree only at 3 MeV. The present  $\sigma_{L_2}/\sigma_{L_3}$  lie about 50% above the theories, the values of Leite et al (1977) describe even larger deviations, figure 6.201.

As was the case for  $\sigma_{L_3}$ ,  $\sigma_{L_2}^{X}$  and  $\sigma_{L_3}^{X}$  are described well by the ECPSSR model, figure 6.202. The other measured values of Tawara et al (1975), Leite et al (1977), and Bhattacharya et al (1980) show close agreement with the present values. The ECPSSR model explains  $\sigma^{\rm X}_{{\rm L}\beta_{24615}}$ quite well but significantly underestimates  $\sigma^{\ X}_{L\beta_{135}}$  and  $\sigma^{\ X}_{L\beta}$ , as shown in figure 6.203. The  $\sigma_{LB}^{X}$  values of Tawara et al (1975) describe better agreement with the ECPSSR model at higher energies than the present data but agree with the present values, as do the data of Bhattacharya et al (1980), at lower energies.  $\sigma^{X}_{L\gamma_{2368}}$  values measured in this work, follow the ECPSSR curve closely at Ep < 2 MeV but deviate above the theory at higher energies, figure 6.204. In the case of  $\sigma_{L\gamma_{1,c}}^{\chi}$  and  $\sigma_{L\gamma_{1,c}}^{\chi}$ , shown also in figure 6.204, describe only the energy dependence predicted by the ECPSSR model and lie above the theory. The other experimental  $\sigma_{Ly}^{X}$  values depict even larger descrepencies. Good agreement is observed for the present  $\sigma_{Lt}^{X}$  values with the ECPSSR predictions and with the other experimental data, as illustrated in figure 6.205.

Unlike the previous measurements, the  $\sigma_{L\alpha}^{X}/\sigma_{L\lambda}^{X}$  ratios for incident protons on U, figure 6.206, do not appear to depend on E<sub>p</sub> noticibly and describe good correlation with the constant value predicted by the theory. The other measured data seems to support this observation. All the measured  $\sigma_{L\alpha}^{X}/\sigma_{L\beta}^{X}$  values agree well with each other, figure 6.207, but lie considerably below the predicted curves.  $\sigma_{L\alpha}^{X}/\sigma_{L\gamma}^{X}$  ratio of Bhattacharya et al (1980) shows better agreement with the values of this work than the data of Tawara et al (1975), figure 6.208. However, all values are overpredicted significantly by the theories. The present  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratios agree quite well with the ECPSSR model, in contrast to

the values of other authors which lie considerably below the theories, particularly those of Tawara et al (1975).

6.10 TARGET ATOMIC NUMBER DEPENDENCE

To investigate the dependence of  $\sigma_{Li}$  and  $\sigma_{Lt}$  on target atomic number (Z<sub>2</sub>) the appropriate cross sections were plotted versus Z<sub>2</sub> for 2 MeV incident ions. Figures 6.210-6.212 illustrate the Z<sub>2</sub> dependence for incident protons, deuterons and alpha particles respectively.

For incident protons the ECPSSR model predicts quite well the variation of  $\sigma_{L_1}$  with  $Z_2$  except for Pb and Bi the values of which lie above the theoretical curve, figure 6.210. The PWBA theory yields the better agreement with the measured  $\sigma_{L_2}$  data for Dy, Yb, W, Au, Pb, and Bi. In the case of Th and U the model considerably underestimates the present values.  $\sigma_{L_3}$  and  $\sigma_{Lt}$  for all elements of interest are described well by the ECPSSR predictions, as shown in figure 6.210.

The flattening of the  $\sigma_{L_1}$  curve for incident 2 MeV deuterons at  $Z_2 \approx 80$ , figure 6.211, as predicted by the ECPSSR model, is reproduced quite reasonably by the present data. With regard to  $\sigma_{L_2}$  all values, except those for Pb and Bi, follow closely the trend described by the PWBA model. As with incident proton measurements  $\sigma_{L_3}$  and  $\sigma_{Lt}$ , shown in figure 6.211, show very good agreement with the ECPSSR model.

 $\sigma_{L_1}$ ,  $\sigma_{L_3}$  and  $\sigma_{Lt}$  for 2 MeV incident alpha particles are explained reasonably by the ECPSSR theory whereas the PWBA theory exhibits better correlation with the  $\sigma_{L_2}$  data, as illustrated in figure 6.212. 6.11 GENERAL COMPARISON WITH THE ECPSSR THEORY

The ratio  $R_i = \sigma_{Li}^{exp} / \sigma_{Li}^{ECPSSR}$  (exp = experimental), for the elements under study, has been plotted versus the corrected reduced velocity parameter,  $\xi_{Li}^R$ , defined by equation 4.54, for incident protons, deuterons and alpha particles. The resulting graphs indicate certain trends described by the measured data which are discussed below.

Figures 6.213-6.215 show R<sub>j</sub> for L<sub>1</sub>, L<sub>2</sub> and L<sub>3</sub> subshells for incident protons. R<sub>1</sub> clearly shows the large disagreement from the theory, upto 70%, for  $\xi_{L_1}^R < 0.7$ . Above this value of  $\xi_{L_1}^R$  the ECPSSR model predicts the measured  $\sigma_{L_1}$  to within 15%. The considerable  $\sigma_{L_2}$ deviations noticed for the individual elements are dramatically displayed in the R<sub>2</sub> versus  $\xi_{L_2}^R$  plot, shown in figure 6.214. The magnitude of this deviation appears to increase for heavier elements to about 60% for U. The theory reproduces the  $\sigma_{L_3}$  values for all elements of interest to within 20% although agreement improves as  $\xi_{L_3}^R$  increases, as demonstrated in figure 6.215.

In the case of deuteron impact the  $\sigma_{L_1}$  data, represented by  $R_1$ in figure 6.216, does not appear to depend on  $\xi_{L_1}^R$  as clearly as did the proton data but deviations of nearly 50% are indicated by figure 6.216. With the exception of Dy  $\sigma_{L_1}$  values of the high  $Z_2$  elements tend to be larger than the ECPSSR predictions at all values of  $\xi_{L_1}^R$ , whereas the lower  $Z_2$  elements, Dy, Yb and W tend to yield values smaller than predicted.  $\sigma_{L_2}$  deviations, shown in figure 6.217, range from 10-60% above the theory with deviations tending to increase as  $\xi_{L_2}^R$  decreases In contrast elements with intermediate  $Z_2$  values appear to yield smaller  $\sigma_{L_3}$  than predicted by the ECPSSR model, as shown in figure 6.218. This plot of  $R_3$  reveals the much better description of  $\sigma_{L_3}$  by the ECPSSR model than for  $\sigma_{L_1}$  and  $\sigma_{L_2}$ .

With regard to incident alpha particles disagreement for  $\sigma_{L_1}$  highlighted by the R<sub>1</sub> versus  $\xi_{L_1}^R$  plot shown in figure 6.219, ranges upto nearly 50%. With the exception of Bi,  $\sigma_{L_1}$  data for higher  $Z_2$  elements tend to be larger than the ECPSSR values and those of Yb and W are smaller at all  $\xi_{L_1}^R$  values studied. Gross  $\sigma_{L_2}$  deviations are highlighted by figure 6.220, especially at  $\xi_{L_2}^R < 0.4$  where experiment and ECPSSR theory differ by as much as a factor of 3.5. These

particularly large discrepencies are displayed by Pb and Bi. Furthermore agreement between theory and experiments at best is only 25%. In general,  $\sigma_{L_3}$  is explained well by the ECPSSR model and deviation do not appear to exceed 30%, as demonstrated in figure 6.221. With the exception of Yb all other R<sub>3</sub> values appear to crossover the R<sub>3</sub> = 1 line at  $\xi_{L_3}^R \approx 0.4$ .

Much of the above observations are supported by the recent works of Cohen (1983) and Mukoyama and Sarkadi (1983a, b) for proton and helium impact, although the present  $\sigma_{L_1}$  data indicate larger discrepencies than reported by these authors. A comparison of deuteron impact measurements does not appear to be available. The considerable deviations revealed by the present, and other measurements of  $\sigma_{Li}$ discussed in this thesis, clearly highlight the need for a more detail approach to the inner-shell ionisation phenomena. The possible reasons for these large disagreements, particularly for the  $L_2$  subshell, are considered below. Firstly these disagreements may point directly at the approximate nature of the PWBA theory. More realistic atomic wave functions, instead of the hydrogenic type, would be desriable. Recently Mukoyama and Sarkadi (1983a, b) have employed relativistic, but still hydrogenic, wave functions and have noticed improvements in the calculated values of  $\sigma_{Li}$ . The relativistic Hartree-Fock type wave functions have been employed by Pauli et al (1978) in their impact-parameter-dependent treatment of inner-shell ionisations and they have observed significant improvements in  $\sigma_{Li}$  values. Secondly, the ECPSSR theory evaluates the Coulomb and binding energy correction by assuming the validity of the monopole approximation (Brandt and Lapicki 1979). As pointed out by Mukoyama and Sarkardi (1983b) dipole and quadrupole transitions may play an important role in the case of  $L_2$  and  $L_3$  subhsell ionisation. Sarkardi and Mukoyama (1981)

have proposed a futher reason for these disagreements. They emphasise the need for taking into account collision-induced intra-shell transitions which will also affect  $\sigma_{Li}$ . Finally, the significant uncertainties in the atomic parameters, discussed in chapter 2, which are required to deduce  $\sigma_{Li}$  from  $\sigma_{Lj}^{X}$ , are also a source of concern and increase the difficulty in reaching precise conclusions regarding the actual reasons for the aforementioned discrepencies. Consequently, much more work is required in this field before the phenomena of innershell ionisation can be adequately understood and quantified.





- \* i To obtain the numerical values of the cross sections multiply by the factor indicated.
- ii Error bars are omitted where they are too small to be seen clearly.



Figure 6.2. Experimental  ${}^{\sigma}L_1 / {}^{\sigma}L_2$  ratio for proton impact on Dy.



proton impact on Dy.



Figure 6.4. Experimental LL and L $\alpha$ + $\eta$  x-ray production cross sections for proton impact on Dy.



Figure 6.5. Experimental total LB and partial LB<sub>j</sub> x-ray production cross sections for proton impact on Dy.



Proton energy (MeV)

Figure 6.6. Experimental total  $L_{\gamma}$  and partial  $L_{\gamma j}$  x-ray production cross-sections for proton impact on Dy.



Proton energy (MeV)







Figure 6.9. Experimental  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\beta}^{X}$  ratio for proton impact on Dy.





Figure 6.10. Experimental  $\sigma_{L\alpha+\eta}^{X}/\sigma_{L\gamma}^{X}$  and  $\sigma_{L\beta}^{X}/\sigma_{L\gamma}^{X}$  ratios for proton impact on Dy.



Deuteron energy (MeV)

Figure 6.11. Experimental total (L<sub>t</sub>) and individual L<sub>i</sub> subshell ionisation cross sections for deuteron impact on Dy.



Deuteron energy (MeV)

Figure 6.12. Experimental  $\sigma_{L_1}/\sigma_{L_2}$ ,  $\sigma_{L_1}/\sigma_{L_3}$  and  $\sigma_{L_2}/\sigma_{L_3}$  ratios for deuteron impact on Dy.



Figure 6.13. Experimental L and L  $_{\alpha+\eta}$  x-ray production cross sections for deuteron impact on Dy.



Deuteron energy (MeV)

Figure 6.14. Experimental total  $L_{\beta}$  and partial  $L_{\beta}$  x-ray production cross sections for deuteron impact on Dy.



















cross sections for proton impact on Yb.


































Figure 6.40. Experimental  $L_1$  and  $L_2$  subshell ionisation cross sections for alpha particle impact on Yb.





Figure 6.41. Experimental total L shell and  $L_3$  subshell ionisation cross sections for alpha impact on Yb.



Figure 6.42. Experimental  $\sigma_{L_1}/\sigma_{L_2}$  ratio for alpha particle impact on Yb.



Figure 6.43. Experimental  $\sigma_{L_1}/\sigma_{L_3}$  ratio for alpha particle impact on Yb.





Figure 6.44. Experimental  $\sigma_{L_2}/\sigma_{L_3}$  ratio for alpha particle impact on Yb.





Figure 6.45. Experimental L and L array production cross sections for alpha particle impact on Yb.



Alpha particle energy (Mev)

Figure 6.46. Experimental total  $L_{\beta}$  and partial  $L_{\beta j}$  x-ray production cross sections alpha particle impact on Yb.



Figure 6.47. Experimental total Ly and partial Ly j x-ray production cross sections for alpha particle impact on Yb.



Figure 6.48. Experimental total L x-ray production cross section for alpha particle impact on Yb.



alpha particle impact on Yb.



Figure 6.50. Experimental  $\sigma_{L_{\alpha+\eta}}^{X} / \sigma_{L_{\beta}}^{X}$  ratio for alpha particle impact on Yb.



Figure 6.51. Experimental  $\sigma_{L_{\alpha+\eta}}^{X} / \sigma_{L_{\gamma}}^{X}$  and  $\sigma_{L_{\beta}}^{X} / \sigma_{L_{\gamma}}^{X}$  ratios for alpha particle impact on Yb.



Figure 6.52. Experimental L subshell ionisation cross sections for proton impact on W.



Figure 6.53. Experimental total L shell ionisation cross section for proton impact on W.



Figure 6.54. Experimental  ${}^{\sigma}L_1/{}^{\sigma}L_2$  ratio for proton impact on W.



proton impact on W.



Figure 6.56. Experimental  $L_{l}$  and  $L_{\alpha+\eta}$  x-ray production cross sections for proton impact on W.



Figure 6.57. Experimental total  $L_{\beta}$  and partial  $L_{\beta}$  x-ray production cross sections for proton<sup>j</sup> impact on W.









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Figure 6.63. Experimental  $L_1$  and  $L_2$  subshell ionisation cross sections for deuteron impact on W.




























Figure 6.75. Experimental  $L_3$  subshell and total L shell ionisation cross sections for alpha particle impact on W.





Figure 6.76. Experimental  $\sigma_{L_1}/\sigma_{L_2}$  ratio for alpha particle impact on W.



Figure 6.77. Experimental  $\sigma_{L_1}/\sigma_{L_3}$  ratio for alpha particle impact on W.



 $\sigma_{L_2}/\sigma_{L_3}$ 

Figure 6.78. Experimental  $\sigma_{L_2}/\sigma_{L_3}$  ratio for alpha particle impact on W.



Figure 6.79. Experimental  $L_{g}$  and  $L_{\alpha+\eta}$  x-ray production ratios for alpha particle impact on W.















Figure 6.82. Experimental total L shell x-ray production cross section for alpha particle impact on W.























sections for proton impact on Au.











proton impact on Au.
















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on Pb.























impact on Pb.






 $\sigma_{L\alpha/\sigma_{L\beta}^{\times}}^{\times}$ 











impact on Pb

351















impact on Pb.

•



impact on Pb.





 $^{\sigma}\!L_1/^{\sigma}\!L_2$ 











•





















 $\sigma_{L\alpha/\sigma_{Lk}^{\times}}^{\times}$ 










impact on Bi.











impact on Bi.











impact on Bi.



 $\sigma_{L_1}$  and  $\sigma_{L_2}$  (barns)

Figure 6.184. Experimental  $L_1$  and  $L_2$  subshell ionisation cross sections for proton impact on Th.



Figure 6.185. Experimental  $L_3$  subshell and total L shell ionisation cross sections for proton impact on Th.







Figure 6.187. Experimental  $\sigma_{L_1}/\sigma_{L_3}$  ratio for proton impact on Th.



proton impact on Th.











Figure 6.190. Experimental total  $L_{\beta}$  and partial  $L_{\beta j}$  x-ray production cross sections for proton impact on Th.







Figure 6.192. Experimental total L shell x-ray production cross section for proton impact on Th.











La /or

proton impact on Th.







Proton energy (MeV)





Figure 6.198. Experimental  $L_3$  subshell and total L shell ionisation cross section for proton impact on U.



 $\sigma_{L_1}^{}/\sigma_{L_2}^{}$ 

Figure 6.199. Experimental  $\sigma_{L_1}/\sigma_{L_2}$  ratio for proton impact on U.



Figure 6.200. Experimental  $\sigma_{L_1}/\sigma_{L_3}$  ratio for proton impact on U.



proton impact on U.















on U.


















 $R_{1} = \frac{\alpha exp}{\alpha L_{1}} / \frac{ECPSSR}{\alpha L_{1}}$ 







 $R_{3} = \frac{\sigma_{L_{3}}^{exp}}{\sigma_{L_{3}}^{o}}/\sigma_{L_{3}}^{o}$ 



 $R_{1} = \frac{\sigma_{exp}}{\sigma_{L_{1}}} / \sigma_{L_{1}}^{ECPSSR}$ 



\*









CHAPTER 7

CONCLUSIONS

A systematic study of L shell ionisation by incident protons (p) deuterons (d) and alpha particles ( $\alpha$ ) on selected medium to high atomic number elements has been performed. L shell x-ray production  $(\sigma_{Lj}^{X})$  and ionisation  $(\sigma_{Li})$  cross sections have been measured for p and d impact on Dy, p, d and  $\alpha$  impact on Yb, W, Au, Pb and Bi and p impact on Th and U. To avoid any systematic uncertainties being introduced into  $\sigma_{Lj}^{X}$  and  $\sigma_{Li}$  by the Si(Li) detector efficiency and the target thickness these quantities were measured independently. In order to deduce  $\sigma_{Li}$  from  $\sigma_{Lj}^{X}$  a spectrum fitting programme has been written in Fortran 77 to extract the partially resolved components of L<sub>y</sub>.

Comparisons of  $\sigma_{Lj}^{X}$  and  $\sigma_{Li}$  have been made with the available recent data and with the PWBA and the ECPSSR theories for incident protons and alpha particles. In the case of deuteron impact there does not appear to be any available published data for the elements of interest and consequently comparison was performed only with the theories. A comprehensive compilation of all the available tabulated experimental data of  $\sigma_{Lj}^{X}$  and  $\sigma_{Li}$  for proton bombardment from 1975 to November 1982 has been prepared (Sokhi and Crumpton 1984 and see Appendix E). This greatly facilitated the comparison of proton impact measurements.

Large discrepencies between the present  $\sigma_{Lj}^{x}$  and  $\sigma_{Li}$  data and the ECPSSR model have been revealed. These disagreements are dramatically apparent when comparing the ratio  $R_i = \sigma_{Li}^{exp} / \sigma_{Li}^{ECPSSR}$ (exp = experimental) versus the corrected reduced velocity parameter  $(\xi_{l,i}^{R})$  of the ECPSSR theory.

In the case of proton impact R<sub>1</sub> highlighted discrepencies of upto 70% at  $\xi_{L_1}^R < 0.7$ , above which deviations of about 15% were observed. The ECPSSR theory consistently underpredicts the  $\sigma_{L_2}$  data. Z<sub>2</sub>

dependent discrepencies of upto 60% have been revealed by the  $R_2$  plot. The ECPSSR theory, however, is successful to within 20% in explaining  $\sigma_{1,2}$ .

With regard to incident deuterons deviations of upto 50% are indicated by R<sub>1</sub> and 60% by R<sub>2</sub> whereas R<sub>3</sub> shows much better agreement with the ECPSSR predictions. For alpha particle impact R<sub>1</sub> reveals disagreements of upto 50% and upto 30% for R<sub>3</sub>. In the case of R<sub>2</sub> the ECPSSR theory underestimates the experimental  $\sigma_{L_2}$  data by as much as a factor of 3.5, particularly for high Z<sub>2</sub> elements and at  $\xi_{L_2}^{R} < 0.4$ .

Similar observations have been reported by Cohen (1983) and Mukoyama and Sarkardi (1983a, b) for proton and helium impact. The present data, however, tends to indicate larger L1 discrepencies than those found by these workers. Possible reasons for the considerable discrepencies highlighted by the present measurements have been discussed in section 6.11. Essentially a more realistic treatment for explaining inner-shell ionisation is required instead of the present theory which relies on the inadequate assumptions of the plane-wave Born approximation. This would probably entail a many-body approach to the inner-shell ionisation problem although such a treatment admittedly is very difficult. Much experimental work also needs to be conducted, not only in connection with absoluted Li subshell ionisation cross section measurements but also in allied research field such as impact-parameter-dependent cross section measurements. In addition investigation of the inner-shell alignment effect would provide further insight into the inner-shell ionisation mechanism. The  $\sigma_{L\alpha}^{X}/\sigma_{L\alpha}^{X}$  ratio measurements performed in this study indicate directly the need for incorporating this effect into the final theory.

In conclusion, this study has highlighted significant inadequacies in the ECPSSR theory when applied to the phenomena of L shell ionisation

during highly asymmetric ion-atom collisions. Satisfactory explanation of L shell ionisation is obviously a prerequisite before ionisation mechanisms of higher and more complicated electronic shells can be understood and certainly before the advent of a unified theory of inner-shell ionisation can be envisaged. It is hoped that this study has provided useful information not only regarding the precise measurements of L shell x-ray production and ionisation cross sections but also regarding the future direction of research in this field.

# APPENDIX A

# SEMI-CLASSICAL AND BINARY

# ENCOUNTER APPROXIMATIONS

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## A.1 INTRODUCTION

This appendix reviews the principles and developments of the semiclassical and the binary encounter approximations. Although these theories offer alternative interpretations of the inner-shell ionisation phenomena to that of the plane-wave Born approximation (PWBA), discussed in chapter 4, the fact that they can be related to the PWBA has been noted in this appendix.

Emphasis has been placed on discussing the main assumptions on which the two models are based and only the final expressions, required for calculating the ionisation cross sections, are quoted, although sources which offer greater detail have been referenced. As in Chapter 4 cgs units have been adopted.

## A.2 SEMI-CLASSICAL APPROXIMATION

An approach which relies on a classical description of the projectile motion and a quantum mechanical description of the atomic inner-shell electron was introduced by Bang and Hansteen (1959) to study atomic Coulomb excitation. The applicability of this semi-classical approximation (SCA) rests on the Bohr's criterion (Bohr 1948) for a classical treatment of an incoming ionising charged particle being fulfilled, that is, the distance of closest approach (2d) in a head-on collision must be much greater than the de Broglie wavelength (x) for the projectile, or

$$\kappa = \frac{2d}{\hbar} = \frac{2Z_1Z_2e^2}{\hbar v_1} >> 1$$
 A.1

where d =  $Z_1Z_2e^2/(M_1v_1^2)$ ,  $Z_1$  is the atomic number of the projectile of mass  $M_1$  and velocity  $v_1$  and  $Z_2$  is the atomic number of the target atom. Provided that  $Z_1 << Z_2$  and that the projectile is light and swift, the Coulomb interaction between the projectile and the inner-shell electron causing the latter to be ejected from the tightly bound inner-shell to the continuum can be treated as a time-dependent perturbation of the target atom, V(t), (Madison and Merzbacher 1975). This perturbing potential has the form

$$V(t) = \frac{Z_1 e^2}{|r - R(t)|}$$

where  $\underline{R}(t)$  represents the time-dependent position vector of the projectile and  $\underline{r}$  the position vector of the atomic electron. In order to reduce computational difficulties associated with the SCA model the projectile is assumed to be moving with a uniform velocity in a straight line. This assumption is valid provided that (Madison and Merabacher 1975)

A.2

 (i) the contribution of the elastic nuclear scattering to the inelastic collision at small impact parameters is negligible, and

 (ii) the velocity of the incident particle does not change significantly as a consequence of the inelastic interaction.

The first condition requires that the radius of the Coulomb barrier be small compared with the radius of the inner-shell orbit and this is satisfied if  $Z_1$  is small and if the incident particle energy is much greater than the relevent atomic ionisation potential. The minimum momentum transfer to the atom  $(q_{min})$  is given by equation 4.2.4 provided that the energy lost  $(\varepsilon)$  by the projectile is much less than its initial energy. Thus, condition (ii) is fulfilled if

$$A_{\min} \leq k_i$$
 A.3

where k<sub>i</sub> is the initial momentum wave number of the motion (see equation 4.22) and, therefore, the deflection of the projectile may be neglected making the straight-line trajectory description of the projectile appropriate. The minimum momentum transfer is usually approximated as

$$\hbar q_{\min} \simeq \frac{\varepsilon}{v_1}$$
 A.4

(provided  $\varepsilon \ll E$ ) and where

$$\varepsilon = I_{li} + E_f$$
 A.5

 $I_{Li}$  being the binding energy of the inner-shell electron, L-shell in the present context, and  $E_f$  the final energy of this electron after ejection.

As with the PWBA the electronic states are described by non-relativistic

hydrogenic wave functions. The inner and outer screening effects are taken into account in the same fashion as for the PWBA. An important difference between the SCA and the PWBA is that the classical description of the incident particle introduces the impact parameter in the formulation of the SCA (Hansteen and Mosebekk 1973). Details of this formulation are given by Bang and Hansteen (1959), Hansteen (1975) and Madison and Merzbacher (1975) and only the final results are given here.

A coordinate system centred at the target nucleus is employed, the z-axis of which is in the direction of the incident particle moving in the y-z plane. For an incident particle with impact parameter, b, the differential Coulomb ionisation probability per energy interval  $dE_f$  of the ejected electron is given by (Hansteen and Mosebekk 1973)

$$\frac{dI_{b}}{dE_{f}} = \frac{1}{\hbar^{2}} \left| \int_{-\infty} e^{i\omega t} < f|V(t)| i > dt \right|^{2}$$
 A.6

where i and f represent the initial and final states of the electron respectively and the frequency  $\omega = \varepsilon/\hbar$  ( $\varepsilon$  is given by equation 4.70). Disregarding the Coulomb deflection of the projectile and assuming a straight-line trajectory equation A.6 may be rewritten as (Bang and Hansteen 1959)

$$\frac{dI_{b}}{dE_{f}} = \frac{2Z_{1}^{2}M_{1}e^{4}}{E\hbar^{2}}|M_{b}|^{2} \qquad A.7$$

with

$$M_{p} = \int d\tau \ \psi_{f}^{*} \ \psi_{i} e^{iq_{min}Z} \kappa_{0}(q_{min}\rho)$$
 A.8

where  $M_p$  is the matrix element,  $d\tau = dxdydz$ ,  $\psi_i$  and  $\psi_f$  are the screened hydrogenic wave functions for the inital and final atomic electron states,  $K_0(q_{min}\rho)$  is the modified Bessel function of the third kind and zeroth order with

$$q_{\min} = \omega / v_1$$
 A.9

and

$$\rho^2 = x^2 + (b - y)^2$$
 A.10

The Coulomb ionisation probability is now given by (Hansteen et al 1975)

$$b = \int_{0}^{\infty} \left( \frac{dIb}{dEf} \right) dEf$$
 A.11

and the total Coulomb ionisation cross section by

I

$$\sigma^{\text{SCA}} = 2\pi \int_{0}^{\infty} bdb I_{b} \qquad A.12$$

The matrix element  $M_p$  has been evaluated numerically by Hansteen et al (1975) with a maximum uncertainty of about 5%. These authors have expressed the straight-line SCA equations A.11 and A.12 in terms of special variables which allow the expressions to be scaled approximately for different target atoms. For a given subshell, belonging to the L-shell in the present case, characterised by hydrogenic quantum numbers  $n_L$  and  $\ell_{Li}$ , the ionisation probability,  $I_{bLi}$ , can be expressed in terms of the generalised ionisation probability functions  $G_{n_\ell}$  ( $X_{Li}$ ,  $B_{Li}$ ),

$$I_{bLi} = \begin{pmatrix} 2j_{Li} + 1 \\ Z\ell_{Li} + 1 \end{pmatrix} \frac{Z_1^2}{Z_2^2 L^{\theta} L_i} G_{nL\ell_{Li}} (X_{Li}, B_L)$$
 A.13

where  $n_{L} = 2$ ,  $\ell_{L} = 0$ ,  $\ell_{L_{2}} = \ell_{L_{3}} = 1$ ,

 $j_{L_1} = j_{L_2} = \frac{1}{2}$  and  $j_{L_3} = 3/2$ . The term in parenthesis is a statistical factor. The generalised ionisation probability functions in equation A.13 is a function of the quantities defined as

$$X_{\text{Li}} = \frac{Z_{2\text{L}}\theta_{\text{Li}}}{n_{\text{L}}E^{\frac{1}{2}}}$$
 A.14

where E is the projectile energy in MeV/amu and

$$B_{L} = \frac{b Z_{2L}}{n_{L} a_{0}}$$

where b is the impact parameter and  $a_0$  is the Bohr radius = 5.29 x  $10^{-9}$  cm. By substituting equation A.13 into A.12 and performing the integration the total cross section can be expressed as

$$\sigma_{Li}^{SCA} = \left(\frac{2j_{Li}+1}{2\ell_{Li}+1}\right) \frac{Z_1^2}{Z_2^4 L^{\theta} L^i} F_{n_L} \ell_{Li} (X_{Li})$$
 A.16

with

$$F_{n_{L}\ell_{Li}}(X_{Li}) = 2\pi a_{0}^{2} n_{L}^{2} \int B_{L} dB_{L}G_{n_{L}\ell_{Li}}(X_{Li}, B_{L})$$
 A.17

where  $F_{n_{L}\ell Li}$  is the generalised function for the total cross section and has the dimensions of length squared. The  $Z_2$  - scaling relations A.13 and A.16 are valid only for  $X_{Li} > 5$  (which holds for this work) but only to a few percent. For higher energies ( $X_{Li} \leq 5$ ) Hansteen et al (1975) have determined a correction factor,  $\mu_n \ell_{Li}$ , which is dependent on  $\theta_{Li}$  and  $X_{Li}$ . For this energy range the corrected cross sections are obtained by multiplying expression A.16 by  $\mu_n \ell_{Li} (\theta_{Li}, X_{Li})$  tabulated by Hansteen et al (1975). For different projectiles the simple  $Z_1^2$  - scaling law can be employed (as for the PWBA),

$$\sigma_{Li}^{SCA}(Z_1, v_1) = Z_1^2 \sigma_{Li}^{SCA}(Z_1 = 1, v_1)$$
 A.18

However, since the magnitude of the perturbation depends on  $Z_1$  and that the SCA, like the PWBA, is based on the assumption that the perturbation is small, the above scaling law is applicable only for light charged particles, such as those considered in this work.

The following points should be noted in connection with the SCA model

- (i) The straight line trajectory is only applicable in collisions where the ionisation process does not significantly effect the projectile path. This is justified when the energy of the projectile is much greater than the binding energy of the inner-shell in consideration (Madison and Merzbacher 1975).
- (ii) The SCA model allows the ionisation cross sections to be calculated as a function of the impact parameter, thus making it possible to test the inequality A.1 (Hansteen and Mosebekk 1973).
- (iii) The maximum contribution to inner-shell ionisation arises from impact parameters of a certain value denoted by  $b_{max}$ . For adiabatic collisions ( $v_1 << v_{2L}$ )  $b_{max}$  lies deep inside the respective electron shell (Hansteen and Mosebekk 1970). As the collision loses its adiabaticity, that is, as the projectile energy increases,  $b_{max}$ , also increases and lies in the vicinity of the Bohr radius of the electron shell

- (iv) In relation to the total L-shell ionisation cross section for gold Hansteen and Mosebekk (1973) have shown the relative contributions from the three L-subshells. In the extremities of the projectile energies the 2s state contributes the most to the total ionisation cross section where as in the intermediate energy region, which is studied here, the 2p states are the major contributors. This behaviour is a reflection of the relative, radial electron distributions for a hydrogen-like gold atom (Hansteen and Mosebekk 1973).
- (v) Bearing in mind points (iii) and (iv) the plateau exhibited by the  $2s_{\frac{1}{2}}$  ionisation cross section at low energies can be explained (Hansteen 1975). At low bombarding energies impact parameters comparable to or less than the adiabatic radius,  $r_{ad}$ , defined as

$$r_{ad} \simeq \frac{1}{q_{min}} = \frac{\hbar v_1}{\epsilon}$$
 A.19

dominate in the ionisation process. Here the  $2s_{\frac{1}{2}}$  electrons give the largest contributions to the cross section. As the projectile energy increases so does  $b_{max}$  and the  $2s_{\frac{1}{2}}$  radial electron density distribution function exhibits a node while the 2p functions increase monotonically and become increasingly important. This node is reflected as a plateau in the  $2s_{\frac{1}{2}}$  ionisation cross section whereas the 2p cross sections show a monotonic behaviour.

(vi) For total ionisation cross section the equivalence of the straight-line SCA and the PWBA has been established (Frame 1931, Bang and Hansteen 1959, Bethe and Jackiw 1968, Madison and Merzbacher 1975 and Taulbjerg 1977) provided that identical wave functions are chosen (Aashamar and Kochbach 1977 and Kocbach et al 1980). This, however, apparently leads to a paradox, in that the straight-line SCA which depends on  $\kappa \gg 1$  yields equivalent results as the PWBA which is based on the opposite condition  $\kappa \ll 1$ . However, the SCA condition requires that the deflection as well as the orbit of the projectile must be well-

defined (Williams 1945) and therefore, if the scattering angle is not involved then the condition is no longer important (Hansteen 1975). In addition, in the region where  $\kappa << 1$  the Coulomb ionisation cross sections originate predominantly from forward angle scattering and the contribution from other angles can be neglected. This imples that, provided that the projectile angle is not involved, the Coulomb ionisation cross sections may be predicted from the SCA model for all values of  $\kappa$  as long as  $Z_1 << Z_2$  and  $\varepsilon << E$  (Hansteen 1975) thus removing the contradictory nature of the validity conditions for total cross sections.

(vii) Examining equation A.16 and A.17 shows that the straight line SCA predicts a universal scaling relationship,

$$\left[ \frac{2\ell_{Li} + 1}{2j_{Li} + 1} \right] \frac{\sigma_{Li}^{SCA} Z_{2L}^{4} \theta_{Li}}{Z_{1}^{2}} = F_{n_{L}} \ell_{Li}(X_{Li})$$
 A.20

Thus, plotting the left hand side factor versus  $X_{Li}$  yields a universal curve.

A.3 CORRECTIONS TO THE SEMI-CLASSICAL APPROXIMATION

When  $\varepsilon$  is not negligible compared to E the straight-line SCA model is no longer satisfactory. This situation arises at low projectile velocities and for inner-shells of heavy target atoms because (Madison and Merzbacher 1975)

- (i) the Rutherford scattering from the target nucleus becomes appreciable, since the nuclear elastic scattering cross section is proportional to  $Z_2^2$  (section 3.2.3), and as a result, the projectile suffers a deviation from its straight line path, and
- (ii) for a given impact parameter the ionising collision itself may cause significant momentum transfers making the contributions to the ionisation cross section from all deflection angles appreciable.
  Under the above circumstances the influence of the ionisation process

on the incident particle cannot be neglected and the straight-line classical description of the projectile trajectory has to be reconsidered. Also the influence of the projectile on the atomic electron has to be taken into account through a quantum mechanical treatment (Madison and Merzbacher 1975). The possible corrections to the straight-line SCA model are considered below. It should be noted, however, that the collision circumstances that necessitate these corrections are similar to those already discussed in section 4.3. A.3.1 Distortion of the Projectile Motion

In the adiabatic projectile energy region the assumption that the projectile travels in a straight-line with uniform velocity is not valid since the projectile suffers deviations from its initial path by the Coulomb field of the target nucleus. The decrease in the projectile velocity, resulting from these deviations, causes a reduction in the ionisation cross section (Kocbach et al 1980). This Coulomb deflection effect was first studied by Bang and Hansteen (1959) who proposed an approximate multiplicative correction for the K-shell,

$$C(q_{min}d) = exp(-\pi q_{min}d)$$
 A.21

valid only for a limited projectile energy range. Bang and Hansteen (1959) arrived at this correction by employing hyperbolic trajectories for the projectile and a rather involved mathematical treatment. Anholt (1978) has proposed another Coulomb correction factor by comparing directly the straightline and hyperbolic SCA calculation,

 $C(q_{min}d) = [0.22 + 0.78 \exp(1.9\pi q_{min}d)]^{-1}$ A.22 Several theoreticians involved in this field of ion-atom collisions have performed SCA calculations with hyperbolic trajectories to account for the deflection effect which have been reviewed by Kocbach et al (1980). Trautmann and Rosel (1980) have compared SCA cross section for hyperbolic trajectories and relativistic Hartree-Fock-Slater wave functions with experimental measurements of L-shell ionisation probability as a function

of impact parameter and have observed very good agreement. Atomic ionisation has been recently considered by Montenegro and de Pinho (1982b) in the framework of hyperbolic semi-classical approximation who have derived an analytic expression for the Coulomb deflection factor which is in reasonable agreement with numerical calculations of Kocbach (1976).

#### A.3.2 Relativistic Improvements

The increase of the inner-shell ionisation cross section caused by the relativistic behaviour of the inner-shell electron was studied in the SCA model by Amundsen and Kocbach (1975). Further work on the relativistic description of the atomic electron has been summarised by Kocbach et al (1980). Amundsen et al (1976) have attempted to derive a multiplicative correction factor for the relativistic effect applied to K-shell ionisation but the accuracy of this factor is questionable when the magnitdue of the correction is high, as in the case of heavy target atoms (Kocbach et al 1980). Amundsen (1977b) has studied the relativistic effect for L-shell ionisation by light ions. This author has employed relativistic Coulomb wave functions in the SCA model and has noticed significant improvements in the agreement of theoretical (SCA) and experimental results at low projectile energies. The relativistic effect is explained in terms of an increase of high-momentum components of the electronic wave functions, thus making it easier to obtain sufficient momentum transfer for a given energy transfer in order for an electronic transition to occur. Amundsen (1977b) predicts that the relativistic effect for the  $2s_{\frac{1}{2}}$  and  $2p_{\frac{1}{2}}$  states will be of the same order but greater than the effect on the  $2p_{3/2}$  state. This is explained by the circumstance that the relativistic effect reflects the change in the highmomentum part of the wave function and the magnitude of this change is of the same order for the  $2s_1$  and  $2p_3$  state. The relativistic effect has also been studied by Trautmann and Rosel (1980). They have accounted for Coulomb deflection effect by using hyperbolic trajectories, as mentioned in the

previous section. By using Dirac wave functions an improvement of the ionisation probability predicted by the SCA has been achieved when comparing with experimental results, but a much greater degree of agreement has been attained by employing the more realistic relativistic Hartree-Fock-Slater wave functions.

A.3.3 Binding and Polarisation Effects

A perturbed stationary state approach has been used by Brandt and his colleagues to account for the binding effect (see subsection 4.3.2)(Basbas et al 1973b, Brandt and Lapicki 1974, 1979). A semi-classical approximation based on the first order time-dependent perturbation theory was used by these authors. The interaction potential V(t) is replaced by its instantaneous counterpart, V(0), that is, at the point of closest approach (t = 0). Similarly, the projectile velocity, the energy transfer and the initial and final atomic state wave functions, calculated for the instantaneous targetprojectile configuration, are used (Madison and Merzbacher 1975). With these modification the binding effect has been taken into account (Brandt and Lapicki 1974). Trautmann and Rosel (1980) have employed a binding energy correction dependent on R to correct their relativistic SCA K-shell cross sections for alpha-particle impact on lead target and considerable improvement has been achieved. At higher velocities the polarisation effect gains significance and may be accounted for in terms of the second-order perturbation theory (Madison and Merzbacher 1975). Cross sections, which in the first order theory are propotional to  $Z_1^2$ , would now be expected to be increased by additive  $Z_1^3$  - proportional terms. If 'distant' collisions are considered (R >> r) then a multipole expansion of V(t) can be used in the second order perturbation calculations. Ashley et al (1972) and Hill and Merzbacher (1974) have used this method for a harmonic oscillator model of an atom. This approach was also adopted by Brandt and Lapicki (1979). These calculations have shown that the polarisation of the inner-shell

electron is due to the quadruple component  $\propto R^{-3}$  of the Coulomb interaction, that is, the electric dipole and quadrupole excitations collectively distort the atom during the collision and produce the  $Z_1^3$  term (Madison and Merzbacher 1975 and Brandt and Lapicki 1979).

Trautmann and Rosel (1980) have highlighted three other effects which affect the ionisation probability and are now briefly mentioned.

## A.3.4. Nuclear Distortion

As long as the projectile energy is below the Coulomb barrier, the Coulomb distortion by the target nucleus can be assumed to lead to hyperbolic trajectories in the semi-classical model. At energies where the projectile experiences only weak nuclear forces hyperbolic paths can still be used provided that the elastic scattering cross section of the projectile in the mean optical nuclear field of the target is accounted for. For higher energies a full quantum mechanical treatment would be required. A.3.5 Influence of Screening Effect on Projectile Trajectory

At large impact parameters the trajectory of the projectile is influenced by the screeing effects of the target electrons. In this case, a trajectory due to a screened Coulomb potential has to be used. Trautmann and Rosel point out however, that his effect will only be small, even for shells higher than the K-shell.

# A.3.6 Target Recoil Effect

In the SCA model the target mass is assumed to be infinitely heavy compared to the mass of the projectile  $(M_2 \gg M_1)$ . When this is not the case, that is, for a finite target mass, the Coulombic interaction term has to be modified,

$$V(\underline{r}, \underline{R}) \simeq \frac{-Z_1 e^2}{|\underline{r} - \underline{R}|} + \Delta V(\underline{r}, \underline{R})$$
 A.23

 $\Delta V(\underline{r}, \underline{R})$  leads to a dipole contribution ( $\propto R^{-2}$ ) to the interaction and may make a correction to the ionisation probability necessary. The magnitude of such a correction, however, would be significant only for low-Z<sub>2</sub> target

atoms when considering ionisation by light projectiles and may probably be neglected for the collision regimes under investigation in this work.

Trautmann et al (1983) have incorporated all these effects in their SCA model, based on a fully quantal approach, and, in general, have been successful in explaining the experimental data.

## A.4 BINARY ENCOUNTER APPROXIMATION

The interest in a classical description of inner-shell ionisation by heavy charged particles was stimulated by the work of Gryzinski (1965) who developed a classical theory for calculating atomic collision cross sections. Following Gryzinski's procedure Garcia (1968 and 1970a,b) applied this classical theory to inner-shell ionisation phenomena. In this theory the dominant interaction, which causes an electronic transition to occur, is viewed as andirect energy exchange between the projectile and the bound atomic electron (impulse approximation)(Garcia 1970a). The nucleus and the other electrons of the target atom are, therefore, assumed to play only a passive role and simply help to establish the momentum distribution for the 'active' electron involved in the Coulombic collision and to ensure that the energy transferred to this electron exceeds the minimum energy required to ionise it in the field of the target atom. In other words, the energy transferred must be greater than the ionisation potential of the electron (Hansen 1973 and Briggs and Taulbjerg 1978). The collision is thus treated as a two-body interaction between an incident charged particle and a free electron, and as a result, this assumption is referred to as the 'Binary Encounter Approximation' (BEA). The differential cross section,  $d\sigma/d\Delta E$ , for an exchange of energy,  $\Delta E$ , in the laboratory frame, between the incident particle and the bound electron is obtained by utilising the result that the classical and quantum mechanical differential cross sections in the centre-of-mass system are identical (Gerjouy 1966, Garcia 1970a). The cross section,  $\sigma_i(v_1, v_2)$ , for removal of an electron from subshell, i, with binding energy, u,

(retaining Garcia's (1970a) notation) is obtained by integrating over all allowed energy exchanges from  $\Delta E = u$  to  $\Delta E = E_1$ , where  $E_1$  is the energy of the projectile with velocity  $v_1$  and  $v_2$  is the velocity of the electron.

$$\sigma_{i}(v_{1}, v_{2}) = \int_{u}^{E_{1}} \frac{d\sigma}{d\Delta E} d\Delta E \qquad A.24$$

The ionisation cross section,  $\sigma^{\text{BEA}}(v_1)$ , is arrived at by averaging over all speed distributions,  $f_{n\ell}(v_2)$ , of the atomic electrons and summing over all electrons in the subshell,

$$\sigma^{\text{BEA}}(v_1) = N_i \int_0^\infty \sigma_i (v_1, v_2) f_{n\ell} (v_2) dv_2$$
 A.25

where n and & denote the principal and the orbital quantum numbers respectively and N<sub>i</sub> is the number of equivalent electrons with binding energy u. The expression for f<sub>n0</sub> (v<sub>2</sub>) most commonly used is

$$f_{n_{\ell}}(v_2) = \frac{32}{\pi} v_0^5 \left( \frac{v_2^2}{(v_2^2 - v_0^2)^4} \right)$$
 A.26

with  $v_0 = (2u/m)^{\frac{1}{2}}$ 

and can be obtained classically or quantum mechanically for hydrogenic states (Garcia 1970a and Hansen 1973). It is assumed in the BEA calculations that  $f_{n,\ell}(v_2)$  remains unchanged as the projectile passes through the atom (static approximation) (McGuire and Richard 1973). The effects of nuclear repulsion on the projectile motion, namely the delfection and the reduction of its kinetic energy, have been incorporated into expression A.25 by assuming that the repulsion is due to a point charge Z' and evaluating the ionisation cross section at a reduced projectile energy of  $E_1 - (2Z'/Z_2)u$  (for protons) (Thomas and Garcia 1969 and Garcia 1970a). For large  $Z_2$  the point charge Z' has been replaced by  $Z_2$  for K-shell ionisation (Garcia 1970a).

The following points should be noted in relation to the BEA model.

 Provided hydrogenic velocity distributions are used the cross sections for a given subshell obey the following scaling law (Garcia et al 1973)

$$\frac{u^2 \sigma^{\text{BEA}}}{Z_1^2} = g \left( \frac{E_1}{\lambda u}, \lambda \right)$$
 A.27

where  $\lambda = M_1/m$ . Thus plotting the left-hand-side of A.27 versus  $E_1/\lambda u$  yields a universal curve. Garcia et al (1973) have presented tabulated values of  $u^2\sigma^{\text{BEA}}/Z_1^2$  versus  $E_1/\lambda u$ .

- (ii) Several authors have demonstrated that the BEA total cross section can also be obtained from the PWBA model (Vriens 1970, Bates and McDonough 1970, 1972 and Madison and Merzbacher 1975). Taulbjerg (1976) has compared the two models under indentical conditions for the K and L-shell and has concluded that the PWBA, and its equivalent the straight-line SCA, are essentially identical as far as total ionisation cross sections are concerned. This has been substantiated for the BEA and the PWBA theories by Langenberg and van Eck (1978) who employed realistic velocity distributions for the target electron instead of the hydrogenic type and achieved agreement between the two models to within 20%.
- (iii) Hansen (1973) has transformed the BEA model from its usual momentum space into configuration space. To do this a consistent relationship between the velocity of a bound electron and its distance from the nucleus has to be formulated (Gryzinski 1965). By reexpressing the BEA theory in the impact-parameter representation, Hansen (1973) has developed a model to describe the interaction between a bound electron and a particle of fixed trajectory, referred to as the Constrained Binary Encounter Approximation (CBEA). Cross sections calculated from this theory are usually smaller than those predicted by the BEA. Hansen (1973) points out that the prescription of assigning exactly one electron velocity for a given distance from the nucleus is idealised and would lead to an overestimation of the ionisation probability for close collisions and an underestimation for distant collisions.

(iv) The characteristic 'knee' in the  $2s_1$  ionisation cross section is less pronounced in the CBEA description of Hansen (1973) than in the PWBA. The cross sections calculated from the two models in the vicinity of this 'knee' differ by nearly a factor of two (Taulbjerg 1976). The quantum mechanical description of the PWBA exhibits closer agreement with experimental measurements (Madison 1976). By using realistic electron velocity distributions Langenberg and van Eck (1978) have shown that the BEA can also duplicate qualitatively the behaviour of the  $2s_1$  cross section.

A.5 CORRECTIONS TO THE BINARY ENCOUNTER APPROXIMATION

Several corrections have been proposed to improve agreement between the BEA predictions and experimentally measured ionisation cross sections. These are considered here briefly.

A.5.1 Nuclear Repulsion Effects

The loss of kinetic energy sufferred by the projectile during close collisions due to the Coulombic repulsion of the target nucleus can be accounted for by assuming that the projectile interacts at some average distance from the nucleus, namely at the adiabatic radius  $r_{ad}$ . The loss of energy experienced by the projectile, before causing ionisation, is  $Z_1Z_2e^2/r_{ad}$ . Magno et al (1979) have used an effective projectile energy by reducing the incident energy by the amount  $Z_1(T + u)$  where T is the kinetic energy of the electron.

A.5.2 Relativistic Effect

In exact BEA calculations for medium and high  $Z_2$  elements relativistic electronic wave functions should be used to generate the appropriate momentum distributions (Hansen 1973). An approximate correction has been proposed by Hansen (1973) which assumes that the kinetic energy of the electron can be correctly expressed in terms of the non-relativistic equation  $T = \frac{1}{2}m_0 v_2^2$ , where  $v_2$  is the velocity of the electron. The

relativistic velocity, v<sub>rel</sub>, and mass m<sub>rel</sub> of the electron can then be calculated from

$$v_{rel} = \left| \left( \frac{R}{1+R} \right) \right|^{\frac{1}{2}} c$$
 A.28

and

rel = 
$$\left(\frac{m_0}{1-\beta^2}\right)^{\frac{1}{2}}$$
 A.29

where  $R = (T/m c^2)^2 + 2 (T/m_0 c^2)$  and  $\beta = v_{rel}/c$ , c being the velocity of light and  $m_0$  the rest mass of the electron. These values can now be used in the cross section calculations. Recently Avaldi et al (1982) have derived the electron momentum distributions using relativistic wave functions to study K-shell ionisation of Ho and Au by proton impact. Reasonable agreement with experimental results is only achieved when corrections are made for the energy loss of the proton. As with the PWBA and the SCA scaling laws do not hold when these corrections are made.

## A.5.3 Binding Energy Effect

m

This effect has been considered only qualitatively by Hansen (1973) and an expression for this correction has not been given. Magno et al (1979) in their study of K-shell ionisation have corrected the BEA for the binding effect on the basis of the work of Basbas et al (1973a).

A.5.4 Improvement of Electron Momentum Distribution

In the BEA model Zeff/n is replaced by  $(u/R_{\infty})^{\frac{1}{2}}$  in the electronic wave functions. Here Zeff is the effective atomic number of the target atom, n is the principal quantum number, u is the binding energy of the appropriate inner-shell and  $R_{\infty}$  is the Rydberg. A more plausible Zeff is determined from simple semi-empirical screening procedures, such as reducing  $Z_2$  by the Slater's constant for the particular shell (Hansen 1973). The importance of employing realistic electron momentum distributions has been demonstrated by the work of Langenberg and van Eck (1978) and Avaldi et al (1982).

# APPENDIX B

# PRESENT EXPERIMENTAL L SHELL X-RAY PRODUCTION AND IONISATION CROSS SECTIONS

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B.1	PROTON IMPACT	453
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#### EXPLANATIONS

Tabulated experimental L shell x-ray production and ionisation cross sections measured in this study are presented in order of increasing atomic number

- (1) L, BETA and GAMMA denote  $\sigma_{L\ell}^{X}$ ,  $\sigma_{L\beta}^{X}$  and  $\sigma_{L\gamma}^{X}$  respectively.
- (2) ALPHA denotes  $\sigma_{L\alpha+\eta}^{X}$  for Dy, and Yb and W and  $\sigma_{L\alpha}^{X}$  for Au, Pb, Bi, Th and U.
- (3) BETA1 denotes  $\sigma_{L\beta_{1346}}^{X}$  for Dy and Yb,  $\sigma_{L\beta_{146}}^{X}$  for W and  $\sigma_{L\beta_{135}}^{X}$  for Th and U.
- (4) BETA2 denotes  $\sigma_{L\beta_{2715}}^{X}$  for Dy and Yb,  $\sigma_{L\beta_{25715}}^{X}$  for W and  $\sigma_{L\beta_{24615}}^{X}$  for Th and U.
- (5) BETA = BETA1 + BETA2 where appropriate.
- (6) GAMMA1 denotes  $\sigma_{L\gamma_{15}}^{X}$  for all elements.
- (7) GAMMA2 denotes  $\sigma_{L\gamma_{23844}}^{X}$  for Dy and Yb,  $\sigma_{L\gamma_{236844}}^{X}$  for W, Au, Pb and Bi (protons only) and  $\sigma_{L\gamma_{2368}}^{X}$  for Bi (deuterons and alpha particles), Th and U.
- (8) GAMMA = GAMMA1 + GAMMA2 where appropriate
- (9) TOTAL = L + ALPHA + BETA + GAMMA
- (10) LA/LL, LA/LB, LA/LG and LB/LG denote  $\sigma_{L\alpha}^{x}/\sigma_{L\ell}^{x}$ ,  $\sigma_{L\alpha}^{x}/\sigma_{L\beta}^{x}$ ,  $\sigma_{L\alpha}^{x}/\sigma_{L\gamma}^{x}$ and  $\sigma_{L\beta}^{x}/\sigma_{L\gamma}^{x}$  ratios respectively.
- (11) L1 and L2 and L3 denotes  $\sigma_{L_1}$ ,  $\sigma_{L_2}$  and  $\sigma_{L_3}$  respectively.
- (12) L1/L2, L1/L3 and L2/L3 denote  $\sigma_{L_1}/\sigma_{L_2}$ ,  $\sigma_{L_1}/\sigma_{L_3}$  and  $\sigma_{L_2}/\sigma_{L_3}$  respectively.
- (13) TOTAL = L1+ L2 + L3
- (14) Percentage experimental uncertainties are shown in parenthesis. Wherever uncertainties are omitted the preceding value applies.
# DYSPROSIUM(Z2=66)

EXPERIMENTAL	L	SHELL	X-RAY	PRODUCTION	CROSS	SECTIONS
		FOR	PROTON	IMPACT		

ENERGY	L	ALPHA	BETA	GAMMP	a GAMM	A1 GAMMA2	TOTAL
MeV				BARNS	5		Lie Late
1.0 1.2 1.4 1.4 1.6 0 2.2 1.4 1.6 0 2.2 2.4 2.2 2.2 2.2 2.0 3.0	.665(7) .986 1.521 1.828 2.228 2.632 3.179 3.642 3.947(6) 4.382 4.413	14.53(4) 24.08 32.37 39.33 52.85 61.26 69.79 84.59 92.228) 105.44 115.27	8.15(5) 13.04 19.32 24.59 29.95 37.95 45.73 52.82 62.21(3) 71.32 82.88	.943 1.723 2.528 3.234 4.270 5.471 6.626 8.143 9.148 10.719 12.106	3(6)         .82           1.51         2.16           2.64         3.32           4.09         3.32           5.71         5.71           3(4)         6.35           7.21         7.97	77 .1169) 2 .211 9 .369 4 .390 4 .946 9 1.371 9 1.866 7 2.427 95 2.7880 2 3.507 6 4.130	24.29(3) 39.82 55.74 68.98 99.30 107.31 125.22 149.19 167.52(2) 191.86 214.67
ENERGY	BETA1	BETR2	LA/1	LL	LA/LB	LA/LG	LB/LG
MeV	BAR	RNS					
1.0 1.2 1.4 1.6 8 9 2 2 2 2 2 2 2 2 3 9	5.549(6) 8.991 13.617 17.603 21.534 27.345 33.967 39.018 45.828(4) 53.174 61.984	2.613(8) 4.046 5.704 6.984 8.413 10.604 11.758 13.798 16.380(5) 18.145 20.900	) 21. 24. 21. 23. 23. 23. 23. 23. 23. 24. 24. 25.	83( <b>8</b> ) 43 28 51 72 28 99 23 36(7) 86 12	1.782(6) 1.847 1.675 1.600 1.765 1.614 1.524 1.602 1.482(4) 1.478 1.391	15.41(7) 13.97 12.80 12.16 12.38 11.20 10.52 10.39 10.08(5) 9.84 9.52	8.658(8) 7.565 7.642 7.602 7.013 6.937 6.900 6.486 6.800 (5) 6.654 6.847

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.0246000246000	5.97(9) 10.88 19.14 30.92 49.83 72.47 98.89 128.71 147.96(7) 186.37 219 63	29.83(7) 54.52 77.19 93.07 114.95 139.67 159.35 189.50 209.92(5) 234.51 256.79	95.15(5) 156.52 208.29 250.60 335.76 383.17 430.41 520.10 563.90(3) 639.89 594.19	.200(1) .200 .248 .332 .433 .519 .621 .621 .705(9) .795	.063(0) .070 .092 .123 .148 .169 .230 .247 .262(8) .291 .215	.314(9) .348 .371 .371 .342 .365 .379 .364 .372(6) .364 .372(6)	130.95 (4) 221.92 304.62 374.59 500.54 595.31 688.65 838.31 921.78(2.5) 1060.77

#### YTTERBIUM(Z2=70)

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA	11 GAMMA	2 TOTAL
MeV				BARNS			
1.0 1.2 1.4 1.6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 0 2 4 6 0 0 2 4 6 0 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 0 2 4 6 0 2 4 6 0 2 4 6 0 2 4 6 0 2 4 6 0 2 4 6 0 2 4 6 0 2 2 4 6 0 2 2 4 6 0 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	.400(8) .626 .397 1.268 1.524 1.842 2.216 2.642(6) 2.970 3.271 3.688	7.78 (5) 12.19 17.46 24.76 30.16 38.50 47.85 56.95 (4) 62.66 71.37 81.59	4.55 (6) 7.40 10.41 14.76 19.03 24.43 30.60 36.52 (4) 45.11 52.05 60.11	.627( 1.017 1.418 2.084 2.758 3.648 3.648 5.373 6.490 7.746 8.819	(7) .539 .899 1.210 1.751 2.240 2.895 3.364 3.909 4.549 5.378 5.942	(8) .088 .118 .208 .333 .518 .754 1.126 (6) 1.464 1.351 2.369 2.877	$ \begin{array}{c} (0) & 13.35 (4) \\ 21.23 \\ 30.19 \\ 42.86 \\ 53.47 \\ 68.42 \\ 85.16 \\ (8) & 101.49 \\ 117.15 \\ 134.43 \\ 154.20 \end{array} $
ENERGY	BETA1	BETA	<u>2</u> - LF	9/LL	LA/LB	LA/LG	LB/LG
MeV		BARNS					
1.0246000 1.14600046000	3.161 5.060 7.301 10.484 13.220 17.345 22.121 26.719 33.458 38.003 43.860	(7) 2.31 3.10 4.27 5.80 7.08 8.47 9.80 11.65 14.04 16.24	9(9) <sup>•</sup> 19 6 19 6 19 7 20 6 19 7 20 7 20 21 21 21 21 21 21 21 21 21 21 21 21 21	9.42(9) 9.46 9.47 9.52 9.79 9.59 1.59 1.56(7) 1.82 2.12	1.709(7) 1.648 1.678 1.585 1.585 1.576 1.564 1.559(5) 1.389 1.371 1.357	12.39(8) 11.98 12.31 11.88 10.94 10.55 10.66 10.66(5) 9.79 9.21 9.25	7.253 (8) 7.270 7.339 7.082 6.899 6.697 6.815 6.797 (6) 7.049 6.719 6.816

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.024600046000	3.65(0) 4.32 8.62 13.32 21.62 31.54 47.34 61.69(8) 78.07 100.02 121.61	15.25(8) 25.69 34.16 49.20 62.19 79.66 90.57 103.96(6) 119.80 140.14 152.76	41.73(6) 65.40 93.59 132.04 158.94 201.57 249.32 295.61(4) 321.08 361.47 412.14	.239((3) .188 .252 .281 .348 .396 .523 .593((0) .652 .714 .796	. 087(12) .074 .092 .105 .136 .156 .156 .190 .209(9) .243 .277 .295	.365(10) .393 .365 .373 .391 .395 .363 .352(7) .373 .388 .371	60.63 (5) 95.91 136.37 195.06 242.75 312.77 387.23 461.26 (3) 518.95 601.63 686.51

#### TUNGSTEN(Z2=74)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA	1 GAMMA2	TOTAL
MeV				BARNS			
1.0 1.4 1.6 0 0 1.4 6 0 0 2 4 6 0 0 2 2 2 2 2 2 3 0	.282(8) .437 .670 .358 1.105 1.334 1.543 1.829 2.057(6) 2.315 2.687	5.72(5) 9.10 14.38 18.49 23.83 30.66 34.99 41.47 47.21 54.03 62.09	3.04 (6 4.97 7.73 10.31 13.66 17.98 22.13 26.64 30.40 34.93 40.21	<ul> <li>.4040</li> <li>.662</li> <li>1.100</li> <li>1.451</li> <li>2.028</li> <li>2.696</li> <li>3.324</li> <li>4.124</li> <li>4.7750</li> <li>5.568</li> <li>6.743</li> </ul>	7) .338 .563 .926 1.205 1.645 2.137 2.550 3.071 3.427 3.803 4.624	<ul> <li>(3) .0663</li> <li>.0985</li> <li>.175</li> <li>.247</li> <li>.383</li> <li>.559</li> <li>.774</li> <li>1.052</li> <li>1.348</li> <li>1.765</li> <li>2.119</li> </ul>	(10) 9.44 (5) 15.17 23.88 31.11 40.63 52.68 61.99 74.07 (8) 84.44 (3) 96.84 111.73
ENERGY	BETAL	BETR	12 L	A/LL	LA/LB	LA/LG	LB/LG
MeV		BARNS					
1.0 1.24 1.6 1.0 2.24 2.6 2.0 2.4 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0	1.821 3.006 4.849 6.643 8.894 11.737 14.206 17.705 20.446 23.557 27.312	(7) 1.21 1.96 2.88 3.66 4.76 6.24 7.92 8.93 (6) 9.95 11.37 12.96	5 (9) and a second seco	20.28 (9) 20.84 21.54 21.54 21.57 22.98 22.67 22.67 22.95 (8) 23.34 23.10	1.884(7) 1.832 1.859 1.793 1.745 1.705 1.581 1.557 1.553(6) 1.547 1.544	14.14(8) 13.75 13.07 12.74 11.75 11.37 10.53 10.06 9.89(6) 9.70 9.21	7.508 (9) 7.504 7.031 7.106 6.736 6.671 6.658 6.460 6.368 (8) 6.273 5.964

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

.

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.0 1.24 1.6 0 2.24 1.6 0 2.24 2.22 2.22 2.23 2.23 2.23 2.24 2.23 2.24 2.24	1.74(10) 2.52 4.55 6.53 10.39 15.41 21.78 30.03 38.99(8) 51.76 62.09	7.67(8) 12.86 21.06 27.30 37.04 47.80 56.46 57.36 74.22(6) 80.92 98.53	26.13(6) 41.53 65.33 83.78 107.08 137.09 154.86 182.14 206.22(5) 234.48 267.73	.227(3) .196 .216 .239 .281 .322 .386 .446 .525(0) .630	.0666(12) .0696 .0696 .0779 .0970 .112 .141 .165 .189(9) .221	.294 ((0) .310 .322 .326 .346 .349 .365 .365 .360 (8) .345 .368	35.54 (5) 56.91 90.94 117.61 154.51 200.30 233.10 279.53 319.43 (4) 367.16 428.35

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# GOLD(22=79)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		*	
1.0 1.2 1.4 1.6 1.0 0 2.2 4 1.0 0 2.2 4 2.0 2 2.0 2 2.0 0 2.2 4 2.0 2 2.2 4 2.0 2 2.2 4 2.0 2 2.4 4 1.0 2 2.4 4 1.0 2 2.4 4 1.0 2 2.4 4 1.0 2 2.4 4 2.0 2.4 4 2.0 2.4 4 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0	.192(7) .303 .475 .610 .802 .965 1.194 1.414 1.688(S) 1.936 2.232	3.66(4) 5.88 9.39 12.21 15.79 19.53 24.36 29.60 33.82(3) 39.49 44.40	1.96(5) 3.13 4.99 6.75 8.82 11.14 14.13 16.94 18.82(4) 22.98 25.34	.248 (6) .424 .642 .859 1.143 1.470 1.856 2.208 2.541 (5) 3.103 3.463	. 198(7) .348 .538 .723 .952 1.217 1.217 1.529 1.767 1.996 (5) 2.415 2.637	.0504(9) .0758 .103 .135 .190 .253 .327 .442 .545(7) .688 .826	6.07 (4) 9.74 15.50 20.43 26.46 33.10 41.54 50.17 56.87 (3) 67.50 75.44
ENERGY MeV	LA/	LL	LA/LB	LA/LG	L	B∕LG	
1.0 1.4 1.6 0.0 1.4 1.6 0.0 2.4 0.0 2.4 0.0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	19. 19. 19. 20. 20. 20. 20. 20. 20. 20. 20. 20. 20	09 (7) 39 75 81 58 25 40 93 84 (5) 40 90	1.865 (S) 1.878 1.882 1.808 1.780 1.754 1.724 1.724 1.747 1.797 (4) 1.719 1.752	14.78 13.87 14.63 14.22 13.73 13.29 13.13 13.41 13.31 12.73 12.82	(b) 77 77 77 77 77 77 77 77 77 7	.921(7) .384 .771 .861 .717 .575 .612 .674 .406(6) .405 .319	

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.0 1.2 1.4 1.6 1.0 2.2 2.2 2.0 2.0 2.0 2.0 2.0 2.0 0 3.0	1.38(9) 1.75 2.13 2.79 4.08 5.63 7.45 11.29 14.68(7) 18.98 23.86	3.45(7) 6.15 9.60 12.92 16.93 21.57 27.05 30.87 34.62(5) 41.71 45.10	13.41(5) 21.63 34.93 45.41 58.00 71.81 89.31 107.54 121.96(4) 141.23 157.65	.377(11) .285 .222 .209 .241 .261 .275 .366 .424(9) .455 .529	.0969(//) .0809 .0610 .0595 .0703 .0784 .0834 .105 .120(S) .134 .151	.257(9) .284 .275 .285 .292 .300 .303 .287 .284(6) .295 .286	18.16(4) 29.53 46.66 61.03 79.01 99.01 123.81 149.70 171.26(3) 201.92 226.61

## LEAD(Z2=82)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		I SALAN AND	
1.0 1.146000 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.14600 1.146000 1.14600000000000000000000000000000000000	.117(7) .200 .303 .420 .579 .746 .889 1.001 1.200(6) 1.417 1.603	2.01 (5) 3.79 5.37 7.61 10.90 14.92 18.27 21.01 24.91(4) 29.10 33.01	1.08(6) 2.06 3.08 4.33 6.29 8.82 11.00 12.76 15.03(4) 17.93 20.89	.173 (6) .296 .441 .554 .917 1.262 1.599 2.040 2.402(5) 2.793 3.423	.130(7) .234 .360 .532 .740 1.026 1.269 1.614 1.885(5) 2.091 2.554	.0430(9) .0624 .0814 .122 .178 .236 .330 .426 .517(8) .702 .869	3.39(4) 5.34 9.20 13.01 18.69 25.76 31.75 36.81 43.55(3) 51.24 58.92
ENERGY MeV	LAZ	"LL	LA/LB	LA/LG	L	B∕LG	
1.0 1.24 1.60 0.24 1.60 0.24 0.00 0.24 0.00 0.24 0.00 0.00 0.0	17. 18. 17. 18. 20. 20. 20. 20. 20. 20. 20. 20. 20.	15(8) 99 73 11 82 81 55 99 76(7) 53	1.854(7) 1.340 1.745 1.756 1.734 1.691 1.661 1.647 1.657(5) 1.623 1.530	11.62 12.80 12.19 11.63 11.89 11.83 11.42 10.30 10.37 10.42	<ul> <li>(7) 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6</li></ul>	.269 (S) .956 .984 .622 .858 .992 .878 .255 .259 (6) .419	

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.0 1.2 1.6 0 0 0 1.6 0 0 0 1.6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1.04(9) 1.29 1.41 2.14 3.30 4.15 6.67 8.67 10.95(8) 17.19 21.47	1.97(7) 3.61 5.62 8.31 11.50 16.02 19.61 24.93 29.01(6) 31.59 38.52	5.33(6) 12.35 17.71 24.94 35.66 48.99 59.99 59.92 66.99 79.12(6) 99.06 109.65	.528(11) .357 .251 .258 .287 .259 .349 .349 .377(10) .544 .557	.164(U) .104 .0796 .0858 .0925 .0847 .113 .130 .138(9) .135(9) .191 .213	.311(9) .292 .317 .333 .322 .327 .332 .332 .372 .351 .383	9.34 (4) 17.25 24.74 35.39 50.46 69.16 85.30 100.62 119.88 138.84 169.64

# BISMUTH(Z2=83)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GRMMA2	TOTAL
MeV				BARNS			
1.2 1.4 1.6 2.2 2.4 2.2 2.4 2.2 2.2 2.2 2.2 2.2 3.0	.204(3) .319 .424 .565 .703 .847 1.021 1.200 1.356(6) 1.590	3.70 (5) 5.59 7.59 10.21 12.71 15.36 18.90 22.12 25.70 (4) 29.91	) 1.84 (6) 3.07 4.53 6.12 7.63 9.25 11.43 13.53 15.79 (4) 18.45	.237 (6) .435 .617 .818 1.050 1.302 1.629 2.011 2.363(5) 2.731	.229(7) .353 .499 .661 .851 1.045 1.300 1.587 1.861(6) 2.123	.0585(9) .0818 .118 .157 .198 .257 .329 .424 .502(8) .608	6.03 <del>4</del> 9.42 13.16 17.71 22.09 26.76 32.98 38.86 45.21 (3) 52.68
ENERGY MeV	LA/	LL	LA/LB	LA/LG	LI	8/LG	
1.24 1.46 1.20 2.24 2.20 2.24 2.20 2.20 2.20 2.20 2	18. 17. 17. 18. 18. 18. 18. 18. 18. 18.	12(9) 52 91 86 88 15 52 43 96 (7) 81	2.011 (7) 1.825 1.675 1.669 1.663 1.661 1.634 1.634 1.628 (5) 1.621	12.89 12.86 12.30 12.48 12.10 11.80 11.60 11.00 10.88 10.95	(7) 67777777 777777777 (6) 65	408 ( <b>8</b> ) 049 344 480 270 105 816 729 683 ( <b>6</b> ) 755	•

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.24 1.46 1.00 2.44 2.00 2.44 2.00 2.44 2.00 2.00 2	1.03(9) 1.27 1.88 2.52 3.09 4.30 5.72 7.81 9.35(8) 11.96	3.49(3) 5.30 7.47 9.90 12.77 15.61 19.38 23.56 27.61(7) 31.36	11.81(6) 18.02 24.32 32.74 40.72 48.87 59.86 69.27 80.32(5) 92.90	.303(12) .249 .252 .255 .242 .275 .295 .331 .339(11) .381	. 0872(U) . 0705 . 0773 . 0779 . 0759 . 0359 . 0956 . 113 . 115(9) . 129	.288 (10) .294 .397 .302 .314 .319 .324 .340 .344 (9) .338	15.24 (5) 24.39 33.57 45.15 56.58 58.78 94.95 100.54 117.28(4) 135.22

# THORIUM(Z2=90)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS	Station States	Same -	ALC: N
1.24 1.6 8 9 2 4 6 9 9 2 2 2 2 2 2 2 2 2 2 2 3 9 9 2 2 2 2	.104 (9) .168 .252 .332 .396 .517 .648 .810 (7) .981 1.103	1.62 (6) 2.54 3.91 5.42 6.74 8.95 11.20 13.42 (4) 15.86 18.65	.913 (6) 1.45 2.21 3.16 3.95 5.42 7.02 8.06 (5) 9.63 11.27	.123 (7) .198 .300 .428 .577 .790 .983 1.167 (6) 1.359 1.625	.0937(8) .154 .237 .342 .461 .629 .782 .928(7) 1.079 1.283	.8294(10) .0444 .8632 .8856 .116 .160 .282 .238(8) .281 .343	2.76 (4) 4.35 6.67 9.34 11.67 15.68 19.86 23.45 (3) 27.83 32.65
ENERGY	BETA1	BETR		LL LAZ	LB LA,	1G LB/1	.G
MeV	1	BARNS					
1.24 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.46 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.0	.490 .773 1.215 1.739 2.197 3.092 4.046 4.551 5.701 6.763	(7) .42. .67: .99: 1.42 1.75: 2.32: 2.32: 2.32: 3.58: 3.92: 4.56:	4(8)       15.         15.       15.         15.       15.         15.       15.         16.       17.         17.       17.         16.       17.         16.       16.         16.       16.         16.       16.         16.       16.	51(10) 1.7 49 1.7 30 1.7 33 1.7 33 1.6 58(8) 1.6 18 1.6 90 1.6	71(8) 13. 54 12. 64 13. 14 12. 87 11. 52 11. 55 11. 55 11.	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	19 (8) 34 37 33 33 34 43 36 (7) 35 32

#### EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

FOR PROTON IMPACT

ENERGY	L1	L2	L3	·L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.24 1.46 1.00 2.44 2.00 2.44 0.00 2.44 0.00 2.00 2	.385 (0) .503 .608 .692 .954 1.36 1.78 2.67(8) 2.54 3.31	1.08(9) 1.78 2.76 4.00 5.39 7.35 9.12 10.84(8) 12.57 14.92	4.29(7) 6.78 10.54 14.69 18.19 24.07 30.08 36.08 (6) 42.62 49.90	.356(13) .283 .220 .173 .177 .185 .195 .195(11) .202 .222	.0897(12) .0742 .0577 .0471 .0524 .0565 .0592 .0574(0) .0596 .0663	.252(1) .263 .262 .272 .296 .385 .383 .383 .383 (0) .295 .299	5.76 (6) 9.06 13.91 19.38 24.53 32.78 40.38 48.99 (5) 57.73 68.13

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#### URANIUM(Z2=92)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.24 1.46 1.20 2.22 2.22 2.22 2.22 2.23	.0894(9) .139 .198 .260 .353 .442 .556 .653(8) .752 .874	1.48 (7) 2.27 3.07 4.09 5.57 6.97 8.80 10.45 12.22 13.76	.795 (6) 1.22 1.70 2.36 3.16 4.18 5.15 6.09(5) 7.45 8.42	.0920(7) .138 .185 .265 .389 .497 .620 .767 (6) .913 1.055	.0679(9) .104 .140 .204 .304 .385 .480 .600(7) .710 .815	.0241 (1) .0345 .0450(10) .0606 .0856 .112 (9) .140 .166 (3) .203 .240	2.45 (5) 3.77 5.15 6.98 9.47 12.09 15.13 17.96 (3) 21.34 24.10
ENERGY	BETA1	BETR2	LAZI	L LAZI	B LA	LG LBA	_G
MeV		BARNS					
1.2 1.4 1.6 1.8 2.2 2.4 2.6 2.2 2.3 3.0	.380 .609 .871 1.227 1.693 2.111 2.730 3.289 4.039 4.039	<ul> <li>(3) .414</li> <li>.614</li> <li>.830</li> <li>1.136</li> <li>1.467</li> <li>2.068</li> <li>2.423</li> <li>2.799(</li> <li>3.413</li> <li>3.816</li> </ul>	(9) 16.1 15.1 15.1 15.1 15.1 15.1 15.1 15.1	55(11)       1.83         52       1.83         52       1.83         73       1.75         79       1.66         33       1.75         340(9)       1.75         326       1.66         337       1.75         340(9)       1.75         356       1.66         357       1.65	51(9) 16 56 16 35 16 32 15 52 14 59 14 17(7) 13 40 13 55 13	.08(0) 8.6 41 8.8 64 9.2 30 8.1 30 8.1 30 8.1 63 8.4 53(8) 7.9 39 8.16 39 8.16	40 (9) 42 19 15 15 16 39 16 39 16 39 16 39 27 35 78

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

FOR PROTON IMPACT

ENERGY	LI	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.446000 1.446000 1.446000 1.446000	.343(1) .452 .562(10) .657 .328 1.15 (9) 1.45 1.56 (8) 2.83 2.56	.788((0) 1.21 1.63 2.40 3.58(9) 4.53 5.65 7.08(8) 8.36 9.58	3.79(8) 5.73 7.78 19.38 14.11 17.60 22.22 26.43(6) 38.77 34.45	. 435 (/5) .374 .345(14) .274 .231 .254(13) .257 .228(11) .243 .267	.8927(14 .8789 .9722(13) .8633 .8653 .8653(12) .8653 .85590(0) .8668 .8743	213 (3) .211 .210 .210 .254(12) .254(12) .255 .254 .268 (0) .272 .278	4.83 (G) 7.39 9.97 13.44 18.52 23.28 29.32 35.87 (G) 41.16 46.59

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#### DYSPROSIUM(Z2=66)

EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR DEUTERON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		1. 10. 10	
1.24 1.46 0.00 246 0.00 246 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.	.196(8) .279 .434 .536 .676 .853 1.011 1.249(7) 1.406 1.557	4.04(4) 6.12 9.13 12.04 15.20 18.63 22.38 28.53(3) 31.24 37.85	2.24(5) 3.42 4.99 6.66 8.47 10.67 12.73 16.57(3) 19.28 23.14	.291 (6) .439 .642 .858 1.043 1.351 1.680 2.137(5) 2.570 3.118	.248(7) .376 .576 .925 1.195 1.451 1.814(5) 2.143 2.542	.052(9 .063 .067 .093 .118 .157 .229 .323(8) .427 .576	) 6.77 10.26 15.20 20.09 25.39 31.51 37.81 ) 48.49 54.49 55.67
ENERGY	BETA1	BETA2	LA/LI	LAZ		A/LG	LB/LG
MeV	BAR	NS	•				
1.2 1.4 1.6 1.8 2.0 2.4 2.4 2.8 3.0	1.521(6) 2.299 3.339 4.439 5.716 7.247 8.668 11.386(4) 13.362 16.251	.723 ( 1.117 1.653 2.222 2.754 3.423 4.063 5.187 ( 5.918 6.888	<ul> <li>20.5</li> <li>21.9</li> <li>21.0</li> <li>22.4</li> <li>22.5</li> <li>21.8</li> <li>22.1</li> <li>22.1</li> <li>22.3</li> <li>22.2</li> <li>22.3</li> <li>22.2</li> <li>24.3</li> </ul>	3 (9)       1.8         1       1.7         5       1.8         5       1.8         6       1.7         4       1.7         5       1.8         4       1.7         5       1.8         4       1.7         5       1.7         4       1.7         5       1.6         1       1.6	99(6)     11       92     11       92     11       97     14       95     14       95     14       58     11       21(4)     11       20     11       36     11	3.88(7) 3.94 4.22 4.03 4.57 3.79 3.32 3.35(6) 2.15 2.14	7.713 7.781 7.777 7.763 8.121 7.898 7.578 7.755 (3) 7.502 7.421

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

FOR DEUTERON IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.4 1.6 1.0 0 0 1.4 0 0 0 1.4 0 0 0 1.4 0 0 0 0 1.4 0 0 0 0 1.4 0 0 0 0 1.4 0 0 0 0 1.4 0 0 0 0 1.4 0 0 0 0 0 1.4 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2.79(9) 3.24 3.40 4.74 6.08 8.05 11.86 16.81(8) 22.26 30.16	8.45(7) 13.47 29.89 27.75 33.45 43.17 52.05 64.78(5) 76.00 89.42	26.09(5) 39.70 59.56 78.40 99.25 121.09 144.70 184.14(3) 199.46 241.10	.329(1) .241 .163 .171 .182 .186 .268(9) .293 .337	. 103 (1) .082 .057 .060 .061 .066 .082 .082 .082 .091(9) .112 .125	.324(9) .339 .351 .354 .337 .357 .357 .360 .351(6) .381 .371	37.24(4) 56.41 93.85 110.89 138.78 172.31 208.61 265.65(2.5) 297.72 360.68

### YTTERBIUM(Z2=70)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR DEUTERON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMM	A1 GAMM	IA2 TOTAL
MeV				BARNS			
1.2 1.4 1.6 2.2 2.2 2.2 2.2 2.3 3.0	.117(8) .179 .251 .333 .421 .539 .653(7) .794 .926 1.057	2.18 (5) 3.38 4.88 6.52 8.50 10.92 13.19(4) 16.46 19.13 22.40	1.35 (6) 1.97 2.77 3.73 4.90 6.26 7.65 (4) 9.61 11.16 13.09	.188 .275 .367 .499 .686 .894 1.094 1.416 1.663 1.958	(7) .15 .22 .31 .44 .61 .77 (6) .93 1.21 1.42 1.65	10 (8) .03 19 .04 7 .05 7 .06 6 .11 8 (7) .15 3 .20 10 .24 14 .30	(34 (0) 3.84 (4)) (54 5.81) (00 8.26) (51 11.08) (92 14.52) (8 18.62) (6 (9) 22.59 (3)) (3 28.29) (3 32.87) (4 38.51)
ENERGY	BETAI	BETA	2 LA	/11	LA/LB	LA/LG	LB/LG
MeV		BARNS					
1.241.68024680	.930 1.326 1.839 2.525 3.269 4.253 5.172 5.172 6.453 7.612 9.065	(7) .42 .64 .93 1.21 1.63 2.00 3.16 3.54 4.02	$\begin{array}{cccc} 1 (9) & 18 \\ 5 & 13 \\ 0 & 19 \\ 6 & 20 \\ 9 & 20 \\ 9 & 20 \\ 1 & 20 \\ 1 & 20 \\ 1 & 20 \\ 7 & 21 \\ \end{array}$	.74(9) .90 .45 .56 .19 .25(8) .75 .65 .19	1.617 (7) 1.716 1.761 1.745 1.734 1.744 1.723 (6) 1.712 1.714 1.711	11.60(C) 12.32 13.23 13.05 12.39 12.21 12.05 11.63 11.50 11.44	7.172 (8) 7.181 7.543 7.481 7.147 7.001 6.996 (7) 6.789 6.788 6.586

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.2	1.61(10)	4.12(8)	11.56 ()	.391((3)	.139(11)	.356(10)	17.29 (5)
1.4	1.89	5.44	18.09	.293	.104	.356	26.42
1.6	2.06	8.99	26.34	.229	.0782	.341	37.39
1.8	2.25	12.71	35.25	.177	.0638	.361	50.21
2.0	2.81	17.72	45.85	.159	.0613	.386	66.38
2.4	4.87	22.04	58.60	.221	.0831	.376	35.51
	5.46(9)	26.52(7)	78.59 (5)	.244(U)	.0915(0)	.376(9)	103.57 (4)
	8.41	34.29	87.80	.245	.0958	.391	130.50
	10.07	40.10	101.86	.251	.0989	.394	152.03
	12.59	46.56	119.13	.270	.106	.391	173.28

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#### TUNGSTEN(Z2=74)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR DEUTERON IMPACT

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.2 1.4 1.8 0 2.2 4 0 2.2 4 0 2.2 2.8 0 2.0 2.0 3.0	.0718(9) .115 .170 .225 .296 .368(8) .455 .529 .629(7) .755	1.48 (G) 2.24 3.32 4.52 5.99 7.62 9.57 11.48 13.75 (S) 16.42	.812 (6) 1.22 1.78 2.42 3.23 4.06 5.26 6.19 7.59 (5) 8.99	.118(7) .178 .243 .330 .443 .554 .711 .850 1.070 1.290	.0817(9) .129 .190 .273 .373 .466 .609 .727 .920(8) 1.111	.8364(10) .8490 .8538 .8575 .8783 .8879(9) .182 .123 .149 (3) .179	2.41 (4) 3.76 5.52 7.50 9.96 12.60 15.99 18.97 23.03 27.46
ENERGY	BETAI	BETR2	LAZ	LL LA	/LB LA.	LG LB.	LG
MeV		BARNS					
1.2 1.4 1.8 2.2 2.4 2.2 2.4 2.3 3.0	.524 .767 1.106 1.511 2.059 2.435 3.267 3.988 4.838 5.669	(8) .288 .456 .677 .912 1.174 1.626 1.990 2.201 (6) 2.748 3.321	(a) 19. 19. 19. 20. 20. 20. 21. (1) 21. 21.	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	730 (8)       11         832       12         864       13         865       13         853       13         877       13         820       13         843       13         812 (6)       12         827       12	.89 (8) 6.8 57 6.8 66 7.3 69 7.3 52 7.2 77 7.3 46 7.3 46 7.3 46 7.3 42 7.2 85 7.8 73 6.9	73 ( <b>3</b> ) 52 29 40 34 35 35 30 33 58

## EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

FOR DEUTERON IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL	
MeV		BARNS					BARNS	
1.24 1.46 1.60 1.46 1.60 1.46 1.60 1.46 1.60 1.46 1.60 1.46 1.60 1.46 1.60 1.46 1.60 1.46 1.60 1.46 1.60 1.60 1.60 1.60 1.60 1.60 1.60 1.6	1.06(10) 1.41 1.48 1.53 1.83 2.29(9) 2.58 3.13 3.76(8) 4.51	1.74(9) 2.80 4.23 6.17 8.48 10.61(8) 13.94 16.62 21.08(7) 25.43	6.24(7) 10.04 15.07 20.58 27.29 34.77 43.64 51.99 62.58(6) 74.61	.609(3) .504 .350 .248 .216 .216(12) .185 .178(11) .177	.179 (2) .140 .0982 .0743 .0671 .0659(11) .0591 .0602 .0602(10) .0684	.279 (10) .279 .281 .300 .311 .305 .319 .320 .337(9) .341	9.04 14.25 20.78 28.28 27.60 47.67 60.16 71.74 87.34 104.55	(5)

# GOLD(22=79)

EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR DEUTERON IMPACT

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.24 1.46 1.00 2.22 2.60 2.24 2.00 2.20 2.00 2.00 2.00 2.00 2.0	.0466(8) .0742 .113 .157 .202 .258 .320(6) .390 .460 .538	.809 G 1.31 2.01 2.78 3.69 4.79 5.99 G 7.37 8.74 10.45	<ul> <li>.468 (6)</li> <li>.738</li> <li>1.10</li> <li>1.48</li> <li>1.96</li> <li>2.53</li> <li>3.15 (5)</li> <li>3.86</li> <li>4.59</li> <li>5.38</li> </ul>	.0640(7) .0973 .142 .199 .256 .324 .424(6) .505 .608 .716	.0386(9) .0664 .102 .150 .200 .258 .347(7) .417 .503 .593	0.0254(10) .0309 .0396 .0485 .0559 .0660 .0777(9) .0875 .105 .123	1.39 (4) 2.21 3.37 4.62 6.11 7.91 9.88 (3) 12.12 14.40 17.08
ENERGY MeV	LAZI	LL	LA/LB	LA/LG	LB	VLG	
1.2 1.4 1.6 2.0 2.2 2.4 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0	17. 17. 17. 17. 18. 18. 18. 18. 19.	35(9) 59 78 76 26 54 79(7) 89 81 40	1.739 (7) 1.787 1.823 1.874 1.882 1.891 1.899 (6) 1.913 1.903 1.942	12.64 13.42 14.15 13.97 14.48 14.78 14.78 14.68 14.68 14.59	(a) 7.77777777777777777777777777777777777	308 (8) 507 761 455 656 819 432 (7) 634 554 512	

EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

FOR DEUTERON IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.24 1.46 1.68 2.04 2.04 2.00 2.04 2.00 2.00 2.00 2.00	.908(0) 1.02 1.24 1.42 1.52 1.71 1.84(9) 1.96 2.33 2.71	.582(8) 1.08 1.71 2.57 3.46 4.50 6.10(7) 7.39 8.92 10.52	2.64(7) 4.49 7:08 9.94 13.38 17.53 22.01(5) 27.29 32.33 38.69	1.560(3) .944 .725 .553 .439 .380 .382(11) .261 .258	.344(12) .227 .175 .143 .114 .0975 .0836(0) .0718 .0721 .0790	.228 (0) .241 .242 .259 .259 .257 .277 (8) .271 .276 .272	4.13 (5) 6.59 10.03 13.93 18.36 23.74 29.95 (4) 36.64 43.58 51.92

#### LEAD(Z2=82)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR DEUTERON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.2 1.4 1.6 1.0 0 2.2 2.4 2.0 0 2.0 2.0 0 3.0	.0346 (8) .0579 .0840 .114 .155 .201 .244 .292(7) .355 .413	.571 (9) .970 1.41 2.67 3.54 4.40 5.40(4) 5.61 7.79	.339 (6) .550 .781 1.10 1.46 1.95 2.43 3.60 3.66 4.27	. 0503 (7) . 0803 . 110 . 155 . 205 . 270 . 342 . 428 (6) . 534 . 570	.0302(9) .0543 .0767 .114 .155 .209 .271 .343(7) .429 .543	).0201(11) .0260 .0331 .0413 .0501 .0508 .0708 .0849(0) .105 .127	.995 (#) 1.66 2.38 3.38 4.50 5.96 7.42 9.12(3) 11.16 13.85
ENERGY MeV	LA/L	LI	LA/LB	LA/LG	LE	WLG	
1.24 1.46 1.80 2.02 4.60 2.02 2.02 2.03 0 3.00	16.5 16.7 16.7 17.5 17.6 17.6 18.0 18.4 18.6	19 5 5 9 9 9 9 9 9 9 9 9 9 9 1 9 9 1 9	1.688 (9) 1.762 1.802 1.824 1.829 1.820 1.810 1.810 1.802 (6) 1.804	11.36 12.07 12.89 12.95 13.05 13.13 12.86 12.62 12.38 11.49	(3) 6. 6. 7. 7. 7. 7. 7. 6.	732 (8) 853 182 898 134 211 185 868 378	

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.2 1.4 1.6 0.0 0.4 0.0 0.4 0.0 0.0 0.0 0.0 0.0 0.0	.638(11) .752 .918 1.06 1.20 1.35 1.43 1.63(10) 1.98 2.28	.410 (9) .783 1.13 1.70 2.35 3.20 4.19 5.33 (8) 5.67 8.47	1.61(7) 2.92 4.35 5.34 8.57 11.49 14.38 17.72(6) 21.66 25.17	1.556(14) .960 .812 .624 .511 .422 .341 .386(13) .297 .269	.396(13) .258 .211 .167 .140 .117 .0994 .8928(12) .8914 .8906	.255(L) .268 .260 .268 .274 .279 .291 .391(L0) .308 .337	2.55(5) 4.46 5.40 9.10 12.12 15.04 20.00 24.53 35.92

# BISMUTH(Z2=83)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR DEUTERON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS	and so a		
1.4 1.6 1.6 2.0 2.4 2.0 2.4 2.0 2.0 2.0 2.0 2.0 0 0 0 0 0 0	.8542(9) .8862 .109 .146 .183(8) .228 .286 .334(7) .381	.950 1.47 1.85 2.52 3.25 4.93 5.29 6.26 7.81	() .557 (7) .806 .998 1.36 1.78 (6) 2.22 2.89 3.55 (5) 3.95	.0700(7) .105 .131 .180 .233 .298 .388 .484 .536	.0478(9) .0753 .0950 .133 .178 .233 .310 .392(8) .435	) .8222(0 .8296 .8361 .9466 .8558 .8558 .8652 .8788 .8918(9) .101	) 1.63 (4) 2.47 3.09 4.21 5.45 6.78 8.77 10.63 (3) 11.88
ENERGY MeV	LA/L	.L	LA/LB	· LA/LG	LB	VLG	
1.4 1.8 2.2 2.2 2.2 2.2 2.2 2.2 2.2 2.2 2.2 2	17.5 17.0 17.0 17.2 17.7 17.6 18.1 18.7 18.4	13(10) 14 12 12 14 15 15 16 16 16 16 16 16 16 16 16 16 16 16 16	1.794 (8) 1.824 1.857 1.849 1.824 1.814 1.799 1.755 (6) 1.775	13.57 ( 13.99 14.15 14.00 13.94 13.53 13.41 12.94 13.08	(B) 7. 7. 7. 7. 7. 7. 7. 7. 7. 7.	963 (9) 672 618 571 644 460 452 334 ( <b>3</b> ) 368	

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

ENERGY	LI	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS	Lunite and				BARNS
1.46 1.00 2.22 2.24 2.20 2.20 2.20 2.20 2.20 2	.589(10) .724 .868 1.07 1.15 1.26 1.34 1.44(9) 1.56	.678(9) 1.08 1.37 1.93 2.61 3.45 4.62 5.88 (8) 6.53	2.86(7) 4.53 5.75 7.87 10.27 12.83 16.69 20.16(6) 22.61	.879(13) .678 .634 .554 .441 .365 .298 .245(12) .239	.206(2) .150 .151 .136 .112 .0982 .0803 .0714(1) .0590	. 234 (U) . 238 . 238 . 245 . 254 . 254 . 269 . 277 . 292 (O) . 289	4.12 (S) 5.33 7.99 10.87 14.03 17.54 22.65 27.48 30.70

#### YTTERBIUM(Z2=70)

#### EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.2 1.4 1.6 2.2 2.2 2.2 2.2 2.2 2.3	.0297 (8) .0542 .0944 .144 .216 .280 .356 .445 (7) .519 .614	.545 (b) .982 1.71 2.63 4.04 5.43 6.93 9.03 (c) 10.61 12.55	.439 (6) .703 1.13 1.72 2.57 (5) 3.33 4.21 5.24 (4) 6.37 7.45	.0777(7) .129 .198 .302 .421 .559 .677 .810 (6) .982 1.152	.0471(8) .0858 .134 .222 .314 .431 .537 .657(7) .812 .974	.0306(11) .0431 .0635 .0798 .108 .127 .140 .153(9) .170 .178	1.09(4) 1.37 3.14 4.79 7.25 9.60 12.17 15.53 18.48 21.77
ENERGY	BETA1	BETR2	LAZ	LL LAZI	LB LA	LG LB	LG
MeV	1	BARNS					
1.2 1.4 1.6 1.8 2.2 2.4 2.4 2.8 3.0	.310 .503 .795 1.221 1.804 2.316 2.885 3.594 4.479 5.170	(8) .129 .200 .340 .494 (6) .770 1.016 1.323 (5) 1.645 1.889 2.283	<ul> <li>(b) 18.</li> <li>18.</li> <li>18.</li> <li>18.</li> <li>18.</li> <li>18.</li> <li>19.</li> <li>19.</li> <li>20.</li> <li>20.</li> <li>20.</li> </ul>	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	40 (8) 7 36 7 87 8 32 8 70(7) 9 29 9 46 10 24 (6) 11 66 10 84 10	.81(3) 5.6 .62 5.4 .66 5.7 .71 5.6 .79 6.1 .72 5.9 .15(7) 6.4 .89 6.4	54(3) 55 44 18 65 118 65 118 65 65 65 65 7 84 67

### EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV	an avite	BARNS					BARNS
1.24	1.30(11) 1.82 2.68 3.36 4.52 5.34 5.86 6.40(9) 7.07 7.40	1.15(9) 2.20 3.47 5.94 8.42 11.76 14.78(8) 22.69 27.41	2.57(1) 4.78 9.55 13.29 28.85 36.12 47.78(1) 55.94 66.39	1.130(4) .827 .772 .566 .537 .454 .351(12) .312 .270	.506(13) .381 .253 .218 .190 .162 .134(11) .126 .111	.447 (11) .460 .406 .447 .406 .419 .409 .382(9) .406 .413	5.02 (5) 8.80 14.70 22.59 33.70 45.75 56.76 72.31 85.70 101.20

#### TUNGSTEN(Z2=74)

# EXPERIMENTAL L'SHELL X-RAY PRODUCTION CROSS SECTIONS FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETA	(	JAMMA	GAMMA	1	GAMMA:	2	TOTAL
MeV				1	BARNS			Sec. 4		
1.2468924689	.0179(9) .0336 .0566 .0873 .130 .179 .238(7) .300 .378 .421	.333 (6) .622 1.09 1.67 2.49 3.38 4.74 (5) 6.11 7.57 8.57	.271 .454 .724 1.10 1.58 2.00 2.68 3.32 4.14 4.80	(J) (J)	.0464 .0796 .123 .192 .250 .320 .406 .503 .638 .709	7) .023 .042 .072 .121 .159 .209 .274 .348 .464 .518	3(9) 6 8 (8)	.023 .037 .051 .070 .090 .111 .131 .155 .174 .191	2(11) 9 4 9 5 (10)	.669 (5) 1.19 1.99 3.05 4.44 5.87 8.06 (4) 10.22 12.72 14.50
ENERGY	BETA1	BETR2		LA/LI	L LF	1/LB	LA/	LG	LB/1	_G
MeV		BARNS								
1.2 1.4 1.6 2.2 2.4 2.2 2.4 2.2 2.2 2.2 2.2 2.2	.182 .307 .492 .758 1.040 1.340 1.807 2.206 2.674 3.104	(9) .088 .147 .232 .341 .540 .660 .874 1.109 1.465 1.693	6 (9) (2)	18.5 19.2 19.1 19.1 19.1 19.9 20.3 20.3 20.3	9 (10) 1. 3 1. 6 1. 9 1. 4 1. 3 (8) 1. 7 1. 7 1.	238(8) 371 501 523 574 688 767(7) 842 829 786	7. 7. 8. 9. 10. 11. 12. 12.	18 (8) 82 81 72 95 54 68(7) 14 86 98	5555566666	38 (9) 35 78 26 22 46 10 (3) 32 36 53

#### EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

#### FOR ALPHA IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.4600044000 1.000044000 0.0000	.707(11) 1.12 1.55 2.11 2.69 3.30 3.36(0) 4.54 5.01 5.51	.428(0) .314 1.43 2.50 3.31 4.36 5.83(8) 7.43 10.09 11.27	1.55(8) 2.96 5.30 8.18 12.36 16.92 24.03(7) 31.12 38.62 43.81	1.652(15) 1.376 1.084 .844 .813 .757 .662(13) .611 .497 .489	.456 (4) .378 .292 .258 .218 .195 .161(12) .146 .130 .126	.276(13) .275 .270 .306 .268 .258 .243 (1) .239 .261 .257	2.69 4.89 8.28 12.79 18.36 24.58 33.72 43.09 53.72 60.59

GOLD(22=79)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.4 1.0 1.0 0 0 0 1.4 0 0 0 0 1.4 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	.0211(9) .0351 .0590 .0797 .110 .142 .184(7) .235 .266	.3750 .621 1.06 1.52 2.10 2.87 3.900 5.66	6) .250(7) .418 .657 .915 1.25 1.64 0 1.96(6) 2.50 2.65	.0478(7) .0681 .0987 .131 .185 .233 .283(6) .346 .378	.0248(9) .0351 .0572 .0770 .115 .146 .186(8) .238 .263	.0230(1) .0330 .0415 .0540 .0699 .0862 .0972(10) .108 .115	.694 (4) 1.14 1.87 2.64 3.64 4.88 6.32 8.13 8.95
ENERGY MeV	LAZL	L	LA/LB	LA/LG	LI	3/LG	
1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.4 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 1.6 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0	17.8 17.7 17.9 19.0 20.2 21.2 21.4 21.4	1(10) 1 16 13 19 19 19 19 19 19 19 19 19 19 19 19 19	1.503(8) 1.486 1.614 1.658 1.681 1.755 1.989(7) 2.025 2.135	7.85 9.13 10.74 11.57 11.33 12.32 13.77( 14.60 14.97	(8) 5. 6.6.6.7.6.7.7. (7) 7.	224(9) 142 652 982 742 021 .921(8) 212 809	

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS FOR ALPHA IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.4 1.6 1.0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	.862(11) 1.24 1.51 1.95 2.46 3.02 3.32(10) 3.55 3.74	.336(9) .472 .841 1.14 1.77 2.27 2.95(8) 3.88 4.31	.976(8) 1.73 3.28 4.81 6.75 9.46 13.29 (6) 17.63 19.88	2.565(14) 2.627 1.795 1.711 1.390 1.330 1.125(13) .915 .868	.883(14) .717 .460 .405 .364 .319 .250(2) .201 .188	.344(12) .273 .256 .237 .262 .240 .222(10) .220 .217	2.17 (A) 3.44 5.63 7.90 10.98 14.75 19.56 25.06 27.93

#### LEAD(22=82)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		and -	
1.4 1.6 1.6 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0	.0155(10) .0287 .0426 .0609 .0802(9) .106 .141 .170 (8) .200	.269 (6) .462 .700 1.02 1.44 1.89 2.42 3.01(5) 3.79	) .177(7) .298 .435 .615 .866 1.12 1.43 1.75(6) 2.12	.0300(8) .0495 .0711 .0930 .126 .168 .210 .261(7) .311	.0186(00 .0291 .0414 .0566 .0784 .109 .138 .177(9) .213	) .0114(12) .0204 .0297 .0363 .0473(11) .0586 .0721 .0840(0) .0984	.492 (4) .339 1.25 1.79 2.51 3.29 4.20 5.20 6.42
ENERGY MeV	LA/L	L	LA/LB	LA/LG	LE	VLG	
1.4 1.6 1.8 2.2 2.4 2.4 2.5 2.3 2.5 2.5 2.5 2.5 2.5 3.5	17.4 16.6 16.4 16.8 17.9 17.8 17.1 17.6	43(11) 39 42 31 32(10) 30 18 59(9) 35	1.521(8) 1.559 1.609 1.653 1.658 1.691 1.695 1.722(7) 1.784	8.98 9.34 9.85 11.01 11.40 11.25 11.55 12.18	(9) 5. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6.	903 (10) 023 119 613 873 659 800 786 ( <b>9</b> ) 825	

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL		
MeV	an salar	BARNS							
1.4 1.6 1.8 2.2 2.4 2.4 2.8 2.8 2.9	.354(2) .659 .963 1.15 1.47 (1) 1.76 2.15 2.42(0) 2.81	.258(10) .389 .550 .774 1.09 1.55 1.96 2.56(9) 3.99	.721(8) 1.21 1.86 2.88 4.13 5.53 7.14 9.03(6) 11.59	1.372(19) 1.694 1.751 1.486 1.349(15) 1.135 1.097 .945(13)	. 491(14) .545 .518 .399 .356 .318 .301 .268(73) .244	.358 (3) .321 .296 .269 .264 .280 .275 .283(1) .263	1.33 ( 2.26 3.37 4.80 6.69 8.84 11.25 14.25 14.25	(3) (5)	

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# BISMUTH(Z2=83)

# EXPERIMENTAL L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L AL	PHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV			540	BARNS	•	State of	
1.4 1.6 1.8 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0	.0136(10) .0237 .0382 .0519 .0715 .0902 .115(3) .148 .187	.239 (6) .386 .633 .867 1.22 1.57 2.01 (5) 2.58 3.31	.156(7) .250 .413 .531 .775 .956 1.20 1.49 1.88	.0230(8) .0359 .0576 .0786 .110 .140 .176(7) .216 .270	.0121(4 .0207 .0345 .0488 .0706 .0917 .117 (9) .147 .190	) .0110 (12 .0152 .0230 .0298 .0395 .0485 0 .0595(1) .0685 .0804	) .432 (4) .696 1.14 1.53 2.17 2.75 3.50 4.43 5.64
ENERGY MeV	LA/LL	Lf	₽∕LB	LA/LG	LI	3/LG	
1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.4 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 9.0 1.6 1.6 9.0 1.6 1.6 1.6 1.6 1.6 1.6 1.6 1.6 1.6 1.6	17.51 16.30 16.58 16.70 17.03 17.36 17.42 17.39 17.71	(11) 1. 11. 11. 11. (9) 1. 11.	.527 (8) .544 .534 .632 .571 .639 .678 (7) .731	10.39( 10.76 11.00 11.03 11.07 11.19 11.41( 11.92 12.24	(9) 6.67.67.68 6.67.67.68 8) 6.66	882 <i>(10)</i> 966 169 845 825 888 888 962	

# EXPERIMENTAL L SUBSHELL IONISATION CROSS SECTIONS FOR ALPHA IMPACT

ENERGY	L1	L2	L3	L1/L2	L1/L3	L2/L3	TOTAL
MeV		BARNS					BARNS
1.4 1.0 0.0 0.4 1.0 0.0 0.4 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0	.350(12) .463 .687 .867 1.12 1.35 1.63(11) 1.82 2.04	.147(/0) .268 .456 .656 .962 1.26 1.61(9) 2.07 2.69	.682(8) 1.83 1.73 2.41 3.44 4.48 5.88(7) 7.68 9.92	2.381(16) 1.728 1.507 1.322 1.164 1.071 1.012(14) .879 .758	.581(/4) .450 .397 .360 .326 .301 .281(/3) .239 .206	.244(13) .260 .264 .272 .280 .281 .278(1) .272 .271	1.10 (6) 1.76 2.87 3.93 5.52 7.09 9.04 (5) 11.49 14.65

# APPENDIX C THEORETICAL L SHELL X-RAY PRODUCTION AND IONISATION CROSS SECTIONS

CONTEN	rs Page
PROTON IMPACT	473
DEUTERON IMPACT	489

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C.3 ALPHA PARTICLE IMPACT

C.1

C.2

Theoretical L shell x-ray production and ionisation cross sections are presented for each element in order of increasing atomic number. See page 452 for explanations.

# C.1 PROTON IMPACT

## DYSPROSIUM(Z2=66)

ENERG	Y <u>L</u>	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		1-1-2.3	
1.0246000046000 1.1.1.2.2.2.2.2.2.0 2.2.2.2.2.2.2.2.2.2.2.2.2	.698 1.032 1.410 1.829 2.279 2.751 3.242 3.736 4.251 4.254	16.653 24.620 33.634 43.640 54.380 65.667 77.394 89.215 101.510 113.530 125.725	3.543 12.996 18.397 24.637 31.842 39.637 47.989 56.694 65.828 74.943 94.363	1.057 1.642 2.392 3.303 4.373 5.574 6.876 8.258 9.724 11.193 12.731	.931 1.420 1.997 2.648 3.374 4.152 4.971 5.824 6.699 7.583 8.483	.126 .223 .396 .999 1.422 1.905 2.435 3.625 3.611 4.248	26.813 40.080 55.537 73.076 92.375 113.035 134.765 157.041 180.321 203.297 226.826
	ENERGY	BETA1	BETR2	LA/LB	LA/LG	LB	VLG
	MeV	BAR	NS				
	1.024.68024.680	5.725 8.830 12.708 17.317 22.649 28.557 34.909 41.618 48.677 55.762 63.124	2.818 4.164 5.688 7.378 9.192 11.098 13.078 15.074 17.149 19.177 21.235	1.933 1.878 1.312 1.751 1.692 1.640 1.597 1.558 1.527 1.500 1.475	15.618 14.862 13.935 13.092 12.321 11.670 11.149 10.639 10.397 10.042 9.777	87777866666	.079 .913 .690 .476 .282 .114 .980 .865 .770 .695 .627

# PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR PROTON IMPACT

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERG	Y L	ALFHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.0 1.2 1.4 1.6 2.2 2.4 2.2 2.2 2.2 2.0 3.0	.533 .827 1.171 1.559 1.983 2.436 2.904 3.388 3.888 4.387 4.895	12.718 19.721 27.924 37.200 47.331 58.137 69.326 80.894 92.837 104.761 116.907	6.532 10.437 15.293 21.059 27.722 35.046 42.912 51.294 59.978 68.920 73.024	.811 1.323 1.994 2.821 3.812 4.927 6.147 7.467 8.845 10.280 11.746	.709 1.136 1.653 2.929 3.657 4.436 5.260 6.098 6.967 7.839	.102 .187 .340 .572 .883 1.271 1.711 2.207 2.748 3.313 3.908	20.489 32.140 46.136 62.306 80.414 100.005 120.632 142.264 164.646 187.315 210.412
	ENERGY	BETRI	BETA2	LA/LB	LA/LG	LB	VLG
	MeV	BAR	INS				
	1.0211.44	4.380 7.100 10.570 14.768 19.720 25.218 31.195 37.624 44.292 51.220 58.275	2.152 3.336 4.722 6.290 8.001 9.826 11.715 13.668 15.685 17.697 19.747	1.931 1.873 1.810 1.751 1.692 1.643 1.600 1.563 1.505 1.505 1.483	15.555 14.774 13.883 13.066 12.303 11.639 11.172 10.729 10.393 10.091 9.854	37.7.7.7.666.66	.856 .886 .671 .464 .272 .113 .981 .870 .781 .785 .642

DYSPROSIUM(22=66)

L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

LIS	JESHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV	•			BARNS		The said of the		2.0
1.00 1.20 1.40 1.50 2.20 2.40 2.40 2.40 2.40 2.50 2.50 2.50 2.50	6.51 11.54 20.66 34.43 52.67 75.18 100.92 129.12 160.60 191.82 225.83	7.83 14.54 25.98 42.35 62.97 87.52 115.66 145.85 175.65 245.98	5.45 8.95 15.88 26.89 42.88 60.94 83.37 109.28 136.26 166.51 196.64	6.42 11.33 20.12 33.29 50.74 72.37 96.68 123.92 153.52 184.27 216.59	4.59 7.86 14.32 24.71 39.20 57.36 79.11 104.37 130.82 160.55 190.29	5.41 9.94 18.14 30.59 47.27 68.12 91.74 118.35 147.39 177.68 209.59	4.46 7.68 14.04 24.29 38.61 56.60 78.15 103.21 129.48 159.03 188.61	5.26 9.72 17.79 30.07 46.56 67.21 90.63 117.04 145.39 176.00 207.74
L 2 3	UBSHELL							
ENERGY	PWBR	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS	-		1.3 m. 18-	
1.00 1.20 1.40 1.50 2.00 2.40 2.50 2.50 2.50 3.00	33.60 50.93 70.79 92.54 116.26 141.10 166.83 193.39 220.17 247.32 274.53	37.69 56.21 77.15 99.86 124.40 150.23 176.72 203.65 231.32 258.62 286.57	27.22 42.43 60.16 79.95 101.51 124.70 149.20 174.41 200.13 226.59 252.92	30.91 47.12 65.82 86.51 109.44 133.20 158.31 184.47 210.54 237.55 264.27	23.19 37.56 54.62 73.89 95.03 117.88 142.12 167.13 192.72 219.07 245.35	26.33 41.72 59.77 79.95 102.46 125.92 150.80 176.77 202.74 229.67 256.36	$\begin{array}{r} 22.48\\ 36.62\\ 53.46\\ 72.51\\ 93.46\\ 116.14\\ 140.22\\ 165.08\\ 190.54\\ 216.78\\ 242.95\end{array}$	25.53 40.67 58.49 78.46 100.77 124.06 148.78 174.61 200.46 227.27 253.36
L3SU	UBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 2.20 2.20 2.20 2.20 2.20 2.20 2.20 2	109.30 160.74 217.75 279.87 345.33 413.02 482.58 551.84 623.30 692.85 762.69	120.56 174.90 234.60 298.75 366.02 434.98 505.76 576.81 648.56 719.72 739.25	89.43 134.67 186.22 243.47 304.90 369.03 434.81 502.71 571.19 640.59 709.55	99.23 147.01 201.06 260.47 323.76 389.94 457.36 526.08 596.50 666.02 736.54	77.30 120.56 170.60 226.66 287.19 350.68 416.04 483.65 551.29 690.27	85.76 131.61 184.19 242.49 304.95 370.55 437.62 506.13 576.43 645.95 716.52	75.17 117.81 167.29 222.84 282.90 345.98 410.99 478.28 546.32 615.39 684.17	83.40 128.62 180.62 238.40 300.40 365.59 432.31 500.51 570.53 639.83 710.19
,	TOTAL ECP	SSR L SHE	ILL IONISP	ATION CROS	S SECTION	45 AND SUE	SHELL RAT	10S
			FOR	PROTON IM	PACT			
	ENERGY MeV		TOTAL BARNS	L1/L2		L1/L3	L2/1	.3
	1.00 1.40 1.40 1.60 1.60 2.20 2.20 2.20 2.20 2.20 2.20 2.20 2	111000 4 00 40 00 00 00 00 00 00 00 00 00 0	14.19 79.01 56.90 46.93 447.73 55.36 71.71 92.15 916.87 943.09 71.79	.206 .239 .384 .383 .462 .549 .678 .728 .774 .818		.063 .098 .126 .155 .184 .210 .256 .275 .293	.306 .311 .324 .335 .335 .349 .349 .355 .355	

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#### YTTERBIUM(Z2=70)

ENERGY	/ L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV	19 29 20			BARNS			
1.021.4680244680	.482 .727 1.009 1.321 1.665 2.032 2.417 2.812 3.223 3.635 4.062	10.967 16.529 22.950 30.054 37.882 46.254 55.030 64.031 73.400 82.785 92.527	5.474 8.399 11.983 16.216 21.102 26.531 32.488 38.885 45.645 59.851	.677 1.045 1.521 2.112 2.320 3.631 4.543 5.548 6.617 7.750 8.916	.587 .918 1.314 1.773 2.288 2.844 3.451 4.296 4.763 5.462 5.161	.0894 .127 .206 .338 .530 .755 1.090 1.450 1.851 2.255 2.751	17.515 26.566 37.272 49.446 63.136 78.035 93.977 110.680 128.167 146.021 164.459
E	INERGY	BETA1	BETR2	LA/LB	LA/LG	l	B/LG
	MeV	BAR	NS				
	1.0 1.24 1.6 1.80 2.0 2.4 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0	3.602 5.579 8.069 11.092 14.644 18.647 23.110 27.975 33.116 38.544 44.092	1.872 2.820 3.914 5.125 6.458 7.884 9.378 10.378 10.2505 14.101 15.759	1.988 1.952 1.899 1.837 1.779 1.728 1.678 1.678 1.631 1.594 1.557 1.531	16.080 15.689 14.965 14.110 13.317 12.626 12.002 11.434 10.986 10.579 10.278		3.088 3.037 7.879 7.679 7.484 7.307 7.151 7.009 5.894 5.793 5.713

#### PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR PROTON IMPACT

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV		1		BARNS			
1.02 1.4 1.6 2024 1.6 2024 1.6 2024 2020 2020 2020 2020 2020 2020 202	.364 .578 .832 1.120 1.444 1.794 2.160 2.544 2.944 3.347 3.765	8.286 13.150 18.933 25.478 32.862 40.823 49.186 57.934 67.934 67.050 76.243 85.752	4.148 6.719 9.952 13.841 18.384 23.500 29.167 35.276 41.754 48.537 55.519	.514 .841 1.271 1.814 2.469 3.230 4.096 5.049 6.071 7.159 8.282	.444 .732 1.098 1.507 1.982 2.505 3.085 3.698 4.342 5.017 5.699	.0703 .108 .183 .307 .486 .724 1.009 1.349 1.349 1.349 1.726 2.138 2.579	13.248 21.182 30.830 42.034 54.871 68.984 84.162 100.266 117.189 134.557 152.489
E	HERGY	BETA1	BETR2	LA/LB	LA/LG	L	B/LG
	MeV	BAR	NS				
	1.0 1.2 1.4 1.6 2.2 2.4 2.2 2.6 2.3 3.0	2.734 4.476 6.723 9.497 12.782 16.542 20.785 25.405 30.331 35.550 40.913	1.414 2.229 4.344 5.602 6.958 8.382 9.871 11.423 12.987 14.606	1.982 1.941 1.887 1.825 1.772 1.722 1.627 1.591 1.556 1.530	15.981 15.513 14.757 13.921 13.191 12.524 11.398 11.367 10.940 10.549 10.254	37777777770660	.062 .992 .628 .445 .274 .120 .986 .877 .780 .704

#### YTTERBIUM(22=70)

L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

L 1 SUBSHELL

ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR			
MeV				BARNS				16/17/6			
1.00 1.20 1.40 1.60 2.00 2.20 2.40 2.60 2.80 3.00	3.68 5.19 8.48 14.01 22.13 32.87 45.77 61.01 78.02 96.40 116.17	4.19 6.43 11.06 18.24 28.13 40.61 55.74 72.33 91.05 110.73 131.97	3.33 4.33 6.71 10.94 17.46 26.27 37.40 50.60 55.53 82.37 99.97	3.79 5.35 8.79 14.42 22.56 33.21 45.39 60.37 77.43 95.42 114.58	2.70 3.69 5.91 9.86 16.01 24.39 35.07 47.82 62.33 78.76 96.02	3.00 4.56 7.74 13.00 20.68 30.83 43.03 57.53 73.65 91.25 110.05	2.62 3.59 5.77 15.73 24.01 34.29 47.29 61.59 95.03	2.90 4.44 7.57 12.75 20.32 30.36 42.43 56.79 72.77 90.25 108.92			
L 2 50	L 2 SUBSHELL										
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR			
MeV				BARNS							
1.00 1.20 1.40 1.60 1.80 2.00 2.20 2.40 2.50 2.50 3.00	16.68 26.19 37.30 49.83 63.53 77.96 93.48 109.66 126.18 143.38 160.31	19.47 29.82 41.77 55.05 69.38 84.81 100.83 117.62 134.72 152.11 169.70	13.46 21.62 31.44 42.63 55.01 68.38 82.91 97.98 113.88 129.99 146.65	15.90 24.94 35.52 47.52 60.61 74.58 89.82 105.53 121.80 138.66 155.45	11.05 18.61 27.92 38.68 50.72 63.80 78.09 92.96 108.70 124.69 141.25	13.0521.4631.5443.1355.8869.5984.59100.13116.26133.00149.73	10.66 18.07 27.22 37.34 49.75 62.71 76.87 91.64 107.27 123.17 139.65	12.59 20.84 30.76 42.19 54.81 68.39 83.27 98.70 114.73 131.38 148.03			
L 3 5	UBSHELL										
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR			
MeV				BARNS							
1.00 1.20 1.40 1.60 1.60 2.00 2.20 2.20 2.40 2.60 2.80 3.00	60.14 90.58 125.20 162.85 203.70 246.76 291.30 336.29 332.80 428.85 476.58	68.29 100.99 137.33 177.22 219.61 263.99 309.87 356.26 403.28 450.84 498.59	48.38 75.46 106.26 140.46 178.61 218.40 260.39 304.06 348.22 393.42 438.98	55.98 84.54 117.32 153.30 193.03 234.97 278.16 322.61 368.51 414.10 461.12	40.94 65.96 95.52 128.74 166.07 205.26 246.77 290.07 334.00 379.03 424.49	46.38 73.89 105.46 140.51 179.47 220.83 263.61 305.45 398.95 445.90	39.64 64.23 93.39 126.24 163.21 202.09 243.32 286.37 330.37 374.90 420.13	45.40 71.96 103.10 137.78 176.39 217.42 259.92 303.84 349.29 394.60 441.37			
	TOTAL ECPSSR L SHELL IONISATION CROSS SECTIONS AND SUBSHELL RATIOS										
			FUR	FROTON IM	IFHC1						
	ENERGY		TOTAL	L1/L2	-	L1/L3	L2/1	.3			

MeV	BARNS			
1.00	60.88	.231	.064	.277
1.20	97.23	.213	.062	.290
1.40	141.43	.246	.073	.298
1.50	192.72	.302	. 093	.306
1.80	251.52	.371	.115	.311
2.00	316.17	. 444	.140	.315
2.20	385.63	.510	.163	.320
2.40	459.33	.575	.137	.325
2.50	536.80	.634	.208	. 328
2.30	616.23	. 687	.229	. 333
3.00	698.32	.736	.247	.335

#### TUNGSTEN(Z2=74)

# PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS	C. With		
1.0 1.4 1.6 1.2 1.6 1.2 1.6 1.2 1.6 2.2 2.4 2.2 2.2 2.2 2.2 2.2 2.2 2.2 2.2	.336 .513 .731 .970 .1,231 1.518 1.321 2.135 2.471 2.306 3.155	7.231 11.148 15.726 20.883 26.515 32.704 39.230 46.080 53.250 60.489 68.020 BETR1	3.562 5.515 7.916 10.769 14.063 17.825 21.992 26.554 31.457 36.649 42.077 BETA2	.455 .698 1.010 1.400 1.872 2.430 3.070 3.070 3.792 4.581 5.440 6.342	.365 .586 .357 1.173 1.530 1.927 2.360 2.824 3.319 3.838 4.375	.0899 .112 .153 .227 .341 .502 .710 .966 1.261 1.601 1.966	11.533 17.797 25.263 33.859 43.468 54.208 65.784 78.170 91.296 104.849 118.984 B/LG
	MeV	BAR	NS				
	1.0 1.2 1.4 1.6 1.3 2.2 2.2 2.6 2.3 3.0	2.094 3.305 4.811 6.604 8.677 11.030 13.640 16.494 19.564 22.825 26.223	1.319 2.834 2.868 3.808 4.834 5.961 7.149 8.396 9.396 9.701 11.018 12.388	2.016 2.006 1.972 1.924 1.870 1.820 1.769 1.769 1.769 1.678 1.636 1.602	15.767 15.853 15.453 14.800 14.052 13.349 12.669 12.047 11.522 11.021 10.630	7777776666	.822 .901 .638 .693 .513 .336 .163 .902 .866 .737 .635

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			100
1.02 1.14 1.1.00 1.1.1 1.00 1.1.0 1.1.0 1.0 1.0 1	.252 .410 .821 1.065 1.339 1.628 1.935 2.2586 2.586 2.928	5.417 3.827 12.941 17.683 22.948 28.848 35.068 41.692 48.663 55.731 63.130	2.678 4.395 6.572 9.213 12.305 15.883 19.863 24.255 29.005 34.026 39.325	.343 .559 .846 1.210 1.656 2.187 2.801 3.495 4.259 5.086 5.964	.276 .467 .710 .999 1.332 1.706 2.117 2.563 3.041 3.541 4.065	.0674 .0920 .136 .211 .324 .482 .684 .932 1.218 1.544 1.897	8.652 14.125 20.860 28.798 37.789 48.019 59.065 71.020 83.761 96.934 110.780
Eł	IERGY	BETR1	BETA2	LA/LB	LA/LG	L	B/LG
٢	leV	BAR	INS				
	024500246000	1.579 2.639 3.999 5.651 7.589 9.816 12.305 15.046 13.015 21.160 24.473	.988 1.610 2.360 3.224 4.193 5.258 6.390 7.596 3.855 10.151 11.498	2.008 1.994 1.954 1.964 1.850 1.801 1.751 1.764 1.663 1.623 1.591	15.678 15.664 15.183 14.498 13.748 13.079 12.416 11.827 11.327 10.862 10.491	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	.807 .857 .614 .432 .261 .992 .940 .811 .691 .594

TUNGSTEN(Z2=74)

L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

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L 1 0	UBSHELL							
ENERGY	PUBA	PNBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.30 1.20 1.40 1.50 2.20 2.20 2.20 2.20 2.20 2.20 2.30 2.3	2.46 2.92 3.93 9.18 13.85 27.61 366.56 57.51	2.67 3.63 3.63 1.03 1.03 1.03 1.05 1.05 1.05 1.05 1.05 0.05 0.05 0.05	2.31 2.63 3.34 4.80 7.36 11.09 16.21 22.55 30.23 39.23 39.23 48.99	2.47 3.03 4.24 6.51 10.03 14.97 21.31 29.09 38.01 48.20 59.19	$1.79 \\ 2.17 \\ 2.86 \\ 4.23 \\ 5.62 \\ 10.13 \\ 14.99 \\ 21.05 \\ 28.45 \\ 37.80 \\ 46.64 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 10.17 \\ 1$	$\begin{array}{c} 1.91\\ 2.49\\ 3.63\\ 5.74\\ 9.02\\ 13.68\\ 19.70\\ 27.16\\ 35.74\\ 45.35\\ 56.35\end{array}$	$\begin{array}{c} 1.72\\ 2.19\\ 2.79\\ 4.13\\ 5.49\\ 9.95\\ 14.75\\ 20.74\\ 23.06\\ 36.53\\ 46.09\end{array}$	1.94 2.42 3.54 5.61 3.43 19.38 26.76 35.28 45.86 55.68
L 2 SI	UBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.50 2.20 2.40 2.40 2.40 2.50 2.30 3.00	8.20 13.33 19.55 26.66 34.54 43.11 52.27 61.93 72.62 93.43	10.07 15.82 22.65 30.39 38.93 48.09 57.69 68.05 78.05 789.61 100.68	6.61 10.95 16.34 22.66 29.78 37.65 37.65 55.02 64.54 84.78	8.21 13.19 19.23 26.13 33.78 42.14 51.11 60.61 70.65 80.98 91.69	5.19 9.12 14.14 20.12 26.96 34.60 42.80 51.59 61.80 78.75 80.98	6.45 10.98 16.63 23.29 38.59 38.72 47.59 56.84 66.74 76.96 87.58	4.98 8.81 13.73 19.62 26.36 33.91 42.02 50.74 50.74 50.07 69.75 79.92	6.19 10.61 16.15 22.62 29.91 37.95 46.64 55.73 75.87 86.43
L 3 S	UBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.50 1.50 2.20 2.40 2.20 2.40 2.20 2.40 2.20 2.2	33.19 51.33 72.35 95.74 120.94 148.30 176.76 206.25 236.37 267.33 298.93	39.09 58.96 81.60 106.44 133.19 161.68 191.60 222.19 253.32 285.15 316.98	25.84 42.55 61.08 32.15 105.23 130.30 156.97 185.15 213.85 243.56 273.63	31.93 49.22 69.35 91.87 116.26 143.11 170.83 199.87 230.10 260.21 291.60	21.68 36.18 53.72 76.38 120.96 147.12 174.93 203.35 232.85 262.77	25.30 41.36 60.99 82.71 106.48 132.79 160.11 188.34 218.30 248.77 280.02	20.89 35.09 52.35 72:32 94.49 118.77 144.77 172.38 200.62 229.95 259.71	24.36 40.60 59.43 80.38 104.39 130.45 157.55 186.08 215.36 245.67 276.77
	TOTAL ECP	PSSR L SHE	ILL IONISA	ATION CROS	S SECTION	NS AND SUI	SHELL RAT	rios
	ENERGY MeV		TOTAL BARNS	L1/L2		L1/L3	L2/L	.3
	1.00 240 1.400 2.400 2.400 2.4400 2.4400 2.4400 2.4400 2.4400 2.4400 2.4400 2.4400 2.4400 2.4400 2.4400 2.4400 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.4000 2.40000 2.40000 2.40000000000		32.88 53.63 79.12 89.11 43.14 81.83 23.57 268.74 516.87 266.60 18.88	.298 .229 .229 .248 .296 .356 .416 .4179 .534 .534 .544		.074 .069 .059 .085 .103 .123 .123 .123 .123 .123 .123 .123 .12	.249 .261 .272 .280 .287 .291 .296 .300 .300 .309 .312	

#### GOLD(22=79)

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV	123/19	1.2.1		BARNS		- 22 -	
1.0 1.2 1.4 1.6 1.3 2.2 2.4 2.8 2.2 2.8 3.0	.220 .345 .496 .669 .864 1.079 1.306 1.555 1.817 2.091 2.379	4.364 6.863 9.865 13.308 17.169 21.444 25.953 30.904 36.113 41.569 47.269	2.027 3.210 4.670 6.404 3.410 10.694 13.163 15.953 18.953 22.127 25.529	.252 .397 .579 .803 1.071 1.384 1.736 2.134 2.576 3.050 3.568	.195 .322 .484 .677 .901 1.155 1.430 1.731 2.056 2.394 2.757	.0574 .0741 .0954 .126 .169 .229 .305 .402 .519 .635 .810	6.362 10.315 15.610 21.185 27.513 34.601 42.177 50.546 59.459 68.837 78.744
	ENE Me	RGY	LA/LB	LA/LG	LB/	ĽG	
	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	02463024680	2.153 2.138 2.112 2.078 2.042 2.005 1.969 1.937 1.905 1.879 1.852	17.308 17.304 17.031 16.556 16.037 15.495 14.951 14.480 14.017 13.628 13.247	8.0 8.0 8.0 77.5 7.5 7.5 7.5 7.5 7.5 7.5 7.5 7.5 7.	38 92 62 72 55 27 94 75 54 55 55	

## PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR PROTON IMPACT

ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		Side In 19	
1.0 1.2 1.4 1.6 1.8 0 2.2 4 6 0 2.0 2 3.0	.163 .273 .409 .569 .751 .953 1.173 1.416 1.671 1.940 2.222	3.244 5.425 9.127 11.302 14.926 18.952 23.321 28.145 33.219 38.574 44.168	1.513 2.554 3.882 5.490 7.387 9.560 11.978 14.676 17.604 20.726 24.073	.189 .317 .485 .695 .950 1.252 1.596 1.985 2.418 2.886 3.397	.147 .259 .404 .583 .793 1.032 1.296 1.586 1.901 2.231 2.588	.0415 .0582 .0805 .112 .157 .219 .299 .398 .516 .554 .807	5.109 3.568 12.903 18.056 24.013 30.718 38.068 46.222 54.912 54.912 64.127 73.860
	ENE Me	RGY	LA/LB	LA/LG	LB/	LG	
	1. 1. 1. 1. 2. 2. 2. 2. 2. 2. 2. 2. 2. 3.	02468024680	2.144 2.124 2.094 2.059 2.021 1.982 1.947 1.918 1.887 1.361 1.835	17.201 17.109 16.748 16.262 15.706 15.136 14.612 14.177 13.735 13.364 13.003	8.0 8.0 7.9 7.5 7.5 7.5 7.5 7.5 7.5 7.5 7.5 7.5 7.5	25 54 99 00 73 35 93 93 93 93 87 80 87	

#### GOLD(22=79)

L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

L 1 SL	JBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 1.80 2.20 2.40 2.50 2.50 2.50 2.50 2.50 2.50 2.50 2.5	1.61 1.79 2.02 2.50 3.39 4.36 5.95 9.78 13.37 17.65 22.67	1.74 1.96 2.41 3.27 4.75 9.89 13.68 18.23 29.49	1.50 1.69 1.68 2.23 2.87 3.98 5.69 10.98 14.65 19.02	1.64 1.83 2.16 2.79 3.93 5.70 8.14 11.32 15.22 19.90 25.11	1.09 1.32 1.54 1.90 2.51 3.55 5.14 7.33 10.17 13.68 17.87	1.19 1.43 1.78 2.38 3.43 5.08 7.38 10.38 14.19 18.58 23.60	1.04 1.27 1.50 1.45 2.45 3.48 5.04 7.20 10.00 13.47 17.62	1.14 1.38 1.72 2.31 3.35 4.98 7.23 10.20 13.87 18.30 23.27
L 2 SL	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.500 1.500 1.500 2.240 2.240 2.240 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.250 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.500 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.5000 2.50000 2.50000 2.50000 2.50000000000	3.35 5.67 8.60 12.09 16.08 20.53 25.29 30.43 35.39 41.51 47.47	$\begin{array}{r} 4.44 \\ 7.22 \\ 10.61 \\ 14.58 \\ 18.98 \\ 29.95 \\ 34.53 \\ 46.40 \\ 52.74 \end{array}$	2.68 4.66 7.19 10.25 13.80 17.76 22.12 26.87 31.85 37.19 42.71	3.62 6.00 8.95 12.44 16.41 20.83 25.58 30.67 36.11 41.69 47.68	1.98 3.70 5.98 8.82 12.16 15.95 20.16 24.76 24.68 34.30	2.67 4.76 7.45 10.70 14.47 18.71 23.31 28.27 33.59 39.08 44.99	1.88 3.55 5.78 8.56 11.84 15.57 19.72 24.28 29.28 39.67	2.54 4.56 7.19 10.38 14.09 18.26 22.80 27.71 32.98 38.42 44.28
L 3 St	JESHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.50 2.00 2.20 2.40 2.50 2.50 3.00	16.03 25.57 37.00 49.98 64.33 79.95 96.12 113.59 131.63 150.25 169.39	19.91 30.84 43.51 57.69 79.49 107.28 125.37 144.45 163.78 183.61	12.89 21.10 31.11 42.72 55.59 69.66 84.74 101.06 118.01 135.82 153.87	16.27 25.64 36.83 49.53 63.59 78.57 94.82 112.20 130.05 148.53 167.55	9.89 17.24 26.52 37.48 49.43 63.16 94.15 110.83 128.41 146.29	12.48 20.96 31.38 43.46 57.00 71.75 87.46 104.53 122.15 140.43 159.30	$\begin{array}{r} 9.46\\ 16.63\\ 25.72\\ 36.51\\ 48.68\\ 62.14\\ 76.70\\ 92.54\\ 109.09\\ 126.54\\ 144.31\end{array}$	11.94 20.22 30.44 42.33 55.69 785.32 102.74 120.22 138.38 157.14
	TOTAL ECP	SSR L SHE	ELL IONISF	TION CROS	S SECTION	NS AND SUE	SHELL RAT	IOS
			FUR	PRUTUN IM	PHCT			
	ENERGY MeV		TOTAL BARNS	L1/L2		L1/L3	L2/L	.3
	1.00 1.20 1.40 1.60 1.60 2.20 2.40 2.40 2.60 2.60 2.60 2.60 2.60 2.60 2.60 2.6		15.62 26.16 39.36 55.02 73.12 93.51 15.86 40.65 167.08 167.08 195.10 224.69	.448 .302 .239 .223 .238 .272 .317 .368 .420 .476 .526		.095 .068 .057 .055 .060 .071 .084 .099 .115 .132 .148	.212 .226 .236 .245 .253 .260 .256 .279 .279 .279 .279	

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## LEAD(22=82)

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.0 1.1.4.6 0.0 0.1.4.6 0.0 0.1.4.6 0.0 0.1.4.6 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0	.167 .267 .398 .529 .687 .861 1.053 1.254 1.475 1.704 1.948	3.164 5.064 7.370 10.031 13.027 16.345 19.981 23.789 27.987 32.322 36.953	1.438 2.316 3.407 4.703 6.207 7.915 9.823 11.888 14.185 16.607 19.241	.177 .283 .416 .580 .776 1.005 1.266 1.558 1.887 2.242 2.634	.129 .219 .335 .476 .641 .830 1.039 1.265 1.514 1.774 2.056	.0476 .0634 .0814 .104 .135 .175 .228 .293 .374 .469 .579	4.946 7.930 11.582 15.843 20.696 26.126 32.123 38.489 45.535 52.875 60.776
	ENE Me	RGY V	LA/LB	LA/LG	LB/	LG	
	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	024600246000	2.200 2.136 2.163 2.133 2.039 2.065 2.034 2.001 1.973 1.946 1.920	17.907 17.920 17.696 17.291 16.786 16.265 15.780 15.267 14.828 14.417 14.029	8.11 8.11 8.11 9.87 7.77 7.765 4.3	38 97 98 98 98 98 76 29 29 16 08 08	

#### PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR PROTON IMPACT

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV		•	- ALANTA	BARNS			
1.0211.44	.124 .211 .321 .599 .766 .949 1.146 1.364 1.589 1.830	2.353 4.010 6.091 8.555 11.366 14.524 18.009 21.750 25.870 30.153 34.712	1.075 1.350 2.346 4.058 5.480 7.120 8.980 11.011 13.270 15.675 18.265	.132 .227 .351 .506 .694 .916 1.176 1.464 1.790 2.145 2.531	.0983 .178 .284 .415 .570 .749 .952 1.171 1.412 1.568 1.942	.0341 .0490 .0673 .0917 .124 .167 .224 .294 .378 .477 .590	3.685 6.298 9.609 13.571 18.139 23.325 29.113 35.372 42.293 49.562 57.338
	ENE Me	RGY	LA/LB	LA/LG	LB/	LO	
	1	024600246000	2.189 2.168 2.141 2.08 2.074 2.040 2.005 1.975 1.950 1.924 1.900	17.779 17.664 17.352 16.392 16.381 15.858 15.319 14.852 14.453 14.060 13.713	8.1 8.1 8.1 8.7 77.6 5 7.7 7 7.7 7 7 7 7 7 7 7 7 7	23 48 96 13 98 73 98 73 98 13 13 13 99 15	

# LEAD(Z2=82)

L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

L 1 St	JBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS			19. 34	
1.00 1.20 1.40 1.60 1.60 2.20 2.20 2.40 2.60 2.60 2.60 3.00	$\begin{array}{c} 1.23\\ 1.40\\ 1.53\\ 1.71\\ 2.10\\ 2.76\\ 3.78\\ 5.23\\ 7.16\\ 9.59\\ 12.51\end{array}$	1.38 1.52 1.71 2.11 2.83 3.97 5.56 7.72 10.45 13.62 17.46	1.13 1.32 1.45 1.60 1.88 2.35 3.13 4.34 5.92 7.94 10.49	1.30 1.44 1.60 1.90 2.43 3.29 4.65 6.43 8.69 11.49 14.73	.782 .995 1.16 1.33 1.62 2.80 3.93 5.42 7.34 9.77	.895 1.08 1.28 1.28 1.29 2.09 2.88 4.15 5.82 7.96 10.62 13.72	.743 .955 1.129 1.297 1.592 2.74 3.322 5.322 9.62	.850 1.04 1.23 1.54 2.03 2.82 4.06 5.71 7.82 10.44 13.51
L 2 St	JBSHELL	•				•		
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV			121	BARNS			-	
1.00 1.20 1.40 1.60 1.60 2.00 2.40 2.60 2.60 2.60 2.60 2.60 2.60 2.60 2.6	1.93 3.36 5.21 7.46 10.07 13.02 16.26 19.73 23.50 27.39 31.58	2.71 4.49 6.71 9.33 12.34 15.61 19.19 23.05 27.07 31.37 35.71	1.552.754.346.308.6211.2414.1617.3720.7724.4428.26	2.22 3.74 5.58 7.98 10.63 13.61 16.91 20.38 24.17 28.09 32.24	1.09 2.11 3.51 5.30 7.46 9.94 12.72 15.82 19.12 22.69 26.43	1.56 2.87 4.60 6.71 9.20 12.04 15.20 18.56 22.24 26.08 30.15	1.03 2.01 3.38 5.13 7.24 9.68 12.42 15.48 18.73 22.27 25.97	1.48 2.74 4.42 6.49 8.93 11.72 14.83 18.16 21.79 25.59 29.63
L3SU	JBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 1.60 2.00 2.20 2.40 2.60 2.60 2.30	10.35 16.87 24.82 33.96 44.13 55.25 67.26 79.60 93.01 106.60 120.92	13.41 20.99 29.98 40.16 51.40 63.41 76.06 89.66 103.60 118.31 132.94	8.36 13.87 20.74 28.85 38.83 48.14 58.98 70.56 82.96 95.95 109.34	10.95 17.51 25.44 34.51 44.57 55.57 67.37 79.74 93.15 106.73 120.98	6.19 11.03 17.30 24.87 33.59 43.30 53.81 55.11 77.26 90.04 103.25	8.11 13.93 21.22 29.75 39.37 49.99 61.47 73.59 86.75 100.15 114.24	5.89 10.60 16.73 24.16 32.74 42.32 52.71 63.89 75.93 88.60 101.71	7.73 13.39 20.52 28.90 38.37 48.86 60.21 72.21 85.25 98.55 112.54
	TOTAL ECP	SSR L SHE	ILL IONIS	ATION CROSS	S SECTION	IS AND SUB	SHELL RAT	TOS
			FOR	PROTON IMP	PACT			
	ENERGY MeV		TOTAL BARNS	L1/L2		L1/L3	L2/L	.3
	1.00 1.20 1.40 1.60 1.30 2.00 2.40 2.40 2.60 2.80 3.00	1	10.05 17.17 26.18 36.93 49.34 63.40 79.11 96.07 14.86 34.59 55.67	.576 .380 .279 .237 .228 .240 .274 .314 .359 .408 .456		.110 .078 .050 .053 .053 .058 .057 .079 .092 .106 .120	. 191 . 205 . 225 . 223 . 246 . 256 . 266 . 266	

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#### BISMUTH(Z2=83)

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL	
MeV	1		Star Star	BARNS		Alexander .	1	
1.0 1.2 1.4 1.6 1.8 2.2 2.4 2.2 2.3 0	.152 2.83 .244 4.55 .356 6.65 .487 9.09 .634 11.85 .798 14.91 .974 18.21 1.164 21.75 1.369 25.58 1.585 29.61 1.813 33.88		1.281 2.077 3.065 4.246 5.617 7.173 3.893 10.300 12.874 15.110 17.504	.157 .253 .374 .522 .700 .906 1.141 1.410 1.705 2.031 2.386	.112 .296 .423 .573 .743 .932 1.140 1.364 1.365 1.859	.0448 .0606 .0773 .0991 .127 .163 .209 .269 .269 .341 .426 .526	4.422 7.130 10.450 14.353 18.804 23.790 29.220 35.127 41.535 48.344 55.584	
	ENE Me	RGY V	LA/LB	LA/LO	LB/	1.0		
	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	02460024600	2.213 2.194 2.172 2.143 2.110 2.079 2.048 2.014 1.968 1.960 1.936	18.080 18.007 17.305 17.423 16.937 16.456 15.964 15.433 15.009 14.583	8.1 8.2 9.1 8.0 9.7 7.6 7.7 7.7 7.7	70 98 98 31 926 915 96 96 96 96 951 940 97		

# PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR PROTON IMPACT

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.02 1.24 1.4 1.6 0.24 1.6 0.24 0.24 0.24 0.24 0.20 2.22 0.20 0.00 0.0	.113 .193 .295 .415 .554 .710 .882 1.065 1.269 1.480 1.706	2.105 3.609 5.507 7.764 10.352 13.275 16.479 19.911 23.710 27.673 31.896	.958 1.660 2.564 3.666 4.965 6.476 8.161 10.019 12.089 14.297 16.681	.113 .204 .316 .456 .626 .831 1.064 1.328 1.626 1.950 2.396	.0854 .157 .252 .370 .511 .675 .857 1.059 1.279 1.514 1.766	.0322 .0467 .0641 .0865 .116 .156 .207 .269 .346 .436 .540	3.293 5.666 8.682 12.302 16.497 21.292 26.585 32.323 38.694 45.400 52.589
	ENE Me	RGY V	LA/LB	LA/LG	LB/	LG	
	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	00440000440000	2.198 2.174 2.148 2.085 2.050 2.019 1.987 1.961 1.936 1.912	17.895 17.730 17.442 17.019 16.529 15.978 15.490 14.995 14.585 14.189 13.833	8.1 8.1 8.1 8.7 7.65 7.75 7.65 7.75 7.75 7.75 7.75 7.	42 550 236 27 94 71 45 31 34	

#### BISMUTH(Z2=83)

L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

L 1 SU	IBSHELL							
ENERGY	PUBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS			1950 - 191	
1.00 1.20 1.40 1.60 1.30 2.00 2.20 2.40 2.60 2.80 3.00	1.11 1.29 1.41 1.56 1.85 2.33 3.09 4.28 5.83 7.80 10.25	1.27 1.41 1.57 1.88 2.43 3.32 4.63 6.39 8.62 11.34 14.51	1.03 1.21 1.33 1.46 1.66 2.62 2.64 3.52 6.48 8.52	1.20 1.33 1.47 1.79 2.09 2.31 3.89 5.32 7.22 9.55 12.30	.699 .903 1.06 1.20 1.42 1.76 2.35 3.21 4.40 5.96 7.91	.813 .991 1.16 1.40 1.78 2.45 3.45 4.79 6.58 8.79 11.42	.663 .865 1.82 1.17 1.38 1.72 2.38 3.14 4.31 5.86 7.78	.771 .950 1.12 1.36 1.73 2.39 3.38 4.69 5.46 8.64 11.24
L 2 SL	JBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 1.30 2.20 2.40 2.60 2.60 2.80 3.00	1.60 2.82 4.40 6.34 8.61 11.18 14.00 17.08 20.35 23.84 27.49	2.30 3.84 5.77 8.05 10.66 13.56 16.74 20.11 23.72 27.48 31.41	1.29 2.31 3.67 5.36 7.35 9.63 12.21 15.00 18.00 21.4 24.61	1.88 3.19 4.87 6.87 9.20 11.84 14.70 17.80 21.14 24.63 28.33	.892 1.75 2.95 4.48 6.32 8.47 10.92 13.60 16.50 19.65 22.95	1.31 2.42 3.90 5.74 7.91 10.41 13.15 16.14 19.38 22.79 26.41	.341 1.66 2.33 4.32 6.12 8.24 10.65 13.29 16.16 19.27 22.54	1.23 2.31 3.75 5.54 7.67 10.13 12.82 15.78 12.35 22.94
L3SU	JBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 2.00 2.20 2.40 2.50 2.50 3.00	8.97 14.69 21.71 29.86 38.97 48.99 59.64 70.85 82.83 95.22 108.11	11.79 18.53 26.57 35.71 45.76 56.56 68.05 80.21 92.96 106.11 119.63	-7.21 12.10 18.17 25.39 33.57 42.54 52.33 62.89 73.84 85.71 97.66	9.62 15.43 22.48 30.60 39.66 49.51 60.25 71.37 83.45 95.77 108.70	5.27 9.53 15.05 21.76 29.50 38.10 47.56 57.84 68.56 30.21 92.00	7.03 12.15 18.61 26.22 34.85 44.43 54.76 65.64 77.48 89.63 102.39	5.82 9.15 14.54 21.12 287.21 46.56 56.34 56.39 90.59	6.69 11.67 17.98 25.45 33.95 43.95 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.50 53.50 53.50 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.60 53.50 53.50 53.60 53.60 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 53.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 55.50 5
	ТОТАЦ ЕСР	SSR L SHE	LL IONISF FOR	ATION CROSS PROTON IMP	SECTION	IS AND SUB	SHELL RAT	105
	ENERGY		TOTAL	L1/L2		L1/L3	L2/L	.3
	1.00 1.20 1.40 1.60 2.20 2.20 2.40 2.60 2.60 3.00	1 1 1	8.69 14.93 22.85 32.35 43.35 55.91 69.80 84.84 01.54 19.14 38.00	. 626 . 412 . 298 . 245 . 226 . 236 . 263 . 298 . 340 . 387 . 433		.115 .081 .062 .053 .055 .063 .073 .085 .098 .111	.1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1998 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1977 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997 .1997	

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#### THORIUM(Z2=90)

# PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR PROTON IMPACT

ENERG	7 L	ALPHA	BETR	GAMMA	GAMMA 1	GAMMA2	TOTAL
MeV				BARNS	The Barrier	5.7%	
	.0767 .129 .195 .274 .364 .465 .576 .597 .325 .964 1.107	1.284 2.165 3.274 4.593 6.103 7.794 9.636 11.686 13.339 16.164 18.566	.562 .947 1.439 2.035 2.732 3.533 4.422 5.501 7.686 8.949	.9639 .197 .164 .234 .319 .419 .531 .662 .967 1.144 .	.0402 .0729 .117 .174 .244 .326 .418 .523 .637 .762 .997	.0236 .0346 .0465 .0597 .0747 .0926 .113 .139 .169 .204 .247	1.986 3.348 5.070 7.131 9.511 12.201 15.170 18.446 21.944 25.747 29.725
1	ENERGY	BETRI	BETR2	LA/LB	LA/LG	L	B/LG
	MeV	BARI	NS				
	1.024 1.1.4 1.000 1.1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.4 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.00000 1.00000 1.00000 1.00000 1.00000 1.000000 1.00000000	.250 .433 .674 .976 1.339 1.764 2.238 2.782 3.373 4.026 4.731	.312 .514 .765 1.059 1.394 1.769 2.184 2.640 3.128 3.660 4.218	2.257 2.256 2.247 2.228 2.205 2.177 2.155 2.127 2.127 2.127 2.075 2.047	20.028 20.062 19.895 19.526 19.057 18.514 18.091 17.555 17.076 16.621 16.130	8.8 8.8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	.874 .892 .855 .764 .644 .505 .255 .130 .010 .381

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV	-	- States	a the second	BARNS		The second	
1.1.1.1.000440888	.0576 .104 .164 .238 .324 .422 .529 .649 .549 .5776 .913 1.058	.963 1.741 2.749 3.981 5.435 7.066 9.876 10.836 13.819 15.319 17.746	.427 .773 1.228 1.795 2.476 3.258 4.151 5.150 6.249 7.446 3.743	.0492 .0892 .143 .212 .295 .395 .512 .644 .795 .961 1.146	.0319 .0623 .105 .160 .228 .309 .402 .505 .622 .747 .884	.0172 .0270 .0381 .0513 .0671 .0861 .110 .139 .173 .214 .262	1.498 2.706 4.281 6.220 8.523 11.128 14.052 17.308 20.810 24.605 28.651
ENERGY		BETAI	BETA2	LA/LB	LA/LO	LI	B/LG
	MeV	BARI	NS .				
1.0.4400000440000 1.1.1.1.0000440000		.194 .362 .590 .882 1.238 1.655 2.139 2.680 3.949 4.673	.233 .411 .638 1.238 1.238 1.603 2.012 2.470 2.960 3.497 4.070	2.233 2.226 2.218 2.189 2.166 2.140 2.140 2.140 2.086 2.055 2.030 2.092	19.536 19.425 19.137 18.725 18.297 17.804 17.243 16.810 16.271 15.339	8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.	749 729 659 556 .447 .319 .173 059 .917 803 .683

THORIUM(22=90)

L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

#### L 1 SUBSHELL

ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV				BARNS		Carl Carl		· · · · ·	
1.00 1.20 1.40 1.50 2.00 2.40 2.40 2.50 2.50 2.50 3.00	.527 .685 .882 .944 1.82 1.12 1.32 1.59 1.99 2.55	.715 .830 .907 .971 1.08 1.25 1.49 1.91 2.47 3.22 4.15	.476 .629 .750 .335 .998 .954 1.05 1.19 1.40 1.73 2.16	.663 .706 .930 1.01 1.14 1.35 1.67 2.12 2.76 3.54	.283 .423 .547 .645 .723 .794 .895 1.84 1.24 1.55 1.95	.394 .528 .632 .719 .946 1.15 1.45 1.87 2.47 3.20	.264 .401 .522 .620 .698 .769 .370 1.01 1.21 1.51 1.91	.368 .500 .603 .788 .917 1.12 1.42 1.42 1.33 2.41 3.14	
L 2 SU	BSHELL								
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV				BARNS	195.55		-		
1.00 1.20 1.40 1.50 1.50 2.20 2.40 2.50 2.50 2.30 3.00	.430 .803 1.32 1.99 2.81 3.78 4.809 7.42 8.87 10.42	.739 1.28 1.99 2.87 3.91 5.07 6.38 7.83 9.37 11.04 12.77	.346 .560 1.10 1.68 2.39 3.24 4.21 5.52 7.85 9.26	.612 1.08 1.69 2.46 3.37 4.42 5.61 6.934 9.85 11.48	.211 .453 .816 1.31 1.95 2.72 3.62 4.65 5.79 7.07 8.42	.373 .738 1.25 2.74 3.71 4.82 6.04 7.41 8.86 10.44	.196 .425 .775 1.26 1.37 2.52 3.51 4.52 5.54 5.59 8.23	.346 .694 1.19 1.84 2.64 3.58 4.67 5.37 7.22 8.65 10.21	
Ļ 3 SU	BSHELL								
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV				BARNS					
1.00 1.20 1.40 1.60 1.30 2.00 2.20 2.40 2.50 2.90 3.00	3.31 5.69 8.73 12.37 16.55 21.22 26.35 31.88 37.71 43.94 50.28	4.90 7.93 11.63 15.96 20.82 26.17 31.94 38.03 44.55 51.15 58.22	2.65 4.65 7.25 10.42 14.13 18.35 23.00 28.00 33.47 39.12 45.15	4.02 6.61 9.84 13.57 18.05 22.87 28.10 33.79 39.71 45.98 52.48	1.76 3.40 5.66 8.50 11.92 15.68 20.28 25.08 30.35 35.85 41.74	2.66 4.83 7.68 11.16 15.23 19.79 24.78 30.27 36.02 42.14 48.51	1.65 3.24 5.42 8.20 11.54 15.42 19.76 29.70 35.13 40.96	$\begin{array}{r} 2.50\\ 4.60\\ 7.36\\ 10.75\\ 14.75\\ 14.75\\ 24.14\\ 29.56\\ 35.24\\ 41.30\\ 47.61 \end{array}$	
TOTAL ECROSE L. CHELL TONICATION CROCE CROTTONS OUT AUTOMOTION									
FOR PROTON IMPACT									
	ENERGY TOTAL MeV BARNS			L1/L2	L	L1/L3		1	
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$			1.063 .721 .507 .275 .299 .256 .240 .241 .253 .279 .307	.147 .13 .109 .19 .082 .16 .082 .17 .084 .17 .048 .18 .048 .18 .046 .19 .048 .19		.138 .151 .162 .171 .175 .186 .195 .205 .209 .214		

## URANIUM(22=92)

ENERGY	۲ L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV			and the second	BARNS		Net and	
1.24	.0637 .109 .166 .235 .315 .405 .504 .504 .504 .504 .504 .504 .50	1.032 1.762 2.693 3.308 5.098 6.564 8.170 9.902 11.304 13.776 15.928 BETA1	.436 .743 1.138 1.619 2.180 2.330 3.561 4.361 5.251 5.201 7.247 BETR2	.0465 .0787 .121 .173 .236 .310 .396 .493 .502 .723 .858	.0465 .0273 .0787 .0504 .121 .0824 .173 .124 .236 .175 .310 .235 .396 .305 .493 .383 .602 .470 .723 .565 .858 .668		1.579 2.694 4.119 5.836 7.828 10.106 12.627 15.360 18.376 21.537 24.998
MeV		BAR	45			_	
	1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.4 2.2 3.0	.179 .314 .494 .720 .989 1.307 1.675 2.082 2.537 3.031 3.575	.257 .429 .644 .899 1.191 1.522 1.886 2.279 2.715 3.170 3.672	2.334 2.340 2.335 2.321 2.307 2.288 2.263 2.240 2.217 2.191 2.168	22.116 22.309 22.20 21.87 21.549 21.116 20.535 20.005 19.505 18.952 18.465	9.9.9.9.9.9.9.8.8.8.8.8.8.8.8.8.8.8.8.8	474 532 510 425 341 227 073 931 798 649 518

## PWBA L SHELL X-RAY PRODUCTION. CROSS SECTIONS

FOR PROTON IMPACT

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			2. 20 5
1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.	.0482 .0885 .141 .206 .283 .370 .467 .573 .688 .812 .942	.781 1.432 2.289 3.340 4.578 5.988 7.570 9.287 11.61 13.163 15.283	.333 .611 .980 1.440 1.993 2.633 3.363 4.179 5.078 6.062 7.119	.0361 .0659 .106 .158 .221 .297 .385 .487 .601 .730 .370	.0220 .0437 .0748 .116 .167 .227 .297 .378 .466 .563 .666	.0140 .0222 .0314 .0420 .0544 .0694 .0875 .109 .136 .167 .204	1.199 2.198 3.516 5.143 7.073 9.284 11.780 14.518 17.518 20.751 24.195
E	NERGY	BETA1	BETA2	LA/LB	LA/LG	LI	B/LG
P	1eV	BARI	NS				
1.00 1.14 1.60 1.20 1.60 1.00 1.60 1.60 1.00 1.60 1.00 1.0		.140 .265 .436 .927 1.247 1.615 2.036 2.499 3.012 3.564	.193 .346 .544 .784 1.065 1.386 1.748 2.143 2.580 3.049 3.554	2.312 2.314 2.305 2.289 2.267 2.243 2.292 2.192 2.168 2.142 2.142 2.113	21.572 21.656 21.466 21.115 20.606 20.076 19.568 18.963 18.463 17.943 17.467	9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.	331 360 314 224 090 949 813 651 517 377 249

# URANIUM(22=92)

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L SUBSHELL IONISATION CROSS SECTIONS FOR PROTON IMPACT

L 1 SUBSHELL									
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV				BARNS					
1.30 1.20 1.40 1.50 2.20 2.40 2.20 2.50 2.00 2.00 2.00 2.00 2.00 2.0	.418 .557 .670 .752 .311 .864 .934 1.03 1.20 1.43 1.78	.599 .711 .787 .945 .912 1.00 1.19 1.43 1.30 2.30 2.94	.374 .513 .627 .714 .773 .823 .877 .969 1.09 1.27 1.55	.355 .669 .749 .807 .859 .949 1.08 1.28 1.58 1.97 2.53	.212 .334 .446 .539 .611 .674 .737 .925 .954 1.13 1.39	.315 .435 .532 .610 .679 .776 .911 1.10 1.38 1.75 2.27	.198 .314 .424 .517 .589 .652 .715 .302 .931 1.10 1.36	.293 .410 .506 .584 .655 .751 .884 1.07 1.35 1.71 2.22	
L 2 SU	BSHELL								
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV				BARNS		-		194 M 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
1.00 1.20 1.40 1.60 2.20 2.20 2.40 2.20 2.40 2.80 3.00	294 .560 .933 .943 .943 .943 .955 .943 .555 .555 .68 .5557 .88 .5568 .8557 .88 .5568 .8557 .88 .5568 .8557 .88	.539 .943 1.48 2.14 2.85 4.89 5.23 5.23 8.99 7.52 8.99	.238 .459 .776 1.20 1.73 2.37 3.10 3.94 4.87 5.89 7.09	.447 .791 1.25 1.83 2.54 3.20 4.36 5.62 5.62 8.89	.139 .305 .561 .918 1.38 1.96 2.63 3.429 5.25 6.32	.261 .526 .995 1.41 2.03 2.73 3.62 4.58 5.63 5.63 6.79 8.02	.128 .285 .531 .376 1.33 1.89 2.54 3.31 4.17 5.12 5.16	.241 .492 .857 1.34 1.95 2.67 3.50 4.45 5.62 7.82	
L3SU	BSHELL								
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV				BARNS					
1.20 1.20 1.40 1.50 1.30 2.20 2.40 2.50 2.50 2.60 3.00	2.51 4.377 5.67 13.04 16.87 21.05 25.54 30.43 35.46 40.89	3.87 6.30 9.30 12.83 16.84 21.24 25.97 31.11 36.43 42.04 47.84	2.82 3.58 5.63 11.16 14.54 18.31 22.46 26.85 31.60 36.54	3.18 5.27 7.39 11.01 14.57 13.53 22.89 27.54 32.51 37.74 43.16	1.30 2.56 4.31 6.29 12.44 15.99 19.95 24.17 28.77 33.57	2.04 3.76 6.05 12.13 15.05 20.00 24.46 29.27 34.35 39.66	1.21 2.42 4.12 6.31 8.98 12.07 15.56 19.46 23.62 28.16 32.91	1.91 3.57 5.78 8.51 11.73 15.38 19.46 23.85 28.60 33.63 38.88	
TOTAL ECPSSR L SHELL IONISATION CROSS SECTIONS AND SUBSHELL RATIOS									
FOR PROTON IMPACT									
	ENERGY TOTAL MeV BARNS			L1/L2	L1/L3		L2/L:	L2/L3	
	1.00         2.45           1.20         4.47           1.40         7.14           1.60         10.44           1.80         14.33           2.00         13.80           2.20         23.84           2.40         29.37           2.60         35.42           2.30         41.96           3.00         48.93		1.216 .833 .591 .436 .231 .253 .240 .246 .258 .284	.153 .115 .088 .069 .056 .049 .045 .045 .045 .047 .047 .051 .051		.126 .138 .148 .158 .156 .174 .186 .192 .197 .291			
## C.2 DEUTERON IMPACT

## DYSPROSIUM(Z2=66)

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV		Ser Salar		BARNS	- 10T 3	Sel an	
1.0244600046000	.126 .206 .305 .554 .703 .864 1.838 1.223 1.417 1.621	3.003 4.912 7.251 10.035 13.213 16.750 20.608 24.756 29.165 33.813 38.677	1.609 2.547 3.684 5.856 6.698 3.589 10.715 13.074 15.659 18.472 21.506	.217 .329 .461 .622 .324 1.063 1.339 1.653 2.006 2.400 2.834	.153 .255 .384 .540 .725 .936 1.179 1.428 1.796 2.005 2.322	.0637 .0744 .0774 .0824 .0993 .128 .128 .169 .226 .300 .395 .512	4.932 7.957 11.654 16.055 21.182 26.967 33.354 40.309 47.800 55.805 64.295
Ε	NERGY	BETA1	BETR2	LA/LB	LA/LO	LB.	/LG
	MeY	BAR	NS				
	1.0 1.2 1.4 1.5 1.8 2.0 2.2 2.4 2.8 3.0	1.100 1.716 2.455 3.357 4.462 5.755 7.228 3.386 10.726 12.753 14.965	.508 .832 1.229 1.698 2.236 2.834 3.486 4.187 4.933 5.718 6.540	1.353 1.913 1.956 1.969 1.957 1.934 1.907 1.877 1.877 1.876 1.814 1.782	13.740 14.795 15.627 15.995 15.906 15.626 15.261 14.847 14.441 13.965 13.524	777788888777777	416 733 991 123 129 879 802 908 805 805 897

## PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR DEUTERON IMPACT

### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

NERGY	۲ <u>L</u>	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV			and the second	BARNS	No. Star	Sec. 3	1
1.02	.0892 .154 .236 .336 .453 .585 .731 .889 1.059 1.239 1.432	2.126 3.666 5.627 3.017 10.804 13.952 17.429 21.206 25.259 29.566 34.172	1.159 1.924 2.870 4.076 5.529 7.217 9.134 11.276 13.641 16.229 19.050	.158 .251 .360 .506 .686 .900 1.150 1.435 1.757 2.117 2.519	.110 .193 .300 .435 .597 .784 .995 1.228 1.483 1.758 2.052	.2481 .0582 .9603 .0704 .0888 .116 .155 .207 .274 .360 .465	3.516 5.967 9.048 12.671 17.384 22.538 28.295 34.625 41.496 48.891 56.867
8	ENERGY	BETA1	BETR2	LA/LB	LA/LG	LB.	LG
	MeV	BAR	NS				
	1.0 1.14 1.4 1.6 0.0 1.4 1.6 0.0 1.0 0.0 1.0 0.0 0.0 0.0 0.0 0.0 0.0	.799 1.304 1.917 2.719 3.701 4.856 6.185 7.689 9.368 11.228 13.271	.360 .621 .952 1.357 1.828 2.348 2.948 3.587 4.200 5.778	1.820 1.891 1.945 1.951 1.938 1.917 1.892 1.864 1.836 1.306 1.778	13.328 14.496 15.503 15.732 15.625 15.366 15.032 14.653 14.653 14.253 13.841 13.453	7.7.7.8.8.8.7.7.7.7.7.7.7.	324 668 969 063 062 016 945 359 765 .665

## DYSPROSIUM(Z2=66)

L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

L1S	UBSHELL	4						
ENERGY	PNBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS	1. 1. 1. 1.	1.2.2.2.2.9		100
1.00 1.20 1.40 1.60 1.30 2.20 2.20 2.40 2.60 2.80 3.00	3.38 3.92 4.26 5.11 6.57 8.72 11.69 15.62 29.63 26.83	3.70 4.09 4.09 4.75 6.05 8.05 10.88 14.70 19.64 25.31 33.27	3.01 3.58 3.74 3.63 4.45 5.52 7.11 9.30 12.20 15.95 20.66	3.35 3.78 3.79 5.16 5.65 8.75 11.59 15.30 20.00 25.80	2.35 2.97 3.40 4.02 5.06 5.70 11.51 15.14 19.71	$\begin{array}{c} 2.62\\ 3.14\\ 3.21\\ 3.76\\ 6.10\\ 8.12\\ 10.85\\ 14.43\\ 18.98\\ 24.62 \end{array}$	2.29 2.90 3.16 3.36 4.99 6.51 8.61 11.39 15.30 19.54	2.55 3.15 3.159 4.591 6.02 10.73 14.20 14.20 24.39
L 2 5	UBSHELL							
ENERGY	PNBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV	1.1.98			BARNS				
1.00 1.20 1.40 1.50 1.30 2.00 2.20 2.40 2.60 2.60 2.30 3.00	5.09 8.80 13.59 19.40 26.15 33.76 42.13 51.20 60.87 71.10 81.80	6.31 10.57 15.95 22.36 29.72 37.92 46.87 56.50 66.71 77.45 88.65	3.74 6.65 10.50 15.27 20.92 27.40 34.63 42.56 51.12 60.26 69.91	4.73 8.11 12.48 17.80 24.01 31.04 38.83 47.29 56.38 66.01 76.15	2.97 5.58 9.14 13.63 19.03 25.27 32.29 40.02 40.02 40.41 57.39 66.90	3.75 6.81 19.86 15.89 21.84 28.63 36.20 44.47 53.39 62.38 72.98	2.88 5.44 8.94 13.37 18.71 24.89 31.85 39.52 47.85 56.24	3.64 6.63 19.62 15.47 23.20 25.70 43.27 52.20 52.20 52.16
L 3 S	UBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.50 2.00 2.20 2.40 2.60 2.80 3.00	19.14 31.76 47.44 65.90 36.83 109.94 134.95 161.60 189.67 218.97 249.31	22.93 37.04 54.26 96.68 121.22 147.60 175.55 204.85 235.30 266.73	14.06 24.02 36.75 52.10 69.85 89.77 111.64 135.25 160.40 186.91 215.07	17.12 28.40 42.53 59.29 78.44 99.73 122.92 147.80 174.16 201.82 231.09	11.40 20.48 32.39 46.99 63.40 104.75 127.90 152.65 178.82 206.67	13.88 24.22 37.48 53.47 71.95 92.65 115.33 139.77 165.75 193.08 222.07	11.08 20.00 31.75 46.18 63.09 82.25 103.45 126.45 151.06 177.08 204.80	13.49 23.65 36.74 52.55 91.38 1138.18 138.18 164.01 191.21 220.06
	TUTAL ECA	SOK L SH	FOR	DEUTERON	S SECTION	NS AND SUI	SHELL RAT	TIOS
	ENERGY MeV		TOTAL BARNS	L1/L2		L1/L3	L2/1	.3
	1.00 1.20 1.40 1.60 1.60 2.40 2.40 2.40 2.60 2.40 2.60 2.60 2.60 2.60 2.60 2.60 2.60 2.6		19.68 33.35 50.51 71.79 96.91 125.59 157.62 192.83 231.07 272.21 316.61	.701 .462 .297 .234 .214 .213 .225 .244 .270 .338		.189 .130 .086 .069 .065 .066 .070 .070 .078 .087 .098 .098	.27 .28 .22 .30 .30 .30 .31 .31 .33	70 309 377 309 309 309 309 309 309 309 309 309 309

## YTTERBIUM(22=70)

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		State States	Sec. 1
1.02446800446880 1.1.1.1.02246880	.0793 .133 .202 .283 .378 .485 .603 .731 .868 1.014 1.168	1.801 3.027 4.581 6.436 8.587 11.020 13.708 16.626 19.754 23.075 26.570	.982 1.587 2.338 3.218 4.258 5.487 6.891 8.455 10.179 12.057 14.089	.138 .213 .303 .405 .526 .676 .852 1.053 1.280 1.532 1.811	.0885 .151 .233 .333 .451 .590 .748 .923 1.114 1.321 1.542	.8496 .0619 .8793 .0718 .0746 .0854 .104 .165 .210 .267	2.988 4.938 7.390 10.294 13.584 17.581 21.946 25.731 31.919 37.487 43.413
Ξ	NERGY	BETA1	BETR2	LA/LB	LA/LG	Li	B/LG
	MeV	BAR	NS				
	1.0 1.2 1.4 1.5 2.2 2.2 2.2 2.2 2.0 3.0	.674 1.070 1.556 2.120 2.793 3.606 4.552 5.619 6.309 8.122 9.558	.308 .517 .782 1.099 1.466 1.880 2.339 2.836 3.370 3.936 4.531	1.821 1.894 1.945 1.985 2.001 1.993 1.974 1.951 1.925 1.898 1.870	12.947 14.099 14.998 15.736 16.191 16.172 15.954 15.637 15.309 14.937 14.551	7.7.7.7.8.8.8.8.7.7.7.	109 443 712 953 091 116 087 954 .871 .782

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## PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR DEUTERON IMPACT

### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	' L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		See and	a garden
1.924	.0564 .100 .158 .228 .311 .407 .514 .631 .757 .893 1.036	1.282 2.279 3.583 5.180 7.077 9.252 11.683 14.347 17.229 20.309 23.574	.713 1.212 1.844 2.506 3.552 4.568 5.947 7.386 8.977 10.724 12.523	.102 .164 .240 .328 .443 .581 .744 .930 1.139 1.375 1.635	.0645 .116 .185 .271 .377 .502 .645 .805 .981 1.173 1.379	.0371 .0481 .0548 .0569 .0653 .0788 .0981 .124 .158 .201 .256	2.144 3.739 5.798 8.303 11.328 14.835 16.793 23.177 27.960 33.130 38.669
E	INERGY	BETA1	BETA2	LA/LB	LA/LG	L	3/LG
	MeV	BAR	NS				
	1.0 1.1.4 1.4 1.6 0.0 0 0.0 0 0.0 0 0.0 0 0 0 0 0 0 0 0	.494 .823 1.232 2.344 3.089 3.954 4.939 6.039 7.261 8.603	.219 .389 .612 .384 1.208 1.579 1.993 2.447 2.939 3.463 4.020	1.784 1.867 1.928 1.973 1.977 1.967 1.949 1.927 1.903 1.878 1.852	12.532 13.776 14.820 15.655 15.855 15.791 15.585 15.305 14.995 14.650 14.292	7.5.7.8887.5.7.7.	023 379 585 937 020 929 944 379 302 719

### YTTERBIUM(Z2=70)

L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

L 1	SL	BSI	HE	LL
-----	----	-----	----	----

ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV		aver store		BARNS			N. W.	
1.20 1.20 1.40 1.60 1.30 2.20 2.40 2.50 2.50 3.00	2.10 2.95 2.99 3.08 3.51 4.26 5.33 6.73 8.67 11.06	2.45 2.87 3.03 3.43 4.17 5.25 8.71 11.21 14.33	1.84 2.35 2.71 2.79 2.84 3.16 3.72 4.53 5.61 7.82 8.81	2.20 2.63 2.82 2.81 3.11 3.67 4.50 5.62 7.09 8.98 11.34	1.36 1.37 2.26 2.40 2.51 2.85 3.39 4.17 5.22 6.58 8.32	1.62 2.09 2.35 2.42 2.30 4.10 5.60 8.42 10.71	$\begin{array}{c} 1.31\\ 1.82\\ 2.21\\ 2.36\\ 2.36\\ 2.36\\ 3.35\\ 4.12\\ 5.16\\ 5.51\\ 8.23\end{array}$	1.57 2.03 2.30 2.37 2.70 3.25 4.04 5.12 6.52 8.33 10.60
L 2 SL	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV	•			BARNS	1	-1.4.5		
1.00 1.20 1.40 1.60 2.00 2.20 2.20 2.20 2.20 2.20 2.50 2.5	2.22 3.98 6.33 9.28 12.78 16.81 21.34 26.31 31.70 37.46 43.56	2.94 5.07 7.83 11.20 15.14 19.62 24.58 29.99 35.80 41.97 48.47	1.64 3.01 4.88 7.28 10.19 13.59 17.45 21.75 26.46 31.55 36.99	2.22 3.90 6.13 8.91 12.22 16.03 29.30 25.02 30.13 35.62 41.44	1.23 2.42 4.12 6.33 9.06 12.30 16.01 20.17 24.75 29.71 35.04	1.67 3.15 5.17 7.75 10.87 14.51 18.63 23.19 28.19 28.19 23.54 39.26	1.19 2.35 4.01 5.89 12.89 12.75 19.84 15.87 24.34 34.64	1.61 3.05 5.04 7.58 10.66 14.25 18.33 22.36 27.30 33.13 38.81
L3SL	JBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.50 2.00 2.20 2.40 2.60 2.80 3.00	9.48 16.19 24.77 35.11 47.07 60.48 75.20 91.08 108.00 125.84 144.48	11.96 19.75 29.48 40.99 54.65 84.47 101.42 119.36 138.17 157.73	6.96 12.22 19.13 27.65 37.68 49.12 61.86 75.79 90.78 106.74 123.57	8.96 15.16 23.89 32.67 43.78 56.29 70.88 85.83 101.81 117.93 135.67	5.40 10.07 16.41 24.39 33.93 44.92 57.25 70.81 85.48 101.15 117.73	6.95 12.49 19.81 28.82 39.41 51.47 64.85 79.44 95.11 111.75 129.25	5.22 9.80 16.84 23.90 33.21 56.43 69.88 84.45 180.82 116.50	6.72 12.16 19.36 28.25 38.72 50.66 63.93 78.40 93.97 110.50 127.91
1	TOTAL ECP	SSR L SHE	ILL IONISF FOR	TION CROSS	SECTION	IS AND SUE	SHELL RAT	105
	ENERGY		TOTAL	L1/L2		L1/L3	L2/L	3
	Me'V		BARNS					
	1.20 2.240 2.240 2.240 2.240 2.240 2.240 2.240 2.20 2.2		9.90 17.24 26.70 38.20 52.08 68.16 86.30 106.37 128.29 151.36 177.31	.975 .666 .456 .213 .228 .221 .224 .225 .251 .273		.234 .157 .119 .084 .063 .065 .065 .065 .069 .075 .083		010051729603

### TUNGSTEN(Z2=74)

ENERGY	' L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.0211.463024680	.0501 .0866 .134 .192 .260 .338 .425 .521 .624 .735 .852	1.077 1.362 2.386 4.138 5.601 7.271 9.146 11.284 13.433 15.619 18.346	*.601 .994 1.491 2.090 2.774 3.564 4.491 5.537 6.699 7.972 9.352	.0908 .143 .206 .279 .359 .452 .567 .700 .350 1.019 1.206	.0496 .0874 .138 .202 .279 .368 .472 .589 .719 .861 1.014	.0412 .0555 .0676 .0770 .0804 .0840 .0944 .110 .131 .158 .192	1.812 3.873 4.697 5.671 8.956 11.574 14.563 17.879 21.506 25.424 29.614
E	NERGY	BETR1	BETR2	LAZLB	LA/LO	LI	B∕LG
	MeV	BAR	4S				
	1.0 1.2 1.4 1.6 1.8 2.0 2.2 2.4 2.8 3.0	.329 .554 .845 1.201 1.616 2.101 2.672 3.321 4.044 4.340 5.704	.197 .340 .527 .755 1.822 1.327 1.669 2.844 2.450 2.885 3.346	1.779 1.860 1.922 1.966 2.005 2.026 2.029 1.990 1.990 1.969 1.947	11.778 12.942 13.932 14.724 15.489 15.962 16.018 15.897 15.678 15.403 15.096	6.67.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.	621 957 248 490 .724 .880 .923 .915 .877 .821 .755

## PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS FOR DEUTERON IMPACT

### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	· L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV	B. IN PASS		A PARTY AND	BARNS	SALES CALLER T		Ale -
1.0211.4680044680	.0361 .0661 .107 .157 .217 .287 .367 .455 .550 .653 .764	.776 1.422 2.291 3.375 4.672 6.182 7.891 9.784 11.847 14.069 16.440	.443 .773 1.201 1.714 2.332 3.076 3.939 4.917 6.004 7.202 8.507	.06778 .112 .167 .228 .302 .395 .504 .630 .773 .933 1.111	.0369 .0687 .113 .168 .237 .320 .416 .525 .645 .778 .922	.0309 .0434 .0541 .0600 .0651 .0748 .0661 .106 .128 .128 .189	1.318 2.364 3.750 5.451 7.491 9.896 12.643 15.714 19.084 22.749 26.693
E	INERGY	BETA1	BETR2	LA/LB	LA/LG	L	B/LG
	MeV	BAR	NS				
	1.0 1.2 1.4 1.6 1.8 0 2.2 2 2.2 2 2 2 2 3.0	.245 .435 .687 .994 1.370 1.826 2.965 2.965 2.965 3.641 4.339 5.207	.142 .260 .418 .616 .853 1.128 1.439 1.735 2.161 2.566 2.998	1.738 1.828 1.895 1.956 1.989 1.989 1.985 1.985 1.975 1.958 1.939 1.917	11.367 12.594 13.637 14.672 15.337 15.548 15.548 15.548 15.408 15.408 15.208 14.957 14.679	8.87.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.	.539 .198 .501 .709 .793 .816 .802 .767 .716 .655

# TUNGSTEN(Z2=74)

L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

L 1 SUI	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV		North I		BARNS		12.5		
1.00 1.20 1.40 1.50 1.30 2.00 2.20 2.40 2.60 2.80 3.00	1.25 1.66 1.99 2.22 2.25 2.27 2.49 2.86 3.39 4.10 5.01	1.59 1.96 2.21 2.25 2.52 2.52 2.53 3.52 4.31 5.33 6.60	1.08 1.47 1.80 2.04 2.11 2.14 2.31 2.60 3.01 3.54 4.22	1.40 1.77 2.01 2.15 2.35 2.35 2.35 2.45 3.45	.746 1.11 1.44 1.71 1.82 1.88 2.07 2.36 2.75 3.27 3.93	.974 1.34 1.63 1.76 1.35 2.06 2.39 2.83 3.41 4.15 5.08	.718 1.08 1.40 1.67 1.65 2.03 2.23 2.33 3.89	.936 1.30 1.59 1.72 1.81 2.03 2.35 2.79 3.36 4.10 5.02
L 2 SU	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV	The last	1000		BARNS	VERNE			
1.00 1.20 1.40 1.60 1.30 2.20 2.40 2.40 2.30 3.00	.957 1.78 2.92 4.39 5.19 8.30 10.72 13.42 15.39 19.51 23.06	1.38 2.44 3.85 5.62 7.73 10.16 12.91 15.94 19.24 22.78 26.54	.710 1.35 2.25 3.44 4.92 6.69 8.73 11.05 13.62 16.44 19.48	1.05 1.89 3.83 4.48 6.24 8.30 19.65 13.27 16.15 19.27 22.62	.503 1.04 1.83 2.90 4.27 5.92 7.86 10.08 12.55 15.28 15.28 18.24	.744 1.45 2.46 3.78 5.41 7.35 9.59 12.10 14.38 17.91 21.17	.482 1.00 1.78 2.83 4.17 5.80 7.72 9.91 12.06 17.99	.712 1.40 2.39 3.68 5.29 7.20 9.41 11.90 14.65 17.65 20.89
L 3 SUI	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 2.00 2.20 2.40 2.60 2.60 2.00 2.60 2.00	4.71 8.28 12.99 13.79 25.63 33.43 42.12 51.61 61.84 72.74 84.23	6.33 10.68 16.22 22.90 30.63 39.32 48.89 59.24 70.30 82.00 94.27	3.46 6.25 10.01 14.75 20.44 27.04 34.49 42.74 51.72 61.37 71.65	4.77 8.22 12.72 18.25 24.18 40.46 49.52 59.29 69.76 80.76	2.55 4.95 8.33 12.69 18.02 24.28 31.42 39.38 48.10 57.52 67.58	3.51 6.51 10.58 15.69 21.82 28.89 36.85 45.63 55.15 65.35 76.18	2.46 4.80 8.11 12.40 17.66 23.31 38.79 47.44 56.78 66.78	3.38 5.31 19.39 15.38 28.37 36.35 36.35 54.39 54.52 64.52 64.52
T				TTON CROSS	SECTION			100
			FOR	DEUTERON 1	IMPACT	5 HHD 50D	SHELL KHI	105
	ENERGY MeV		TOTAL BARNS	L1/L2		L1/L3	L2/L	.3
	1.00 1.20 1.40 1.60 1.30 2.20 2.40 2.60 2.80 3.00		5.03 9.01 14.28 20.74 28.49 37.60 48.01 59.63 72.41 86.27 01.13	1.315 .926 .666 .467 .343 .281 .250 .234 .239 .239 .239		.277 .296 .154 .112 .085 .071 .065 .062 .062 .062 .064	.21 .22 .22 .22 .22 .22 .22 .22 .22 .22	19297495949

### GOLD(Z2=79)

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		- 200	
1.021.1.6500.246000	.8382 .8535 .8843 .123 .169 .222 .282 .348 .421 .499 .584	.600 1.064 1.675 2.437 3.351 4.495 5.598 6.929 8.365 9.924 11.609	.290 .506 .788 1.139 1.563 2.055 2.618 3.246 3.945 4.795 5.549	.0398 .0675 .102 .145 .197 .257 .325 .402 .489 .584 .693	.8223 .9429 .9686 .193 .147 .198 .258 .326 .493 .488 .581	.0179 .0255 .0339 .0420 .0583 .0584 .0669 .0757 .0856 .0960 .111	.960 1.691 2.650 3.845 5.279 8.939 8.822 18.917 13.221 15.713 18.435
	ENERGY MeV	L	A/LB	LA/LG	LB/LI	3	
	1.004 1.14 1.0000 1.000 1.14 0.000 1.14 0.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.000000 1.0000 1.0000 1.0000 1.0000 1.00000 1.00000 1.00000 1.00000000	20000000000000000000000000000000000000	.068 .101 .126 .139 .144 .144 .138 .132 .120 .109 .092	15.052 15.753 16.348 16.763 17.019 17.161 17.202 17.196 17.094 16.983 16.748	7.27 7.49 7.69 7.93 8.00 8.04 8.06 8.06 8.05 8.05 8.05	77 66 75 4 7 22 5	

# PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

### FOR DEUTERON IMPACT

ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS	+	-	
1.0 1.2 1.4 1.6 1.2 1.6 1.0 2.0 2.4 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0	.0224 .0419 .0687 .103 .144 .193 .248 .310 .378 .453 .534	.444 .832 1.365 2.046 2.872 3.839 4.940 6.166 7.523 9.012 10.614	.220 .404 .554 .972 1.364 1.824 2.349 2.939 3.682 4.348 5.161	.0309 .0547 .0861 .125 .174 .231 .296 .369 .453 .549 .655	.0177 .0345 .0584 .0901 .131 .179 .236 .300 .373 .455 .545	.0131 .0202 .0276 .0353 .0435 .0518 .0602 .0684 .0789 .0931 .109	.718 1.333 2.174 3.247 4.555 6.087 7.833 9.784 11.957 14.363 16.964
	ENERGY MeV	,	LA/LB	LA/LO	LB/L	3	
	1.14.60004.6000 1.14.60004.6000		2.017 2.058 2.058 2.105 2.105 2.105 2.105 2.103 2.098 2.098 2.073 2.056	14.393 15.206 15.360 16.314 16.478 16.609 16.690 16.706 16.625 15.423 16.204	7.13 7.38 7.59 7.59 7.52 7.89 7.96 7.96 7.96 7.96 7.96		

GOLD(Z2=79)

L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

L 1 SUBS	HELL
----------	------

ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV				BARNS	11000				
1.00 1.20 1.40 1.50 2.00 2.20 2.40 2.50 2.50 2.50 3.00	.619 .897 1.14 1.34 1.51 1.64 1.75 1.84 1.94 2.03 2.29	.907 1.17 1.38 1.55 1.68 1.79 1.89 1.99 2.18 2.52 2.94	.529 .773 1.01 1.21 1.38 1.54 1.68 1.79 1.86 1.91 2.10	.795 1.04 1.25 1.43 1.60 1.74 1.83 1.89 2.03 2.28 2.60	.334 .548 .762 .964 1.14 1.30 1.46 1.58 1.66 1.73 1.92	.501 .733 .949 1.14 1.32 1.47 1.59 1.67 1.81 2.07 2.38	.318 .527 .738 .935 1.11 1.28 1.43 1.55 1.64 1.70 1.89	.478 .706 .919 1.11 1.29 1.44 1.56 1.64 1.64 1.78 2.04 2.35	
L 2 SU	BSHELL								
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV	1.11			BARNS					
1.00 1.20 1.40 1.60 1.30 2.00 2.40 2.60 2.60 2.80 3.00	.333 .546 1.10 1.71 2.48 3.41 4.50 5.74 7.14 8.636 10.36	.547 .993 1.61 2.40 3.36 4.51 5.81 7.29 8.91 10.68 12.59	.249 .492 .852 1.34 1.97 2.74 3.66 4.71 5.91 7.24 8.71	.422 .777 1.27 2.73 3.69 4.80 6.07 7.48 9.02 10.70	.161 .353 .655 1.68 1.64 2.35 3.29 4.19 5.33 6.69 8.01	.273 .558 .980 1.55 2.28 3.16 4.20 5.40 6.74 8.22 9.34	.153 .339 .632 1.05 1.60 2.29 3.13 4.11 5.23 6.49 7.38	.259 .535 .945 1.50 2.22 3.09 4.11 5.29 6.61 8.08 9.69	
L 3 SU	BSHELL							•	
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR	
MeV				BARNS					
1.00 1.20 1.40 1.60 2.20 2.40 2.40 2.60 2.30 3.00	2.00 3.65 5.89 8.73 12.17 16.17 20.71 25.76 31.27 37.22 43.56	2.96 5.11 7.92 11.37 15.44 20.09 25.28 30.98 32.98 33.98 37.13 43.70 50.65	1.48 2.75 4.54 6.84 9.58 13.04 16.89 21.23 26.89 31.23 36.85	2.25 3.95 6.28 9.08 12.44 20.98 15.44 25.24 25.24 37.25 43.25	1.01 2.06 3.61 5.67 8.27 11.40 15.04 19.18 23.78 28.81 34.26	1.54 2.96 4.95 7.53 10.67 14.38 18.61 23.34 28.54 34.18 40.22	.966 1.99 3.50 5.52 8.08 11.16 14.76 18.84 23.39 28.39 33.79	1.47 2.35 4.80 7.33 10.42 14.07 13.25 22.93 28.08 33.57 39.66	
TOTAL ECPSSR L SHELL IONISATION CROSS SECTIONS AND SUBSHELL RATIOS FOR DEUTERON IMPACT									
	ENERGY MeV	ļ	OTAL ARNS	L1/L2	L	.1/L3	L2/L	3	
	1.00 1.40 1.40 1.60 2.00 2.40 2.00 2.40 2.00 2.00 2.00 2.0	11100000 9 00	2.21 4.10 9.94 3.93 8.60 23.92 29.64 29.64 29.64 29.64 29.64 29.64 29.64 29.64 29.64 29.64 29.64 29.64 29.64 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21 20.21	1.846 1.320 .972 .739 .582 .467 .378 .310 .270 .252 .242		325 247 191 152 124 102 065 071 060 059	.176 .187 .205 .213 .219 .225 .231 .236 .240 .240		

## LEAD(22=82)

E

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV		1. 10-2		BARNS		1. 1. 10	1
1.0211.441.6802144680	.0215 .0387 .0621 .0916 .127 .169 .216 .268 .327 .390 .459	.408 .734 1.178 1.738 2.417 3.206 4.099 5.093 6.198 7.405 8.704	.191 .339 .540 .794 1.101 1.462 1.872 2.330 2.850 3.428 4.060	.8257 .9443 .0691 .0999 .137 .180 .229 .284 .347 .419 .499	.0138 .0250 .0435 .0668 .0960 .132 .174 .227 .339 .407	.0113 .0133 .0255 .0331 .0409 .0405 .0553 .0519 .0704 .0808 .0927	.646 1.156 2.723 3.733 5.016 6.416 7.7243 9.7243 11.6722 11.6722
	ENER Mev	RGY /	LAZLB	LA/LG	LB/I	LG	
	1.9 1.4 1.4 1.0 2.0 2.0 2.0 2.0 0.0 0.0 0.0 0.0 0.0 0		2.136 2.154 2.159 2.190 2.195 2.193 2.190 2.196 2.174 2.160 2.144	15.884 16.553 17.060 17.397 17.654 17.789 17.890 17.951 17.842 17.658 17.430	7.4 7.6 7.8 7.8 8 .1 8 .2 1 8 .1	35 49 19 44 44 44 59 11 25 75 31	

# PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR DEUTERON IMPACT

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

NERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		•	
1.0 1.2 1.4 1.6 2.2 2.4 2.2 2.2 2.8 3.0	.0162 .0312 .0518 .0786 .111 .150 .194 .299 .360 .426	.308 .591 .984 1.491 2.110 2.837 3.677 4.624 5.679 6.833 8.078	.148 .280 .461 .695 .981 1.316 1.711 2.159 2.669 3.231 3.845	.0204 .0373 .0601 .0889 .124 .164 .213 .268 .332 .404 .483	.0111 .0222 .0385 .0605 .0885 .123 .164 .210 .265 .325 .391	9.31E-03 .0151 .0216 .0284 .0355 .0417 .0492 .0577 .0676 .0788 .0913	.493 .939 1.556 2.354 3.327 4.468 5.795 7.295 7.295 8.980 10.829 12.831
	ENERGY MeV		LAZLB	LA/LG	LB/	LG	
	1.02 1.14 1.68 2.24 2.24 2.20 2.24 2.20 2.20 2.20 2.20		2.081 2.115 2.134 2.146 2.151 2.156 2.148 2.148 2.142 2.128 2.115 2.101	15.114 15.868 16.376 17.023 17.265 17.269 17.248 17.248 17.931 16.741	7777778888888999	63 01 75 74 14 09 38 53 31 04 63	

LEAD(22=82)

L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

L 1 SUBSHELL	IELL
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ENERGY	PWBR	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS		Service and		
1.00 1.20 1.40 1.60 1.30 2.00 2.20 2.40 2.50 2.50 2.80 3.00	.397 .591 .738 .971 1.13 1.25 1.31 1.33 1.39 1.49 1.62	.633 .348 1.04 1.20 1.31 1.32 1.37 1.47 1.60 1.73 2.00	.339 .511 .691 .363 1.02 1.15 1.24 1.30 1.36 1.45 1.55	.555 .753 .936 1.89 1.22 1.28 1.35 1.44 1.55 1.68 1.35	.200 .342 .502 .665 .819 .955 1.05 1.12 1.20 1.30 1.40	.328 .584 .680 .980 1.06 1.15 1.36 1.50 1.67	.190 .328 .484 .545 .797 .932 1.03 1.10 1.18 1.27 1.38	.311 .483 .636 .954 1.03 1.12 1.22 1.34 1.48 1.64
L 2 SU	BSHELL							
ENERGY	PWBR	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.50 2.00 2.20 2.40 2.60 2.80 3.00	.175 .348 .606 .958 1.41 1.97 2.64 3.41 4.29 5.27 6.35	.316 .582 .954 1.44 2.76 3.60 4.55 5.61 6.77 8.03	.132 .267 .471 .755 1.13 1.59 2.15 2.80 3.55 4.39 5.33	.246 .459 .761 1.16 1.66 2.27 2.98 3.79 4.71 5.72 6.83	.08 .182 .348 .590 .916 1.33 1.84 2.45 3.95 4.84	.149 .314 .907 1.35 1.90 2.56 3.32 4.18 5.15 6.21	.0756 .174 .335 .570 .888 1.30 1.80 2.39 3.09 3.87 4.75	.141 .299 .541 .876 1.31 1.85 2.50 3.24 4.10 5.05 6.10
L 3 SU	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 2.00 2.20 2.40 2.60 2.80 3.00	1.20 2.23 3.67 5.52 7.80 10.48 13.56 17.01 20.82 24.96 29.40	1.90 3.32 5.20 7.54 10.33 13.54 17.16 21.16 25.51 30.13 35.15	.890 1.69 2.83 4.33 6.20 8.44 11.04 13.99 17.28 20.89 24.80	1.45 2.58 4.10 6.03 8.36 11.09 14.19 17.65 21.44 25.56 29.97	.579 1.222 2.18 3.50 5.19 7.25 9.647 15.60 19.07 22.84	.945 1.86 3.17 4.88 7.80 9.53 12.44 15.736 23.33 27.60	.551 1.17 2.11 3.40 5.05 7.08 9.48 12.23 15.33 18.76 22.50	.899 1.79 3.06 4.74 6.82 9.31 12.18 15.42 19.82 22.95 27.18

TOTAL ECPSSR L SHELL IONISATION CROSS SECTIONS AND SUBSHELL RATIOS FOR DEUTERON IMPACT

ENERGY MeV	TOTAL BARNS	L1/L2	L1/L3	L2./L3
1.00 1.20 1.40 1.50 2.00 2.20 2.40 2.60 2.30 3.00	1.35 2.57 4.26 6.43 9.89 12.19 15.89 19.89 24.45 29.47 34.92	2.205 1.613 1.214 .932 .727 .559 .450 .377 .327 .293 .269	.345 .270 .214 .172 .140 .111 .092 .079 .079 .070 .064 .060	.157 .167 .185 .192 .199 .205 .215 .220 .224

## BISMUTH(Z2=83)

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		Capit Grates	
1.0 1.2 1.4 1.5 2.2 2.4 2.6 3.0 3.0	.0176 .0324 .0530 .0791 .111 .149 .192 .240 .293 .350 .413	.330 .606 .990 1.479 2.082 2.781 3.587 4.477 5.477 5.546 7.727	.153 .278 .450 .669 .940 1.259 1.624 2.039 2.507 3.015 3.579	.0192 .0340 .0543 .0801 .112 .150 .192 .243 .299 .362 .431	.0107 .0204 .0348 .0542 .0791 .110 .146 .188 .237 .291 .351	3.52E-03 .0136 .0195 .0259 .0326 .0396 .0396 .0467 .0541 .0622 .0709 .0804	.520 .951 1.547 2.307 3.245 4.338 5.595 6.999 8.578 10.273 12.151
	ENER	RGY	LA/LB	LA/LG	LB/1	LG	
	1.92 1.4 1.4 1.6 1.9 2.9 2.9 2.9 2.9 2.9 2.9 2.9 2.9 2.9 2		2.150 2.181 2.201 2.209 2.215 2.209 2.209 2.208 2.196 2.195 2.171 2.159	17.198 17.318 18.244 18.458 18.639 18.590 18.634 18.459 18.303 18.101 17.914	9.00 9.11 9.334 9.44 9.35 9.44 9.35 9.65 9.65 9.65 9.65 9.65 9.65 9.65 9.6	20 58 58 57 15 17 38 37 38 37 36 37	

## PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR DEUTERON IMPACT

### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV		-		BARNS		and the second	
1.0 1.2 1.4 1.6 2.2 2.4 2.2 2.2 2.3 2.3 2.3 2.3 3	.0136 .0256 .0449 .0687 .0983 .133 .173 .218 .269 .324 .385	.254 .497 .839 1.284 1.337 2.486 3.243 4.083 5.031 6.062 7.188	.121 .234 .391 .595 .849 1.147 1.499 1.898 2.347 2.845 3.395	.0156 .0294 .0484 .0729 .103 .139 .181 .230 .236 .348 .417	8.72E-03 .0178 .0315 .0502 .0743 .104 .139 .181 .228 .281 .341	6.88E-03 .0115 .0228 .0289 .0353 .0421 .0495 .0575 .0665 .0767	.405 .324 2.021 2.087 3.905 5.097 6.429 7.933 9.579 11.305
	ENER Mev	164 1	LA/LB	LAZLG	LB/L	G	
			2.091 2.126 2.146 2.157 2.155 2.165 2.165 2.163 2.152 2.143 2.131 2.117	16.285 16.925 17.335 17.606 17.811 17.887 17.876 17.726 17.616 17.616 17.227	7.78 7.96 8.07 8.122 8.25 8.25 8.23 8.23 8.21 8.13	719267599907	

L SUBSHELL IONISATION CROSS SECTIONS FOR DEUTERON IMPACT

L 1 SU	BSHELL							
ENERGY	PNBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.50 2.20 2.20 2.20 2.20 2.20 2.20 2.20 2	.318 .486 .664 .332 .981 1.11 1.21 1.28 1.35 1.41 1.47	.534 .728 .996 1.06 1.18 1.27 1.34 1.40 1.47 1.56 1.67	.270 .419 .581 .741 .890 1.02 1.12 1.21 1.27 1.38 1.38	.470 .632 .972 1.09 1.19 1.27 1.33 1.39 1.46 1.55	.155 .275 .416 .564 .708 .948 1.04 1.12 1.18 1.25	.271 .429 .591 .740 .980 1.07 1.14 1.21 1.29 1.39	.147 .263 .401 .546 .688 .319 .926 1.02 1.10 1.16 1.22	.256 .410 .569 .717 .345 .955 1.04 1.12 1.19 1.27 1.37
L 2 SL	BSHELL							
ENERGY	PWBR	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				1.1.2
1.00 1.20 1.40 1.60 2.00 2.20 2.40 2.60 2.60 2.60 3.00	.129 .261 .462 .743 1.11 1.57 2.11 2.76 3.50 4.32 5.24	.243 .455 .755 1.15 2.956 2.96 3.66 5.67 4.66 5.67	.2969 .200 .359 .584 .881 1.26 1.71 2.88 3.60 4.38	.190 .359 .602 .929 1.34 1.84 2.45 3.91 4.78 5.74	.0575 .134 .262 .451 .710 1.04 1.46 1.96 2.54 3.22 3.96	.113 .241 .439 .718 1.88 1.53 2.89 2.72 3.46 4.27 5.19	.0541 .128 .251 .435 .588 1.02 1.42 1.92 2.49 3.16 3.89	.106 .229 .422 .693 1.05 1.49 2.03 2.56 3.38 4.19 5.09
L 3 SU	BSHELL							
ENERGY	РИВН	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
nev 1. oo				BARNS			1.	
1.20 1.40 1.50 1.30 2.20 2.40 2.40 2.60 2.60 2.60 2.60 2.60 2.60 2.60 2.6	1.78 2.954 6.50 8.79 11.46 14.43 17.77 21.34 25.29	2.73 4.33 6.36 8.77 11.58 14.70 18.23 22.02 26.16 30.51	.635 1.35 2.29 3.55 5.14 7.07 9.29 11.88 14.69 17.86 21.24	1.18 2.13 3.42 5.07 7.09 9.44 12.17 15.16 18.50 22.11 26.02	.444 .959 1.75 2.85 4.27 6.03 8.10 10.53 13.20 16.24 19.50	.753 1.51 2.61 4.07 5.89 8.06 10.61 13.44 16.63 29.10 23.88	.422 .920 1.69 2.76 4.16 5.93 10.32 12.96 15.96 19.19	.715 1.45 2.52 3.94 5.74 7.38 13.17 16.33 19.76 23.50
		SOR L SHEL	FOR D	EUTERON I	MPACT	AND SUBS	HELL RATI	:05
	ENERGY MeV	I	OTAL ARNS	L1/L2	- L	1/L3	L2/L3	
	1.00 1.20 1.40 1.50 2.00 2.20 2.60 2.60 2.60 2.60 2.60 5.00		1.08 2.09 3.51 5.35 9.31 3.46 6.95 9.90 25.22 9.97	2.419 1.798 1.350 1.034 .641 .513 .421 .304 .269		358 283 226 182 147 121 101 085 973 964 958	.148 .158 .167 .176 .182 .199 .196 .202 .207 .212 .217	

500

YTTERBIUM(22=70)

			FOI	R ALPHA IMP	ACT		
ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS		1	
1.02 1.24 1.30 2.24 5.00 2.45 2.02 2.20 2.00 3.00 3.00 3.00 3.00 3.00	.0334 .0634 .106 .164 .236 .323 .425 .542 .542 .542 .820 .979	.758 1.441 2.419 3.718 5.355 7.334 9.658 12.320 15.312 18.627 22.252	.512 .911 1.454 2.147 2.994 3.994 5.147 5.147 5.1449 7.901 9.499 11.239	.0856 .146 .224 .320 .432 .561 .706 .965 1.040 1.230 1.434	.0374 .0700 .117 .180 .261 .360 .478 .615 .772 .947 1.142	.0481 .0757 .107 .139 .171 .200 .227 .249 .258 .282 .292	1.384 2.551 4.186 6.321 3.979 12.159 15.366 20.086 24.815 30.038 35.738
Ξ	NERGY	BETA1	BETR2	LA/LB	LA/LG	L	B/LG
	MeV	BAR	NS				
	1.0 1.2 1.4 1.6 2.2 2.2 2.6 2.8 2.8 2.8 2.8 2.8 2.8 2.8 2.8 2.8 2.8	.383 .665 1.041 1.512 2.080 2.741 3.497 4.345 5.287 6.319 7.441	.129 .246 .413 .635 .914 1.252 1.649 2.103 2.614 3.180 3.798	1.469 1.571 1.652 1.720 1.776 1.823 1.863 1.897 1.924 1.947 1.965	8.797 9.821 10.728 11.553 12.301 12.980 13.589 14.135 14.612 15.033 15.398	566677777777	.987 .251 .495 .719 .927 .119 .294 .453 .595 .723 .836

## PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV		The state		BARNS			- NALS
1.02 1.24 1.46 0.02 46 0.02 2.20 2.20 2.20 2.20 2.20 2.20 2.2	.0113 .0254 .0476 .0795 .122 .176 .241 .318 .408 .509 .621	.257 .576 1.882 1.886 2.772 3.992 5.477 7.237 9.269 11.563 14.126	.199 .400 .709 1.127 1.658 2.307 3.075 3.964 4.973 6.079 7.296	.0333 .0671 .115 .176 .251 .338 .438 .551 .676 .807 .948	.0135 .0300 .0559 .0929 .142 .205 .282 .374 .481 .603 .739	.0197 .0371 .0588 .0588 .108 .133 .156 .177 .194 .204 .208	.490 1.064 1.945 3.175 4.782 6.782 9.191 12.016 15.256 18.871 22.384
Ε	INERGY	BETA1	BET92	L9/LB	LA/LG	L	B/LG
	MeV	BAR	NS			•	
	1.0211.4	.147 .301 .524 .819 1.185 1.625 2.140 2.729 3.391 4.106 4.385	.0438 .0984 .185 .308 .473 .681 .935 1.235 1.235 1.235 1.974 2.411	1.339 1.432 1.515 1.590 1.639 1.718 1.718 1.718 1.812 1.850 1.988 1.921	7.666 8.523 9.362 10.183 10.981 11.723 12.404 13.614 13.614 14.219 14.786	5555566677777	.726 .954 .180 .403 .621 .825 .016 .195 .360 .533 .695

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YTTERBIUM(Z2=70)
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L SUBSHELL IONISATION CROSS SECTIONS FOR ALPHA IMPACT

LISU	JESHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV			5 2.5. Sel	BARNS				
1.00 1.20 1.40 1.50 1.50 2.00 2.40 2.50 2.50 2.50 3.00	2.05 3.22 4.53 5.90 7.24 8.48 9.59 10.52 11.27 11.83 12.21	3.14 4.56 6.03 7.45 8.75 9.87 10.30 11.52 12.03 12.10 11.99	1.38 2.12 3.11 4.19 5.32 5.43 7.48 9.24 9.24 9.34 10.49	2.12 3.29 4.38 5.59 6.77 7.35 8.81 9.61 10.26 10.48 10.48	.534 1.08 1.82 2.76 4.70 5.70 5.70 5.70 5.23 8.23 8.34	.874 1.63 2.56 3.68 5.71 5.71 8.63 8.63 8.63	.513 1.25 1.77 2.66 4.62 1.66 6.61 4.55 39 3.7 4.55 39 3.7 4.55 39 3.7 4.55 5.53 3.7 5.53 5.53 5.53 5.53 5.53 5.	
L 2 SL	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV			212	BARNS				
1.20 1.20 1.40 1.60 1.80 2.20 2.20 2.60 2.60 2.80 3.80	.718 1.46 2.61 4.22 6.36 9.06 12.34 16.22 20.71 25.30 31.48	1.16 2.23 3.79 5.92 9.64 12.00 16.00 20.64 25.93 31.85 38.39	.339 .713 1.31 2.19 3.40 4.96 6.93 9.32 12.14 15.42 19.16	.584 1.15 2.23 4.83 6.86 9.34 12.29 15.65 19.65 24.07	.146 .376 .791 1.45 2.40 3.636 7.43 9.94 12.31	.252 .508 1.21 2.13 3.41 5.10 7.22 9.81 12.88 16.44 20.49	.140 .363 .768 1.41 2.35 3.62 5.26 7.32 9.80 12.72 16.11	.241 .587 1.18 2.08 3.34 5.00 7.10 9.66 12.69 16.22 20.23
L3SL	JESHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS	P. 191	-	C. C. C. C. C.	
1.00 1.20 1.40 1.60 2.00 2.20 2.40 2.60 2.80 3.00	3.65 7.14 12.24 19.12 27.90 38.62 51.30 65.91 82.41 100.76 120.88	5.49 10.16 16.72 25.29 35.95 48.69 63.51 80.34 99.13 119.79 142.25	1.65 3.36 6.00 9.73 14.69 20.97 28.64 37.76 48.34 60.39 73.90	2.64 5.07 8.64 13.50 19.76 27.51 36.77 47.59 59.96 73.88 89.31	.772 1.89 3.79 6.69 10.73 16.04 22.71 30.81 40.36 51.40 63.92	1.23 2.84 5.46 9.28 14.44 21.04 29.16 38.83 50.07 62.88 77.25	.742 1.83 3.79 6.54 10.52 15.76 22.36 30.37 39.84 50.78 63.20	1.19 2.76 5.32 9.07 14.16 20.60 28.28 49.42 62.12 76.38
	TOTAL ECP	SSR L SHE	LL IONISA	TION CROSS	SECTIONS	S AND SUB:	SHELL RAT	IOS
			FUR	ALFAA IMPA	CI			
	ENERGY MeV	1	TOTAL BARNS	L1/L2	L	.1/L3	L2/L:	3
	1.00 1.20 1.40 1.60 2.20 2.20 2.20 2.60 2.30 3.00	10	2.27 4.92 9.00 14.58 31.31 42.40 70.30 86.91 35.35	3.484 2.587 2.118 1.696 1.376 1.127 .930 .773 .545 .528 .432		707 572 469 389 324 273 230 195 166 138 114	.203 .213 .221 .229 .236 .242 .247 .257 .257 .251 .261	

TUNGSTEN(Z2=74)

## PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETR	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV			the second	BARNS			
1.0 1.24 1.6 1.24 1.6 2.24 2.24 2.20 2.20 2.20 2.20 2.20 2.20	.0189 .0369 .0636 .0998 .146 .204 .273 .353 .444 .546 .659	.407 .794 1.367 2.145 3.149 4.388 5.868 7.586 9.547 11.743 14.171	.287 .529 .847 1.276 1.807 2.446 3.193 4.043 5.001 6.063 7.226	.0516 .0894 .140 .204 .209 .369 .469 .580 .702 .835 .978	.0190 .0362 .0619 .0977 .144 .202 .273 .356 .453 .563 .686	.0326 .0531 .0784 .106 .136 .167 .196 .224 .250 .273 .292	.762 1.434 2.409 3.711 5.362 7.379 9.765 12.512 15.632 19.108 22.939
	1eV	BARN	3				
	1.0 1.2 1.4 1.6 2.0 2.2 2.4 2.6 2.3 3.0	.152 .276 .452 .638 .982 1.341 1.765 2.254 2.812 3.436 4.126	.0744 .145 .250 .392 .575 .301 1.071 1.385 1.743 2.144 2.587	1:411 1.518 1.603 1.671 1.732 1.732 1.826 1.826 1.864 1.896 1.924 1.948	7.845 8.821 9.680 10.437 11.167 11.821 12.430 12.992 13.501 13.963 14.386	000000000	559 812 039 248 633 807 970 120 258 .386

. ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

ENERG	Y L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV			•	BARNS			
1.0 1.24 1.68 0.24 68 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	6.26E-03 .0147 .0287 .0491 .0771 .113 .158 .211 .273 .345 .426	3 .135 .316 .617 1.057 1.658 2.432 3.389 4.538 5.882 7.423 9.160	.104 .228 .419 .682 1.026 1.451 1.956 2.549 3.229 3.229 3.996 4.347	.0195 .0412 .0730 .115 .167 .229 .300 .380 .470 .569 .676	6.71E-03 .0155 .0302 .0515 .0808 .119 .166 .223 .291 .370 .460	.0123 .0256 .0428 .0631 .0360 .110 .133 .157 .178 .199 .217	.263 .598 1.133 1.895 2.917 4.208 5.779 7.647 9.814 12.281 15.045
	ENERGY	BETA1	BETA2	LA/LB	LA/LO	L	B/LG
	MeV	BARN	15				
	1.0 1.2 1.4 1.6 1.8 2.2 2.4 2.2 2.4 2.3 3.0	.0554 .123 .227 .373 .565 .805 1.094 1.436 1.834 2.286 2.792	.0246 .0577 .113 .193 .303 .444 .619 .828 1.073 1.355 1.672	1.289 1.377 1.461 1.538 1.606 1.665 1.721 1.769 1.809 1.845 1.875	6.871 7.620 8.387 9.149 9.873 10.560 11.238 11.238 11.360 12.429 12.955 13.450	ត្រូលលេសសុសុសុសុសុក ក	331 534 741 948 148 341 529 706 871 023 158

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## TUNGSTEN(22=74)

L SUBSHELL IONISATION CROSS SECTIONS FOR ALPHA IMPACT

L 1 SUBSHELL

ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS		A set		
1.00 1.20 1.40 1.60 1.30 2.00 2.20 2.40 2.60 2.60 3.00	1.01 1.54 2.26 4.15 5.05 5.91 6.70 7.41 8.02 8.52	1.76 2.63 3.58 4.55 5.51 5.40 7.19 7.87 8.43 8.96 9.13	.645 1.09 1.659 2.000 3.74 4.19 5.679 5.49 7.04	1.22 1.37 2.60 3.29 4.98 5.72 6.40 7.90 7.51 7.93	.229 .481 .860 1.92 2.52 .52 .52 .52 .52 .52 .52 .52 .52	.416 .823 1.36 1.99 2.69 3.41 4.11 4.79 5.41 5.97 6.45	.210 .463 .834 1.31 1.88 2.50 3.16 3.82 4.47 5.09 5.65	.396 .792 1.32 1.94 2.63 3.34 4.04 4.71 5.33 5.89 6.36
L 2 SU	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 1.30 2.20 2.40 2.60 2.60 2.30 3.00	.276 .576 1.05 1.75 2.69 3.91 5.43 7.26 9.43 7.242 11.73	.507 .987 1.70 2.70 4.00 5.63 7.61 9.94 12.69 19.10	.136 .290 .543 .924 1.46 2.17 3.07 4.19 5.54 7.13 8.96	.266 .529 .934 1.51 2.29 3.28 .4.51 5.99 7.75 12.04	.049 .133 .294 .558 .955 1.51 2.25 3.151 2.25 3.37 4.374 7.37	.096 .244 .505 .913 1.50 2.30 4.50 6.05 9.90	.046 .128 .284 .542 .931 1.48 2.20 3.13 4.27 5.65 7.26	.091 .234 .488 .886 1.46 2.24 3.23 4.47 5.97 7.73 9.76
L 3 SU	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 1.80 2.00 2.20 2.40 2.60 2.60 2.80 3.00	1.63 3.275 9.17 13.21 25.92 33.76 42.76 52.88 64.12	2.72 5.11 8.53 13.08 18.83 25.90 43.47 54.12 65.97 78.95	.758 1.57 2.86 4.71 7.23 10.47 14.48 19.32 25.01 31.57 39.01	1.35 2.62 4.50 7.10 10.49 14.73 19.85 25.89 32.86 40.77 49.61	.305 .787 1.65 3.01 4.96 7.59 10.97 15.14 20.15 26.02 32.77	.545 1.31 2.60 4.53 7.20 10.68 15.03 20.29 26.47 33.60 41.68	.292 .759 1.60 2.93 4.85 7.44 10.77 14.89 19.85 25.66 32.35	.520 1.26 2.52 4.41 7.04 10.47 14.76 19.96 26.08 33.14 41.14
т	OTAL ECP:	SSR L SHE	L IONISAT	TON CROSS	SECTIONS	S AND SUBS	SHELL RAT	IOS
	ENERGY MeV		TOTAL BARNS	L1/L2	L	.1./L3	L2/L	3
	1.00 1.40 1.40 1.60 2.00 2.40 2.60 2.60 2.60 2.60 2.60 2.60 2.60 2.6		1.01 2.29 4.33 7.24 11.12 16.04 22.03 29.14 37.38 46.75 57.27	4.340 3.390 2.703 2.190 1.798 1.492 1.249 1.053 .762 .652		.761 .627 .523 .319 .274 .236 .204 .178 .155	.17 .18 .19 .20 .21 .21 .21 .21 .22 .23 .23	55317494937

### GOLD(22=79)

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.0211.44	.0108 .0212 .0369 .0587 .0874 .123 .167 .218 .277 .343 .417	.214 .422 .734 1.168 1.737 2.448 3.315 4.332 5.498 6.819 8.295	.117 .220 .372 .580 .850 1.182 1.588 2.061 2.599 3.205 3.885	.0184 .0334 .0545 .0830 .119 .162 .215 .275 .342 .416 .499	7.79E-03 .0152 .0266 .0430 .0650 .0932 .129 .171 .221 .279 .346	.0106 .0131 .0279 .0400 .0538 .0689 .0860 .103 .120 .137 .153	.360 .697 1.197 1.390 2.793 3.915 5.284 6.386 8.715 10.734 13.097
	ENER Mev	1 GY	LA/LB	LA/LG	L3/L	.G	
	1.9 1.46009 1.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.46009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.40009 2.4000000000000000000000000000000000000		1.839 1.918 1.975 2.013 2.045 2.071 2.088 2.102 2.116 2.127 2.135	11.636 12.654 13.464 14.071 14.615 15.094 15.447 15.768 16.092 16.382 16.607	6.33 6.81 6.89 7.14 7.29 7.50 7.50 7.70 7.77	7900009994600	

### PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

## ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV	1.2.1.1.1			BARNS			
1.02114	3.54E-03 8.66E-03 .0173 .0303 .0482 .0713 .100 .136 .177 .225 .230	.0703 .172 .343 .601 .958 1.418 1.995 2.695 3.520 4.470 5.557	.0402 .0954 .186 .317 .496 .722 1.000 1.338 1.731 2.180 2.595	6.59E-03 .0152 .0287 .0478 .0730 .104 .141 .185 .236 .293 .358	2.66E-03 6.60E-03 .0134 .0237 .0385 .0578 .0825 .114 .150 .194 .244	3.93E-03 8.58E-03 .0153 .0240 .0345 .0459 .0583 .0716 .0852 .0990 .113	.121 .291 .575 .997 1.575 2.315 3.237 4.353 5.664 7.168 8.889
	ENERG MeV	Υ	LA/LB	LA/LG	LB/L	G	
	1.024 600 24 600		1.750 1.804 1.850 1.897 1.931 1.965 1.994 2.014 2.034 2.050 2.050	10.661 11.329 11.948 12.595 13.125 13.661 14.158 14.547 14.926 15.258 15.529	6.09 6.245 6.679 6.679 7.734 7.734 7.7453	31316402920	

## GOLD(22=79)

L SUBSHELL IONISATION CROSS SECTIONS FOR ALPHA IMPACT

1	1	SU	RGL	HEI I	
-	*	ಿಲ್	1001	1	-

ENERGY	PWBA	PUBAR	PSS	Peep	rpes	00000		500000
Mey				RAPNS	0.00	Grook	20100	
1.00 1.20 1.40 1.60 1.80 2.00 2.20 2.40 2.50 2.80 3.00	.413 .698 1.06 1.50 1.99 2.51 3.63 4.13 4.59 5.02	.879 1.34 1.87 2.44 3.67 4.71 5.55 5.90	.267 .471 .738 1.06 1.43 1.84 2.71 3.14 3.57 3.97	.629 .976 1.33 1.83 2.32 2.80 3.72 4.16 4.57 4.95	.0692 .168 .326 .544 .817 1.14 1.50 1.58 2.23 2.67 3.06	.163 .349 .611 .939 1.32 1.736 2.59 3.01 2.60 3.01 3.02 3.01 3.01 3.02 3.01 3.02 3.01 3.02 3.01 3.02 3.01 3.02 3.02 3.02 3.02 3.02 3.02 3.02 3.02	.9651 .161 .314 .526 .795 1.11 1.47 1.47 1.485 2.24 2.53 3.01	.154 .333 .588 .909 1.29 1.69 1.59 2.56 2.36 2.36 3.76
L 2 SU	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 1.30 2.20 2.20 2.40 2.60 2.80 3.00	.0853 .182 .341 .580 .916 1.36 1.93 2.64 3.49 4.49 5.65	.189 .370 .648 1.56 2.23 3.05 4.05 5.22 5.55 8.07	.0442 .0955 .182 .316 .508 .769 1.11 1.54 2.07 2.71 3.46	.105 .209 .370 .604 .923 1.34 1.36 2.49 3.25 4.14 5.15	.0123 .0360 .0839 .167 .298 .489 .750 1.09 1.53 2.06 2.70	.0291 .0786 .171 .320 .542 .849 1.25 1.77 2.39 3.15 4.03	.0115 .0342 .0805 .152 .299 .475 .732 1.07 1.50 2.02 2.65	.0273 .0747 .164 .309 .526 .826 1.22 1.73 2.35 3.09 3.96
L 3 SU	BSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV ·				BARNS				
1.00	~	1.19	.297	. 621	.0966	.202	.0914	. 191
1.20 1.40 1.60 1.30 2.00 2.20 2.40 2.60 2.80 3.00	.614 1.27 2.29 3.74 5.69 8.17 11.23 14.88 19.13 24.00 29.48	2.27 3.34 5.97 8.70 12.03 16.11 20.81 26.13 32.21 38.90	.628 1.16 1.95 3.05 4.49 6.31 8.54 11.20 14.32 17.89	1.21 2.09 3.32 4.95 7.01 9.54 12.54 16.04 20.05 24.58	.267 .590 1.12 1.91 3.02 4.47 6.31 8.57 11.27 14.42	.513 1.06 1.91 3.11 4.71 6.76 9.27 12.27 12.27 15.78 19.30	.256 .569 1.895 1.895 4.19 4.19 8.142 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885 11.885	.491 1.02 1.85 3.83 4.60 5.61 9.09 12.06 15.52 19.51
1.20 1.40 1.60 1.30 2.00 2.20 2.40 2.60 2.80 3.00	.614 1.27 2.29 3.74 5.69 8.17 11.23 14.88 19.13 24.00 29.48	2.27 3.84 5.97 12.08 16.11 20.81 26.18 32.21 38.90 SR L SHEI	.628 1.16 1.95 3.05 4.49 6.31 8.54 11.20 14.32 17.39 L IONISAT FOR A	1.21 2.09 3.32 4.95 7.01 9.54 12.54 16.04 20.05 24.58 ION CROSS	.267 .590 1.12 1.91 3.02 4.47 6.31 8.57 11.27 14.42 SECTIONS	.513 1.06 1.91 3.11 4.71 6.76 9.27 12.27 15.78 19.30 AND SUBS	.256 .569 1.09 1.86 2.95 4.38 6.19 8.42 11.08 14.20 HELL RAT:	.491 1.02 1.85 3.03 4.60 5.61 9.09 12.06 15.52 19.51
1.20 1.40 1.60 1.30 2.20 2.40 2.40 2.50 2.80 3.00	.614 1.27 2.29 3.74 5.69 8.17 11.23 14.88 19.13 24.00 29.48 OTAL ECPS ENERGY MeV	2.27 3.84 5.97 12.08 16.11 20.81 26.18 32.21 38.90 SR L SHE	.628 1.16 1.95 3.05 4.49 6.31 8.54 11.20 14.32 17.39 LL IONISAT FOR A	1.21 2.09 3.32 4.95 7.01 9.54 12.54 16.04 20.05 24.58 ION CROSS LPHA IMPA	.267 .590 1.12 1.91 3.02 4.47 6.31 8.57 11.27 14.42 SECTIONS CT	.513 1.06 1.91 3.11 4.71 6.76 9.27 12.27 15.78 19.30 AND SUBS	.256 .569 1.89 1.86 2.95 4.38 6.19 8.42 11.08 14.20 HELL RAT:	. 491 1.02 1.85 3.03 4.60 5.51 9.09 12.06 15.52 19.51 105

### LEAD(22=82)

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.2244580246880	6.19E-03 .0127 .0229 .0373 .0568 .0815 .112 .149 .192 .241 .296	.117 .241 .435 .707 1.078 1.547 2.130 2.832 3.636 4.581 5.618	.0603 .120 .211 .338 .508 .722 .986 1.301 1.663 2.088 2.557	9.24E-03 .0177 .0302 .0473 .0694 .0969 .130 .169 .214 .256 .323	3.64E-03 7.55E-03 .0138 .0229 .0354 .0520 .0731 .0990 .130 .167 .209	5.59E-03 .0102 .0155 .0244 .0340 .0450 .0570 .0702 .0841 .0987 .113	.193 .391 .639 1.130 1.712 2.447 3.358 4.451 5.705 8.794
	ENERG MeV	iy .	LAZLB	LAZLO	LB/L	.6	
	1.0 1.2 1.4 1.5 2.2 2.4 2.6 2.2 2.4 6 2.3 0 3.0		1.948 2.008 2.059 2.089 2.122 2.143 2.161 2.177 2.186 2.194 2.197	12.711 13.588 14.385 14.939 15.536 15.961 16.378 16.738 17.002 17.251 17.400	6.52 6.98 7.15 7.32 7.57 7.57 7.57 7.86 7.78 7.92	25 56 57 59 59 57 77 51 59 57 51	

# PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

#### ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV				BARNS			
1.0 1.2 1.4 1.6 1.8 0 2.2 2.2 2.3 0	2.03E-03 5.28E-03 .0110 .0198 .0325 .0490 .0702 .0961 .127 .163 .204	.0385 .100 .209 .376 .617 .929 1.332 1.323 2.410 3.094 3.877	.0207 .0527 .108 .191 .307 .458 .649 .380 1.154 1.473 1.835	3.31E-03 8.19E-03 .0163 .0282 .0444 .0650 .0904 .121 .156 .196 .242	1.25E-03 3.34E-03 7.14E-03 .0131 .0219 .0338 .0493 .0493 .0689 .0927 .121 .154	2.05E-03 4.35E-03 9.19E-03 .0151 .0225 .0312 .0411 .0517 .0631 .0571 .0874	.0645 .166 .344 .615 1.001 1.502 2.142 2.920 3.847 4.927 6.158
	ENERO MeV	ÿΥ	LA/LB	LA/LG	L3/L	.G	
	1.0 1.2 1.4 1.6 2.2 2.4 6 2.2 4 6 2.2 4 6 2.2 2 .0 3		1.859 1.901 1.940 1.971 2.007 2.029 2.053 2.071 2.088 2.100 2.113	11.633 12.228 12.798 13.305 13.883 14.291 14.745 15.119 15.465 15.756 15.954	5.25 5.575 5.575 5.94 7.129 7.7.7 7.7.59	77 198 198 199 199 199 199 199 199 199 199	

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LEAD(22=82)
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L SUBSHELL IONISATION CROSS SECTIONS FOR ALPHA IMPACT

L 1	SUBSHELL							
ENERGY	PNBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV			1992	BARNS				
1.00 1.20 1.40 1.60 1.60 2.20 2.20 2.40 2.60 2.60 3.00	.202 .363 .579 .847 1.16 1.51 1.88 2.27 2.66 3.05 3.42	.527 .826 1.13 1.58 2.00 2.43 2.87 3.28 3.69 4.04 4.39	.130 .240 .392 .565 .318 1.09 1.38 1.70 2.03 2.03 2.36 2.71	.373 .595 .865 1.18 1.52 1.88 2.25 2.62 2.98 3.33 3.65	.0279 .0743 .154 .273 .432 .530 .961 1.12 1.41 1.70 2.01	.0799 .184 .341 .548 .303 1.09 1.40 1.73 2.05 2.40 2.71	.0260 .0705 .148 .263 .413 .613 .613 .840 1.09 1.38 1.67 1.98	.0746 .174 .326 .529 .778 1.06 1.37 1.69 2.02 2.35 2.67
L 2	SUBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.50 1.50 2.00 2.20 2.40 2.50 2.50 2.80 3.00	.0344 .0779 .152 .267 .431 .555 .950 1.32 1.77 2.32 2.96	.0917 .185 .331 .541 .826 1.19 1.66 2.22 2.89 3.67 4.57	.0179 .0412 .0819 .146 .241 .372 .547 .772 1.05 1.40 1.30	.0521 .106 .192 .318 .493 .722 1.01 1.38 1.81 2.33 2.92	4.13E-0 .0135 .0358 .0709 .131 .221 .349 .520 .741 1.02 1.36	3 .0120 .0349 .0794 .154 .269 .430 .547 .929 1.28 1.70 2.20	3.84E- .0122 .0322 .0681 .127 .215 .339 .508 .724 1.000 1.33	03 .0112 .0329 .0757 .148 .259 .417 .529 .906 1.25 1.67 2.16
L3	SUBSHELL					•	•	
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS				
1.00 1.20 1.40 1.60 1.30 2.00 2.20 2.40 2.60 2.60 3.00	.295 .635 1.19 1.99 3.11 4.55 6.38 8.61 11.20 14.28 17.69	.653 1.27 2.20 3.49 5.18 7.28 9.84 12.86 16.33 20.28 24.77	.143 .316 .607 1.05 1.67 2.50 3.58 4.92 6.53 8.47 10.67	.347 .690 1.22 1.97 2.97 4.25 5.85 7.77 10.02 12.63 15.58	.0402 .121 .282 .559 .987 1.60 2.42 3.50 4.62 5.50 4.62 6.46 8.36	.0974 .263 .565 1.05 1.76 2.71 3.96 5.52 7.40 9.64 12.21	.0378 .115 .271 .541 .555 2.342 4.35 2.42 4.35 8.22	.0916 .250 .543 1.01 1.71 2.64 3.87 5.40 7.26 9.46 12.01
TOTF	AL ECPSSR	L SHELL	IONISATIO FOR A	N CROSS SE LPHA IMPAC	ECTIONS A	ND SUBSHE	LL RATIO	S

MeV	PUNIAS			
1.00 1.20 1.40 1.50 2.00 2.20 2.40 2.60 2.60 3.00	.177 .945 .945 1.69 2.74 4.12 5.800 10.52 13.48 16.83	6.663 5.297 4.309 3.568 2.998 2.538 2.171 1.870 1.619 1.409 1.233	.814 .697 .601 .521 .456 .400 .353 .313 .278 .278 .248 .222	.122 .139 .1462 .1583 .1463 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .1583 .15833 .15833 .1583 .1583 .15833 .15833 .15833 .15833 .15833 .15833

### BISMUTH(Z2=83)

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV	133. 19			BARNS		C. Start	
1.024460000446000	5.34E-03 .0110 .0200 .0328 .0500 .0721 .0997 .133 .171 .216 .266	.0998 .206 .373 .335 1.348 1.863 2.479 3.205 4.039 4.977	.0509 .102 .180 .291 .439 .626 .858 1.135 1.462 1.834 2.257	7.06E-03 .0137 .0236 .0374 .0555 .0781 .106 .139 .177 .221 .271	2.95E-03 6.16E-03 .0113 .0189 .0295 .0435 .0615 .0836 .111 .142 .179	4.12E-03 7.58E-03 .0123 .0185 .0260 .0346 .0444 .0552 .0667 .0791 .0916	.163 .333 .597 .974 1.480 2.125 2.927 3.886 5.015 6.311 7.771
	ENERG MeV	iγ	LA/LB	LA/LG	LB/L	.0	
	1.004460000446000 1.1.1.1.0000446000 0.00000		1.959 2.019 2.069 2.104 2.131 2.153 2.171 2.184 2.192 2.202 2.205	14.128 15.004 15.790 16.371 16.852 17.253 17.599 17.862 18.857 18.262 18.362	7.21 7.43 7.63 7.79 8.91 8.19 8.19 8.12 8.23 8.33	0 31 30 31 30 30 31 30 30 30 30 30 30 30 30 30 30 30 30 30	

# PWBA L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

# ECPSSR L SHELL X-RAY PRODUCTION CROSS SECTIONS

FOR ALPHA IMPACT

ENERGY	L	ALPHA	BETA	GAMMA	GAMMA1	GAMMA2	TOTAL
MeV	-			BARNS			
1.00 1.1.4.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60 2014.60	1.74E-03 4.59E-03 9.57E-03 .0176 .0288 .0438 .0438 .0630 .0865 .115 .147 .186	.0325 .0859 .181 .329 .538 .819 1.178 1.616 2.147 2.757 3.474	.0173 .0449 .0927 .166 .268 .402 .572 .777 1.024 1.307 1.639	2.50E-03 6.33E-03 .0128 .0226 .0359 .0530 .0744 .100 .130 .165 .205	1.00E-03 2.73E-03 5.91E-03 .0110 .0185 .0287 .0422 .0591 .0797 .105 .134	1.49E-03 3.50E-03 6.92E-03 .0115 .0174 .0243 .0322 .0410 .0507 .0505 .0714	.0540 .142 .296 .535 .870 1.317 1.387 2.580 3.416 4.377 5.504
	ENERG MeV	ÿΨ	LA/LB	LA/LG	LB/1	.G	
	1.024 4 6 8 8 0 2 4 6 8 8 0 2 4 6 8 8 0 2 4 6 8 8 0 2 4 6 8 8 0 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2		1.874 1.915 1.950 1.984 2.009 2.037 2.060 2.079 2.096 2.108 2.119	13.002 13.567 14.084 14.590 14.995 15.449 15.835 16.161 16.465 16.705 16.909	6.93 7.22 7.35 7.35 7.35 7.35 7.35 7.35 7.35 7.35	28 25 21 24 23 26 24 26 25 26 26 26 26 26 26 26 26 26 26 26 26 26	

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BISMUTH(Z2=83)
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L SUBSHELL IONISATION CROSS SECTIONS FOR ALPHA IMPACT

L 1	SUBSHELL							
ENERGY	PUBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
MeV				BARNS	1-5-1-	- 48	1.18	
1.00 1.29 1.40 1.50 2.20 2.20 2.40 2.50 2.50 3.00	.167 .303 .486 .717 .989 1.29 1.62 1.97 2.32 2.69 3.02	.461 .724 1.04 1.39 1.77 2.16 2.56 2.94 3.31 3.65 3.97	.108 .201 .329 .495 .697 .930 1.19 1.47 1.75 2.07 2.37	.328 .523 .762 1.04 1.35 1.67 2.01 2.34 2.68 3.00 3.32	.0216 .0589 .124 .223 .357 .526 .724 .953 1.20 1.47 1.74	.0655 .153 .288 .469 .691 .943 1.23 1.52 1.83 2.12 2.43	.0201 .0557 .119 .215 .346 .511 .706 .931 1.17 1.44 1.71	.0610 .145 .275 .451 .668 .916 1.19 1.48 1.79 2.08 2.39
L 2	SUBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR
. MeV				BARNS				
1.00 1.20 1.40 1.60 2.00 2.20 2.40 2.60 2.80 3.00	.0270 .0614 .120 .345 .523 .768 1.07 1.45 1.89 2.43	.0759 .153 .274 .449 .686 .994 1.39 1.86 2.43 3.08 3.85	.0141 .0328 .0654 .117 .194 .301 .445 .628 .859 1.14 1.48	.8436 .0889 .151 .267 .413 .605 .852 1.16 1.53 1.96 2.47	3.06E-0 .0102 .0259 .0550 .103 .175 .278 .416 .596 .823 1.10	3 9.43E-0 .0277 .0638 .125 .219 .352 .533 .766 1.06 1.41 1.34	3 2.83E 9.63E .0247 .0527 .05990 .169 .270 .405 .582 .805 1.08	83 8.74E-03 .0261 .0607 .120 .211 .341 .518 .746 1.03 1.38 1.30
L 3	SUBSHELL							
ENERGY	PWBA	PWBAR	PSS	PSSR	CPSS	CPSSR	ECPSS	ECPSSR .
MeV				BARNS				
1.00 1.20 1.40 1.60 1.60 2.20 2.40 2.60 2.60 2.60 2.60 3.00	.243 .526 .988 1.67 2.61 3.84 5.40 7.29 9.55 12.17 15.16	.559 1.09 1.89 3.01 4.46 6.29 8.54 11.14 14.21 17.64 21.63	.119 .264 .508 .880 1.41 2.12 3.04 4.13 5.57 7.22 9.15	.300 .597 1.05 1.71 2.57 3.69 5.09 6.76 9.74 11.01 13.64	.0316 .0966 .229 .458 .813 1.32 2.03 2.93 4.06 5.45 7.09	.0801 .218 .474 .887 1.49 2.31 3.39 4.73 6.38 8.31 10.58	.0297 .0919 .219 .442 .788 1.29 1.38 2.86 3.98 5.35 6.97	.0751 .208 .455 .857 1.44 2.25 3.31 4.63 6.25 8.15 10.40
TOTA	IL ECPSSR	L SHELL I	ONISATIC	N CROSS SE	ECTIONS AN	D SUBSHE	LL RATIOS	
			FOR A	LPHA IMPA	CT			
ENERGY MeV		TOTAL BARNS		L1/L2	L1/L3	L	2/L3	
1.00 1.20 1.40 1.50 1.30 2.00 2.20 2.40 2.60 2.80 3.00		.145 .379 .791 1.43 2.32 3.51 5.03 6.86 9.07 11.62 14.59	6554 3334 334 34 11 11 11	.978 .559 .532 .762 .166 .687 .988 .729 .506 .324	.812 .699 .605 .463 .463 .463 .360 .326 .286 .256 .230		.116 .126 .133 .140 .146 .151 .155 .161 .155 .170 .174	

APPENDIX D

LISTING OF 'SPECTRUM' PACKAGE

1 1	R
2 :	MO \$ADD=ON
3 1	AUF77
4	PROGRAM SPECTRUM
5 .	WRITTEN ON 26th MAY 1982
6	CONSTANTS
7	PARAMETER (PI=3. 1415926)
8	VARIABLES
9	INTEGER INITIAL, FINAL, CH. PARA, REGION, J. CH1, J1, N. N1, NN, SK, P. G.
10	: P1, Q1, G1, K, PEAKS, BGPARA, K1, ITER, CORREC, CPARA, LAM, FITER
11	INTEGER GROUP, GROUPS
12	REAL*6 D(1:70,1:71), FIT(1:300),
13	: X1(1:70), S1(1:70), SD(1:70), DET,
14	RESID(1:70), REFINEDX(1:70), PARAM1(1:70),
15	XX. BGFIT, PFIT, POWER, CPFIT, LAMDA, NU, PARAM2(1:70),
14	YTVI, YT. VI. MCDUNT, SUMSOREG, SUMSOM, MSUM, EX(1: 20), SUMSOI,
17	COUNT(1:300), PSG, PARAM, ERPORY, ECOUNT(1:300), SUMSG2.
10	
10	
17	
20	
21	
22	CHARACTER ELEMENT #23
23	CUMMUN/MAIRICES/(1/1/1/200) 1/200/ 1/1/1/200, 1/200/ 1/200/ 1/200/
24	CUMMUN/DERIVMAT/XX(1:300,1:70), PARAM(1:70), ERBRA(1:70)
25	CUMMUN/GAUSSMAT/0(1:/0,1:/1), D1(1:/0,1:/1), X(1:/0)
26	FITER=130
27	READ(16, *)GROOPS, PRECIS
28	FOR GROUP=1, GROUPS
29	READ(16, *)ELEMENT
30	READ(16, *) BGPARA, PEAKS, CORREC
31	CPARA=CDRREC*2
32	PARA=BGPARA+PEAKS+CORREC
33	N=PARA
34	READ(16, *) INITIAL, FINAL
35	REGION=FINAL-INITIAL
36	DF=REGIDN-PEAKS*2-CPARA-BGPARA
37	PRINT*, "ELEMENT=", ELEMENT, BGPARA+PEAKS*3+CPARA,
38	: "PARAMETER LEAST SQUARE FIT"
39	PRINT*, "PEAKS=", PEAKS, "BGPARA=", BGPARA, "CORREC=", CORREC
40	: , "REGION=", REGION
41	PRINT*, "DEGREES OF FREEDOM=", DF
42	READ(16, *)(EX(K), K=1, PEAKS)
43	J=BGPARA
44	FOR K=1, PEAKS
45	
46	PARAM(J+1)=(14.3442+24.523*EX(K))-INITIAL
47	PARAM(J+2)=(1, 5339+, 4446*EX(K))*2.0
48	PRINT*, "ENERGY=", EX(K), "CENTROID=", PARAM(J+1), "25IGMA2=",
49	: PARAM(J+2)
50	J=J+2+CORREC
51	END FOR
52	51 READ(16, *)(COUNT(CH), CH=1, REGION)

53		FOR CH=1, REGION
54		IF (COUNT (CH) EQ O) THEN
		COUNT/CH) =1
33		CDONT (CH)=1
56		ELSE
57		ENDIF
50		ECOLINT (CH) = COLINT (CH)
20		
59		END FOR
60		MSUM=0
61		FOR CH=1, REGION
10		
04		
63		END FOR
64		MCOUNT=MSUM/REGION
45		PRINTA. "MEAN COUNT=". MCOUNT
66 *		
67		FOR CH=1, REGION
68		POWER=1.0
40		YY(CH, 1)=1
07		
70		FOR KI=2, BGPARA
71		XX(CH, K1)=(CH*1.0)**POWER
77		FYIT FOR IF(K1 FO BORARA)
70		
13		PUWER=FUWER+1.0
74		END FOR
75		K1=0
74		I=BCPARA
/0		
77		FOR K=1, PEAKS
78		ل=ال=ال
79		IF (CH. LT. PARAM(J+1)) THEN
80		ALTH-O. O
81		ELSE
82		ALPHA=1.0
83		ENDIE
0.5		
84		XX(CH, BGPARA+K+X1)=EXP(-((CH-PARAM(J+1))**2)/PARAM(J+2))
85		IF (CORREC. EG. 0) THEN
86		J=J+2
07		COTO BI
0/		4010 DI
38		ELSE
89		PARAM(J+4)=PARAM(J+1)+SQRT(2*PARAM(J+2))
90		ENDIF
01		K1-K1+1
71		
92		XX(CH, BGPARA+K+K1) = EXP(-((CH-PARAM(J+4))**2)/PARAM(J+2))
93		ل=ل+4
94	81	END FOR
	404	
42	401	END FUR
96		ITER=0
97		G0T061
00	400	PRINT ( (3Y. A. 10Y. A) ( "COUNTS", "SASAAMATRIYAAAA"
20		
77		FOR CH-I, REGION
100		PRINT*,
101		: CH, COUNT(CH), (XX(CH, J), J=1, PARA)
102		END FOR
102		
103	51	Du .
104		LAMDA1=1. 0E-5
105		LAMDA=LAMDA1
104		NUE10
100		
107		WNU=U ·
108		IF (ITER. EQ. 0) THEN
109		KAPPA=0
110		ELSE LECTTER OF 1 AND ITER LE TOTTEN
110		KARA KARA O ONO
111		AAFFA=AAFFA+0. 0010
112		ELSE IF (ITER. GT. 10. AND. (KAPPA+(ITER-10)/100. 0). LT. 1. 0) THEN

113			KAPPA=KAPPA+(ITER-10)/100.0
114			ELSE IF (ITER. GT. 10. AND. KAPPA. GE. 1. 0) THEN
115			KAPPA=1. 0
116			ELSE
117			KAPPA=1.0
118			ENDIF
119	*		TRANSPOSE OF MATRIX
120			FOR CH=1, REGION
121			FOR J=1. PARA
122			VI (CH, J)=XX (CH, J)
123			XT (J, CH) = XX (CH, J)
124			END FOR
125			END FOR
124			
127			FOR CHELL REGION
120			
120			
120			
130			CALL YMATRIY/COUNT BARA SEATON BARA LOU CULL
131			COTO 23
102	*		
100	*		
134			BRINTA (YTUT / L CUI) CUI = 1 BARAS
135			
130			
137		23	
138			
1.37			
1 4 1			
1471			YTUT( PAPAT) = YTUT( PAPAT) +YT( CH) *COUNT(CH) /CCOUNT(CH)
140			
140			
145			
145	*		SCALING THE ALIGNENTED MATRIX
147	-	90	TECTER NE OTTEN
140		10	
140			FOR CHIEL, PARA
150			IF (J NE CHI) THEN
151			YTUI(), CHI)=YTUI(), CHI)/SOPT(YTUI(), ))*YTUI(CHI, CHI))
157			FI SE
157			ENDIE
154			
155			YTUT (.), PAPA+1)=YTUT (.), PAPA+1) (CAPT (YTUT (
154			
157			
158			ENDIE
150		89	
140	*		
161	-	84	FOR J=1, N
162			FOR CH1=1, N+1
143			U(J, CH1)=XTVI(J, CH1)
164			END FOR
165			END FOR
166	*		MARQUARDT'S ALGORITHM
167			IF (ITER, NE, O) THEN
168			FOR CH1=1, PARA
169			U(CH1, CH1)=XTVI(CH1, CH1)+LAMDA
170			END FOR
171			ELSE
172			ENDIF

173	\$ADD	REFINE
174		IF (ITER. EQ. 0) THEN
175		GOTO 28
174		FIGE
170		
1//		
178		IF (LAM. EG. O. AND. WNO. EG. O) THEN
179		PARAM1(J)=0
180		PARAM1(J)=PARAM(J)
181		ELSE
182		ENDIF
183		PARAM(J)=PARAM1(J)+REFINEDX(J)*KAPPA
104		IF ( ( ) FO 1 OF OT BOPARA) AND PARAM( ) IT OTHEN
104		
100		
186		ELSE
187		ENDIF
188		END FOR
189		END IF
190		GOTO 29
191	*	INITIAL PARAMETERS
192	28	K=0
193		FOR J=1, PEAKS+CORREC+BGPARA
194		TE (BOPARA EQ 1 AND CORREC NE O AND (J/2 O) NE INT(J/2 O) AND J
105		CT BCPAPA+1)THEN
175		
176		THE STATE AND CORRESPONDED AND A LOD ON THE ANTALY ON
197		ELSE IF (BGPARA, EG. 1. AND. CURREC. NE. O. AND. (5/2. 0). EG. INT(5/2. 0)
198		: AND. J. GT. BGPARA+1) THEN
199		K=K+1
200		ELSE IF (CORREC. NE. 0, AND. (J/2. 0), EQ. INT (J/2. 0), AND. J. GT. BGPARA+1
201		: . AND. BGPARA. GT. 1) THEN
202		K=K+2
203		· ELSE IF (CORREC, NE. O. AND. (J/2, O), NE. INT (J/2, O), AND. J. GT. BGPARA+1
204		AND BORARA GT 1) THEN
205		
200		THE TECODDEC ED O AND I OT BOBADATITUEN
200		ELSE IF (CORREC. Ed. C. MID. C. GT. BGFMRHTI) THEN
207		K=K+Z
508		ELSE
209		K=0
210		ENDIF
211		PRINT*, "J=", J, "REF=", REFINEDX(J), "K=", K
212		PARAM(J+K)=REFINEDX(J)
213		IF ((J. EG. 1. DR. J. GT. BGPARA), AND. PARAM(J+K), LT. 0) THEN
214		PARAM(J+K)=(SQRT(PARAM(J+K)**2))/10.0
215		FLSE
214		ENDIE
210		
21/		
218		PARANCI PARANCI // I. O
219		IF (BGPARA, EG. 2) THEN
220		PARAM(2)=. 1000
221		ELSE
222		ENDIF
223		GOTO 29
224		PRINT*, "PARAMETERS", "ITER=", ITER, "LAM=", LAM, "LAMDA=", LAMDA
225		PRINT*, (PARAM(J), J=1, PEAKS*3+CPARA+BGPARA)
224	29	FOR CH=1, REGION
227		FIT(CH)=0
220		BOFIT=0
220		9577-0
229		
530		
231		BGF11=FARAM(1)
232		POWER=1.0

233	FOR K=2, BGPARA
234	BGFIT=BGFIT+PARAM(K)*CH**POWER
235	EXIT FOR IF (K. EG. BGPARA)
236	POWER=POWER+1.0
237	
238	FUR J-BGFARATI, FEASTSTCFARATBGFARA
237	
240	FI SE
242	ALPHA=1.0
243	ENDIF
244	PFIT=PFIT+PARAM(J)*EXP(-((CH-PARAM(J+1))**2)/PARAM(J+2))
245	IF (CORREC. EQ. 0) THEN
246	+2=ل
247	CPFIT=0
248	GDTD 82
249	ELSE
250	ENDIF
251	CPFIT=PARAM(J+3)*EXP(-((CH-PARAM(J+4))**2)/PARAM(J+2))
252	
253	82 EXIT FUR IF (J. EU. PEAKS#3+CPARA+BGFARA)
234	CIND FOR
255	
257	SUMSGREG=0
258	SUMSOM=0
259	CHISG=0
260	SUMSG=0
261.	FOR CH=1, REGION
262	SUMSGREG=SUMSGREG+(FIT(CH)-MCDUNT)**2
263	SUMSQM=SUMSQM+(ECOUNT(CH)-MCOUNT)**2
264	SUMSG=SUMSG+((ECOUNT(CH)-FIT(CH))**2)
265	CHISG=CHISG+((ECOUNT(CH)-FIT(CH))**2)/ECOUNT(CH)
266	END FOR
267	
268	EVIT DO LEGADT ((CHISAD_CHISA)**2) LE PRECIS AND ITER GT 10 CR
270	ITER FO 150)
271	IF (LAM, EG. O) THEN
272	SUMSQ1=SUMSQ
273	CHISQ1=CHISQ
274	RSQ1=RSQ
275	FOR J=1, PEAKS*3+CPARA+BGPARA
276	PARAM2(J)=PARAM(J)
277	END FOR
278	LAMDA=LAMDA1/NU
279	
280	
281	
202	
284	CHISQ2=CHISQ
285	ELSE IF (CHISQ1, LE. CHISQ2) THEN
286	LAMDA=LAMDA1
287	SUMSQ2=SUMSQ1
288	CHISQ2=CHISQ1
289	RSG=RSG1
290	FOR J=1, PEAKS*3+CPARA+BGPARA
291	PARAM(J)=PARAM2(J)
292	END FOR

293	ELSE IF (CHISQ1. GT. CHISQ2. AND. CHISQ. GT. CHISQ2) THEN
294	KAPPA=KAPPA+0. 1
295	UNU=UNU+2
204	LAMDA1 = LAMDA1 SNI 1822 0
270	
271	
298	EXIT DU IF (LAMDA. GT. 1. OE+IU)
299	G010 89
300	ELSE
301	ENDIF
302	ELSE
303	SUMSQ2=SUMSQ
304	CHISG2=CHISG
205	ENDIE
300	
300	
307	GUIU 71
308	PRINT*, "**** ITER **** =", ITER
309	PRINT*, "WNU=", WNU, "LAMDA=", LAMDA, "KAPPA=", KAPPA
310	PRINT*, "BACKGROUND PARAMETERS"
311	PRINT*, (PARAM(J), J=1, BGPARA)
312	PRINT*, "PEAK PARAMETERS"
313	91 FOR K=1, PEAKS
314	ARFA(K)=PARAM(BCPARA+1+(K-1)*3)*SCOPT(2 (3PT)
315	
315	ACTO 19
318	
317	PRINT*, (PARAM(J), J=8GPARA+1+(K-1)*3, 8GPARA+(K*3))
318	: , "AREA", K, "=", AREA(K)
319	68 END FOR
320	GOTO 52
321	PRINT*, "COEFFICIENT OF REGRESSION=", RSQ
322	: , "CHI SQUARED=", CHISQ
777	PRINT*, "REDUCED CHISG=", RCHISG
224	52 CALL DEPTU (PEAKS, PERAPA, CPAPA, PEATON K, LCH)
SET	
325	
326	
327	CDUNT(CH) = ECDUNT(CH) - FIT(CH)
358	IF(ITER. EQ. FITER) THEN
329	PRINT'(3X, I3, 3X, 2(F10, 3, 3X), F10, 3)',
330	: CH+INITIAL, ECOUNT(CH), FIT(CH), COUNT(CH)
331	ELSE
332	ENDIF
333	71 END FOR
334	WRITE (3, *) FI EMENT, "ITER=", ITER
225	
335	WATELS, */ CAISE / CAISE, KCAISE / KCAISE
336	64 FARA-FEARA*STUFARATBGFARA
337	NEPAKA
338	ITER=ITER+1
339	UNTIL(ITER. EQ. FITER+1)
340	PRINT*, "***** ITER ***** =", ITER
341	PRINT*, "WNU=", WNU, "LAMDA=", LAMDA, "KAPPA=", KAPPA
342	PRINT*, "BACKGROUND PARAMATERS"
343	PRINT*, (PARAM(J), J=1, BGPARA)
344	PRINT*, "PEAK PARAMETERS"
345	
343	
346	-RIN(#) (FARAN(U), J=8GFARA+1+(K-1)+3, BGFARA+(K+3))
347	; , "AREA", A, "=", AREA(X)
348	END FOR
349	PRINT*, "RSQ=", RSQ, "CHISQ=", CHISQ
350	PRINT*, "SUMSQ=", SUMSQ, "RCHISQ=", RCHISQ
351	PRINT*, "====================================
252	·

353	END FOR
354	WRITE(3,*)"****** PROGRAM COMPLETE ******"
355	100 END
356	SUBROUTINE XMATRIX (ECOUNT, LIMIT1, LIMIT2, LIMIT3, S1, S2, S3)
357	INTEGER LIMIT1, LIMIT2, LIMIT3, S1, S2, S3
358	REAL*6 XMAT, MAT1, MAT2, ECOUNT(1: 300)
359	COMMON/MATRICES/XMAT(1:300,1:300), MAT1(1:300,1:300),
360	: MAT2(1:300, 1:300)
361	FOR S1=1, LIMIT1
362	FOR S3=1, LIMIT3
363	XMAT(S1, S3)=0
364	END FOR
365	END FOR
366	FOR S1=1, LIMIT1
367	FOR S3=1, LIMIT3
368	FOR S2=1, LIMIT2
369	XMAT(S1, S3)=XMAT(S1, S3)+MAT1(S1, S2)*MAT2(S2, S3)/ECOUNT(S2)
370	END FOR
371	END FOR
372	GOTO 300
373	PRINT*, "S1=", S1
374	PRINT*, (XMAT(S1, S3), S3=1, LIMIT2)
375	300 END FOR
376	END
377	SADD GAUSS
378	SUBROUTINE DERIV (PEAKS, BGPARA, CPARA, REGION, K, J, CH)
379	REAL*6 PARAM, ERRORX, ZO, ZSUM, ZSUMBG, ZSUMP, DELTA,
380	: POWERE, POWERP, ZSUMCP
381	INTEGER PEAKS, REGION, K, J, CH, BOPARA, CPARA, K1
382	COMMON/DERIVMAT/ZO(1: 300, 1: 70), PARAM(1: 70), ERRORX(1: 70)
383	FOR K=1, PEAKS*3+CPARA+BGPARA
384	ERRORX (K)=0
385	ERRORX (K) = PARAM(K)
386	END FOR
387	FOR CH=1, REGION
388	FOR J=1, PEAKS*3+CPARA+BGPARA
389	ZSUM=0
390	ZSUMBC=0
391	ZSUMP=0
392	ZSUMCP=0
393	DELTA=PARAM(J)/500.0
394	ERRORX (J) =PARAM (J) +DELTA
395	PARAM(J)=PARAM(J)-DELTA
396	FOR K1=1, BGPARA
397	ZSUMBG=ZSUMBG+ERRORX(K1)-PARAM(K1)
398	EXIT FOR IF (K1, EQ. BGPARA)
399	IF (BGPARA, EG. 2) THEN
400	POWERE=1.0
401	POWERP=1. 0
402	ELSE
403	POWERE=ERRORX(K1+2)
404	POWERP=PARAM(K1+2)
405	ENDIF
406	ZSUMBG=ZSUMBG+ERRORX(K1+1)*CH++POWERE
407	-PARAM(K1+1)*CH**POWERP
408	K1=K1+1
409	EXIT FOR IF (K1. EQ. BGPARA)
410	END FOR
411	FOR K=BGPARA+1, PEAKS*3+CPARA+BGPARA
412	IF (CH. LT. PARAM(K+1)) THEN

413	ALPHA=0. 0	
414	ELSE	
415	ALPHA=1, 0	
416	ENDIF	
417	ZSUMP=ZSUMP+ERRORX(K)*EXP(-((CH-ERRORX(K+1))**2)/ERRORX(K+2)	)
418	: -PARAM(K)*EXP(-((CH-PARAM(K+1))**2)/PARAM(K+2))	
419	IF (CPARA. EG. O) THEN	
420	K=K+2	
421	ZSUMCP=0	
422	GOTO 83	
423	ELSE	
424	ENDIF	
425	ZSUMCP=ZSUMCP+ERRORX(K+3)*EXP(-((CH-ERRORX(K+4))**2)	
426	: /ERRORX(K+2))	
427	: -PARAM(K+3)*EXP(-((CH-PARAM(K+4))**2)/PARAM(K+2))	
428	К=К+4	
429	B3 EXIT FOR IF (K. EQ. PEAKS*3+CPARA+BGPARA)	
430	END FOR	
431	ZSUM=ZSUMBG+ZSUMP+ZSUMCP	
432	PARAM(J)=PARAM(J)+DELTA	
433	ERRORX(J)=PARAM(J)	
434	ZO(CH, J)=ZSUM/(2. 0*DELTA)	
435	END FOR	
436	END FOR	
437	END	
438	\$MO \$ADD=OFF	
439	\$0	
440	LIB *LIBERY	
441	BE	
442	AS 6=*	
443	AS 16-SPDATA	
444		
445		
446	skow	
EOF.		

1	*		SUBPROGRAM IS CALLED 'REFINE'
2	*		THIS SUBPRODGRAM SOLVES SIMULTANEOUS EQUATIONS BY
3	*		THE GAUSSIAN ELIMINATION METHOD AND INCLUDES
4	*		ITERATIVE REFINEMENT
5	*		PIVOTAL CONDENSATION IS ALSO INCORDENTED
4	*		STORE MATRIX
7			
-			
9			
7			
10		22	CUNTINOE
11		11	CONTINUE
12			SK=0
13			N1=N+1
14			CALL GAUSS (SK, N1, N, P, G, P, NN)
15	*		RESTORE ORIGINAL MATRIX
16		2	DO 227 P=1, N
17			X1(P)=X(P)
18			DD 228 G=1, N+1
10			H(P, Q) = D(P, Q)
20		200	CONTINUE
20		220	
21		221	
55	*		RESIDUAL CALCULATION
53			DO 331 P=1, N
24			S1(P)=0
25			DO 332 Q=1, N
26			S1(P)=S1(P)+U(P,Q)*X1(Q)
27		332	CONTINUE
28			RESID(P)=U(P, N+1)-S1(P)
29		331	CONTINUE
30	*		REPLACE U(N+1) COLUMN WITH RESIDUAL
31			DO 333 P=1.N
32			H(P, N+1)=RESTD(P)
22		222	CONTINUE
33		333	
34	*		
35			54=0
36			DO 334 P=1, N
37			X(P)=0
38		334	CONTINUE
39			CALL GAUSS(SK, N1, N, P, Q, P, NN)
40			GOTO 41
41			PRINT'(1X, A, 1X, A, 2X, A)', "APPROX SOLUTION", "REFINEMENT", "SOLUTION"
42		41	DO 335 P=1, N
43			ERRORX(P)=X(P)
44			REFINEDX(P) = X1(P) + ERRORX(P)
45			entn 335
44			PRINTY, X1(P), FRORX(P), REFINEDY(P)
47		225	
40		000	
40	*		
49			
50			
51			U(P,Q) = D(P,Q)
52		445	CONTINUE

53		444	CONTINUE
54			GOTO 78
55	*		NORMALISED DETERMINANT
56			DO 336 P=1, N
57			SD(P)=0 .
58			DO 337 Q=1, N
59			SD(P)=SD(P)+U(P,Q)**2
60		337	CONTINUE
61		336	CONTINUE
62			DO 338 P=1, N
63			DO 339 G=1, N
64			D1(P,Q)=U(P,Q)/SQRT(SD(P))
65		339	CONTINUE
66		338	CONTINUE
67			DO 441 P=1, N
68			DO 442 G=1, N
69			U(P,Q)=D1(P,Q)
70		442	CONTINUE
71		441	CONTINUE
72			SK=1
73			N1=N
74			CALL GAUSS (SK, N1, N, P, Q, P, NN)
75			DET=1
76			DO 443 P=1, N
77			DET=DET*U(P,P)
78		443	CONTINUE
79		78	DET=DET*(-1)**NN

1	-	OBROOTINE GROOD CAR ALL ALL ALL ALL ALL ALL ALL ALL ALL A
2	I	NTEGER N, N1, NN, SK, P, G, P1, G1, G1
3	F	EAL*6 U, D1, X, U1, SP(1:70)
4	c	COMMON/GAUSSMAT/U(1:70, 1:71), D1(1:70, 1:71), X(1:70)
5 *	-	
6	N	IN=0
7	I	0 44 G1=1, N
à		DO 55 P1=01+1, N
		IE (ABS(U(P1, G1)) GT. ABS(U(G1, G1))) THEN
10		
10		DO 44 G=1. N1
11		
12		
13		
14		U(P1, G) = 01
15	66	CONTINUE
16		ELSE
17		ENDIF
18	55	CONTINUE
19		IF (SK. NE. 1) THEN
20 *		DIAGONALISE & STORE MATRIX
21		DO 77 P=Q1, N
22		DO 88 G=G1, N+1
23		D1(P, Q) = U(P, Q) / U(P, Q1)
24	99	CONTINUE
25	77	CONTINUE
25		EI GE
20		DO DO PEI.N
21		DO 112 0-1 N
58		
29		
30	112	CONTINUE
31	99	CONTINUE
32		ENDIF
33 *		
34		DO 114 G1=G1+1, N
35		DC 115 G=1, N1
36		D1(G1, G) = U(G1, G) - U(G1, G) * U(G1, G1) / U(G1, G1)
37	115	CONTINUE
38	114	CONTINUE
39 *		RESTORE MATRIX
40		DO 116 P=1, N
41		DO 127 G=1, N1
42		U(P, Q) = D1(P, Q)
43	127	CONTINUE
44	116	CONTINUE
45		GOTO 44
44		PRINT*, "ELIMINATION=", Q1
47		DO 113 P=1.N
40		PRINTA. "P=". P
40		PRINT+, (1)(P. G), G=1, N1)
47	110	CONTINUE
50	113	
51	44	
52		IF (SA. NE. I) ITEN

ALICE CEL NI

....

53	*		LU DECOMPOSITION
54			FOR P=1, N
55			SP(P)=0
56			X(P)=0
57			END FOR
58			FOR P=N, 1, -1
59			FOR G=N, 1, -1
60			SP(P)=SP(P)+U(P, Q)*X(Q)
61			END FOR
62			X(P)=U(P, N+1)-SP(P)
63			END FOR
64			GOTO 30
65	*		REDUCTION
66	*		STORE MATRIX
67		24	DO 117 P=1, N
58			DO 118 G=1, N1
69			D1(P,Q)=0
70			D1(P, Q)=U(P, Q)
71		118	CONTINUE
72		117	CONTINUE
73			DO 119 G1=1, N-1
74			DO 221 P=1, N-Q1
75			DO 222 G=1, N+1
76			D1(P, G)=U(P, G)-U(P, P+G1)+U(P+G1, G)
77		222	CONTINUE
78		221	CONTINUE
79	*		RESTORE MATRIX
80			DO 223 P=1, N
81			DO 224 G=1, N1
82			U(P, G)=0
83			U(P, Q) = O1(P, Q)
84		224	CONTINUE
85			X(P)=U(P, N+1)
86	-	223	CONTINUE
87		119	CONTINUE
88			GOTO 30
89			PRINT*, "REDUCTION"
90			DO 225 P=1, N
91			PRINT*, "P=", P
92			PRINT*, (U(P, Q), Q=1, N1)
93		225	CONTINUE
94			GOTO 30
95			DO 226 P=1, N
96			PRINT*, "X(P)=", X(P), "P=", P
97		226	CONTINUE
98			ELSE
99		30	ENDIF
100	)	and really	RETURN
101			END
EOF			

# APPENDIX E

## PUBLICATIONS

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Nuclear Instruments and Methods 181 (1981) 5-9 © North-Holland Publishing Company

### THIN TARGET MEASUREMENTS OF PROTON INDUCED L-SHELL X-RAY CROSS-SECTIONS

### R.S. SOKHI and D. CRUMPTON

Physics Department, University of Aston in Birmingham, Gosta Green, Birmingham, B4 7ET, England

Measurements have been made of the L X-ray production from Te, Dy, and Au. Thin targets have been employed and the L Xray yields measured as a function of proton energy up to 3 MeV. From these measurements the total, and where appropriate the individual X-ray line cross-sections have been calculated and compared with the experimental results reported by other authors and with the plane-wave Born approximation with and without binding energy and Coulomb deflection corrections.

## 1. Introduction

The measurement of L-shell cross-sections is important for two main reasons. Firstly, there is a need for a reliable set of L-shell cross-section data for analytical work involving high atomic number elements, and secondly such measurements provide a means of testing the validity of current theories on inner-shell ionization by charged particles. These reasons have resulted in considerable work in this field [1-5]. Earlier work on thick target L-shell cross-section measurements performed at this laboratory has been reported in a previous publication [6]. The present paper reports on thin target measurements of L-shell production cross-sections for Te and Dy using protons of 0.6-3 MeV energy and for Au in the proton energy range of 1.1-3 MeV. Cross-section ratios  $\sigma_{(L\alpha/L\beta)}$ ,  $\sigma_{(L\alpha/L\gamma)}$  and  $\sigma_{(L\alpha/Li)}$  have also been determined for Dy and Au. The experimental data is compared with the PWBA theory, with and without binding energy and Coulomb deflection corrections, and with measurements reported by other authors. The need for an accurate set of related data, such as mass attenuation coefficients, fluorescence yields and Coster-Kronig transitions required for experimental and theoretical calculations is discussed.

## 2. Procedure

#### 2.1. Experimental

A proton beam from the 3 MV Dynamitron accelerator at the Birmingham Radiation Centre was collimated to 1.5 mm diameter and directed on to

thin targets placed at 45° to the beam axis. Target thicknesses typically 50 µg/cm<sup>2</sup> were employed in order to avoid self absorption corrections. A Si(Li) detector with a resolution of 164 eV at 5.898 keV was placed at 90° to the beam axis to detect the characteristic X-rays. The X-rays passed through a 50 µm thick melinex window, 3.2 cm air gap and 12.4 µm thick beryllium detector window before reaching the detector. Beam currents up to 10 nA were used and were measured using a Faraday cup and a Keithley electrometer. The signals from the detector were processed by a pulsed optical feedback preamplifier and then by a spectroscopy amplifier. The shaped pulses were then fed into a 200 MHz ADC of a Hewlett-Packard 5406A computer system which was employed for the data handling.

The  $L_{\alpha}$ ,  $L_{\beta}$  and  $L_{\gamma}$  lines were only resolved for Dy and Au and X-ray counts under the peaks were accumulated until the counts associated with the L, line, the least intense peak of the three, were 200 or more. The background counts under the  $L_{\alpha}$  and  $L_{\beta}$  peaks were negligible compared with characteristic counts under the appropriate peak. For the  $L_{\gamma}$  peak the background was no more than 6% of the characteristic Ly counts. X-ray yields in photons per proton,  $Y_{Li}$ , were measured for the individual lines for Dy and Au. The lines were unresolved for Te and hence the total of the characteristic counts was converted into X-ray yield. Measurements of the X-ray yield were performed in steps of 100 keV at the lower and higher energy region and every 200 keV in the middle energy region to establish the energy dependence accurately.

### I. X-RAY PRODUCTION AND ATTENUATION

## 2.2. Theoretical

The individual L-shell production cross-sections,  $\sigma_{Li}$ , for Dy and Au were derived from the appropriate X-ray yields by employing the following expression:

$$\sigma_{Li} = \frac{Y_{Li}A \ 4\pi}{NC_i \ d\Omega(\rho t) \ \epsilon_i} , \quad (i = \alpha, \beta, \gamma, 1) , \quad (4)$$

where A is the atomic weight of the target, N is Avogadro's number,  $d\Omega$  is the detector solid angle,  $(\rho t)$  is the areal density of the target,  $\epsilon_i$  is the intrinsic efficiency of the Si(Li) detector and  $C_i$  represents the total absorption correction factors for melinex, air and beryllium. Absorption corrections and the detector efficiency were weighted with the appropriate L X-ray relative intensities. These values and any additional data required for the calculation of  $C_i$ and  $\epsilon_i$  were extracted from the tabulations by Storm and Israel [7]. The total L-shell production crosssection,  $\sigma_{Lx}$ , was obtained by summing the individual cross-sections, that is,

$$\sigma_{Lx} = \sigma_{L\alpha} + \sigma_{L\beta} + \sigma_{L\gamma} + \sigma_{Ll}.$$
 (2)

For Te,  $Y_{Li}$  represents the total X-ray yield in photons per proton and in this case expression (1) gives the total production cross-sections.

Theoretical values of the total and individual crosssections for  $L_{\alpha}$ ,  $L_{\beta}$ ,  $L_{\gamma}$  and  $L_{1}$  lines were determined by using the relationships given by Tawara et al. [8]. The values for fluorescence yields and Coster-Kronig transitions were taken from the tables published by Krause [9]. The values for radiative widths were extracted from the tabulation by Scofield [10]. The tabulation of the PWBA calculation by Benka and Kropf [11] was employed to derive the individual subshell ionization cross-sections. Binding energy and Coulomb deflection corrections were calculated from the expressions given by Brandt and Lapicki [12].

#### 3. Experimental uncertainties

The sources of uncertainties associated with measured cross-sections are: (1) the counting statistics, 1-10%, (2) the target thickness, 5% (quoted by the manufacturers), (3) the solid angle, 2% (4) the current measurement, 1% and (5) the absorption corrections and detector efficiency calculations, 6-18%.

The errors in the counting statistics are only important for the  $L_{\gamma}$  and  $L_{1}$  peaks. The maximum

background under the Ly and L1 peaks was 6% and 8% of the characteristic counts respectively. This gives a maximum error of 7.5% and 11% in the counts associated with the Ly and Ly peaks respectively. Factors (2), (3) and (4) appear in the calculations systematically and hence are eliminated in the calculation of the cross-section ratios. The errors in the absorption corrections were due to the uncertainties in the mass-absorption coefficients tabulated by Storm and Israel. They quote an error of 10% for X-ray energies less than 6 keV and 3% for higher enegies. The large uncertainty at the low X-ray region introduces an 18% error in the absorption correction for Te. In the case of Dy and Au this error is reduced to 6% since the X-ray energies are greater than 6 keV. A large error in the mass absorption coefficient, at low X-ray energies, however, introduces no significnat uncertainty in the detector efficiency. Also in this X-ray energy range (3.8-13.4 keV) variation in the silicon crystal thickness has negligible effect on the efficiency calculation.

The total experimental uncertainty in  $\sigma_{Lx}$  for Te was calculated to be 19% for the whole proton energy range. The combined error in  $\sigma_{Lx}$ , associated with eq. (2) varied from 16% for energies above 1 MeV for Dy and 1.4 MeV for Au, to 21% for lower energies. The total uncertainties in  $\sigma_{L\alpha}$  and  $\sigma_{L\beta}$  for both elements were about 8%. For  $\sigma_{L\gamma}$  the total error was determined to be 8% for energies above 1 MeV for Dy and 1.4 MeV for Au. Below these energies the uncertainties increased to 11%. For the  $\sigma_{L1}$  the final error was 9% but increased to 11% below 1 MeV for Dy and 1.6 MeV for Au.

The total uncertainty in the  $\sigma_{(L\alpha/L\beta)}$  ratio remained 9% throughout the energy range. In the case of the  $\sigma_{(L\alpha/L\beta)}$  ratio the uncertainty increased from 9% to 11% at energies below 1 MeV for Dy and 1.4 MeV for Au. The weighted mean of the  $\sigma_{(L\alpha/L1)}$  ratio was determined to a precision of 3% for both elements.

#### 4. Theoretical discrepancies

The use of the tabulated data [9,11] employed in this study has not been reported recently by any other author. This would probably introduce discrepencies between the present PWBA calculations and those reported by other authors [4,6] using less up-to-date data [16,17]. The marked differences between the different sets of data is most obvious in R.S. Sokhi, D. Crumpton / Thin target measurements

the case of fluorescence yields and Coster-Kronig transitions. Krause [9] estimates the uncertainties in his tabulations to be from 3% to 20% in atomic number range of 50-80. Similar uncertainties are quoted by McGuire [16] in his data of fluorescence vields and Coster-Kronig transitions. McGuire also points out the gross differences in experimental and theoretical values. Apart from these internal discrepancies there are large differences between the two sets of data. In the case of Au, for example, the Coster-Kronig transitions differ by nearly 50%. Similar discrepancies occur in the case of other elements. Using the two sets of data independently in the PWBA calculations will obviously yield very different results for the cross-sections. This makes the comparison of experimental data with theoretical prediction more difficult. In light of these discrepancies much care has to be taken when comparing the extent of experimental to theoretical agreement with the work of other authors.

## 5. Results and discussion

The excitation functions for Te, Dy and Au are presented in fig. 1. For all three elements the experimental data generally lies below the theoretical predictions. For Te the difference between the experimental and the PWBA values increases from 17% at 3 MeV to nearly 90% at lower energies. The binding energy and the Coulomb deflection corrections (BC) greatly reduces the disagreement to below 12% for energies above 1.8 MeV and below 21% at lower proton energies. For Dy the BC correction is only about 3% at higher energies but increases to nearly 45% at lower enegies. The agreement with the PWBABC is not better than 25%. Similar characteristics are shown by Au where the BC correction is about 35% at lower energies and the difference between the experimental data and PWBABC varies from 13% to 35% at energies around 1.1 MeV. The present data for Dy and Au lies 18-25% above the data reported by Khan et al. [6] but agrees within experimental uncertainties with the data obtained by Chen et al. [14].

To eliminate systematic uncertainties the ratios  $\sigma_{(L\alpha/L\beta)}$  and  $\sigma_{(L\alpha/L\gamma)}$  were calculated and are presented in figs. 2 and 3 as a function of proton energy. The data for  $\sigma_{(L\alpha/L\beta)}$  decreases slowly with increasing energy as predicted by the PWBA theory. The present data lies systematically higher than the



Fig. 1. Total L X-ray production cross-section as a function of proton energy. Bars represent typical uncertainties.

data obtained by Khan et al. [6] by about 5% for Dy and Au. This difference, however, is within the experimental error. For Au, closer agreement is shown by the data published by Tawara et al. [4]. The BC corrections for Au are important throughout the energy range where as for Dy the corrections are negligible at energies above 1 MeV. The experimental  $\sigma_{(L\alpha/L\gamma)}$  ratio for Dy shows a less sharp increase with decreasing energy than predicted by the PWBA. The predicted maximum for Dy at 0.75 MeV was not observed. The sparse data of Close et al. [13] is well within the experimental errors while the data obtained by Khan et al. [6] differs by up to 20%. The



Fig. 2.  $\sigma(L\alpha/L\beta)$  ratio as a function of proton energy.

**1. X-RAY PRODUCTION AND ATTENUATION** 



Fig. 3.  $\sigma(L\alpha/L\gamma)$  ratio as a function of proton energy.

 $\sigma_{(L\alpha/L\gamma)}$  ratio for Au remains in good agreement with the PWBABC till about 2 MeV, below which the experimental data deviates markedly. Generally the data by Khan et al. [6] and Tawara et al. [4] lie within the experimental errors but deviate at lower energies by about 20%.

The  $\sigma_{(L\alpha/Ll)}$  ratios were also measured and are presented in table 1. The  $\sigma_{(L\alpha/Ll)}$  ratios are independent of the proton energy because the  $L_{\alpha}$  and  $L_{1}$  transitions are to the same subshell,  $L_{III}$ . The experimental values were also found to be constant throughout the energy range. The values for Dy differ from the predicted values by 12% but the predicted ratio for Au lies within the experimental uncertainty. The value for Dy agrees with that obtained by Khan et al. [6] but differs from the value quoted by Abrath [15] by 33%. Exact agreement is found for Au with the value obtained by Khan et al. [6]. The present

Table 1

 $\sigma(L\alpha/L1)$  ratio. Numbers in ( ) represent % errors.

Experimental Ele-Theory ment Ref. Others Present Dy 23.7 26.7 (3) 27 (7)Khan 6 19 (14) Abrath 15 20.3 (3) 19.9 20.3 (3) Khan 6 Au 18.9 (8) Tawara 4 19.7 (5) Chen 14

value lies within the experimental uncertainties quoted by Tawara et al. [4] and Chen et al. [14].

### 6. Conclusion

Reasonable agreement was observed with the previous thick target results obtained by Khan et al. [6] at this laboratory. However, in some areas disagreements do exist.

Generally the differences between the theoretical and experimental values cannot be explained in terms of the experimental uncertainties alone. This highlights the need for more detailed experimental and theoretical studies.

Discrepancies also exist between fluorescence yields and Coster-Kronig transitions published by different authors [9,16].

Errors in the absorption corrections introduce serious uncertainties in the cross-section values. This is mainly due to the lack of reasonably accurate mass absorption coefficient data especially at low X-ray energies. Hubble et al. [18] have also reported serious systematic uncertainties in the absorption correction caused by the large errors in the mass absorption coefficients.

Because of the above problems the accuracy of the X-ray cross-section calculation suffers heavily. This makes detailed comparison of theoretical and experimental data very difficult.

We are most grateful to the staff at the Birmingham Radiation Centre for their assistance with the experimental work. One of us (R.S.S.) also wishes to thank the Science Research Council for supporting this work.

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I. X-RAY PRODUCTION AND ATTENUATION

Nuclear Instruments and Methods 192 (1982) 121-127 North-Holland Publishing Company

## MEASUREMENT OF PROTON-INDUCED L-SHELL X-RAY PRODUCTION CROSS-SECTIONS AND THEIR COMPARISON WITH THEORY

## R.S. SOKHI and D. CRUMPTON

Department of Physics, University of Aston, Birmingham B4 7ET, England

Thin targets of Dy and Pb were bombarded by protons of energy up to 3 MeV and the L-shell X-rays observed were measured as a function of proton energy. The individual X-ray production cross-sections have been derived from these measurements. These, and the cross-section ratios, have been compared with the results reported by other workers and with the CPSSR theory.

#### 1. Introduction

It is clear from the content and number of recent papers [1] on proton-induced X-ray emission (PIXE) analysis that the technique is making a significant contribution to the solution of many analytical problems in a variety of disciplines. Arising out of this has been an increasing requirement for a knowledge of accurate K and L shell proton-induced X-ray production crosssection data. Accurate data is also required for comparison with the predictions of current theories of inner-shell ionization by light ions, in which there is currently considerable interest [2].

In this paper we report on the measurements we have made on the L X-ray emission from thin targets of dysprosium and lead for protons in the energy range 0.6-3 MeV. From these yields the cross-sections  $\sigma_{L\alpha}$ ,  $\sigma_{L\beta}$ ,  $\sigma_{L\gamma}$  and  $\sigma_{L}$  have been derived together with the cross-section ratios  $(\sigma_{L\alpha}/\sigma_{L\beta})$ ,  $(\sigma_{L\alpha}/\sigma_{L\gamma})$  and  $(\sigma_{L\alpha}/\sigma_{L})$ . These measurements were made as part of a comprehensive programme of K and L shell cross-section measurements undertaken at Aston over the last few years [3-5]. The results are compared with the CPSSR theory of Brandt and Lapicki [6].

### 2. Experimental arrangement

The details of the experimental arrangement have been briefly reported in a previous communication [7]. A beam of energetic protons celerator was allowed to impinge on thin targets of dysprosium and lead mounted on a multiple target holder which positioned the targets sequentially at 45° to the incoming beam. Targets employed had areal densities of typically  $50 \,\mu \,\text{g/cm}^2$  and were deposited on polycarbonate backings of areal density 1 mg/cm<sup>2</sup>. The diameter of the targets employed was 1 cm. The proton beam was collimated to give a beam spot of less than 1.5 mm diameter so that the geometry with respect to the X-ray detector could be accurately controlled. Beam currents employed were limited to a few nanoampere thus limiting the current density and preventing target damage. The target chamber was isolated and acted as a Faraday cup so that the current could be accurately measured using a Keithley electrometer. The measured currents were checked from time to time against a calibrated Ortec current digitizer.

from the Universities 3 MV Dynamitron ac-

The X-rays emerged from the target chamber at 90° to the beam direction and passed through a 50  $\mu$ m thick melinex window, 3.2 cm air gap and a 12.4  $\mu$ m thick beryllium detector window before reaching the detector. The Si(Li) detector employed had a working resolution of 164 eV at 5.898 keV and the output from the associated pulsed optical amplifier system was fed to a 200 MHz ADC of a Hewlett-Packard data acquisition and computer system.

An accurately defined aperture was positioned in front of the detector to define the detection solid angle and to ensure that the X-rays im-

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pinged only on the centre of the active area of the silicon crystal. The effective active area of the detector was obtained by scanning a highly collimated X-ray beam across the detector and recording the detector response. The active area was found to be in good agreement with the manufacturers quoted value. In selecting the aperture diameter to define the detection solid angle, due allowance was made for the fact that the detector was positioned several mm's behind the beryllium window. This distance was determined by recording the response of the detector to a point source of X-rays as a function of source-detector separation and then making a  $1/r^2$  plot in the usual manner.

## 3. Measurements

Measurements of the X-ray yield were performed from 0.6 to 3 MeV for dysprosium and from 0.9 to 3 MeV for lead, in steps of 100 keV at the lower and higher energies and every 200 keV in the middle energy region to establish the energy dependence. The  $L_{\alpha}$ ,  $L_{\beta}$ ,  $L_{\gamma}$ , and  $L_{i}$ lines were readily resolved as can be seen in fig. 1, which shows a typical lead spectrum generated by 3 MeV protons. The X-ray accumulation time was selected so that the areas under the  $L_{\gamma}$  peak in the spectrum was at least 200. The area under each peak was obtained using an appropriate software routine to remove the background and integrate the peaks. The background counts un-



X-ray Energy

Fig. 1. Typical Pb L-shell X-ray spectrum produced by 3 MeV protons.

der the  $L_{\alpha}$  and  $L_{\beta}$  peaks were negligible in comparison with the characteristic count. For the  $L_{\gamma}$  peak, backgrounds were typically 3% for lead and 6% for dysprosium.

Assuming isotropic emission of the radiation the individual L-shell X-ray production crosssections,  $\sigma_{\text{L}}$ , were derived from the appropriate X-ray yield per proton,  $Y_{\text{L}}$ , at a proton energy *E* using the relationship:

$$\sigma_{\rm Li}(E) = \frac{Y_{\rm Li}(E)A4\pi}{N_{\rm A}(\rho t) \,\mathrm{d}\Omega C_i \varepsilon_i},\tag{1}$$

where A is the atomic weight of the target,  $N_A$  is Avogadro's number,  $d\Omega$  is the detection solid angle,  $(\rho t)$  is the areal density of the target,  $\varepsilon_i$  is the intrinsic efficiency of the Si(Li) detector and C, represents the total absorption correction factors for melinex, air and beryllium. The mass absorption coefficients employed in the calculation of the absorption corrections and the detector efficiency for each Li X-ray peak were extracted from the tabulation by Storm and Israel [8]. As each of the Li peaks is composed of two or more X-ray lines the absorption coefficients were weighted by the appropriate relative L X-ray line intensities to allow for the hardening of the X-ray spectrum produced by absorption.

## 4. Experimental uncertainties

The uncertainties associated with each of the derived L-shell X-ray production cross-sections,  $\sigma_{Li}$ , are as follows:

(1) the counting statistics associated with the area of each X-ray peak, 1-10%; (2) the beam current measurement, 1%; (3) the detection solid angle, 2%; (4) the target thickness, 5%, as quoted by the suppliers; (5) the absorption corrections and detector efficiency calculations, 6%; and (6) the proton energy.

In the X-ray energy region of interest, 6.4-14.8 keV, the uncertainty in the mass absorption coefficients quoted by Storm and Israel [8] is 3%. This introduces no significant uncertainty in the intrinsic detector efficiency, neither does any variation in the silicon crystal thickness.

The energy calibration of the Dynamitron, which is performed regularly, is known to be

better than 2 keV. This introduces an uncertainty of less than 1% even at low proton energies.

The uncertainties in the first two parameters are random. However, for a particular element although the errors in the parameters (3), (4) and (5) appear systematically in the  $\sigma_{Li}$  calculations. the errors in these parameters are actually random in nature. The uncertainties were therefore, treated as random errors and hence combined quadratically. The total uncertainty in  $\sigma_{L\alpha}$  and  $\sigma_{1,8}$  for both elements was 6-8%. For  $\sigma_{L_y}$  and  $\sigma_{L_y}$ the uncertainties were estimated to be about 8% for energies above 1 MeV, and increasing to 12% below 1 MeV. In general the uncertainties for lead were lower than those for dysprosium by 1-2%.

In the determination of the cross-section ratios the beam current, target thickness and detection solid angle are eliminated together with their uncertainties. The uncertainty in the  $(\sigma_{La}/\sigma_{LB})$ ratio was estimated to be about 8% for lead and 10% for dysprosium throughout the energy range employed. For the  $(\sigma_{La}/\sigma_{Ly})$  and  $(\sigma_{La}/\sigma_{Ll})$ ratios the uncertainties ranged from 9% and 10%, respectively at 3 MeV to 12-14% at energies below 1 MeV.

### 5. Results and discussion

The individual L-shell X-ray production crosssections derived from the measurements are tabulated in table 1 and graphically presented in figs. 2 and 3 with the predictions of the CPSSR theory.

The theoretical values for the individual crosssections  $\sigma_{La}$ ,  $\sigma_{L\beta}$ ,  $\sigma_{L\gamma}$  and  $\sigma_{LI}$  were determined by using the relationships given by Tawara et al. [9] relating the sub-shell ionization cross-sections  $\sigma_{LI}$ ,  $\sigma_{LII}$  and  $\sigma_{LIII}$  to the production cross-sections, namely

$$\sigma_{La} = (\sigma_{LI}f_{13} + \sigma_{LI}f_{12}f_{23} + \sigma_{LII}f_{23} + \sigma_{LII})\omega_{3}F_{3a}; \quad (2)$$

$$\sigma_{L\beta} = \sigma_{L1}\omega_1 F_{1\beta} + (\sigma_{L1}f_{12} + \sigma_{L11})\omega_2 F_{2\beta}$$
$$+ (\sigma_{L1}f_{12} + \sigma_{L11})\omega_2 F_{2\beta} \qquad (3)$$

$$\sigma_{1,\gamma} = \sigma_{1,1}\omega_1 F_{1,\gamma} + (\sigma_{1,1}f_{1,2} + \sigma_{1,1})\omega_2 F_{2,\gamma}; \qquad (4)$$

$$\sigma_{\rm LI} = (\sigma_{\rm LI} f_{13} + \sigma_{\rm LI} f_{12} f_{23} + \sigma_{\rm LII} f_{23} + \sigma_{\rm LII}) \omega_3 F_{31} \,. \tag{5}$$

 $\sigma_{Ly} = \sigma_{LI}\omega_1F_{1y} + (\sigma_{LI}f_{12} + \sigma_{LII})\omega_2F_{2y};$ 

The values of sub-shell fluorescent yields  $\omega_1, \omega_2$ and  $\omega_3$  and the Coster-Kronig yields  $f_{12}$ ,  $f_{13}$  and

Table 1

L-shell X-ray production cross-sections in barns. Numbers in parenthesis represent % uncertainties, which also refer to the lines below. unless stated otherwise.

E (MeV)	Dy				РЬ			
	La	Lø	L,	Li	L,	Lø	L,	L
0.6	3.6 (8)	2.0 (8)	0.25 (12)	0.11 (13)				
0.7	5.5	3.1	0.39	0.22				
0.8	8.0	4.4	0.78	0.34				
0.9	10.7	6.1	0.78	0.30	1.8 (6)	0.91 (6)	0.12 (10)	0.12 (12)
1.0	14	7.9	1.0 (8)	0.35 (9)	2.4	1.3	0.16	0.13
1.1	_	-	-	-	3.2	1.7	0.22	0.20
1.2	20	12	1.6	1.1	4.0	2.1	0.30	0.27
1.4	29	17	2.6	1.0	6.0	3.3	0.45 (7)	0.35 (9)
1.6	38	23	3.3	1.3	8.6	4.6	0.72	0.47
1.8	48	30	4.2	1.8	11.2	5.9	0.97	0.61
2.0	56	36	5.7	2.0	13.9	8.0	1.2	0.68
2.2	68	47	6.4	2.6	19	10.6	1.7	1.0
2.4	80	54	8.1	2.9	23	13.2	1.9	1.2
2.5	86	61	9.6	3.1	25	13.7	2.1	1.3
2.6	90	63	9.3	3.3	27	15	2.2	1.4
2.7	98	70	10.8	3.8	29	17	2.6	1.6
2.8	102	72	11.2	4.1	30	18	2.9	1.7
2.9	106	76	12	3.9	33	19	2.7	2.3
3.0	115	85	13	4.2	35	21	3.3	1.9

R.S. Sokhi, D. Crumpton / L-shell cross-sections



Fig. 2. L-shell X-ray production cross-sections for Dy as a function of proton energy. Bars represent typical uncertainties. Triangles: present work, circles: Khan [5] and solid line: CPSSR [6].

 $f_{23}$  were taken from the internally consistent set of best values presented in the recent publication by Krause [10]. The relative radiative widths Fwere extracted from the compilation of Scofield [11]. The L-subhsell ionization cross-sections were obtained from the CPSSR theory in the manner described by Brandt and Lapicki [6] using the tabulations of Benka and Kropf [12]. Due to the discrepancies that exist in the fluorescent yields and Coster-Kronig yields care must be taken in making comparisons with the experimental work of other authors and theory, as previously discussed [7].

In the energy range 0.9-3 MeV the CPSSR predictions of  $\sigma_{L\sigma}$  are in excellent agreement with the experimental data of both lead and dysprosium. In the case of dysprosium, however, below 1 MeV the data lie systematically above the predicted values. Also there is good agreement in the energy region 1.2-3 MeV be-



Fig. 3. L-shell X-ray production cross-sections for Pb as a function of proton energy. Solid triangles: present work, open triangles: Leite [14] and solid line: CPSSR [6].

tween the  $\sigma_{L\beta}$  data and theory and a measure of agreement in the 1.8–2.6 MeV region for the  $\sigma_{L\gamma}$ . The data for  $\sigma_{L\beta}$  and  $\sigma_{L\gamma}$  cross-sections for lead lie systematically above the predictions of the theory. In the case of the  $\sigma_{Ll}$  cross-sections there is reasonable agreement between the lead data and the theoretical predictions, the dysprosium data, however, lie below the predictions above 1.2 MeV by some 14%. Below 1.2 MeV the statistics associated with the data are rather poor and data is scattered above and below the predicted line.

The  $\sigma_{L\alpha}$ ,  $\sigma_{L\beta}$  and  $\sigma_{L\gamma}$  data for dysprosium derived from a study of thick targets and reported previously by Khan et al. [5] lie systematically below the present data. This discrepancy may be related in a systematic way to the specific energy loss which is required for thick target measurements and clearly warrants further investigations.

For lead the graphical data of Gray et al. [13]

for  $\sigma_{L\alpha}$  appears to be in agreement with the present data, while the tabulated data of Leite et al. [14] is lower than the present data at 3 MeV by 11% but agrees within experimental uncertainty at 1 and 2 MeV. Also included in the tabulation of Leite et al. [14] are the values at 1 and 3 MeV of Bearse et al. [15] and interpolated values at 2 and 3 MeV from the data of Tawara et al. [9]. The values of Bearse et al. [15] are about 25% below the present values while the data of Tawara is 6% higher at 2.0 MeV and 9% lower at 3 MeV.

The measured cross-section ratios  $(\sigma_{La}/\sigma_{L\beta})$ are shown in fig. 4 together with theoretical predictions and the measurements of other authors. The ratios decrease slowly with increasing energy as predicted by the theory and are in agreement with other measurements. The data for lead are, however, 7-10% lower than predicted by the CPSSR theory.

The dysprosium and lead data for the crosssection ratios  $(\sigma_{La}/\sigma_{Lv})$  follow the energy dependence predicted by the CPSSR as shown in fig. 5, but lie systematically below the predictions. The ratio obtained for dysprosium is in reasonable agreement with the sparse data of Close et al. [16] but is less than the data of Khan et al. [5]. The results of Close et al. [16], however, have only been presented graphically



Fig. 4.  $(\sigma_{La}/\sigma_{LB})$  ratio as a function of proton energy. Solid triangles: present work, open circles: Cohen [19], open triangles: Madison [18], solid line: CPSSR [6] and solid circles: Khan [5].



Fig. 5.  $(\sigma_{La}/\sigma_{Ly})$  ratio as a function of proton energy. Solid triangles: present work, open circles: Cohen [19], open triangles: Busch [20], solid circles: Kahn [5] and solid line: CPSSR [6].

in their paper and hence have not been plotted in fig. 5. The precision of the present measurements was such that the theoretically predicted maximum at 0.75 MeV could not be confirmed. The values tabulated by Busch et al. [18] for lead are typically 10-30% higher than the present data, however, the value at 2 MeV reported by Cohen [19] agrees with the present data.

In the case of the  $(\sigma_{La}/\sigma_{Ll})$  ratio a third order polynomial of the form

$$\ln(\sigma_{\rm LI}) = \sum_{i=0}^{3} K_i [\ln(E)]^i;$$

where  $K_i$  are constants and E is the proton energy, was fitted to the  $\sigma_{Ll}$  data for both elements. This was necessary because of the scatter in the  $\sigma_{Ll}$  data at low proton energies, due solely to the poor statistics. The ratios were calculated using the  $\sigma_{Ll}$  values predicted by the polynomials. Within experimental uncertainties the  $(\sigma_{La}/\sigma_{Ll})$  ratios were found to be independent of energy as predicted by theory. The weighted mean values for  $(\sigma_{La}/\sigma_{Ll})$  for dysprosium and lead are given in table 2 together with the results

Table 2 Cross-section ratio  $(\sigma_{La}/\sigma_{Li})$ .

		Experimen	ntal		
Element	Theoretical	Present	Others		Ref.
Dy	23.7	$27.4 \pm 0.8$	19.0 ± 2.7	Abrath	17
			$27 \pm 1.9$	Khan	5
Pb	18.95	$17.3 \pm 0.4$	$19.7 \pm 1.0$	Chen	21
			$19.2 \pm 0.1$	Busch	20
			$17.9 \pm 0.1$	Cohen	19
			$20.9 \pm 0.1$ (thin)	Cohen	19

of other workers. The weighted average of the  $(\sigma_{La}/\sigma_{Li})$  ratios for dysprosium was found to be  $27.4 \pm 0.8$  in good agreement with the value obtained earlier, Khan et al. [5], but differs from the value quoted by Abrath [17] by 30%. The weighted average of  $(\sigma_{1a}/\sigma_{1i})$  for lead was found to be  $17.3 \pm 0.4$  in good agreement with the value obtained by Cohen [19] using thick targets. The values reported by Cohen [19], from his thin target measurements, and Chen et al. [21] are respectively 21% and 14% higher than the present value. With the precision achieved in the present work there was no evidence of a minimum in the ratio between 0.5 and 2 MeV, as reported by Busch et al. [20]. Above 3 MeV the ratio was reported to be constant and equal to  $19.2 \pm 0.1$ . Cohen [19] and Chen et al. [21] both report that their data are consistent with a constant value for  $(\sigma_{La}/\sigma_{Li})$ .

## 6. Conclusions

It must be borne in mind that inherent in any procedure adopted for the comparison of theory with experiment is the difficulty that the theoretical predictions contain the uncertainties associated with the fluorescence yields and Coster-Kronig yields through the use of eqs. (2)-(5). An alternative approach is to derive from the experimental data values for the sub-shell ionization cross-sections  $\sigma_{LI}$ ,  $\sigma_{LII}$  and  $\sigma_{LIII}$  which can then be compared directly with the theoretical predictions. This approach, however has an additional difficulty since the solution of eqs. (2)-(5) for  $\sigma_{LI}$ ,  $\sigma_{LII}$  and  $\sigma_{LIII}$  invariably results in a set of ill-conditioned equations, in as much as small changes in the experimental data can produce large changes in the predicted values of the sub-shell ionization cross-sections, leading to physically unmeaningful results. A comparison of experimental data then becomes exceedingly difficult. Alternatively one has to employ semiresolved peaks which are often of poor precision.

It clearly would be helpful if experimentalists would present their experimentally measured production cross-section data in addition to any other data they might wish to present. Discrepancies between experimental data could then be easily identified and an accurate set of data eventually established. A more realistic approach to the comparison of experiment and theory would eventually be possible.

We are most grateful to the staff at the Birmingham Radiation Centre for their assistance with the experimental work. One of us (R.S.S.) also wishes to thank the Science Research Council for supporting this work.

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## ATOMIC DATA AND NUCLEAR DATA TABLES 30, 49-124 (1984)

## EXPERIMENTAL L-SHELL X-RAY PRODUCTION AND IONIZATION CROSS SECTIONS FOR PROTON IMPACT

#### R. S. SOKHI and D. CRUMPTON

Department of Physics, University of Aston Birmingham B4 7ET, England

Cross sections for L-shell x-ray production and ionization by protons are tabulated according to target atomic number, target type, and incident proton energy. Cross sections for production of the individual L-shell component x-rays and for ionization of the three L subshells are presented separately. Ratios of  $L\alpha$  to Ll x-ray production cross sections are also listed. Literature is covered from 1975 to November 1982. Experimental details pertaining to the cross-section measurements and the theoretical models employed by the experimenters for comparison with their data are included. It is intended that this information will help the reader to ascertain the most reliable cross-section values without recourse to the literature.

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L-Sheil Cross Sections for Protons

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### INTRODUCTION

#### General Remarks

Considerable effort has been directed in recent years to the study of inner-shell ionization of atoms by charged particles. Progress has been achieved not only in the realms, of theoretical studies<sup>1,2</sup> but also in the field of applications of this phenomenon.<sup>3</sup> A substantial portion of this effort has been devoted to the application of x-rays resulting from inner-shell ionization by protons to trace elemental analysis, and consequently proton-induced x-ray emission analysis has become established as a versatile multitrace elemental analytic tool.<sup>3,4</sup>

As a result of this effort a considerable amount of L-sheil x-ray production cross-section data for proton impact is now available in the literature. Several authors have also derived L-shell ionization cross sections from their x-ray production cross-section measurements. The procedures for achieving this require appropriate values for fluorescence yields, Coster-Kronig yields, and radiative rates for the L shell. The first two quantities have been tabulated by Bambynek et al.<sup>5</sup> and McGuire<sup>5</sup> and more recently by Krause.<sup>7</sup> The radiative rates have been tabulated by Scofield.<sup>8</sup>

This tabulation presents L-shell x-ray production and ionization cross sections separately according to target atomic number, target type, and incident proton energy. Tables containing experimental details have also been presented for each reference quoted. As far as we are aware all x-ray production and iorization cross-section data that are available in tabular form, either in the literature or directly from authors, from 1975 through November 1982 have been included.

#### Relation to Other Tables

Previous tabulations of inner-shell ionization and x-ray production cross sections for charged particle impact9-11 have tended to quote total cross sections only, which are of limited value to the analyst and the theoretician. The present work contains, wherever possible, individual transition group x-ray production and ionization subshell cross sections. Experimental details, which have been sparse in previous works, have also been presented in the tables. The previous tabulation on L-shell x-ray production cross sections by Hardt and Watson<sup>11</sup> presented data for several charged particles; the present work however, concentrates solely on proton impact and consequently is more detailed. In general, references covered by Hardt and Watson11 have been omitted from this work, although there is occasional overlap because in a small number of cases already referenced by Hardt and Watson,11 individual transition group x-ray production cross sections became available. Since the above authors had frequently quoted only the total cross sections it was decided to include the individual cross sections in full.

#### Possible Users and General Policy

This tabulation is intended to be of use both to the analyst involved in the application of proton-induced xray emission analysis and to the theoretician studying light ion-atom collisions. To the theoretician both x-ray production and ionization cross sections are of importance, while to the analyst only the former is of interest. With these two requirements in mind the cross sections have been tabulated separately. The cross sections have also been segregated, wherever necessary, according to gas and solid targets; the latter is further subdivided into thin, semithick, and thick. This has been done because the data require stopping-power corrections to varying degrees depending on the type of target.

"Experimental details" tables have been presented not only to provide a source for comparison of procedures adopted by different laboratories but also as an aid to the reader in deciding the "best" cross-section values to use. As far as possible this compilation has been formulated to be self-explanatory for the most part; however, a comprehensive section, Explanation of Tables and Policies, has been included for completeness.

It is hoped that this tabulation will offer an overview of this field and be of some assistance in determining future research directions.

#### Data Sources and Presentation

References for the cross sections were obtained by computer and manual searches of the literature. An online information retrieval service was employed with the data base INSPEC<sup>12</sup> containing science abstracts. Tabular cross-section data were then collected from the literature or acquired by correspondence with the authors. Several attempts were made where contact had proven difficult. In the few instances where only graphical data were available the references were omitted. The combined experimental results for the *L*-shell x-ray production and ionization cross sections, respectively, are listed by element in Tables AII and BII.

Experimental details and the theories<sup>13-33</sup> used for comparison with the experimental results were extracted from each reference. They are given for each element in Tables AI and BI, immediately preceding the corresponding cross-section tables. In Table AIII we list the ratio  $L\alpha/Ll$  for each experiment, if available. Where authors had not specifically quoted the  $L\alpha/Ll$  cross-section ratios, they were computed from the individual  $L\alpha$  and Ll cross sections.

Experimental errors on the cross sections are given in Tables AI and BI, respectively. In Tables AII and BII, experimental errors are not given directly. Instead, we have adopted the policy of indicating the typical uncerL-Shell Cross Sections for Protons

tainty by restricting the number of significant figures as follows:

(i) For cross-section values <0.5b three decimal places are quoted.

(ii) For values ≥0.5b and <5.0b two decimal places are quoted.

(iii) For values  $\geq 5.0b$  and < 50b one decimal place is quoted.

(iv) For values ≥50b no decimal places are quoted.

#### Acknowledgment

One of us (R.S.S.) wishes to thank the Science and Engineering Research Council for supporting this work.

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## **EXPLANATION OF TABLES AND POLICIES**

## TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

TABLE AI	Experimental Details
REF	Publication reference
ENERGY	Incident proton beam energy range in MeV
RANGE	
AREAL	Target areal density. E-6G/CMSQ is equivalent to $\mu g/$
DENSITY	$cm^2$ and $+-$ is equivalent to $\pm$ . Wherever the
	areal densities were not quoted by the expen-
	menters, targets have been classified into GAS,
	THIN, SEMI-THICK, AND THICK.
BEAM	Incident proton beam current in Amperes (A). Ex-
CURRENT	ponential notation is used: $10E-9 \equiv 10 \times 10^{-3}$ .
BEAM	(B) Incident proton beam diameter in mm. (C) Ap-
COLL	erture size in mm of the final collimator. Aperture
	size is presented wherever the beam diameter was
FVD	not available.
EXP	Percentage experimental uncertainties in the cross-
ERROR	section values. wherever the uncertainty is not
	constant at different proton energies, the mini-
	have been shown
TATE	La La La Ll La and total L-shell x-ray production
LA, LD,	cross sections, respectively, I G 8-12 indicates an
LO, LL, IF IT	uncertainty of 8 to $12\%$ in the $L_{\infty}$ cross sections
IX	This notation is used wherever the experimenter has
LA	generalized the uncertainties in all the <i>I</i> transi-
	tions to a single value.
THEORIES	Theories employed by the experimenter for compar-
	ison with his measured data. Reference numbers
	refer to those given in the Introduction.
BEA	Binary-encounter approximation
BEA (G1)	Garcia et al., 1967 <sup>13</sup>
BEA (G2)	Garcia, 1970 <sup>14</sup>
BEA (G3)	Garcia et al., 1973 <sup>15</sup>
BEA (G4)	Garcia, 1970 <sup>16</sup>
BEA (V)	Vriens and Bonsen, 1968 <sup>17</sup>
BEA (H)	Hansen, 1973 <sup>18</sup>
BEA (M)	McGuire and Omidvar, 1974 <sup>19</sup>
CBEA	Constrained binary-encounter approximation <sup>18</sup>
SCA	Semiclassical approximation
SCA1	Hansteen and Mosebekk, 1973 <sup>20</sup>
SCA2	Hansteen et al., 1975 <sup>21</sup>
RSCA	Amundsen, 1977 <sup>22</sup>
PWBA	Plane wave Born approximation
PWBA1	Merzbacher and Lewis, 195823
PWBA2	Khandelwal et al., 1969-
PWBA3	Choi et al., 19/3-
PWBA4	Benka and Kropi, 19/8
PWBA5	Pepper, 19/4-
PWBAR	PWBA with relativistic corrections

PWBABC PWBABTR	PWBA with binding energy and Coulomb corrections <sup>29</sup> PWBA with binding energy, trajectory, and relativistic
IDW/DAD	PWBA with relativistic corrections by Ishii et al. <sup>30</sup>
IPWBABCR	PWBA with binding energy, Coulomb, and relativistic corrections by Ishii et al. <sup>30</sup>
MPWBABCR	As above except by Merzbacher and Lewis <sup>23</sup>
PWBABCR	PWBA with binding energy, Coulomb, and relativistic corrections <sup>28</sup>
RPWBABC	As above, Mukoyama and Sarkadi <sup>31</sup>
PSS	Perturbed stationary state <sup>29</sup>
PSSR	PSS with relativistic corrections <sup>32</sup>
CPSSR	PSS with Coulomb and relativistic corrections <sup>28</sup>
ECPSSR	PSS with Coulomb, relativistic, and energy loss cor- rections <sup>33</sup>
COMMENTS	Comments in this column refer to the experimental setup and the procedure adopted by the experi- menter. The comments are, in general, self-ex- planatory; however, a few less obvious ones are explained below:
RBS EMPLOYED	Rutherford backscattering spectrometry employed to determine the target thickness and/or to monitor
	the beam current
EFFICIENCY MEASURED/	This indicates whether the efficiency of the x-ray de- tector was measured or calculated.
Si(Li)	Lithium-drifted silicon detector, mentioned only when other detectors were also used
BETA $(2 + 15)$	LB215
GAMMA (1)	Ly
TABLE AII	Experimental X-Ray Production Cross Sections
	For many elements only the total L-shell cross sections were available. Cross sections, in barns, have been tabulated separately for GAS, THIN, SEMI- THICK and THICK targets.
ENERGY	Incident proton beam energy in MeV
ALPHA.	L-shell x-ray production cross sections, in barns, for
BETA.	the $L\alpha$ , $L\beta$ , $L\gamma$ , $Ll$ , and $L\eta$ transitions. $L\alpha$ , $L\beta$ ,
GAMMA, L,	and $L\gamma$ are transition groups and wherever the
ETA	experimenter had quoted cross sections for in-
	dividual transitions belonging to one group they
	were summed to give the total cross section for
	each group. For cross-section values less than 0.01
	barn the following exponential notation is employed: $8.1\text{E-}03 = 8.1 \times 10^{-3}$ .
TOTAL	Total L-shell x-ray production cross section in barns.
	Wherever the total cross section was not specif-
	ically quoted it was obtained by summing the individual cross sections.
REF	Publication reference. Wherever the reference has been
	omitted the preceding reference applies.

L-Shell Cross Sections for Protons

TABLE AIII

LALPHA/LL Ratios

ENERGY RANGE TARGET LA/LL REF

TABLE BI

ENERGY

BEAM

BEAM

EXP

COLL

ERROR

L1. L2. L3. LT

R1, R2

RANGE AREAL

DENSITY

REF

Incident proton energy range in MeV

Targets classified as THIN or THICK. Ratio of La to Ll x-ray production cross sections Publication reference

## TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

Values of the ionization cross sections are taken directly as given in the respective references. In deriving L-shell ionization cross sections from x-ray production data, authors typically used atomic parameters from Refs. 5-8. Where Refs. 5-8 have not been employed, this is noted in the COM-MENTS in BI. Experimental Details Publication reference Incident proton beam energy range in MeV Target areal density E-6G/CMSQ is equivalent to  $\mu$ g/cm<sup>2</sup> and +- is equivalent to ±. Wherever the areal densities were not quoted by the experimenters, targets have been classified as THIN and THICK. Incident proton beam current in Amperes (A). Exponential notation is used:  $10E-9 = 10 \times 10^{-9}$ . CURRENT

- (B) Incident proton beam diameter in mm. (C) Aperture size in mm of the final collimator. This has been presented wherever the beam diameter was not available.
- Percentage experimental uncertainties in the cross section values and ratios. Wherever the uncertainty is not constant at different proton energies, the minimum and maximum percentage uncertainties have been shown.
- 2s1/2, 2p1/2 and 2p3/2 L-subshell and total L-shell ionization cross sections, respectively
- Ratios of  $2s_{1/2}$  to  $2p_{1/2}$  and of  $2s_{1/2}$  to  $2p_{3/2}$  subshell ionization cross sections, respectively. R1 22-28 therefore indicates a range of uncertainties of 22 to 28% in the ratio R1.

THEORIES COMMENTS

- See Explanations for Table AI
- See Explanations for Table AI

TABLE BII	Experimental Ionization Cross Sections					
	Total L-shell ionization cross sections have been tab- ulated wherever the subshell cross sections were not available. Cross section, in barns, have been tabulated separately for THIN and THICK targets.					
L1, L2, L3	$2s_{1/2}$ , $2p_{1/2}$ and $2p_{3/2}$ subshell ionization cross sections, in barns, respectively					
L1/L2 L1/L3	Ratio of $2s_{1/2}$ to $2p_{1/2}$ and $2s_{1/2}$ to $2p_{3/2}$ subshell cross - sections, respectively					
TOTAL	Total L-shell ionization cross sections in barns. Wher- ever the total cross section was not specifically quoted it was obtained by summing the individual subshell cross sections.					
REF	Publication reference. Wherever the reference has been omitted the preceding reference applies.					

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Z=18 ARGON(AR) TABLE AI EXPERIMENTAL DETAILS ENERGY AREAL BEAM BEAM EXP RANGE DENSITY CURRENT COLL ERROR MeV E-6G/CMSQ A mm % REF THEORIES COMMENTS 10E-6 2.0(B) LT 11 LANA75 .028-.5 GAS SQUARE BEAM. PROPORTIONAL COUNTER USED. EFFICIENCY PWBA3 PWBABC MEASURED. L2 AND L3 SUBSHELL X-RAYS MEASURED. FLUORESCENCE YIELD MEASURED. e- H2+ He+ He2+ IMPACT STUDIED.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

GAS TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY Mev	TOTAL BARNS	REF
.0280 .0373 .0483 .0580 .0676 .0773 .0870 .0966 .1060 .1160 .1200	82 139 222 296 365 427 498 561 650 764	LANA75	.1250 .1260 .1350 .1500 .1700 .2000 .2500 .3000 .4000 .5000	823 815 860 990 1150 1300 1570 1730 2090 2270	LANA75

## Z=28 NICKEL(NI)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
PETV80	.0745	THICK	•	-	LT 25	PWBA 1	PROPORTIONAL COUNTER USED. EFFICIENCY

MEASURED.

Z=28 NICKEL(NI) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THICK TARGET

1

ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	TOTAL BARNS	REF
.070 .085 .100 .140 .165 .200	37.0 53 71 113 159 203	PETV80	.250 .300 .350 .400 .450	255 345 431 504 621	PETV80

Z=29 COPPER(CU)

TABLE	AI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
ETV80	.0745	THICK	-	-	LT 25	PWBA1	PROPORTIONAL COUNTER USED. EFFICIENCY MEASURED.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS . THICK TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY Mev	TOTAL	REF
.070 .085 .100 .120 .140 .165	20.0 32.5 50 63 105 165	PETV80	.200 .250 .300 .350 .400 .450	213 276 388 497 637 769	PETV80

## Z=30 ZINC(ZN)

TABLE	AI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
PETV80	.0745	THICK	-	-	LT 25	PWBA 1	PROPORTIONAL COUNTER USED. EFFICIENCY MEASURED.

REF

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

## Z=30 ZINC(ZN) CONTINUED

TABLE AIL EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THICK TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY Mev	TOTAL BARNS	REF
.070 .085 .100 .120 .140 .165	17.4 27.1 45.3 64 106 163	PETV80	.200 .250 .300 .350 .400 .450	241 313 460 616 787 976	PETV80

## Z=37 RUBIDIUM(RB)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
ILM76	.950	60		2.0(B)	LT 15	BEA(G3)	SQUARE BEAM. RBS EMPLOYED. EFFICIENCY CALCULATED. RbCl TARGET OF CARBON BACKING

TABLE AIL EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS THIN TARGET TOTAL REF BARNS ENERGY MeV TOTAL ENERGY MeV

.95 .405 MILM76

## Z=38 STRONTIUM(SR)

TABLE	AI		EXPERIMEN	TAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
30NG78	3.0	THIN	-	•	LT 8	BEA(G3)	RBS EMPOLYED. EFFICIENCY MEASURED. K-SHELL STUDIED. METAL TARGET ON CARBON BACKING.
TABLE	AII EXP	ERIMENTAL 3	-RAY PROD	UCTION	CROSS S	SECTIONS	
THIN T.	ARGET						
ENERGY MeV	TOTA	L RI	EF	ENI	ERGY	TOTAL BARNS	REF

3.00 1667 BONG78

548

Z=39 YTTRIUM(Y)

			PYDERTME	NTAL DE	PATIS		
TADLE A	-		DATERINE	ALAL DE			
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
MILM76	.950	70	-	2.0(B)	LT 15	BEA(G3)	SQUARE BEAM. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING.
SERK80 2.	92-39.34	24	•	•	LT 12	BEA(V) PWBA3 PWBA4	RBS EMPLOYED. Metal target on Mylar Backing.
TABLE A	II EXPE	ERIMENTAL 3	K-RAY PRO	DUCTION	CROSS	SECTIONS	
THIN TA	RGET						
ENERGY MeV	TOTAL	RI	EF	EN M	ERGY ev	TOTAL BARNS	REF
.95 2.92 3.97 6.13 12.31	350 1410 1490 1490 1130	MI Se	LM76 RK80	18 24 30 39	.12 .21 .52 .34	937 802 672 537	SERK80
<u>Z=40 ZI</u>	RCONIUM	<u>ZR)</u>					
TABLE A	I		EXPERIME	NTAL DE	TAILS		
REF	ENERGY - RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
KROA82 .1	015742;	2 110+-2 THICK	-	-	LT 16-	18 CPSSR	CRYSTAL SPECTROMETER AND SI(LI) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING. ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET
TABLE A	II EXP	ERIMENTAL	X-RAY PRO	DUCTION	CROSS	SECTIONS	

THIN TARGET

 
 ENERGY MeV
 TOTAL BARNS
 REF
 ENERGY MeV
 TOTAL BARNS
 REF

 .1015
 1.69
 KROA82
 .3179
 61
 KROA82

 .1334
 5.7
 .3991
 104

 .1638
 9.5
 .4903
 145

 .2051
 19.3
 .6011
 223

 .2566
 41.3
 .7422
 334

Z=40 ZIRCONIUM(ZR) CONTINUED

TABLE	AIII	LALPHA/LL	RATIO

ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE MeV	TARGET	LA/LL	REF
0.5	THICK	24.4*	KROA82	0.5	THICK	25.41	KROA82
* Si(L	1) DETECTOR	USED	. CRYSTAL	SPECTRO	METER USE	n	

Z=41 NIOBIUM(NB)

TABL	E AI	-	EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
ROA82	.09167459	55+-3 THICK	-	-	LT 15-17	CPSSR	CRYSTAL SPECTROMETER AND SI(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING. ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS THIN TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY Mev	TOTAL BARNS	REF
.0916 .1115 .1417 .1723 .2129 .2634	.88 1.96 4.58 9.5 17.1 28.4	KROA82	.3239 .4044 .4951 .6058 .7459	46.6 78 121 177 258	KROA82

TABLE AITI

LALPHA/LL RATIO

ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
0.5	THICK	47.2*	KROA82	0.5	THICK	25.21	KROA82
• S1(L	i) DETECTOR	USED	+ CRYSTAL	SPECTRO	METER USE	D.	

## Z=42 MOLYBDENUM(MO)

TABLE	AI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
ETV80	.2-1.05	THICK	-	-	LT 25	PWBA 1	PROPORTIONAL COUNTER USED. EFFICIENCY MEASURED.

TABLE AIL EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THICK TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	TOTAL BARNS	REF
.20 .25 .30 .35 .40 .45	7.4 13.5 23.0 34.0 47.0 59	PETV80	.55 .65 .75 .85 .95 1.05	95 143 194 245 316 347	PETV80

Z=45 RHODIUM(RH)

TABLE	AI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
PETV80	.245	THICK	-	•	LT 25	PWBA 1	PROPORTIONAL COUNTER USED. EFFICIENCY MEASURED.
(ROA82	.09744	88+-5 THICK		•	LT 15-1	19 CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING. ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET.

TABLE AIL EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY Mev	TOTAL BARNS	REF
.0900 .1096 .1393 .1696 .2100	.247 .65 1.78 3.65 7.8	KROA82	.3211 .4019 .4925 .6031 .7440	24.8 42.3 69 104 156	KROA82

## Z=45 RHODIUM(RH) CONTINUED

TABLE	AII	EXPERIMENTAL	X-RAY	PRODUCTION	CROSS	SECTIONS	CONTINUED
THICK	TARGE	T					

ENERGY MeV	TOTAL BARNS	REF	ENERGY Me V	TOTAL BARNS	REF
.20 .25 .30	4.48 7.8 12.5	PETVSO	.35 .40 .45	18.9 29.0 45.4	PETV80

#### TABLE AIII

LALPHA/LL RATIO

ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE MeV	TARGET	LA/LL	REF
0.5	THICK THICK	34.5* 25.0†	KROA82	0.5	THIN	30.0+-2.1*	KROA82

• SI(L1) DETECTOR USED + CRYSTAL SPECTROMETER USED.

## Z=46 PALLADIUM(PD)

TABLE	AI		EXPERIMEN	TAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
CHAR75	3-12	21+-2	-	-	LT 20	BEA(G3) PWBA3	RBS EMPLOYED. EFFICIENCY CALCULATED. 05+ IMPACT STUDIED. METAL TARGET ON CARBON BACKING.
PETV80	.245	THICK	-	-	LT 25	PWBA1	PROPORTIONAL COUNTER USED. EFFICIENCY MEASURED.
KROA82	.097438	99+-6 THICK	-	-	LT 15-2	O CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING. ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET.

## Z=46 PALLADIUM(PD) CONTINUED

TABLE AIL EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY Mev	TOTAL BARNS	REF
.0900 .1093 .1389 .1692 .2094 .2601 .3207 .4015 .4920 .6026 .7438	.192 .52 1.49 3.02 6.5 12.3 22.3 37.8 60 94 137	KROA82	3.0000 4.0000 5.0000 7.0000 8.0000 9.0000 10.0000 11.0000 12.0000	1728 2208 2016 2496 2544 2640 2640 2688 2488 2488 2208	CHAR75
THICK T	RGET				
ENERGY	TOTAL	REF	ENERGY	TOTAL	REF

ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	TOTAL BARNS	REF
.20 .25 .30	3.72 7.5 12.1	PETV80	.35 .40 .45	18.0 28.0 44.0	PETV80

TABLE AIII

LALPHA/LL RATIO

ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
0.5	THICK THICK	31.1* 25.4†	KROA82	0.5	THIN	32.2+-2.4*	KROA82

• S1(L1) DETECTOR USED + CRYSTAL SPECTROMETER USED.

## Z=47 SILVER(AG)

TABLE AI

EXPERIMENTAL DETAILS

REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
CHAR75	3-12	22+-2	-	-	LT 20	BEA(G3) PWBA3	RBS EMPLOYED. EFFICIENCY CALCULATED. 05+ IMPACT STUDIED. METAL TARGET ON CARBON BACKING.
MILM76	.950	70		2.0(B)	LT 10	BEA(G3)	SQUARE BEAM. RBS EMPLOYED. EFFICIENCY CALCULATED. AgC1 TARGET ON CARBON BACKING.

Z=47 SILVER(AG) CONTINUED

TABLE	AI		EXPERIME	NTAL DE	TAILS CO	ONTINUED	
REF	ENERGY RANGE . Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BADT78	4.0	66+-3	1-5E-9	-	LT 9	BEA(G3) PWBA2	EFFICIENCY MEASURED. K-SHELL STUDIED. METAL TARGET ON MYLAR BACKING.
BONG78	3.0	THIN	-	•	LT 7	BEA(G3)	RBS EMPOLYED. EFFICIENCY MEASURED. K-SHELL STUDIED. SELF-SUPPORTING METAL TARGET.
LAPG80	.035300	THICK		-	LT 25-50	D PWBA ECPSSR	H2 AND He4 IMPACT STUDIED. K-SHELL STUDIED. COULOMB DEFLECTION FACTOR DEDUCED.
BAUC81	.3-4 .249-1.91	65+-5 THICK	.5-50E-9 2-500E-9	1.1(B)	LT 14 LT 25	CPSSR	RBS EMPLOYED. EFFICIENCY MEASURED. SELF-SUPPORTING METAL TARGET. He4 N2+ Ne3+ IMPACT STUDIED.
CUZP81	.611-3.85	THIN		-	LT 5-11	BEA(H) SCA2 PWBA3	EFFICIENCY MEASURED. AgIO3 TARGET ON CARBON BACKING. CROSS SECTIONS EVALUATED BY NORMALIZING TO K-SHELL DATA.
SARW8 1	.2540	100+-5 67+-3	3-100E-9	1.0(B)	LA 15 LT 15	PWBABC PWBABCR ECPSSR	RBS EMPLOYED. EFFICIENCY MEASURED. TWO TARGETS USED.
KROA82 .	1397744	95+-3 THICK		*	LT 16	CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING. ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET ENERGY ALPHA BETA GAMMA ETA TOTAL REF L MeV BARNS : .1397 - -.1697 - -.2102 - -: : 1.13 2.43 5.3 KROA82 -

Z=47 SILVER(AG) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.2500	4 86						
2608	4.00			-	-	9.8	SARW81
2000			-		-	10.3	KROA82
. 3000	9.9	-		-	-	18.6	SARW81
. 3000	-	-		-	-	9.2	BAUC81
- 3214	-	-	-	-	-	18.0	KROA82
. 3500	15.2	-	-	-	-	26.9	SARWA1
.4000	19.2	-	-			36.8	SANGOI
.4020	-	-	-	-		21 7	FROM 80
. 4925	-	-	-			51.1	KAUN02
.5000	-	-	-			24 2	
.6034	-	-			-	34.3	BAUCSI
.6110	-				-	80	KROA82
.6500					-	158	CUZP81
7440					-	74	BAUC81
8000					-	126	KROA82
					-	102	BAUC81
.0110		-	-	-		322	CUZP81
.9500	•		-	-	-	278	MILM76
1.0000	-	-	-	-	-	162	BAUCAI
1.0190	-	-	-	-	-	468	CIIZ P8 1
1.2000	-	-	-	-	-	599	000101
1.4000	-	-	-	-		756	
1.6000	-		-	-	1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 - 1994 -	786	
1.8000	-	-				007	
2.0000	-	-			-	907	
2.0000			State in	-	-	4//	BAUCSI
2.2000	-			-	-	1130	CUZP81
2.4000				-	-	1090	
2.6000	2		-	-	-	1200	
2 8000			-	-	-	1340	
2.0000	-		•	-	-	1580	
3.0000		-	-	-	-	1530	
3.0000	-	-	-	-	-	1620	CHAR75
3.0000	1.7.1	-	-	-	-	950	BONG78
3.2000	-	-	-	-	-	1670	CUZP81
3.4000	-	-	-	-		1690	
3.6000	-	-		-	_	1820	
3.8000	-	-				1810	
3.8500	-	-			-	1800	
4.0000	-				-	1000	
4.0000	_			-	-	2100	CHAR75
4.0000				-	-	1000	BADT78
5.0000			-		-	690	BAUC81
6 0000		-	-	-	-	2376	CHAR75
7 0000	-	-	-	-	-	2646	
8.0000		-	•	-	-	2646	
0.0000	-	-	-	-	-	2484	
9.0000	-	-	-	-	-	2484	
10.0000	•	-	-	-	-	2484	
11.0000	-	-	-	-	-	2322	
12.0000	-	-	-	-	-	2160	

## THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL REF	
MeV			BARNS				
.035		-	-	12		1. 3F-05 1 APC80	
.040	-	-	-	-	-	9.1E-05	
.045	-	-	-	-	-	4.4E-04	
.050	-	-		-	-	1.4E-03	
.055	-	-	-	-	-	3.4E-03	
.060	-	-		-	-	7.2E-03	
.070	-	-	-	-	-	.027	
.080	-	-	-	-	-	.059	
.090	-	-	-	-		120	

R. S. SOKHI and D. CRUMPTON L-Shell Cross Sections for Protons

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

## Z=47 SILVER(AG) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
. 100	-				2. S. S.	240	1.10080
.110	-	_				.240	LAPGOU
. 120	-		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-	. 300	
.130				-	-		
.140	-			-	-	.02	
. 150				-	-	1.10	
160			-	-	-	1.40	
180		-	•	-	-	1.90	
200	-	-	-	-	-	2.80	
.200	-	· · · · · · · · · · · · · · · · · · ·	-	-	-	3.60	
.220	-	-		-	-	4.80	
.240	-	-	•	-	-	6.1	
.249	-	-	-	-	-	7.6	BAUC81
.260	-	-		-	-	7.2	LAPG80
.280	•		-		-	9.0	
.300	-		-	-	-	12.0	BAUC81
.300		-	-	-	-	11.1	LAPC80
.353	-	-	-	-	-	17.3	BAUCS1
.403	-	-	-	_	-	22 8	DAGCOT
.484	-	-	-	_		22.6	
.552	-	-				111 2	
.635	-	-				50	
.720	-	-				29	
.810		-		-		11	
900						100	
1 100						125	
1 200	-	-		-	-	187	
520			-	-		242	
1.720		-	•		-	304	
. 720		-		-	-	350	
1.910	-		-	-	-	381	

TABLE AIII

#### LALPHA/LL RATIO

ENERGY RANGE MeV	TARGET	LA/LL	,	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
0.5	THICK THICK	30.4* 25.1†		KROA82	0.5	THIN	28.8+-2.0*	KROA82

\* Si(L1) DETECTOR USED + CRYSTAL SPECTROMETER USED.

Z=48 CADMIUM(CD)

TABLE AI

EXPERIMENTAL DETAILS

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BONG78	3.0	THIN	-	-	LT 8	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED. K-SHELL STUDIED

METAL TARGET ON CARBON BACKING.

Z=48 CADMIUM(CD) CONTINUED

TABLE	IA 3		EXPERIME	NTAL DET	TAILS	CONTINUED	
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
PETV80	.0745	THICK	-	·	LT 25	PWBA1	PROPORTIONAL Counter Used. Efficiency Measured.
СНМЈ8 1	.1242	32+-2 26+-2	-	-	LT 15	-17 PWBA3 CPSSR	HP GE DETECTOR USED. RBS EMPLOYED. EFFICIENCY MEASURED. TWO METAL TARGETS ON CARBON BACKING USED. ALPHA/BETA ALPHA/GAMMA AND BETA/GAMMA INTENSITY RATIOS PRESENTED.
SARW81	.2540	79+-4	3-100E-9	1.0(B)	LA 15 LT 15	PWBABC PWBABCR ECPSSR	RBS EMPLOYED. EFFICIENCY MEASURED.
KROA82	.13727422	126+-4 THICK		-	LT 14	-16 CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON VITRIOUS CARBON BACKING. ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
1200			-	-	-	.262	CHMJ81
1272				-	-	.79	KROA82
1400				_	-	.53	CHMJ81
. 1400	-	- 24				.83	
. 1600	-	-				1 76	KROA82
. 1673	-		-			1 40	CHM 181
.1800	-	-	-	•	-	1.49	CHMOOI
.2000	-	-	-	-	-	2.00	
.2076	-	-		-	-	3.85	KROA82
.2200	-	-	· · · · · · · · · · · · · · · · · · ·	-	-	2.93	CHMJ81
2400	-	-		-	-	4.11	
2500	3 60				-	7.2	SARW81
2581	3.00				-	7.8	KROA82
.2501	-	-				5 1	CHMJ81
.2000	-		-	-	-	6.2	
.2800	-	-	-	-	-	0.2	
.3000	7.4	-	-	-	-	14.1	SARNO
. 3000	-	-	-	-	-	7.4	CHMJ81
.3188		-	-	-	-	14.1	KROA82

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

## Z=48 CADMIUM(CD) CONTINUED

TABLE A	II	EXPERIMENTAL	X-RAY PRODU	CTION CRO	SS SECTIONS	CONTINU	ED
THIN TAN	RGET						
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
. 3200		-	-		-	9.2	CHMJ81
.3400	-	-		-	-	11.2	
.3500	9.5	-	-	-		20.1	SARW81
. 3600	-	-	-	-	- T- T-	13.2	CHMJ81
.3800	-	-	-	-	-	15.3	
3997	-	-	-	-	-	25.4	KROA82
.4000	15.0	-	-	-	-	30.8	SARW81
. 4000	-	-	-			17.6	CHMJ81
4200	-	-	-	-	-	19.4	
. 4906	-		-	-	-	42.6	KROA82
6015	-		-		-	69	
7422	-	-	-	-	-	110	
3.0000	-	-				916	BONG78

THICK TA	RGET					
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL
MeV			BARNS			
.070			-	-		.060
.085	-	-	-	-	-	.120
.100	-	-	-	-	-	.235
. 120	-	-	-	-	-	.440
. 140	-	-	-	-	-	.66
. 165	-	-	-	-	-	1.05
.200	-		-		-	2.20
.250	-	-	-	-	-	4.68
.300	-	-		-	-	8.8
.350	-	-	-	-	-	14.0
.400	-	-	-	-	-	18.2
.450	-			-	-	21.3

TABLE AI EXPERIMENTAL DETAILS

	-			-	-	+	
ΓA	в	LE	A	1	T	1	

LALPHA/LL RATIO

ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE MeV	TARGET	LA/LL	REF
0.5	THICK THICK	29.2* 28.7*	KROA82	0.5	THIN	27.0+-1.9*	KROA82
• S1(L	1.) DETECTOR	USED	+ CRYSTAL	SPECTRO	METER US	ED.	

Z=49 INDIUM(IN)

REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT	BEAM	ERF	PROR	THEORIES	•	COMMENTS
CHAR78	1.0-3.0	THICK	•	1.0(C)	LT	14	BEA(G3) CBEA PWBA3		EFFICIENCY CALCULATED

Atomic Data and Nuclear Data Tables, Vol. 30, No. 1, January 198-

REF

PETV80

BACKING.

ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET.

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

Z=49 INDIUM(IN) CONTINUED TABLE AI EXPERIMENTAL DETAILS CONTINUED COLL ERROR ENERGY AREAL BEAM RANGE DENSITY CURRENT Mev E-6G/CMSQ A REF COMMENTS x mm LA 15 LB 15-18 LG 11-13 LT 14-15 FASS82 .118-.399 19+-1 HP Ge DETECTOR CPSSR --HP Ge DETECTOR USED. RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING. BETA(2+15) GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED. CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMPLOYED. KROA82 .1359-.7417 136+-8 - LT 14-16 CPSSR -THICK EFFICIENCY CALCULATED. METAL TARGET ON VITRIOUS CARBON

TABLE AII

EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.1180	. 130	.068	.013	-		.220	FASS82
.1359	-		-	-		.61	KROA82
.1380	.360	.170	.029	-		.56	FASS82
. 1580	.62	.270	.046	-	-	1.01	
. 1661	-	-		-	-	1.43	KROA82
. 1780	.91	. 390	.079	-	-	1 87	FASS82
. 1980	1.40	.56	.089	-		2 21	TAUGUE
.2066		-				2 17	¥20182
.2180	1.93	.77	133			2.02	FASSAS
2380	2.54	1 01	160		-	5.05	LW2205
2573			. 109		-	4.03	¥80480
2580	3 17	1 20	10.8	-	-	0.0	KRUA02
2770	1 02	1 57	. 190		-	4.90	FASS02
2000	4.05	1.23	.230	-	-	0.5	
.2990	4.03	1.01	. 302	-	-	7.0	
.3100			-	-	-	12.2	KROA82
.3190	5.9	2.21	. 328	-	-	9.3	FASS82
.3390	0.9	2.70	.429	-	-	10.8	
.3590	8.1	3.08	. 440	-	-	12.8	
. 3790	9.4	3.51	.53	-	-	14.9	
.3989	-		-	-	-	22.3	KROA82
.3990	10.6	3.94	.58	-	-	16.7	FASS82
.4897	-	-	-	-	-	37.9	KROA82
.6006	-	-		-	-	60	
.7417	-	-		-	-	96	

Z=49 INDIUM(IN) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS	5			
1.0000		S. S. Statistics					
1.2000	_	-	-	-	-	180	KHAR78
1.4000		-	-	-	-	260	
1 6000	10		-	-	-	340	
1 8000	-	-	-	-	-	420	
2.0000	-	-	-	-	-	500	
2.0000	-	-		-	_	500	
2.2000	-	-	-	-		660	
2.4000	•	-				000	
2.6000	-	-				740	
2.8000	-			-	-	800	
3.0000	-			-	-	850	
		1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.		-	-	800	

TABLE AITI

LALPHA/LL RATIO

ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE MeV	TARGET	LA/LL	REF
0.5	THICK THICK	29.0° 29.91	KROA82	0.5	THIN	27.4+-2.0*	KROA82
• Si(L	1) DETECTOR	USED	+ CRYSTAL	SPECTRO	METER USE	ED.	

Z=50 TIN(SN)

TABLE AI

EXPERIMENTAL DETAILS

REF	ENERGY Range Mev	AREAL DENSITY E-60/CMS	BEAM CURRENT Q A	BEAM COLL	EI	EXP RROR	THEORIES	COMMENTS
CHAR75	3-12	29+-3		•	LI	05 1	BEA(G3) PWBA3	RBS EMPLOYED. EFFICIENCY CALCULATED. O5+ IMPACT STUDIED. METAL TARGET ON CARBON BACKING.
BONG78	3.0	THIN		-	LT	7	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED. K-SHELL STUDIED SELF-SUPPORTING METAL TARGET.
KHAR78	1-3.0	THICK	-	1.0(C)	LT	13	BEA(G3) CBEA PWBA3	EFFICIENCY CALCULATED.
SERK80	2.92-39.34	339	-	-	LT	12	BEA(V) PWBA3 PWBA4	RBS EMPLOYED. SELF-SUPPORTING METAL TARGET.
SARW8 1	.3040	14.6+7	3-100E-9	1.0(B)	LA	15 15-23	PWBABC PWBABCR ECPSSR	RBS EMPLOYED. EFFICIENCY MEASURED
Z=50 TIN(SN) CONTINUED

TABLE	AI		EXPERIMEN	NTAL DE	TAILS (	CONTINUED	
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
ROA82	.137743	115+-5 THICK		-	LT 14-	17 CPSSR	CRYSTAL SPECTROMETER AND SI(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON VITRIOUS CARBON BACKING. ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET

EXPERIMENTAL	X-RAY	PRODUCTION	CROSS	SECTIONS
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TABLE AII THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
			BARNS	3			
Mev						aller.	
1270		_	-	-	-	.451	KROA82
1678		_	-	-		1.10	
. 10/0	-		and the state of the	-	-	2.52	
.2001	-			-	-	5.1	
.2591	= 2			-	-	9.8	SARW81
. 3000	2.3			-	-	9.7	KROA82
.3199			1 4 1 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	-	-	15.7	SARW81
. 3500	0.0	-			-	21.0	
. 4000	11.5	-			-	18.8	KROA82
.4007	-	-			-	32.2	
.4915		-	-		-	51	
.6023	-	-	-			81	
.7430	-	-	-	-		868	SERK80
2.9200	-	-	-	-		1273	CHAR75
3.0000	-	-	-	-	-	800	BONG78
3.0000	-	-	-	-	-	1110	SERK80
3.9700	-		-	-	-	1541	CHAR75
4.0000	-	-		-	-	2010	Gunning
5 0000	-	-	-	-	-	2010	
6 0000	-	-		-	-	2144	SEPERA
6 1300		-	-	-	-	1370	CUARTE
7 0000	1000	-	-	-	-	2211	CHARIS
8.0000		-	-	-	-	2278	
0.0000		-	-	-	-	2345	
9.0000				-	-	2211	
10.0000	-		-	-	-	2017	
11.0000	-		-	-	-	2010	
12.0000	-			-	-	1420	SERKSO
12.3100		-		-	-	1270	
18.1200	-			-	-	1100	
24.2100	-	-		-	-	961	
30.5200	-	-			-	827	
20 2000	-	• •	-	-			

### Z=50 TIN(SN) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS	-			
1.00		-	1.2000	-		160	KHAR78
1.20	-		-	-	-	230	
1.40	-	-	-	-	-	310	
1.60	-	-	-	-	-	390	
1.80	-	S. 6 2 1. 1	-	-	-	470	
2.00	-			-	-	550	
2.20	-	-	-	-	-	620	
2.40	-	-		-	-	690	
2.60	-	-	-	-	-	760	
2.80	-	-	-	-	-	810	
2.90	-	-	-	-	-	840	
3.00	-	-	-	-	-	860	

TABLE AITI

LALPHA/LL RATIO

ENERGY RANGE MeV	TARGET	LA/LL	REF	ENERGY RANGE MeV	TARGET	LA/LL	REF
0.5	THICK	29.6*	KROA82	0.5	THIN	29.2+-2.1*	KROA82
	1) DETECTOR	USED	. CRYSTAL	SPECTRO	METER US	ED.	

#### Z=51 ANTIMONY(SB)

TABLE	IAI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
ROA82	.13997433	106+-4 THICK	•	-	LT 15-1	7 CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USED RBS EMPLOYED. EFFICIENCY

AND SI(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING. ONLY LALPHA/LL RATIO AVAILABLE FOR THICK TARGET.

TABLE AII	EXPERIM	ENTAL X-RAY PRO	DUCTION CROSS	SECTIONS	
THIN TARC	DET				
ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	TOTAL BARNS	REF
.1399 .1693 .2096 .2601 .3206	.424 1.01 2.29 5.1 9.7	KROA82	.4017 .4921 .6028 .7433	17.3 29.5 46.4 76	KROA82

.

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

# Z=51 ANTIMONY(SB) CONTINUED

TABLE AI	II		LALPHA/LL	RATIO			
ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
0.5	THICK THICK	29.8* 25.3*	KROA82	0.5	THIN	28.2+-2.2*	KROA82
* S1(L	i) DETECTO	R USED	+ CRYSTA	L SPECTRO	METER US	ED.	

Z=52 TELLURIUM(TE)

TABLE	AI		EXPERIME	NTAL DE	TAILS			
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS	
SOKR8 1	.6-3.0	50+-5	1-10E-9	1.5(C)	LT 19	PWBA4 PWBABC	EFFICIENCY CALCULATED. METAL TARGET NUCLEPORE BACKING.	ON

TABLE AIL EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY Mev	TOTAL BARNS	REF
.60	35.0	SOKR8 1	2.00	380	SOKR81
.70	52		2.20	416	
.80	64		2.40	489	
.90	89		2.50	514	
1.00	114		2.60	539	
1.20	160		2.70	556	
1.40	202		2.80	583	
1.60	251		2.90	616	
1.80	310		3.00	666	

#### Z=53 IODINE(I)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BONG78	3.0-11.0	THIN	-	-	LT 8	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED.

K-SHELL STUDIED. TARGET ON CARBON BACKING.

ž.

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

Z=53 IODINE(I) CONTINUED

TABLE	IA I		EXPERIMEN	NTAL DE	TAILS	CONTINUED	
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
CUZP8 1	.611-3.85	THIN	-	•	LT 5-10	D BEA(H) SCA2 PWBA3	EFFICIENCY MEASURED. AgIO3 TARGET ON CARBON BACKING. CROSS SECTIONS EVALUATED BY NORMALIZING TO K-SHELL DATA.
TABLE	AII EXPE	ERIMENTAL X	-RAY PROD	UCTION	CROSS S	ECTIONS	
THIN	TARGET						
ENERG MeV	Y TOTAL BARNS	RE	F	ENE	RGY	TOTAL BARNS	REF
6	76 -		-0.				

ner	DANNS		mev	BARNS	
.611	36.5	CUZP81	3.000	670	CUZP8 1
.811	81		3.000	630	BONG78
1.019	124		3.200	743	CUZP81
1.200	171		3.400	806	
1.400	229		3,600	881	
1.600	280		3.800	907	
1.800	328		3.850	916	
2.000	425		5.000	1004	BONG78
2.200	435		7.000	1203	Donoro
2.400	484		9.000	1220	
2.600	549		11.000	1181	
2.800	648				

Z=55 CESIUM(CS)

TABLE	AI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BADT78	4.0	47+-2	1-5E-9	•	LT 9	BEA(G3) PWBA2	EFFICIENCY MEASURED. K-SHELL STUDIED CsBr TARGET ON MYLAR BACKING.

TABLE AIL EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TA	RGET
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ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	TOTAL BARNS	REF
4.00	1117	BADT78			

#### Z=58 CERIUM(CE)

24 14

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
BEAR73	1-3.0	129	-	-	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS EMPLOYED. EFFICIENCY MEASURED. Ce203 TARGET.

EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS TABLE AII

THIN TAN	RGET						
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
1.00	23.0		-	-	-	-	BEAR73
2.25	97	-	-	-		-	
3.00	150	-	-	-	-	-	

Z=59 PRASEODYMIUM(PR)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
HER79	.1540	THICK	•	2.0(B)	-	PSS PSSR PWBA3	EFFICIENCY MEASURED. GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THICK TARGET .

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
150	.035		3.7E-03		-	-	WHER79
175	.087	-	8.7E-03	-	-	-	
.200	.180	-	.017	-	-	-	
.250	.55	-	.046	-	-	-	
.300	1.20	-	.094	-	-	-	
.350	2.20	-	. 162	-	-	-	
.400	3.60	-	.246	-	-	-	

Z=60 NEODYMIUM(ND)

THICK TARGET

TABLE	AI		EXPERIME	NTAL DE	TAI	LS		
REF	ENERGY RANGE Mev	AREAL BEAM BEAM EXP DENSITY CURRENT COLL ERRO E-6G/CMSQ A mm %		XP ROR	THEORIES	COMMENTS		
HAR78	1.0-3.0	THICK	-	1.0(C)	LA LB LT	7-10 7-9 8	BEA(G3) CBEA PWBA3	EFFICIENCY CALCULATED.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
1.00	21.0	13.0	-	_		34.0	KHAR78
1.20	32.0	21.0	-	-		54	
1.40	45.0	30.0	-	-	-	79	
1.60	59	41.0	-	-		106	
1.80	74	54	-	-		137	
2.00	90	67	-	-	-	170	
2.20	110	81	-	-		200	
2.40	120	95	-	-	_	240	
2.60	140	108	-	-	_	270	
2.80	150	120	-	-	-	300	
3.00	170	130	-	-	-	330	

Z=62 SAMARIUM(SM)

TABLE	AI		EXPERIME	INTAL DE	TAILS		
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BEAR73	1.0-3.7	83	-	-	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS EMPLOYED. EFFICIENCY MEASURED.
MILM76	.950	100	-	2.0(B)	LX 10 LT 10	BEA(G3)	SQUARE BEAM. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING.
WHER79	.1544	THICK	-	2.0(B)	•	PSS PSSR PWBA3	EFFICIENCY MEASURED. GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED.

#### Z=62 SAMARIUM(SM) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.95	13.8	8.4	1.20	-		23.4	MILM76
1.00	16.0	-	-	-	-		BEAR73
1.10	20.0	-	-	-	-	-	
1.20	24.0	-	-	-	-	-	
1.30	29.0	-	-	-	-	100 C	
1.40	34.0	-	-	-		-	
1.50	39.0	-		-		-	
1.60	45.0	-	-	-	-	-	
1.70	49.0	-	- 1	-		-	
1.80	55 .			-	-	-	
1.90	60		-	-	-	-	
2.00	69	-	-	-	-	-	
2.10	72		-	-	-		
2.20	77		-	-	-	-	
2.25	80	-		-		-	
2.30	83	-	-	-	-	-	
2.40	89	-		-	-	-	
2.50	94	-	-	-	-		
2.60	102	-		-	-	-	
2.70	107	-	-	-	-	-	
2.80	114	-	-	-	- 10	-	
2.90	119	-		-	-	-	
3.00	126	-		-	-	-	
3.10	132	-	-	-	-	-	
3.20	139	-	-	-	-	-	
3.30	142	-	-	-	-	-	
3.40	148	-		-	-		
3.50	152	-	-	-			
3.60	157	-		-	-		
3.70	163	-	-			-	

#### THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
. 150	.014		1.5E-03	-		-	WHER79
.175	.038	-	3.9E-03	-	-	-	
.200	.083	-	8.3E-03	-	-	-	
.250	.270	-	.025	-	-	-	
.300	.64	-	.053	-	-		
.350	1.20	-	.091	-	-	-	
.400	1.90	-	.132	-	-		
.440	2.70	-	. 176	-	-	-	

### Z=64 GADOLINIUM(GD)

TABLE	AI		EXPERIME	NTAL DE	TAI	LS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	ERI	KP ROR	THEORIES	COMMENTS
MILM76	.950	100		2.0(B)	LX LT	10 10	BEA(G3)	SQUARE BEAM. RBS EMPLOYED. EFFICIENCY

CALCULATED. METAL TARGET ON CARBON BACKING.

### Z=64 GADOLINIUM(GD) CONTINUED

TABLE AI	I	EXPERIMENTAL	X-RAY PRODU	ICTION C	ROSS SECTION	S	
THIN TAR	GET						
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS	5			
.95	10.5	6.3	.86	-	-	17.6	MILM76

Z=65 TERBIUM(TB)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
HER79	.1540	THICK	-	2.0(B)	-	PSS PSSR PWBA3	EFFICIENCY MEASURED. GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THICK TA	RGET						
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
. 150	6.0E-03		7.5E-04	-			WHER79
. 175	.017	-	2.1E-03	-	-	-	
.200	.039	-	4.7E-03	-	-		
.250	. 140	-	.015	-	-	1 -	
.300	.370	-	.037	-	-	-	
.350	.77	-	.068	-	-	-	
.400	1.40	-	.111	-	-	-	

#### Z=66 DYSPROSIUM(DY)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BEAR73	1.0-3.0	163	•	-	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS MEASURED EFFICIENCY MEASURED.
KHAR78	1.0-3.0	THICK	-	1.0(C)	LA 4-6 LB 3-6 LG 4-6 LT 4-6	BEA(G3) CBEA PWBA3	EFFICIENCY CALCULATED.

Z=66 DYSPROSIUM(DY) CONTINUED

TABLE	AI		EXPERIME	NTAL DE	TAILS C	ONTINUED	
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
OKR82	.6-3.0	52+-3	1-10E-9	1.5(C)	LA 8 LB 8 LG 8-12 LL 9-13 LT 6	CPSSR	EFFICIENCY CALCULATED. METAL TARGET ON NUCLEPORE BACKING.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

MeV   BARNS     .60   3.60   2.00   .250   .110   -   6.0   SO     .70   5.5   3.10   .390   .220   -   9.2     .80   8.0   4.40   .78   .340   -   13.5     .90   10.7   6.1   .78   .300   -   17.9     1.00   12.0   -   -   -   BEJ     1.20   20.0   12.0   1.60   1.10   -   23.3   SOI	EF
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
.70 5.5 3.10 .390 .220 - 9.2   .80 8.0 4.40 .78 .340 - 13.5   .90 10.7 6.1 .78 .340 - 13.5   .90 10.7 6.1 .78 .300 - 17.9   1.00 12.0 - - - BE/   1.20 20.0 12.0 1.60 1.10 - 23.3 SOI	KR82
.80 8.0 4.40 .78 .340 - 13.5   .90 10.7 6.1 .78 .300 - 17.9   1.00 12.0 - - - - - BE.   1.00 14.0 7.9 1.00 .350 - 23.3 SOI   1.20 20.0 12.0 1.60 1.10 - 24.7	
.90   10.7   6.1   .78   .300   -   17.9     1.00   12.0   -   -   -   -   -   BE/     1.00   14.0   7.9   1.00   .350   -   23.3   SOI     1.20   20.0   12.0   1.60   1.10   -   24.7   SOI	
1.00 12.0 1.00 14.0 7.9 1.00 .350 - 23.3 SOI 1.20 20.0 12.0 1.60 1.10 - 34.7	
1.00 14.0 7.9 1.00 .350 - 23.3 SOI 1.20 20.0 12.0 1.60 1.10 - 24.7	A 873
1.20 20.0 12.0 1.60 1.10 - 34.7	KR82
	KH02
1.40 29.0 17.0 2.60 1.00 - 40.6	
1.60 38.0 23.0 3.30 1.30 - 66	
1.80 48.0 30.0 4.20 1.80 - 84	
2.00 56 36.0 5.7 2.00 - 100	
2.20 68 47.0 6.4 2.60 - 124	
2.25 60 -	073
2,40 80 54 81 200 105 00	1113
2.50 86 61 9.6 2.10 - 145 50	CK02
2,60 90 63 9.3 3.30 - 100	
2.70 98 70 10.8 3.80 - 100	
2,80 102 72 11.2 1.10 - 103	
2 90 106 76 12 0 2.00 - 109	
3.00 94 10 12.0 3.90 - 198	
3.00 115 85 13.0 # 20	R73

THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS	1 I.			
1.00	11.5	6.6	.72	-		18.0	KHAR78
1.10	14.2	8.5	.92	-	-	23.0	
1.20	17.2	10.6	1.15	-	-	28.0	
1.40	24.0	15.5	1.71	-	-	41.0	
1.60	31.0	21.3	2.38	-	-	55	
1.80	40.0	27.8	3.20	-	-	71	
2.00	49.0	35.0	4.00	-	-	89	
2.20	58	43.0	5.0	-	-	108	
2.40	68	51	5.9	-	-	127	
2.50	73	55	6.4	-	-	137	
2.60	78	59	6.9	-	-	147	
2.70	82	63	7.4	-	-	157	
2.80	87	67	7.9	-	-	167	
2.90	91	72	8.4	-	-	177	
3.00	96	76	8.8	-	-	187	

Z=66 DYSPROSIUM(DY) CONTINUED

TABLE AI	II		LALPHA/LL	RATIO			
ENERGY RANGE MeV	TARGET	LA/LL	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
1.0-3.0	THICK	27.0+-1.9	KHAR78	0.6-3.0	THIN	27 4+-0 8	SOKBSO

Z=67 HOLMIUM(HO)

TABLE	AI		EXPERIMENTAL DETAILS						
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS		
HER79	.1540	THICK	•	2.0(B)	-	PSS PSSR PWBA3	EFFICIENCY MEASURED. GGMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED.		

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
. 150	3.5E-03	-	4.0E-04	-			WHER79
. 175	.013	-	1.6E-03	-	-	-	
.200	.035	-	4.3E-03	-	-	-	
.250	.140	-	.016	-	-	-	
. 300	.320	-	.035	-	-	-	
.350	.56	-	.052	-	-	-	
.400	.77	-	.063	-	-	-	

Z=68 ERBIUM(ER)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROT	THEORIES	COMMENTS
SARW81	.3040	15+-1.2	3-100E-9	1.0(B)	LA 10 LT 19	0 PWBABC 5 PWBABCR ECPSSR	RBS EMPLOYED. EFFICIENCY MEASURED. SELF-SUPPORTING METAL TARGET.

Z=68 ERBIUM(ER) CONTINUED

TABLE AI	II	EXPERIMENTAL	X-RAY PRODU	CTION CRO	SS SECTION	S	
THIN TAR	GET						
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.30	. 169		-	-	-	.316	SARW81
.35	.316	:		:	. :	.57	

Z=69 THULIUM(TM)

TABLE	AI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BEAR73	1.0-3.0	100	-	•	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS EMPLOYED. EFFICIENCY MEASURED.

TABLE AII EXPERIMENTAL X-RAY. PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L .	ETA	TOTAL	REF
MeV			BARNS	5			
1.00	7.9	- 12	-	- 11	-	-	BEAR73
2.25	45.0	-	-	-	-	-	
3.00	75	-	-	-	-	-	

#### Z=70 YTTERBIUM(YB)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
WHER79	. 15 40	THICK		2.0(B)	-	PSS PSSR PWBA3	EFFICIENCY MEASURED. GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED.
SARW8 1	.3040	93+-4	3-100E-9	1.0(B)	LA 9 LT 9	PWBABC PWBABCR FCPSSB	RBS EMPLOYED. EFFICIENCY

# TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

### Z=70 YTTERBIUM(YB) CONTINUED

TABLE AI	I	EXPERIMENTAL	X-RAY PRODU	CTION CRO	SS SECTION	S	
THIN TAR	GET						
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.30	. 169	-		-		.317	SARW8
. 35	.247	-	-	-		.441	
.40	.367	-	-	-	-	.65	

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THICK TARGET
```

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
. 150	1.2E-03	-	1.1E-04	-		_	WHER79
. 175	4.6E-03	-	5.2E-04	-		-	
.200	.013	- 70	1.7E-03	-		_	
.250	.058	4	7.7E-03	-			
.300	. 160	-	.019	_	-		
.350	.310	-	.032	-			
.400	.51	-	.041	-	-	-	

Z=72 HAFNIUM(HF)

TABLE	AI		EXPERIMEN	NTAL DE	TAIL	.S		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSC	BEAM CURRENT A	BEAM COLL	EX ERR	P	THEORIES	COMMENTS
JUSE80	.5-2.5	50	30-200E-9	-	LA	4-5	-	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. He+ IMPACT STUDIED.
SARW81	.3040	155+-20	3-100E-9	1.0(B)	LA LT	14 15	PWBABC PWBABCR ECPSSR	RBS EMPLOYED. EFFICIENCY MEASURED.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.30	.133					.240	SARW81
.35	. 160	-	-	-	-	.286	
.40	.268	-	-	-	-	.470	
.50	1.00	-	-	-			JUSE80
.60	1.88	-	-	-	-		000000
.70	3.16	-	-	-	-		
.80	4.49	-	-	-	_		
.90	6.0	-		-	_		
1.00	7.5	-		-	-		
1.10	9.5	-		-			
1.20	12.0	-		-			

# Z=72 HAFNIUM(HF) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
1.30	15.1	-	-	-	-	-	JUSE80
1.40	17.6	-	-	-	-	-	
1.50	20.2	-	-		-	-	
1.60	22.8	-	-	-	-	-	
1.80	29.4	-		-	-	-	
2.00	35.1	-	-	-	-	-	
2.50	54	-	-	-		-	

#### Z=73 TANTALUM(TA)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
ISHK74	1.75-4.17	1340		3.0(C)	LA 15 LB 15 LG 17 LL 17 LT 10	BEA(G2) PWBA3 IPWBAR	RBS EMPLOYED. EFFICIENCY MEASURED. SELF-SUPPORTING SEMI-THICK METAL TARGET. LALPHA/LL RATIO FOUND TO BE ENERGY DEPENDENT
CHEJ76	0.4-2.0	50-100	5-50E-9	3.2(B)	-	BEA(G1) CBEA PWBA3	RBS EMPLOYED. EFFICIENCY MEASURED. LALPHA/LL RATIO ONLY AVAILABLE. METAL TARGET ON CARBON BACKING.
JUSE80	0.6-2.5	50	30-200E-9	-	LA 4-11	-	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. He+ IMPACT STUDIED.
BAUC81	.249-1.91	THICK	2-500E-9	1.1(B)	LT 25	CPSSR	RBS EMPLOYED. EFFICIENCY MEASURED. He4 IMPACT STUDIED.
UDEN81	.2840	20.5+7	-	-	LA 12 LG 9-15 LL 13-19 LT 11-19	CPSSR	HP Ge DETECTOR USED. RBS EMPLOYED. EFFICIENCY MEASURED. GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED

# Z=73 TANTALUM(TA) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS	;			
.28	.051		3.9E-03	3.1E-03	-	.084	UDEN81
.30	.068	-	4.5E-03	3.7E-03	-	.111	
.32	.092	-	6.9E-03	6.1E-03	-	. 155	
.34	.136	-	.010	9.1E-03	-	.288	
.36	.172	-	.012	.011	-	.287	
.38	.229	-	.014	.015	-	.376	
.40	.294	-	.020	.018	-	481	
.60	1.56	-	-				JUSERO
.80	3.78	-	-	_	-		CODECC
1.00	6.9	-	-		-		
1.20	11.0	-	-				
1.30	12.9	-		-	-		
1.40	15.5	-	-				
1.50	18.1	-	-				
1.60	20.8	-					
1.80	27.0	-					
2.00	36.0						
2.50	52			-	-	1	

#### SEMI-THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	Ľ	ETA	TOTAL	REF
MeV			BARN	IS			
1.75	22.0	13.4	1.74	1.10	-	38.2	ISHK74
1.95	20.5	16.9	2.15		-	46.6	
2.10	33.4	21.9	3.04	1.84	-	60	
2.36	43.2	25.0	3.82	2.48	-	75	
2.56	47.9	32.4	4.61	2.77	-	88	
2.76	50	32.5	4.68	2.88	-	90	
2.96	55	38.9	6.0	3.54	-	103	
3.57	77	56	8.3	4.12	-	147	
3.77	81	58	_	6.0	-	153	
3.97	95	70	11.0	6.1	-	182	
4.17	100	75	11.6		-	191	

#### THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
Me V			BARNS				
.249	-	-	ST 115		1 2 1	.096	BAUC81
.300	-	-	-	-	-	.233	
.353	-	-		-	-	.460	
.403	-	-	-	-	-	.73	
. 484	-	-	-	-	-	1.26	
.552	-	-	-	-	-	1.90	
.635	-	-	-	-	-	2.94	
.720	-	-	-	-	-	4.31	
.900	-	-	-	-	-	7.8	
1.100	-	-	-	-	-	12.8	
1.300	-	-	-	-	-	19.2	
1.520	-	-	-	-	-	26.6	
1.720	- 101	-	-	-	-	35.0	
1.910	-	-	-	-	-	46.3	

Z=73 TANTALUM(TA) CONTINUED

TABLE AD	II		LALPHA/LI	RATIO			
ENERGY Range Mev	TARGET	LA/LL	REF	ENERGY Range Mev	TARGET	LA/LL	REF
0.4-2.0	THIN	22.1+-1.2	CHEJ76	0.2840	THIN	15.8+-1.2	UDEN8 1

# Z=74 TUNGSTEN(W)

.

TABLE	AI		EXPERIMEN	NTAL D	ETAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BEAR73	1.0-3.7	81	-	-	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS EMPLOYED. EFFICIENCY MEASURED. WO3 TARGET.
BADT78	4.0	99+-5	1-5E-9	-	LT 7	BEA(G3) PWBA2	EFFICIENCY MEASURED. K-SHELL STUDIED. WO3 TARGET ON MYLAR BACKING.
JUSE80	0.5-2.5	50 3	90-200E-9	-	LA 5-6		RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMYAR BACKING. He+ IMPACT STUDIED.
PETV80	.2-1.05	THICK	-	-	LT 25	PWBA 1	PROPORTIONAL COUNTER USED. EFFICIENCY MEASURED.

EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS TABLE AII

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	DFF
MeV			BARNS				ALT
.50	.72		-	-			
.80	3.34	:	-	-	-	-	JUSE80
.90	4.90	/	102134	-	:	1	
1.00	4.80	-	1	-		-	
1.10	6.0	1				-	JUSE80
1.20	11.0	-	-		:	-	BEAR73
			•	-	-	-	BEAR73

### Z=74 TUNGSTEN(W) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	/ L	ETA	TOTAL	REF
MeV			BARN	IS			
1.30	12.9					-	JUSE80
1.30	8.9		-	-	-	-	BEAR73
1.40	15.5		-	-	-	-	JUSE80
1.40	11.0	-	-	-		-	BEAR73
1.50	16.9	-	-	-	-	_	JUSERO
1.50	13.0	-	-	-		-	BEAR73
1.60	18.9	-	-				IUSERO
1.60	14.0						BEADTO
1.70	21.5						LUSERO
1.70	17.0						DEARTO
1.80	25 0					-	DEARIS
1 80	19 0			-	-	-	305200
1 90	20 8		-		-	-	BEAR/3
1 90	21.0		-	-		-	JUSEBO
2.00	21.0		-		-	-	BEAR73
2.00	32.2				-	-	JUSE80
2.00	23.0	-	-	-	-	-	BEAR73
2.10	20.0		-		-	-	
2.20	27.0	-	-	•	-	-	
2.25	29.0	-	•	-	-	-	
2.30	30.0	-	•	-	-	-	
2.40	33.0	-	-	-	-	-	
2.50	47.0		-	-	-	-	JUSE80
2.50	35.0			-	-	-	BEAR73
2.60	37.0		-	-	-	-	
2.70	41.0	-		-	-	-	
2.80	44.0	-		-	-	-	
2.90	46.0	-	-	-	-	-	
3.00	49.0	-	-	-	-	-	
3.10	52	-	-	-	-	-	
3.20	55	-		-	-	-	
3.30	58	-	-	-	-	-	
3.40	59	-	-	-	-	-	
3.50	63	-	-	-	-		
3.60	67	1000	10 m	1			
3.70	70	-		-			
4.00	-	-	-	-		222	BADT78

#### THICK TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.20		-	-			.024	PETV80
.25	-	-	-	-	-	.046	
.30	-		-	-		. 104	
.35	-	-		-	-	.208	
.40	-	-	-	-	-	.408	
.45	-	-	-	-	-	.83	
.55	-	-		-	-	1.71	
.65	-	-	-	-	-	3.04	
.75	-	-	-	-	-	4.75	
.85	-	-	-	-	-	7.2	
.95	-	-	-	-	-	11.9	
1.05	-	-	-	-	-	16.2	

.

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

# Z=77 IRIDIUM(IR)

TABLE	AI		EXPERIMEN	TAL DE	TAILS		
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
USE80	0.6-2.5	50	30-200E-9	-	LA 4-5	-	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.60	.80		-			-	JUSE80
.70	1.38	-		-	-	-	
.80	2.10	-	-	-	-	-	
.90	3.06	-	-			-	
1.00	4.10	-		-	-	-	
1.10	5.3	-	-		-	-	
1.20	6.6	-	-	-	-	-	
1.30	8.0	-	-	-	-	-	
1.40	9.7	-	-	-	-	-	
1.50	11.5	-	-	-	-	-	
1.60	13.2	-	-	10.000 · 10.000		-	
1.70	15.6	-	-	-	-	-	
1.80	17.6	-	-	-	-	-	
2.00	21.8	-		-	-	-	
2.50	33.8	-	-	-	-	-	

### Z=78 PLATINUM(PT)

TABLE	AI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
CHEJ76	0.4-2.0	50-100	5-508-9	3.2(B)	-	BEA(G1) CBEA PWBA3	RBS EMPLOYED. EFFICIENCY MEASURED. LALPHA/LL RATIO ONLY AVAILABLE. METAL TARGET ON CARBON BACKING.
KHAR78	1.0-3.0	THICK	-	1.0(C)	LA 3-5 LB 3-6 LG 3-5 LT 3-6	BEA(G3) CBEA PWBA3	EFFICIENCY CALCULATED.

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Z=78 PLATINUM(PT) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS THICK TARGET

1	n	1	L	A	1	A	ĸ	u

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
1.00	3.50	1.86	.260	-	-	5.6	KHAR78
1.20	5.6	3.00	.430	-	-	9.0	000000000000000000000000000000000000000
1.40	8.1	4.60	.65	-	-	13.2	
1.60	11.2	6.5	.92	-	-	18.4	
1.80	14.7	8.7	1.26	-	-	24.4	
2.00	18.8	11.2	1.65	-	-	31.2	
2.20	23.1	14.0	2.09	-	-	39.0	
2.40	27.7	17.0	2.57	-		47.0	
2.60	32.4	20.1	3.08	-	-	55	
2.80	37.0	23.3	3.60	-	-	63	
3.00	41.0	26.5	4.13	-	-	71	

TABLE AIII

LALPHA/LL RATIO

ENERGY RANGE MeV	TARGET	LA/LL	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
0.4-2.0	THIN	19.6+-1.0	CHEJ76	1.0-3.0	THICK	21.1+-0.6	KHAR78

Z=79 GOLD(AU)

TABLE AI

EXPERIMENTAL DETAILS

REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BEAR73	1.0-3.0	124	-	•	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS EMPLOYED. EFFICIENCY MEASURED.
TAWH75	1-4.5	348+-35	-	3.0(C)	LA 15 LB 15 LG 15 LL 17 LE 50 LT 10	BEA(G2) BEA(H) PWBA3	RBS EMPLOYED. EFFICIENCY MEASURED. He3+ IMPACT STUDIED. METAL TARGET ON A1 BACKING.
CHEJ76	.4-2.0	50-100	5-50E-9	3.2(B)		BEA(G1) CBEA PWBA3	RBS EMPLOYED. EFFICIENCY MEASURED. LALPHA/LL RATIO ONLY AVAILABLE. METAL TARGET ON CARBON BACKING.
BONG78	3.0-11.0	THIN	-	-	LT 8	BEA(G3) PWBA2	RBS EMPLOYED. EFFICIENCY MEASURED. SELF-SUPPORTING METAL TARGET.

Z=79 GOLD(AU) CONTINUED

TABLE	AI	•	EXPERIME	NTAL DE	TAIL	.s co	NTINUED	
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSC	BEAM CURRENT A	BEAM COLL	EX ERR	PROR	THEORIES	COMMENTS
KHAR78	1.2-3.0	THICK		1.0(C)	LX LT	3-5 3-5	BEA(G3) CBEA PWBA3	EFFICIENCY CALCULATED.
BHAD80	.33-1.81	200+-20	50-300E-9	1.0(C)	LX LT	15 10	PWBA3 PWBABC IPWBABCR	RBS EMPLOYED. EFFICIENCY MEASURED. SELF-SUPPORTING METAL TARGET.
LAPG80	.1430	THICK	-	-	LT	25-50	-	COULOMB DEFLECTION FACTOR DEDUCED.
SARL80	2.0	THIN		,-	LX	15 15	PWBA1 PWBABC MPWBABCR	EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING. C12 N14 O16 IMPACT STUDIED.
SARW81	.3040	64+-3 49+-2	3-100E-9	1.0(B)	LA LT	8-9 15	PWBABC PWBABCR ECPSSR	RBS EMPLOYED. EFFICIENCY MEASURED. TWO METAL TARGETS USED.
SOKR81	1-3.0	35+-2	1-10E-9	1.5(C)	LA LB LG LL LT	8 8 8-11 9-11 6	PWBA4 PWBABC	EFFICIENCY CALCULATED. METAL TARGET ON NUCLEPORE BACKING.
BAUC8 1	.5-4.0	225+-11	.5-50E-9	1.1(B)	LT	11	CPSSR	RBS EMPLOYED. EFFICIENCY MEASURED. He4 N2+ Ne3+ IMPACT STUDIED. SELF-SUPPORTING METAL TARGET.
PINA82	0.5-4.0	50	30-200E-9	-	LA :	5-10	-	RBS EMPLOYED. EFFICIENCY MEASURED. SELF-SUPPORTING METAL TARGET. RADIATIVE DECAY BRANCHING RATIOS MEASURED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TAR	IGET						
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.30	.022	-	1	-	-	.052	SARW81
.33	.090	.053	8.1E-03	-	-	. 151	BHAD80
.35	.055	-	-	-		. 109	SARW81
.37	. 160	.095	.014	-	-	.269	BHAD80
.40	. 107	-		-	-	.215	SARW81
.42	.270	. 150	.021	.016	-	.457	BHAD80
.46	.390	.220	.031	.027	-	.67	

# Z=79 GOLD(AU) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARN	S			
.50	.400	-	-	-	-		PINA82
.50		-	-		-	.380	BAUC81
.52	.460	.260	.036	.030	-	- 19	BHADOU
.50	-37	.310	.042	.030			PINA82
.61	.74	. 410	.053	.046	-	1.25	BHAD80
.65	.97	.53	.069	.061	- (- )	1.63	
.65	-	-		-	-	1.00	BAUCEI
.70	1.17	- 66	088	077		2 03	BHAD80
-70	1.50	.80	.110	.082	14 I I I I I	2.49	DIADOG
.79	1.60	.88	. 120	.094	-	2.69	
.80	1.86	-	-	-	-		PINA82
.80					-	1.80	BAUCSI
.84	1.90	1.00	.130	. 120		3.15	BRADOU
.07	2.60	1.40	. 190				PINA82
.91	3.10	1.60	.210	.180	-	5.1	BHAD80
1.00	2.70	-	-	-	-	-	BEAR73
1.00	4.38	2.31	.334	.251	.027	7.3	TAWH75
1.00	3.52	1.97	.300	.170		0.0	PTNA82
1.00	3.00			-		4.50	BAUCS 1
1.02	4.00	2.10	.270	.250	-	6.6	BHAD80
1.10	5.0	2.50	.330	.240	-	8.1	SOKR81
1.10	4.50	-	-	-	-	-	PINA82
1.11	6.0	3.30	.460	. 340	-	10.1	BHADOU DTNA82
1.20	5-7	2 10	410	300		9.7	SOKR81
1.21	7.2	4.00	.52	.410	-	12.1	BHAD80
1.25	7.2	3.79	.53	.412	.052	12.0	TAWH75
1.30	7.0	-	-		-		PINA82
1.31	8.2	4.50	.58	.480		13.8	BHADOU
1.40	9.0	# 76	-64	470	-	14.6	SOKR81
1.41	10.0	5.3	.80	.54	-	16.6	BHAD80
1.50	10.8	5.9	.85	.59	.079	18.2	TAWH75
1.50	10.0		-	-	-		PINA82
1.51	11.6	6.4	.78	.03	-	19.4	BHADOU DTNA82
1.60	12.0	6.6	96	67	-	20.4	SOKR81
1.61	10.8	6.1	.82	.60	-	18.3	BHAD80
1.70	13.4	-	-	-	-	-	PINA82
1.71	12.4	7.1	.96	.66		21.1	BHAD80
1.75	14.7	8.2	1.23	.78	.098	25.0	TAWH/D DTNARD
1.80	15.0	8 5	1.21	74	-	25.6	SOKR81
1.81	13.8	7.7	1.00	.77	-	23.3	BHAD80
2.00	19.0	-	-	-	-	-	PINA82
2.00	19.9	11.2	1.69	1.08	.130	34.0	TAWH75
2.00	19.2	10.8	1.40	.94	-	32.4	BAUCSI
2.00	10 8	11 8	1.73		-	34.5	SARL80
2.20	23.6	13.8	1.91	1.06	-	40.4	SOKR8 1
2.25	24.2	13.7	2.15	1.29	. 190	41.5	TAWH75
2.25	18.0	-	-		-		BEAR73
2.40	28.4	16.3	2.41	1.35	-	40.4	SUKROI
2.50	28.4	17.4	2.63	1.61	.240	50	TAWH75
2.50	28.8	-		-	-	-	PINA82
2.60	34.0	19.5	2.98	1.81	-	58	SOKR81
2.70	34.6	20.0	3.08	1.70	-	59	TANUTE
2.75	38.6	22.0	3.57	2.04	.270	60	SOKRAI
2.00	41 1	24.8	3.76	1.71	1.1	71	Jonand I
3.00	41.8	25.5	4.08	1.88	-	73	

### Z=79 GOLD(AU) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARM	IS			
3.00	-	-		8 Ja 40	-	65	BONG78
3.00	44.8	27.0	4.32	2.23	.330	79	TAWH75
3.00	32.0	-	-	-	-	-	BEAR73
3.00	38.8	-			-	-	PINA82
3.25	52	32.2	5.1	2.77	.53	93	TAWH75
3.50	49.0	-	-	-	-	-	PINA82
3.50	60	37.6	6.1	2.98	.61	108	TAWH75
3.75	72	45.4	7.2	3.64	.68	129	
4.00	60	-	-			-	PINA82
4.00	-	-	-	-	-	80	BAUC81
4.00	80	49.9	8.3	4.01	.80	143	TAWH75
4.25	90	57	9.5	4.76	.87	163	
4.50	97	62	10.3	4.82	.83	175	
5.00	-	-				169	BONG78
7.00	-	-	-	-	-	261	
9.00		-	-	-		357	
11.00	-	-	-	-	-	433	

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
. 140		-	-	-		4.6E-05	LAPGSO
.150	-			-		1.1E-04	
. 160		-	-	-	-	2 4E-04	
. 170	-	-	-	-	-	4.9E-04	
. 185	-	-	-	-		9.7E-04	
.200	-		-	-	-	2.1E-03	
.215	-	-	-	-	-	4 1E-03	
.230	-	-	-	-	-	6.9E-03	
.245	-		-	-		.011	
.260	-	-	-	-	-	.017	
.275	-	-	-	-	-	.026	
.300	-	-	4.5	-	-	.049	
1.200	4.80	2.60	. 380	-	-	7.8	KHAR78
1.400	7.0	4.00	.56		-	11.6	
1.600	9.7	5.6	.78	-	-	16.2	
1.800	12.7	7.5	1.06	-	-	21.5	
2.000	16.1	9.7	1.39	-	-	27.4	
2.200	19.7	12.1	1.78	-	-	33.8	
2.400	23.5	14.6	2.21	-	-	40.5	
2.600	27.4	17.2	2.63	-	-	47.0	
2.800	31.2	19.7	3.02		-	54	
3.000	35.0	22.3	3.32	-	-	61	

TABLE AI	II		LALPHA/LL	RATIO			
ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
1.0-4.5	THIN THIN THICK	18.9+-1.5 19.7+-1.0 20.3+-0.6	TAWH75 CHEJ76 KHAR78	.33-1.81 1.0-3.0	THIN THIN	16.8+-0.3 20.3+-0.6	BHAD80 SOKR81

#### Z=81 THALLIUM(TL)

TABLE	AI		EXPERIMEN	TAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
EIC77	0.5-3.0	50	30-200E-9	•	LA 6-7 LT 7-8	-	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
		BARNS				
	10 m 10 m					
.330	-	-	-	•	.57	LEIC77
2.97	-	-	-	-	5.1	
9.7	-	-	-	-	16.6	
16.5	-	-	-	-	29.1	
27.0	-	-	-	-	48.1	
33.5	-	-	-	-	61	
	.330 2.97 9.7 16.5 27.0 33.5	<u>ALPHA</u> <u>BETA</u> .330 - 2.97 - 9.7 - 16.5 - 27.0 - 33.5 -	ALPHA BETA GAMMA BARNS -330 2.97 9.7 16.5 27.0 33.5	ALPHA BETA GAMMA L BARNS .330 2.97 9.7 16.5 27.0 33.5	ALPHA BETA GAMMA L ETA BARNS -330 2.97 9.7 16.5 27.0 33.5	ALPHA   BETA   GAMMA   L   ETA   TOTAL     BARNS     .330   -   -   -   .57     2.97   -   -   -   5.1     9.7   -   -   -   16.6     16.5   -   -   -   29.1     27.0   -   -   -   48.1     33.5   -   -   -   61

#### Z=82 LEAD(PB)

TABLE AI EXPERIMENTAL DETAILS

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BEAR73	1.0-3.0	97	•	-	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS EMPLOYED. EFFICIENCY MEASURED.
LIER73	2.5-12	51+-2.6	-	•	LX 10 LT 17	BEA(G3) PWBA2	RBS EMPLOYED. EFFICIENCY MEASURED. K-SHELL STUDIED. METAL TARGET ON CARBON BACKING.
TAWH74	1.8-4.4	500+-50	•	3.0(C)	LA 15 LB 15 LG 17 LL 17 LE 20 LT 10	BEA(G2) PWBA2	RBS EMPLOYED. EFFICIENCY MEASURED. He3+ IMPACT STUDIED. SELF-SUPPORTING METAL TARGET.
CHEJ76	0.4-2.0	50-100	5-50E-9	3.2(B)	-	BEA(G1) CBEA PWBA3	RBS EMPLOYED. EFFICIENCY MEASURED. LALPHA/LL RATIO ONLY AVAILABLE. METAL TARGET ON CARBON BACKING.

Z=82 LEAD(PB) CONTINUED

TABLE	AI		EXPERIMEN	TAL DET	TAILS C	ONTINUED	
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
LEIC77	0.5-3.5	50	30-200E-9	-	LA 7-9 LT 7-8	-	RES EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.
BONG78	3.0	THIN	-	-	LT 5	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING.
SARW8 1	.3040	67+-3	3-100E-9	1.0(B)	LA 9 LT 9	PWBABC PWBABCR ECPSSR	RBS EMPLOYED. EFFICIENCY MEASURED.
SOKR82	.9-3.0	47+-2	1-10E-9	1.5(C)	LA 6 LB 6 LG 7-10 LL 9-12 LT 4	CPSSR 2	EFFICIENCY CALCULATED. METAL TARGET ON NUCLEPORE BACKING.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARN	S			
.30	.012		-			.019	SARW81
35	.028	-		-	-	.046	
	057	-	-	-	-	.095	
50	220	-	-	-	-	.370	LEIC77
. 50	1 80	01	. 120	. 120	-	2.95	SOKR82
	1.80				-	-	BEAR73
1.00	1.00	-			-	3.70	LEIC77
1.00	2.20	1 20	160	120		3.99	SOKR82
1.00	2.40	1.30	. 100	200		5 3	
1.10	3.20	1.70	.220	.200		6.7	
1.20	4.00	2.10	.300	.210		10.1	
1.40	6.0	3.30	.450	. 350	-	11.7	I FTC77
1.50	6.9	-	-	-	-	11-1	CONDES
1.60	8.6	4.60	.72	.470	-	14.4	SUKROZ
1.80	11.2	5.9	.97 .	.61		18.7	
1.80	12.6	7.0	1.01	.66	.087	21.4	TAWH74
2.00	13.9	8.0	1.20	.68	-	23.8	SOKR82
2.00	13.5	-	-	-	-	23.4	LEIC77
2 00	15.1	8.6	1.22	.80	.117	25.8	TAWH74
2 20	19.0	10.6	1.70	1.00	-	32.3	SOKR82
2 20	18 3	10.6	1.56	.93	.137	31.5	TAWH74
2.20	12.0				-		BEAR73
2.25	22.0	12 2	1 90	1.20	-	39.3	SOKR82
2.40	23.0	12.0	1 07	1 02	.158	38.4	TAWH74
2.40	22.4	12.9	1.95	1.02		38.7	LEIC77
2.50	21.9	12 7	2 10	1 30		42.1	SOKR82
2.50	25.0	13.1	2.10	1.50		37 1	LTER73
2.50	22.2	13.1	1.01		176	42 4	TAWH74
2.60	25.0	14.8	2.19	1.19	. 110	10.4	SOFPRO
2.60	27.0	15.0	2.20	1.40	-	50.0	JORNOZ
2.70	29.0	17.0	2.60	1.60		50 5	TAUUTH
2.80	28.5	17.1	2.38	1.34	. 182	49.5	1A#0/4
2 80	30 0	18 0	2.90	1.70		53	SUKROZ

# Z=82 LEAD(PB) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED

THIN TARG	ET							
ENERGY	ALPHA	BETA	GAMMA		L	ETA	TOTAL	REF
MeV			B	RNS				
2.90	33.0	19.0	2.70	-	2.30	-	57	SOKR82
3.00	35.0	21.0	3.30		1.90	-	50	BONG78
3.00	21 7	-	-		-	-	57	LEIC77
3.00	33.4	20.4	3.07		1.54	. 191	59	TAWH74
3.00	24.0	-	-		-	-	=	BEAR73
3.00	32.0	19.5	2.70		1 62	226	63	TAWH74
3.20	35.9	22.3	3.30		-	-	74	LEIC77
3.50	41.2	28.1	4.19		2.05	.312	79	TAWH74
3.80	51	32.8	4.89	:	2.50	. 328	92	
4.00	58	37.4	5.8		2.91	.379	105	LTER73
4.00	52	32.7	4.72		2 10	400	111	TAWH74
4.20	61	39.0	6.3		3.08	.371	112	
4.30	65	42.2	6.6		3.30	.448	118	
4.50	64	40.7	6.0		-	-	111	LIER73
5.00	80	51	7.4		-	-	139	
6.00	97	65	9.4		-		191	
6.50	109	88	12.6			-	237	
8.00	142	93	13.5		-	100	248	
8.50	157	106	15.7		-	-	279	
9.00	167	112	16.7		-	-	290	
10.00	187	122	17.7		-		338	
10.50	191	120	19.0		-	-	352	
12.00	220	147	21.6		-	-	389	
TABLE AI	II		LALPHA/L	L RATI	.0			
ENERGY RANGE MeV	TARGET	LA/LL	REF	EN RA	IERGY INGE IeV	TARGET	LA/LL	REF
1.8-4.4 0.4-2.0	THIN THIN	20.4+-1. 19.7+-1.	5 TAWH74 0 CHEJ76	0.9	)-3.0	THIN	17.3+-0.4	SOKR82
Z=83 BIS	MUTH(BI	2						
TABLE AT	:		EXPERIMEN	TAL DE	TAILS			
REF	ENERGY	AREAL DENSITY	BEAM	BEAM	EXP	THEORIE	S COMM	ENTS
	MeV	E-6G/CMSQ	A	10.00	*			
BEAR73	1-3.0	100		-	LA 15	5 BEA(G4 PWBA2	) RECTAN BEAM. RBS EM EFFICI MEASUR	GULAR PLOYED. ENCY ED.
TAWH75	1-4.5	431+-43	-	3.0(C)	LA 15 LB 15 LG 15 LL 15 LE 35 LT 10	5 BEA(G2 5 BEA(H) 5 PWBA3 7 5 0	) RBS EM EFFICI MEASUR He3+ I STUDIE METAL A1 BAC	PLOYED. ENCY ED. MPACT D. TARGET ON CKING.

Z=83 BISMUTH(BI) CONTINUED

TABLE	AI		EXPERIME	NTAL DE	TAILS C	ONTINUED	
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
LEIC77	0.5-3.0	50	30-200E-9	-	LA 6-7 LT 6-7		RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.
BHAD80	.33-1.81	80+-8	50-300E-9	1.0(C)	LX 15 LT 10	PWBA3 PWBABC IPWBABCR	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING.

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
.33	.012	6.5E-03	-	-	-	.019	BHAD80
.37	.031	.017	2.1E-03	2.0E-03	-	.052	
.42	.062	.034	4.4E-03	4.3E-03	-	.105	
.46	.110	.060	8.6E-03	7.2E-03	-	. 186	
.50	. 180	-		-	-	. 321	LEIC77
51	140	074	9.9E-03	9.0E-03	-	.233	BHAD80
56	210	110	015	.013	-	348	
60	360	190	024	025	_	.60	
	. 500	340	044	047		1.08	
	78	400	053	050	-	1 28	
-70	. 10		.070	071		1 64	
. 74	1.40	. 52	.070	008	100	2 32	
- / 9	1.40	.13	.094	100		2.52	
.04	1.00	.05	. 110	.100		2 12	
.01	1.90	. 90	. 130	. 140	-	3.13	
.91	2.40	1.30	.170	. 150		4.02	TAUUTE
1.00	3.20	1.79	.253	. 109	.022	2.2	IAWN/D
1.00	2.40		-	-	-	4.33	LEICIT
1.00	1.00		-		-		BEAR/3
1.02	3.40	1.80	.230	.220	-	5.7	BHADOO
1.11	4.40	2.30	.320	.280	-	7.3	
1.21	5.0	2.70	.350	.320	-	8.4	
1.25	4.94	2.81	.414	.290	.039	8.5	TAWH75
1.31	6.2	3.30	.470	.450	-	10.4	BHADSO
1.41	7.8	4.30	.59	.52	-	13.2	
1.50	7.3	4.20	.61	.408	.057	12.6	TAWH75
1.50	6.6	-	-	-	-	11.9	LEIC77
1.51	9.2	5.1	.69	.58	-	15.6	BHAD80
1.61	10.7	6.0	.82	.71	-	18.2	
1.71	11.9	6.7	.93	.84	-	20.4	
1.75	10.2	5.9	.89	.56	.067	17.6	TAWH75
1.81	11.1	6.3	.91	.80	-	19.1	BHAD80
2.00	13.5	8.0	1.25	.71	.094	23.6	TAWH75
2.00	11.9		-		-	23.4	LEIC77
2.25	16.1	9.8	1.57	.86	. 120	28.4	TAWH75
2 25	12 0						BEAR73
2 50	10.6	12 0	1 92	1.15	130	34.8	TAWH75
2 50	10 5					36.1	LEIC77
2 75	26.3	16 1	2 70	1 35	170	46.6	TAWHTS
2.00	20.3	10 1	3.00	1 51	180	54	
3.00	27 0	19.1	3.09			51	LETC77
3.00	22.0						BEAR73

R. S. SOKHI and D. CRUMPTON L-Shell Cross Sections for Protons

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

Z=83 BISMUTH(BI) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BA	RNS			
3.25 3.50 3.75 4.00 4.25 4.50	37.0 40.7 49.2 56 63 67	23.5 26.1 32.4 36.6 42.3 44.7	3.89 4.39 5.2 6.2 7.2 7.8	1.87 2.12 2.53 2.95 3.29 3.47	.270 .270 .380 .450 .480 .51	67 74 90 102 117 124	TAWH75
TABLE AI	11 .		LALPHA/LL	RATIO			
ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
1.0-4.5	THIN	18.7+-1.5	TAWH75	.33-1.81	THIN	14.5+-0.2	BHAD80

Z=90 THORIUM(TH)

TABLE	AI		EXPERIMEN	TAL DET	AILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BEAR73	1-3.7	168	•	-	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS EMPLOYED. EFFICIENCY MEASURED. ThF4 TARGET.
LEIC77	0.5-3.0	50	30-200E-9	-	LA 7 LT 6-7	-	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON A1 BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.
SARW81	.40	19+-1	3-100E-9	1.0(B)	LA 29 LT 30	PWBABC PWBABCR ECPSSR	RBS EMPLOYED. EFFICIENCY MEASURED.

TABLE AI	I EXP	ERIMENTAL	X-RAY PRODU	CTION CRO	SS SECTIONS		
THIN TAR	GET						
ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
40	6.8E-03			-	-	9.4E-03	SARW81
.50	.085	-	-	-	-	.160	LEIC77
1.00	1.07	-		-	-	1.00	
1.00	.72	-		-	-	-	BEARIS
1.10	.90	-	-	-	-	-	
1.20	1.20	-	-	-	•	-	
1.30	1.50	-		-	-	-	

R. S. SOKHI and D. CRUMPTON L-Shell Cross Sections for Protons

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

### Z=90 THORIUM(TH) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED

TH	I	N	T	A	R	G	Ε	1

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARNS				
1.40	1.90	-	-	-	-	-	BEAR73
1.50	3.78	-	-	-	-	6.6	LEIC77
1.50	2.30	-	-	-	_	-	BEAR73
1.60	2.80	-	-	-	-	-	
1.70	3.20	-	-	-	-	-	
1.80	3.70	-	-	-	-	-	
1.90	4.20	-	-	-		-	
2.00	8.1	-		-	- *	14.3	LEIC77
2.00	4.80		-	-	-	-	BEAR73
2.10	5.4		-		-	-	
2.20	6.0	-	-		_	-	
2.25	6.4	-				_	
2.30	6.7	-	_	-	-	-	
2.40	7.4		-	_	_		
2.50	13.0		_	_	-	23.4	LETC77
2.50	8.2		and an and a second				BEARTS
2.60	9.0						Seam 5
2.70	9.7						
2.80	11.0						
2 90	12.0						
3 00	18.7					33 0	LETC77
3 00	12 0					55.5	BEAR73
3 10	13.0						Deanis
3 20	14 0						
3.20	15.0			-	1		
3.30	15.0	-	-		-	-	
3.40	17.0	-			-		
3.50	19.0	-			-		
3.00	10.0		-	-			
3 /11				-		-	

#### Z=92 URANIUM(U)

TABLE	AI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BEAR73	1-3.0	122		-	LA 15	BEA(G4) PWBA2	RECTANGULAR BEAM. RBS EMPLOYED. EFFICIENCY MEASURED. UF4 TARGET.
TAWH75	1-4.5	291+-29		3.0(C)	LA 15 LB 15 LG 15 LL 17 LE 50 LT 10	BEA(G2) BEA(H) PWBA3	RBS EMPLOYED. EFFICIENCY MEASURED. He3+ IMPACT STUDIED. URANYLACETATE TARGET ON A1 BACKING.
LEIC77	0.5-3.0	50	30-200E-9	-	LA 6-7 LT 6-7		RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON A1 BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.

Z=92 URANIUM(U) CONTINUED EXPERIMENTAL DETAILS CONTINUED TABLE AI COMMENTS THEORIES AREAL BEAM DENSITY CURRENT BEAM EXP ENERGY REF ERROR COLL RANGE E-6G/CMSQ ..... \* MeV ٨ RBS EMPLOYED. BEA(G3) LT 5 THIN -3.0 . BONG78 PWBA2 EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING. RBS EMPLOYED. EFFICIENCY MEASURED. 4.0+-.4 50-300E-9 1.0(C) LX 15 LT 10 PWBA3 BHAD80 .43-1.81 PWBABC IPWBABCR UC1 TARGET ON A1 BACKING. 132+-26 3-100E-9 1.0(B) LA 30 LT 25 RBS EMPLOYED. EFFICIENCY MEASURED. PWBABC SARW81 .30-.40 PWBABCR ECPSSR

TABLE AIT

EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS

THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV		Mary Service	BARNS	5			
20	3 35-04	-	-	_		3.9E-04	SARW81
. 30	1 08-03		-	-	-	2.8E-03	
	5 25-03			-	-	7.7E-03	
.40	0.36-03	013		-	-	.033	BHAD80
- 43	.020	.075		-	-	.067	
.47	.043	.024			-	.094	LEIC77
.50	.054	- 029			_	.110	BHAD80
.52	.072	.030	-011			. 196	
.57	. 120	.005	.011	011		269	
.61	. 160	.080	.012	.018		416	
.65	.250	.130	.010	.010	-	407	
.71	.300	.150	.024	.023	-	54	
.76	. 330	. 160	.028	.024	-		
.81	. 440	.240	.033	.033	-	. / 5	
.85	.490	.280	.039	.032	-	.04	
.89	.56	.310	.043	.039	-	. 95	
.91	.70	.370	.048	.053	-	1.17	
1.00	.69	-	-	-	-	1.17	LEICIT
1.00	.55	-	-		-	-	BEAR73
1 00	.91	.460	.078	.060	.024	1.53	TAWH75
1 01	1,10	.54	.064	.066	-	1.77	BHADSC
1 11	1 30	.65	.087	.081	-	2.12	
1 21	1 60	82	.110	.100	-	2.63	
1.21	1 60	88	144	.113	.056	2.88	TAWH75
1.25	2.10	1 10	150	.130	-	3.48	BHAD80
1.31	2.10	1 40	180	170	-	4.35	
1.41	2.00	1.40	222	169	.079	4.42	TAWH75
1.50	2.01	1.34	.222	. 10 9		4.37	LEIC77
1.50	2.55			210		5.1	BHADSO
1.51	3.10	1.60	.220	.210		5.8	
1.61	3.40	1.90	.240	.250		6.3	
1.71	3.70	2.10	.270	.250	110	6.5	TAWH79
1.75	3.84	2.02	.298	.200		6.7	BHADS
1.81	4.10	2.10	.270	.200	100	0.1	TAUUT
2.00	5.3	2.78	.454	.328	.150	9.0	LETCT
2.00	5.4	-	-	-	-	9.3	LEICI

R. S. SOKHI and D. CRUMPTON L-Shell Cross Sections for Protons

TABLE A. Experimental L-Shell X-Ray Production Cross Sections for Proton Impact

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Z=92 URANIUM(U) CONTINUED

TABLE AII EXPERIMENTAL X-RAY PRODUCTION CROSS SECTIONS CONTINUED THIN TARGET

ENERGY	ALPHA	BETA	GAMMA	L	ETA	TOTAL	REF
MeV			BARN	S			
2.25	7.1	3.81	.64	.449	.230	12.2	TAWH75
2.25	5.4		-	-	-		BEAR73
2.50	8.7	4.68	.86	.56	.260	15.0	TAWH75
2 50	9.0		-	-	-	15.7	LEIC77
2 75	11.0	6 2	1.03	.67	. 390	19.3	TAWH75
3.00					-	21.8	BONG78
3.00	14 0			-	-	25.0	LEIC77
3.00	12.8	7 3	1.30	.92	. 390	22.7	TAWH75
3.00	10.0	1.5				_	BEAR73
3.00	15.8	0 1	1 6#	1.00	450	28.0	TAWH75
3.25	19.0	10.9	1 85	1 10	57	32.9	
3.50	10.0	10.0	2.00	1 22	62	37 6	
3.75	21.0	12.4	2.29	1.33	.05	117 1	
4.00	24.0	14.3	2.50	1.40		43.1	
4.25	29.6	17.0	3.37	1.85	.00	23	
4.50	31.5	19.1	3 47	2.02	1.00	51	

TABLE AI	II	1	LALPHA/LL	RATIO			
ENERGY RANGE Mev	TARGET	LA/LL	REF	ENERGY RANGE Mev	TARGET	LA/LL	REF
1 0-4 5	THIN	15.6+-1.2	TAWH75	.43-1.81	THIN	14.7+-0.2	BHADSO

### Z=38 STRONTIUM(SR)

TABLE	BI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
30NG78	3.0	THIN	-	•	LT 14	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED. K-SHELL STUDIED. METAL TARGET ON CARBON BACKING.
TABLE	BII	EXPERIMENT	L IONIZA	TION CR	OSS SEC	TIONS	
THIN 1	TARGET						
ENERG: MeV	TOTAL BARNS	S RI	EF	EN	ERGY NeV	TOTAL BARNS	REF
3.00	9261	1 BOI	NG78				
Z=39	TTRIUM(Y)						
							· •
TABLE	BI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
PONM79	4.0-22.0	THIN		6.0(C)	-	BEA(G3) PWBA2 PWBA3	Ge(L1) AND S1(L1) DETECTOR USED. METAL TARGET ON MYLAR BACKING. He4 IMPACT STUDIED.

EXPERIMENTAL IONIZATION CROSS SECTIONS TABLE BII

#### THIN TARGET

.

ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	TOTAL BARNS	REF
4.00 6.00 8.00 10.00 12.00	57100 61000 59000 53500 53100	PONM79	14.00 16.00 18.00 20.00 22.00	47500 45500 41300 38600 36500	PONM79

#### Z=40 ZIRCONIUM(ZR)

TABLE BI			EXPERIMENTAL DETAILS					
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP Error	THEORIES	COMMENTS	
KROA82	.10157422	110+-2			LT 16-11	B CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON	

CARBON BACKING.

EXPERIMENTAL IONIZATION CROSS SECTIONS TABLE BII

THIN TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	BARNS	REF
. 1015 . 1334 . 1638 .2051 . 2566	54 183 303 616 1320	KROA82	.3179 .3991 .4903 .6011 .7422	1950 3300 4640 7110 10700	KROA82

#### Z=41 NIOBIUM(NB)

TABLE BI EXPERIMENTAL DETAILS

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
ROA82	.09167459	55+-3		•	LT 15-1	7 CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USE

D. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING.

#### TABLE BII EXPERIMENTAL IONIZATION CROSS SECTIONS

THIN TARGET

K

ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	TOTAL BARNS	REF
.0916 .1115 .1417 .1723 .2129 .2634	25.7 57 133 274 494 822	KROA82	- 3239 - 4044 - 4951 - 6058 - 7459	1350 2260 3510 5150 7500	KROA82

Z=45 RHODIUM(RH)

TABLE BI			EXPERIMENTAL DETAILS					
REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS	
ROA82	.09744	88+-5	•	-	L1 15-19 L2 15-20 L3 18-24 LT 15-19 R1 22-28 R2 23-31	CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING.	

TABLE BII		EXPERIM	ENTAL IONIZA	SECTIONS			
THIN TA	RGET						
ENERGY	<u>L1</u>	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.0900 .1096 .1393 .1696 .2100 .2604 .3211 .4019 .4925 .6031 .7440	1.08 2.29 4.39 6.4 9.2 11.2 17.0 32.4 86 191 394	1.32 3.58 10.4 22.0 48.5 92 159 272 436 641 943	2.86 8.0 23.1 49.1 108 205 350 592 937 1370 1980	.82 .64 .289 .189 .122 .107 .119 .198 .299 .418	.379 .288 .190 .085 .055 .049 .055 .092 .140 .199	5.3 13.8 38.0 78 166 309 525 896 1460 2200 3310	KROA82

#### Z=46 PALLADIUM(PD)

TABLE BI

#### EXPERIMENTAL DETAILS

REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
CHAR75	3-12	21+-2	-		LT 20	BEA(G3) PWBA3	RBS EMPLOYED. EFFICIENCY CALCULATED. 05+ IMPACT STUDIED. METAL TARGET ON CARBON BACKING.
KROA82	.097438	99+-6	•	-	L1 15-20 L2 15-22 L3 17-20 LT 14-20 R1 21-20 R2 23-3	D CPSSR 2 6 9 3	CRYSTAL SPECTROMETER AND S1(L1) USED RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING.

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# TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

### Z=46 PALLADIUM(PD) CONTINUED

TABLE BII		EXPERIM	ENTAL IONIZA	SECTIONS			
THIN TA	RGET						
ENERGY	<u>L1</u>	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.0900 .1093 .1389 .1692 .2094 .2094 .2094 .3207 .4015 .4920 .6026	.89 1.93 4.13 5.9 8.8 10.4 16.7 31.8 69 153	.90 2.60 7.7 16.4 36.1 71 129 221 350 534	2.03 5.9 17.6 37.6 83 162 294 495 776 1160	.99 .74 .54 .361 .244 .147 .129 .144 .196 .287	.438 .327 .234 .158 .106 .064 .057 .064 .088 .132	3.81 10.4 29.5 60 128 244 440 748 1190 1850	KROA82
. 7438 3.0000 5.0000 6.0000 7.0000 8.0000 9.0000 0.0000 1.0000 2.0000				.431		2720 36000 46000 52000 53000 55000 55000 56000 56000 51000 46000	CHAR75

#### Z=47 SILVER(AG)

TABLE BI			EXPERIMENTAL DETAILS					
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS	
CHAR75	3-12	22+-2		-	LT 20	BEA(G3) PWBA3	RBS EMPLOYED. EFFICIENCY CALCULATED. 05+ IMPACT STUDIED. METAL TARGET ON CARBON BACKING.	
BONG78	3.0	THIN	-	•	LT 15	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED. K-SHELL STUDIED SELF-SUPPORTING METAL TARGET.	
CUZP81	.611-3.85	THIN	-	•	LT 5-11	BEA(H) SCA2 PWBA3	EFFICIENCY MEASURED. AgIO3 TARGET ON CARBON BACKING. CROSS SECTIONS EVALUATED BY NORMALIZING TO K-SHELL DATA.	
KROA82	.1397744	95+-3		-	L1 15-16 L2 15-17 L3 17-20 LT 15-16 R1 21-24 R2 23-26	CPSSR	CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING.	

#### Z=47 SILVER(AG) CONTINUED

TABLE BII EXPERIMENTAL IONIZATION CROSS SECTIONS

THIN	TARGET

ENERGY	L1	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.1397	3.35	5.3	12.4	.63	.270	21.1	KROA82
. 1697	5.3	11.9	27.9	.448	. 191	45.1	
.2102	8.3	26.7	63	.310	.130	98	
.2608	11.3	54	126	.211	.089	191	
. 3214	14.1	95 .	224	.149	.063	333	
.4020	25.1	169	393	. 149	.064	587	
.4925	56	288	661	. 196	.085	1000	
.6034	119	419	948	.284	. 125	1490	
.6110	-	_	-	-	-	2590	CUZP81
.7440	270	640	1430	.422	. 189	2340	KROA82
.8110			-	-	-	5279	CUZP81
1 0190			-	-	-	7672	
1 2000	_	_	-	-	-	9820	
1 4000		-	-		-	12393	
1 6000			-		-	12885	
1 8000					-	14869	
2 0000						18525	
2 2000		-				17869	
2 4000			1	_		19672	
2 6000						21967	
2 8000						25902	
3 0000					-	25082	
3.0000						23750	BONG78
3 0000					-	30000	CHAR75
3 2000						27377	CUZP81
2 4000	1.00					27705	
3.4000						20836	
3.0000				-		20672	
3.8000			-			20508	
3.0500	-					40000	CHAR75
4.0000	-	-			-	40000	CHARTS
5.0000		-			-	44000	
6.0000	-		-		-	49000	
7.0000	-	•	-		-	49000	
0.0000	-	-	-		-	46000	
9.0000	-	•	•		-	46000	
0.0000	-	-				40000	
1.0000	-	-	-	-	-	43000	
2.0000	-	-	-	-		40000	

#### Z=48 CADMIUM(CD)

#### TABLE BI

EXPERIMENTAL DETAILS

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	ERF 9	CP ROR	THEORIES	COMMENTS
BONG78	3.0	THIN		•	LT	12	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED. K-SHELL STUDIED. METAL TARGET ON

CARBON BACKING.

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TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

### Z=48 CADMIUM(CD) CONTINUED

TABLE	BI		EXPERIMEN	NTAL DE	TAILS C	ONTINUED	
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
ROA82	.13727422	126+-4		•	L1 14-1 L2 15-1 L3 17-2 LT 14-1 R1 21-2 R2 22-2	6 CPSSR 7 0 6 4 6	CRYSTAL SPECTROMETER AND S1(L1) USEN RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON VITRIOUS CARBON BACKING.

TABLE E	BII	EXPERIM	ENTAL IONIZA	TION CROSS S	SECTIONS		
THIN TA	RGET						
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.1372 .1673 .2076 .2581 .3188 .3997 .4906 .6015	2.61 4.48 6.8 9.2 11.4 19.7 41.2 93	3.27 7.6 17.3 36.2 67 122 204 329	7.6 18.0 41.7 88 163 293 482 760	.80 .59 .394 .253 .171 .162 .202 .282	.344 .249 .164 .104 .070 .067 .086 .122	13.5 30.1 66 133 241 435 727 1180	KROA82
3.0000	214	509 -	-	.420	- 100	19913	BONG78

#### Z=49 INDIUM(IN)

TABLE BI

#### EXPERIMENTAL DETAILS

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
KROA82	.13597417	136+-8			L1 14- L2 15- L3 17-3 LT 14- R1 20-3 R2 22-3	16 CPSSR 18 22 16 24 28	CRYSTAL SPECTROMETER AND S1(L1) USED. RBS EMLPOYED. EFFICIENCY CALCULATED. METAL TARGET ON VITRIOUS CARBON BACKING.

TABLE BI	I	EXPERIMEN	NTAL IONIZA	TION CROSS	SECTIONS		
THIN TAP	GET						
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.1359 .1661 .2066	2.40 4.35 6.9	2.26 5.5 12.8	5.1 12.8 30.7	1.06 .79 .54	.472 .339 .224	9.7 22.7 50	KROA82

# Z=49 INDIUM(IN) CONTINUED

TABLE BII		EXPERIMEN	TAL IONIZA	TION CROSS	SECTIONS	CONTINUED	
THIN TA	RGET						
ENERGY	<u>L1</u>	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.2573 .3180 .3989 .4897 .6006 .7417	9.3 11.6 17.5 34.0 75 177	27.4 53 98 167 262 411	67 130 239 401 618 940	.340 .220 .179 .204 .285 .430	.138 .090 .073 .085 .121 .188	104 194 353 602 955 1530	KROA82

### Z=50 TIN(SN)

TABLE	BI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
CHAR75	3-12	29+-3	-	-	LT 20	BEA(G3) PWBA3	RBS EMPLOYED. EFFICIENCY CALCULATED. 05+ IMPACT STUDIED. METAL TARGET ON CARBON BACKING.
BONG78	3.0	THIN	·		LT 12	BEA(G3)	RES EMPLOYED. EFFICIENCY MEASURED. K-SHELL STUDIED. SELF-SUPPORTING METAL TARGET.
PONM79	4.0-22.0	THIN	-	6.0(C)	-	BEA(G3) PWBA2 PWBA3	Ge(L1) AND Si(L1) DETECTORS USED. METAL TARGET ON MYLAR BACKING. He4 IMPACT STUDIED.
KROA82	.137743	115+-5	-	-	L1 14-17 L2 15-19 L3 16-19 LT 14-17 R1 21-25 R2 21-25	CPSSR	CRYSTAL SPECTROMETER AND SI(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON VITRIOUS CARBON BACKING.

TABLE BI	I	EXPERIMEN	NTAL IONIZA	TION CROSS	SECTIONS		
THIN TAP	GET						
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.1370 .1678 .2084	1.27 2.45 3.91	1.47 3.78 9.3	4.00 10.2 24.4	.86 .65 .423	.317 .240 .160	6.7 16.4 37.6	KROA82
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# TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

Z=50 TIN(SN) CONTINUED

TABLE BI	I	EXPERIMENTAL	IONIZATION	CROSS	SECTIONS	CONTINUED	
THIN TAR	GET						
ENERGY	L1	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
		10 5	51	273	. 105	76	KROA82
.2591	5.3	19.5	21	188	072	144	
.3199	7.1	38.1	99	126	053	280	
.4007	10.3	76	194	.150	058	1179	
.4915	19.2	130	330	- 141	.090	754	
.6023	40.8	203	510	.201	.000	1200	
7430	95	318	791	.300	.121	1200	BONCTS
3.0000	-	-	5 - 5 N 1 1	-		14015	CUARTE
3 0000	-	- H	-	-	-	19000	CHARIS
1 0000	-	-	-	-	-	23000	
4.0000		-	-	-		16100	PUNMIS
4.0000			-	-	-	30000	CHAR75
5.0000			-	-	-	32000	
6.0000	-		-	-	-	20000	PONM79
6.0000	-			-	-	33000	CHAR75
7.0000	-	•	1.2	-	-	34000	
8.0000	-	-		_	-	20300	PONM79
8.0000	-	-			_	35000	CHAR75
9.0000	-	-				33000	
10.0000	-	-	-	-		20000	PONM79
10.0000	-	-	-	-		31000	CHAR75
11.0000	-	-	•	-		30000	
12.0000	-	-	-	-	-	30000	PONM70
12 0000	-	110 - 1 <b>1</b>	-	-	-	19100	FUNNIS
14 0000			-	-	-	18500	
16 0000	_		-	-		16700	
18 0000			-	-	-	16000	
20.0000			-	-	-	14700	
20.0000			-	-	-	13600	
// 10100	-						

# Z=51 ANTIMONY(SB)

TABLE BI

#### EXPERIMENTAL DETAILS

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
KROA82	.13997433	106+-4		-	L1 15-1 L2 15-2 L3 16-2 LT 15-1 R1 21-2 R2 22-2	7 CPSSR 0 0 7 6 6	CRYSTAL SPECTROMETER AND SI(L1) USED. RBS EMPLOYED. EFFICIENCY CALCULATED. METAL TARGET ON CARBON BACKING.

TABLE BI	I	EXPERIMEN	TAL IONIZAT	TION CROSS	SECTIONS		
THIN TAR	GET						
ENERGY	L1	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.1399 .1693 .2096 .2601 .3206	1.29 2.47 4.09 6.3 8.3	1.28 3.18 7.7 18.0 35.7	3.33 8.3 20.0 46.4 91	1.01 .78 .53 .348 .232	.388 .297 .204 .135 .091	5.9 14.0 31.8 71 135	KROA82

R. S. SOKHI and D. CRUMPTON L-Shell Cross Sections for Protons

TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

#### Z=51 ANTIMONY(SB) CONTINUED

TABLE B	II	EXPERIMEN	TAL IONIZA	TION CROSS	SECTIONS	CONTINUED	
THIN TA	RGET						
ENERGY	<u>L1</u>	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.4017 .4921 .6028 .7433	10.4 17.7 35.5 84	66 112 176 284	165 279 433 688	. 158 . 158 .202 .295	.063 .063 .082 .122	241 409 644 1060	KROA82

Z=53 IODINE(I)

TABLE	BI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BONG78	3.0-11.0	THIN	-		LT 10	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED. K-SHELL STUDIED. TARGET ON CARBON BACKING.
CUZP8 1	.611-3.85	THIN	•	-	LT 5-10	BEA(H) SCA2 PWBA3	EFFICIENCY MEASURED. AgIO3 TARGET ON CARBON BACKING. CROSS SECTIONS EVALUATED BY NORMALIZING TO K-SHELL DATA.

ECTIONS	
TOTAL BARNS	REF
9403 7204 7989 8667 9473 9753 9849 14985 17955 18209 17627	BONG78 CUZP81 BONG78
	TOTAL BARNS 9403 7204 7989 8667 9473 9753 9753 9849 14985 17955 18209 17627

Z=55 CESIUM(CS)

TABLE	BI		EXPERIME	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
ONM79	4.0-22.0	THIN		6.0(C)	-	BEA(G3) PWBA2 PWBA3	Ge(L1) AND S1(L1) DETECTORS USED. METAL TARGET ON MYLAR BACKING. He4 IMPACT STUDIED.

TABLE BII EXPERIMENTAL IONIZATION CROSS SECTIONS

THIN TARGET

ENERGY MeV	TOTAL BARNS	REF	ENERGY Mev	TOTAL	REF
4.00 6.00 8.00 10.00 12.00	3680 5850 6600 7380 7320	PONM79	14.00 16.00 18.00 20.00 22.00	7050 6920 6650 6550 6340	PONM79

Z=58 CERIUM(CE)

TABLE BI

EXPERIMENTAL DETAILS

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
PONM79	4.0-22.0	THIN	-	6.0(C)	-	BEA(G3) PWBA2 PWBA3	Ge(L1) AND S1(L1) DETECTORS USED. METAL TARGET ON MYLAR BACKING. He4 IMPACT STUDIED.

TABLE BIT	EXPER	RIMENTAL IONIZA	TION CROSS SE	CTIONS	
THIN TARC	DET				
ENERGY MeV	TOTAL BARNS	REF	ENERGY MeV	TOTAL BARNS	REF
4.00 6.00 8.00 10.00 12.00	3350 4670 5530 6610 7100	PONM79	14.00 16.00 18.00 20.00 22.00	6540 6050 5870 5400 5150	PONMT

### Z=59 PRASEODYMIUM(PR)

TABLE	BI		EXPERIME	NTAL DE	TAILS			
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMEN	rs
WHER79	.1540	THICK		2.0(B)	L1 20 L2 20 L3 15	PSS PSSR PWBA3	EFFICIEN MEASURED GAMMA(1) GAMMA(2+ SECTIONS	AND 3) CROSS QUOTED.
TABLE	BII	EXPERI	ENTAL IO	NIZATIO	N CROSS	SECTIONS		
THICK	TARGET							
ENERGY	L1	L2	L3		L1/L2	L1/L3	TOTAL	REF
MeV		BARNS					BARNS	
.150 .175 .200 .250 .300 .350 .400	.180 .390 .71 1.60 2.80 4.00 5.0	.044 .130 .290 1.10 2.60 5.3 9.1	.2 .6 1.4 4.5 10.0 19.0 31.0	70 8 0 0	4.09 3.00 2.45 1.45 1.08 .75 .55	.67 .57 .356 .280 .211 .161	.494 1.20 2.40 7.2 15.4 28.3 45.1	WHER79
<u>Z=62</u>	SAMARIUM(SH	<u>4)</u>						
TABLE	BI		EXPERIME	NTAL DE	TAILS			
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMEN	TS
PONM79	4.0-22.0	THIN		6.0(C)	•	BEA(G3) PWBA2 PWBA3	Ge(L1) A S1(L1) D USED. METAL TA MYLAR BA He4 IMPA STUDIED.	ND ETECTORS RGET ON CKING. CT
WHER79	.1544	THICK	-	2.0(B)	L1 20 L2 20 L3 15	PSS PSSR PWBA3	EFFICIEN MEASURED GAMMA(1) GAMMA(2+ SECTIONS	CY AND 3) CROSS QUOTED.
TABLE	BII	EXPERI	MENTAL IO	NIZATIO	N CROSS	SECTIONS		
THIN	TARGET							
ENERG	Y <u>L1</u>	L2	L3		L1/L2	L1/L3	DADAS	REF
MeV		BARNS					BANNS	DOUNDO
4.00 6.00 8.00					÷		4100 5430 5680	PUNM/9

#### Z=62 SAMARIUM(SM) CONTINUED

	EXPERIMENTAL	IONIZATION	CROSS	SECTIONS	CONTINUED	
ET						
LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
	BARNS				BARNS	
	-	-	-	-	6340	PONM79
-		-	-	-	6600	
-	-	-	-	-	6420	
-	•	-	-	-	6240	
-		-	-		6040	
-		•	-	-	5850	
GET	*					
LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
	BARNS				BARNS	
.052 .130 .250 .64 1.10 1.60 2.00 2.30	.021 .064 .150 .56 1.40 2.70 4.50 1 6.1 2	.095 .259 .58 2.00 4.70 8.9 5.0 0.0	2.48 2.03 1.67 1.14 .79 .59 .444 .377	.55 .50 .431 .320 .234 .180 .133 .115	.168 .453 .98 3.20 7.2 13.2 21.5 28.4	WHER79
	ET <u>L1</u> - - - - - - - - - - - - -	EXPERIMENTAL ET L1 L2 BARNS     GET L1 L2 BARNS .052 .021 .130 .064 .250 .150 .64 .56 1.10 1.40 1.60 2.70 2.00 4.50 1 2.30 6.1 2	EXPERIMENTAL IONIZATION ET L1 L2 L3 BARNS     GET L1 L2 L3 BARNS .052 .021 .095 .130 .064 .259 .250 .150 .58 .64 .56 2.00 1.10 1.40 4.70 1.60 2.70 8.9 2.00 4.50 15.0 2.30 6.1 20.0	$\begin{array}{c cccccc} EXPERIMENTAL IONIZATION CROSS \\ ET \\ \hline \\ L1 & L2 & L3 & L1/L2 \\ \hline \\ BARNS \\ \hline \\ \hline \\ BARNS \\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ GET \\ \hline \\ L1 & L2 & L3 & L1/L2 \\ \hline \\ \hline \\ GET \\ \hline \\ L1 & L2 & L3 & L1/L2 \\ \hline \\ \hline \\ GET \\ \hline \\ $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	EXPERIMENTAL IONIZATION CROSS SECTIONS CONTINUED   ET   L1 L2 L3 L1/L2 L1/L3 TOTAL   BARNS   - - - 6340   - - - 6600   - - - 6600   - - - 6420   - - - 6040   - - - 5850   GET   L1 L2 L3 L1/L2 L1/L3 TOTAL   BARNS   .052 .021 .095 2.48 .55 .168   .11/L2 L1/L3 TOTAL   BARNS   .052 .021 .095 2.48 .55 .168   .130 .064 .259 2.03 .50 .453   .052 .021 .095 2.48 .55 .168   .130 .064 .259 2.03 .50 .453   .250 .150 .58 <

#### Z=65 TERBIUM(TB)

EXPERIMENTAL DETAILS TABLE BI ENERGY AREAL BEAM BEAM EXP RANGE DENSITY CURRENT COLL ERROR MeV E-6G/CMSQ A mm % THEORIES COMMENTS REF 2.0(B) L1 20 L2 20 L3 15 EFFICIENCY MEASURED. GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED. PSS PSSR PWBA3 WHER79 .15-.40 THICK -

TABLE BII		EXPERIMENT	EXPERIMENTAL IONIZATION CROSS SECTIONS							
THICK TA	RGET									
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF			
MeV		BARNS				BARNS				
.150 .175 .200 .250 .300 .350	.021 .057 .120 .350 .72 1.20	9.0E-03 .027 .069 .270 .73 1.50 2.80	.032 .092 .220 .82 2.20 4.60 8.4	2.33 2.11 1.74 1.30 .99 .80 .61	.66 .62 .55 .427 .327 .261 .202	.062 .176 .409 1.44 3.65 7.3 12.9	WHER79			

## Z=66 DYSPROSIUM(DY)

TABLE	BI		EXPERIMEN	NTAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
ITW82	0.15-9.5	85	-	-	R1 20-30 R2 20-30	PWBA4 PWBABC RPWBABC CPSSR	BOTH SURFACES OF TARGET COVERD WITH THIN FILM OF CARBON. GAMMA(1)/ALPHA
			•				AND GAMMA(2+3)/ALPHA INTENSITY RATIOS PRESENTED.

		SECTIONS	ON CROSS	IONIZATIO	EXPERIMENTAL		TABLE BII
						ET	THIN TARG
REF	TOTAL	L1/L3	L1/L2	L3	L2	LI	ENERGY
	BARNS				BARNS		MeV
ITW82		.84	3.01	-		-	.150
	-	.83	2.86	-	-	-	165
	-	.82	2.77	-	-	-	.175
	-	.77	2.46	-	-		210
		.69	2.22	-			240
	-	.55	1.83	-			280
	-	.52	1.61	-	-		200
	-	.384	1.18	-	_		350
		. 194	.60	-	_	-	500
	-	.091	.267	-			
	-	.071	.198		A CONTRACTOR OF A CONTRACTOR A CONTRA	-	1 000
	-	.108	284			-	1.000
	-	.307	78		-		1.400
		302	84		-	-	2.500
	-	.432	1.13	-	1	-	9.500
		.62 .77 .69 .55 .52 .384 .194 .091 .071 .108 .307 .302 .432	2.11 2.46 2.22 1.83 1.61 1.18 .60 .267 .198 .284 .284 .84 1.13				.175 .210 .280 .300 .350 .700 1.000 1.400 2.500 3.000 9.500

# Z=67 HOLMIUM(HO)

TABLE	BI		EXPERIME	NTAL DET	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
PONM79	4.0-22.0	THIN	-	6.0(C)	-	BEA(G3) PWBA2 PWBA3	Ge(L1) AND S1(L1) DETECTORS USED. METAL TARGET ON MYLAR BACKING. He4 IMPACT STUDIED.
WHER79	.1540	THICK	-	2.0(B)	L1 20 L2 20 L3 15	PSS PSSR PWBA3	EFFICIENCY MEASURED. GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED.

## Z=67 HOLMIUM(HO) CONTINUED

TABLE BI	I	EXPERIMENT	AL IONIZAT	TION CROSS	SECTIONS		
THIN TAR	GET						
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
4.00 6.00 8.00 12.00 14.00 16.00 18.00 20.00 22.00						1720 2540 3570 4180 4450 4660 4730 4560 4350	PONM79
THICK TAI	RGET						
MeV	<u>L1</u>	BARNS		L1/L2	L1/L3	BARNS	REF
.150 .175 .200 .250 .300 .350 .400	.012 .044 .120 .390 .72 .93 .94	3.4E-03 .015 .045 .210 .55 .96 1.30	.017 .063 .170 .70 1.70 3.00 4.30	3.53 2.93 2.67 1.86 1.31 .97 .72	.71 .70 .71 .56 .424 .310 .219	.032 .122 .335 1.30 2.97 4.89 6.5	WHER79
Z=70 YTT	ERBIUM(YB	2					

TABLE	BI		EXPERIME	NTAL DE	TAI	LS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	ERI	KP ROR	THEORIES	COMMENTS
HER79	.1540	THICK		2.0(B)	L1 L2 L3	20 20 15	PSS PSSR PWBA3	EFFICIENCY MEASURED. GAMMA(1) AND GAMMA(2+3) CROSS SECTIONS QUOTED.

TABLE BII		EXPERIMENT	AL IONIZATI	ON CROSS	SECTIONS		
THICK TA	RGET						
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	RÈF
MeV		BARNS				BARNS	
.150 .175 .200 .250 .300 .350 .400	3.3E-03 .014 .042 .180 .400 .62 .76	7.4E-04 4.2E-03 .015 .087 .240 .440 .60	5.5E-03 .020 .056 .250 .70 1.50 2.40	4.46 3.33 2.80 2.07 1.67 1.41 1.27	.60 .70 .75 .72 .57 .413 .317	9.5E-03 .038 .113 .52 1.34 2.56 3.76	WHER79

Z=72 HAFNIUM(HF)

TABLE	BI		EXPERIMEN	TAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
JUSE80	0.5-2.5	50	30-200E-9	•	L1 7-9 L2 7-9 L3 6-9 LT 7-9 R1 10-12 R2 9-11	PWBA5 PWBABTR	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMYAR BACKING. He+ IMPACT STUDIED.

TABLE BII		EXPERIME	NTAL IONIZA	TION CROSS S	ECTIONS		
THIN TAN	RGET		•				
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.50 .60 .70 .80 1.00 1.10 1.20 1.30 1.30 1.50 1.60 1.80 2.50	1.38 1.90 2.48 3.00 3.24 4.31 5.9 7.7 10.0 11.7 14.5 24.0 31.4	1.22 2.32 4.40 6.5 8.8 11.0 14.3 18.0 22.7 27.4 31.2 34.6 49.0 60 95	5.2 9.9 16.7 23.8 32.1 40.1 51 64 80 93 107 121 154 183 273	1.13 .82 .56 .460 .370 .300 .330 .340 .370 .370 .370 .420 .490 .53 .72	.276 .192 .149 .126 .101 .101 .085 .092 .095 .107 .109 .120 .156 .172 .253	7.8 14.1 23.5 33.0 44.0 55 69 88 111 131 150 170 227 274 437	JUSEBO

# Z=73 TANTALUM(TA)

TABLE	BI		EXPERIMEN	TAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSC	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
JUSE80	0.6-2.5	50	30-200E-9	-	L1 11 L2 7-9 L3 8 LT 9 R1 10 R2 8	PWBA5 PWBABTR	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. He+ IMPACT STUDIED.

### Z=73 TANTALUM(TA) CONTINUED

TABLE BII EXPERIMENTAL IONIZATION CROSS SECTIONS

THIN TARGET

ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.60 .80 1.00 1.20 1.30 1.40 1.50	1.70 2.80 3.50 3.80 4.90 6.1 7.8	2.20 5.8 11.0 19.3 22.9 28.1 33.1	7.3 18.0 33.1 53 62 75 87	.78 .480 .310 .200 .210 .220 .230	.240 .150 .100 .072 .078 .082 .089	11.3 26.6 47.6 76 90 109 128	JUSE80
1.60 1.80 2.00 2.50	11.0 19.0 26.0 57	37.2 48.2 60 97	100 128 171 238	.300 .390 .430 .59	.110 .150 .150 .240	148 195 258 391	

#### Z=74 TUNGSTEN(W)

TABLE	BI		EXPERIME	NTAL DE	TAILS	14	
REF .	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
PONM79	4.0-22.0	THIN		6.0(C)	-	BEA(G3) PWBA2 PWBA3	Ge(L1) AND S1(L1) DETECTORS USED. METAL TARGET ON MYLAR BACKING. He4 IMPACT STUDIED.
JUSE80	0.5-2.5	50	30-200E-9	-	L1 6-13 L2 7-9 L3 7-10 LT 8 R1 7-13 R2 7-14	PWBA5 PWBABTR	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. He+ IMPACT STUDIED.

TABLE B	II	EXPERIME	NTAL IONIZA	TION CROSS	SECTIONS		
THIN TAN	RGET						
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.50 .70 .80 .90 1.00 1.10 1.20 1.30 1.40 1.50	1.19 2.39 2.71 2.97 3.29 3.84 4.29 5.5 6.8 10.0	.80 2.49 4.28 6.1 8.2 11.4 15.1 17.9 20.9 24.9	3.10 9.9 15.3 22.7 30.7 40.6 52 60 73 78	1.49 .96 .63 .489 .402 .337 .285 .306 .328	.384 .241 .178 .131 .107 .095 .083 .091 .093	5.1 14.8 22.2 31.8 42.2 56 71 84 100	JUSE80

R. S. SOKHI and D. CRUMPTON L-Shell Cross Sections for Protons

TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

TABLE B	II	EXPERIMENTAL	IONIZATION	CROSS	SECTIONS	CONTINUED	
THIN TA	RGET						
ENERGY	<u>L1</u>	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
1.60 1.70 1.80 1.90 2.00	11.9 14.5 19.7 21.6 24.7	27.9 32.5 36.9 43.2 47.3	87 98 114 136 147	.428 .447 .53 .50 .52	.137 .147 .173 .159 .169	127 145 170 201 219	JUSE80
2.50 4.00 6.00 10.00 12.00 14.00 16.00 18.00	51	73		.70	.244	532 530 950 1350 1630 1910 2000 2040 2120	PONH79
20.00	-		-	-	-	2140	

# Z=74 TUNGSTEN(W) CONTINUED

## Z=77 IRIDIUM(IR)

TABLE BI

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
JUSE80	0.6-2.5	50	30-200E-9	-	L1 7-9 L2 8 L3 8 LT 8 R1 9 R2 8	PWBA5 PWBABTR	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING.

EXPERIMENTAL DETAILS

TABLE BII		EXPERIME	NTAL IONIZA	TION CROSS	SECTIONS		
THIN TAL	RGET		*				
ENERGY	L1	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.60 .70 .80 .90 1.00 1.10 1.20 1.30 1.40 1.50 1.60 1.70 1.80	1.41 2.06 2.12 2.44 2.85 3.00 3.35 3.53 4.00 5.8 8.5 10.3	.76 1.27 2.46 3.57 4.79 6.1 8.3 11.5 13.9 15.3 18.2 22.1 24.2	2.84 5.1 8.2 12.2 16.5 21.7 27.0 32.9 40.2 40.2 47.1 54 63 71	1.85 1.63 .86 .60 .493 .405 .307 .287 .373 .372 .386 .426 .426	.496 .404 .260 .200 .173 .138 .124 .107 .100 .122 .125 .134 .145	5.0 8.4 12.7 18.2 24.2 30.8 38.6 47.9 58 68 79 94 106 133	JUSE80
2.00	29.4	47.8	132	.62	.223	209	

Z=79 GOLD(AU)

TABLE	BI		EXPERIMEN	TAL DE	TAILS		
REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
BONG78	3.0-11.0	THIN	•	-	LT 7	BEA(G3) PWBA2	RBS EMPLOYED. EFFICIENCY MEASURED. SELF-SUPPORTING METAL TARGET.
PONM79	4.0-22.0	THIN	-	6.0(C)	-	BEA(G3) PWBA2 PWBA3	Ge(L1) AND S1(L1) DETECTORS USED. METAL TARGET ON MYLAR BACKING. He4 IMPACT STUDIED. M-SHELL STUDIED.
COHD80	1.0-3.0	7.5+2 THICK	15E-9	-	L1 23 L2 20 L3 11 LT 11	PWBA4 PWBAR CPSSR	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING.
SARL80	2.0	THIN	-	-	L1 19 L2 15 L3 15 LT 11	PWBA1 PWBABC MPWBABCR	EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING. C12 N14 016 IMPACT STUDIED. USED ATOMIC PARAMETERS FROM REF(7+8); AND REF(34)*.
JITW82	0.175-10.0	95	-	•	R1 20-3 R2 20-3	D RSCA D PWBA4 PWBABC RPWBABC CPSSR	SELF-SUPPORTING METAL TARGET. GAMMA(1)/ALPHA AND GAMMA(2+3+6)/ ALPHA INTENSITY RATIOS PRESENTED.
PINA82	0.5-4.0	50	30-200E-9	-*	L1 9-11 L2 7-17 L3 6-9 LT 6-9 R1 11 R2 12		RBS EMPLOYED. EFFICIENCY MEASURED. SELF-SUPPORTING METAL TARGET. RADIATIVE DECAY BRANCHING RATIOS MEASURED.

TABLE BI	I	EXPERIMENT	AL IONIZAT	TION CROSS	SECTIONS		
THIN TAR	GET						
ENERGY	L1	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
. 175	-	-	-	4.90	.490	-	JITW82
.210	-	-	-	5.1	.63	-	
.250	-	-	-	4.94	.69	-	
.300	-	-	-	4.20	.69	-	
.350	-	-	-	3.47	.63	-	
.500	-	-	-	1.86	. 398	-	
.500	.59	. 195	1.43	3.02	.413	2.21	PINA82
.600	1.09	.53	2.88	2.07	.378	4.50	
.700			-	.89	.221	-	JITW82

## Z=79 GOLD(AU) CONTINUED

TABLE	TABLE BIL		EXPERIMENTAL IONIZATION CROSS SECTIONS CONTINUE						
THIN T.	ARGET								
ENERGY	<u>L1</u>	L2	L3	L1/L2	. L1/L3	TOTAL	REF		
MeV		BARNS				BARNS			
.700	1.32	.82	4.36	1.62	.303	6.5	PINA82		
.800	1.41	1.53	7.3	.92	. 193	10.2			
.900	1 52	2 28	10.0	.492	.136	-	JITW82		
1.000	1.32	3.11	13.0	.04	.142	14.7	PINA82		
1.000	1.71	3.60	14.6	424	. 102	10.8	COHDSO		
1.100	1.88	4.48	18.4	.420	102	24 8	PINAOZ		
1.200	2.36	5.2	20.4	.453	. 116	27.1	COHDRO		
1.200	a 100 - 11	-	-	.285	.083		JITW82		
1.200	2.18	5.9	23.5	.369	.093	31.5	PINA82		
1.300	2.62	7.7	28.8	.342	.091	39.0			
1.400	3.05	7.9	29.2	.464	. 125	39.7	COHD80		
1.500	2.05	9.0	37.4	.319	.076	49.2	PINA82		
1.500	3.91	10 3	41 1	.231	.071	-	JITW82		
1.600	5.2	11.1	30.5	.300	.095	55	PINA82		
1.600	5.0	12.3	49.1	405	102	22	COHD80		
1.700	5.5	14.2	55	. 386	100	75	PINAOZ		
1.800	7.0	14.8	51	.470	.136	72	COHDSO		
1.800		-	-	.309	. 101	-	JITW82		
1.800	0.2	16.5	64	.375	.096	87	PINA82		
2.000	9.0	19.1	54	.471	.140	91	COHD80		
2.000	6.6	23.0	72	.325	. 108	103	SARL801		
2.000	8.4	21.6	77	.310	.094	98	SARL80		
2.100	-	-		- 305	.109	107	PINA82		
2.200	11.3	23.9	79	473	142	112	JIIWOZ		
2.400	13.9	29.3	95	.474	.147	135	CONDEO		
2.500		-	-	.456	. 157		JTTW82		
2.500	17.6	33.1	114 .	.53	. 155	165	PINA82		
2.600	10.7	35.2	112	.474	. 149	160	COHD80		
2.000	19.0	41.5	130	.477	. 152	187			
3.000	23.1	48 4	150	-		190	BONG78		
3.000		40.4	150	.4//	. 154	216	COHD80		
3.000	29.4	44.9	150	.54	196	225	JITW82		
3:500	40.0	54	189	.74	.212	283	FINAOZ		
4.000	52	66	227	.78	.226	345			
4.000	-	-	-	-	-	260	PONM79		
4.500	-	-	-	.86	.286	-	JITW82		
5.000	-	-	-	-	-	497	BONG78		
6.700	-	-	-			610	PONM79		
7.000	-	-		1.17	.401		JITW82		
8.000	-	-				700	BONG78		
9.000	-	-	-			1050	PONE79		
10.000	-	-	-	1.22	.420		JTTW82		
10.000	-	-	-	-	-	1200	PONM79		
12.000	-	-	-	-	-	1274	BONG78		
14 000	-	-	-	-	-	1420	PONM79		
16.000	-	-		-	-	1650			
18.000	-				-	1920			
20.000	_				-	1960			
22.000	-	-	-			2140			

Z=79 GOLD(AU) CONTINUED

TABLE BII		EXPERIME	NTAL IONIZA	TION CROSS	SECTIONS	CONTINUED	
THICK T	RGET						
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
1.00 1.20 1.40 1.60 1.80 2.00 2.20 2.40 2.60 2.80 2.80	2.03 3.15 4.68 6.6 9.0 11.9 15.2 18.9 23.1 27.6	3.20 5.1 7.5 10.5 14.1 18.3 23.3 29.3 36.1 43.9	14.3 21.8 30.8 41.3 53 67 83 100 119 140 162	.63 .62 .63 .64 .65 .65 .65 .65 .65 .64	.142 .144 .152 .161 .169 .177 .184 .189 .194 .197 .201	18.9 29.2 41.7 57 74 95 118 144 174 206 242	COHD80

#### Z=81 THALLIUM(TL)

TABLE BI

EXPERIMENTAL DETAILS

REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL mm	EXP ERROR	THEORIES	COMMENTS
LEIC77	0.5-3.0	50	30-200E-9	-	L1 8-11 L2 8-18 L3 8 LT 7-9 R1 8-11 R2 11	SCA1 PWBA5	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.

TABLE BII		EXPERIME	NTAL IONIZA	TION CROSS	SECTIONS		
THIN TA	RGET						
ENERGY	L1	L2	L3	L1/L2	L1/L3	TOTAL	REF.
MeV		BARNS				BARNS	
.50 1.00 1.50 2.00 2.50 3.00	.470 1.37 2.08 6.3 13.4 23.6	.170 2.32 8.8 15.9 26.7 32.7	1.06 11.2 37.6 62 100 120	2.82 .59 .240 .400 .50 .72	.440 .123 .055 .101 .134 .196	1.69 14.9 48.4 85 140 176	LEIC77

Z=82 LEAD(PB)

TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

TABLE	TABLE BI		EXPERIMENTAL DETAILS					
REF	ENERGY Range Mev	AREAL DENSITY E-6G/CMSC	BEAM CURRENT	BEAM COLL	EX ERR	IP IOR	THEORIES	COMMENTS
LEIC77	0.5-3.5	50	30-200E-9		L1 L2 L3 LT R1 R2	8-11 7-15 7-9 7 11 12	SCA1 PWBA5	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMYAR BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.
BONG78	3.0	THIN	•	-	LT	7	BEA(G3)	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING.
COHD80	1-3	6.7+1 THICK	15E-9	-	L1 L2 L3 LT	23 20 11 11	PWBA4 PWBAR CPSSR	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON CARBON BACKING.

INDLE D.		EAFERIME	ATAL TUNICA	1104 CR055	SECTIONS		
THIN TAN	RGET				. *		
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.50 1.00 1.00 1.20	.370 1.33 1.07 1.79	.130 1.98 1.94 3.53	.64 8.8 8.0 15.0	2.79 .67 .56 .51	.57 .151 .135 .119	1.14 11.9 11.0 19.8 29.6	LEIC77 COHD80 LEIC77 COHD80
1.50	2.49 3.30 4.45	7.2 8.0 10.8	25.1 30.9 40.3	.350 .414 .412	.099 .107 .110	34.9 41.1 54	LEIC77 COHD80
2.00 2.20 2.40	4.80	15.6 17.8 21.8	49.4 62 74	.310 .435 .456	.097	70 86 104	LEIC77 COHD80
2.50 2.60 2.80	12.2 12.6 15.6	26.1 26.4 32.5 36.5	77 87 101	.470 .477 .480	. 158 . 145 . 154	116 124 145 168	LEIC77 COHD80
3.00 3.00 3.50	19.0 20.8	36.5	111 147	.52	. 170	126 167 214	BONG78 LEIC77
THICK T.	ARGET						
ENERGY	LI	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
1.00 1.20 1.40 1.60 1.80 2.00	1.03 1.59 2.41 3.51 4.80 6.3	2.06 3.41 5.1 7.1 9.6 12.6	9.3 14.9 21.6 29.4 38.6 49.0	.50 .466 .473 .492 .499 .50	.110 .107 .112 .119 .124 .129	12.1 19.4 28.3 39.0 52 66	COHD80

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R. S. SOKHI and D. CRUMPTON L-Shell Cross Sections for Protons

TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

### Z=82 LEAD(PB) CONTINUED

TABLE B	II	EXPERIMENTAL	IONIZATION	CROSS	SECTIONS	CONTINUED	
THICK T	ARGET						
ENERGY	<u>L1</u>	L2	L3	L1/L2	L1/L3	TOTAL	REF
HeV		BARNS				BARNS	
2.20 2.40 2.60 2.80 3.00	8.1 10.0 12.0 14.0 16.2	16.1 20.4 25.2 30.8 37.3	61 74 89 105 123	.50 .488 .476 .455 .434	.133 .134 .135 .133 .133	83 102 123 147 173	COHD80

### Z=83 BISMUTH(BI)

TABLE BI

REF	ENERGY RANGE MeV	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS
.EIC77	0.5-3.0	50	30-200E-9	•	L1 8-12 L2 7-13 L3 7-10 LT 7-10 R1 10 R2 11	SCA1 PWBA5	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON FORMVAR BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.

EXPERIMENTAL DETAILS

TABLE BII		EXPERIMENTAL IONIZATION CROSS SECTIONS							
THIN TAP	GET								
ENERGY	L1	L2	L3	L1/L2	L1/L3	TOTAL	REF		
MeV		BARNS				BARNS			
.50 1.00 1.50 2.00 2.50 3.00	.340 1.29 2.00 4.60 9.6 17.2	.075 1.27 5.8 12.3 18.7 26.8	.480 8.4 23.8 41.7 67 91	4.53 1.00 .340 .380 .51 .64	.71 .153 .084 .111 .143 .190	.89 10.9 31.6 59 96 135	LEIC77		

#### Z=90 THORIUM(TH)

TABLE BI

REF	ENERGY RANGE Mev	AREAL DENSITY E-6G/CMSQ	BEAM CURRENT A	BEAM COLL	EXP ERROR	THEORIES	COMMENTS	
LEIC77	0.5-3.0	50	30-200E-9		L1 7-17 L2 8-11 L3 10-1 LT 9 R1 12 R2 8-12	SCA1 PWBA5 3	RBS EMPLOYED. EFFICIENCY MEASURED. METAL TARGET ON A1 BACKING. RADIATIVE DECAY BRANCHING RATIOS MEASURED.	

EXPERIMENTAL DETAILS

R. S. SOKHI and D. CRUMPTON L-Shell Cross Sections for Protons

# TABLE B. Experimental L-Shell Ionization Cross Sections for Proton Impact

Z=90 T	HORIUM(TH)	CONTINUED					
TABLE I	BII	EXPERIMEN	TAL IONIZAT	ION CROSS	SECTIONS		
THIN T	RGET						
ENERGY	<u>L1</u>	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.50 1.00 1.50 2.00 2.50 3.00	.120 .54 .83 1.59 2.44 5.9	.036 .70 2.85 7.1 12.0 17.6	.160 2.67 10.1 21.7 34.6 48.2	3.30 .77 .290 .220 .200 .330	.75 .200 .082 .073 .070 .120	.320 3.91 13.8 30.4 49.2 72	LEIC77
<u>Z=92 UI</u>	RANIUM(U)						
TABLE I	BI	E)	PERIMENTAL	DETAILS			
REF	ENERGY RANGE Mev	AREAL E DENSITY CU E-6G/CMSQ	BEAM BEA JRRENT COL A mm	M EXP L ERROR	THEORIES	COMMEN	TS
EIC77.	0.5-3.5	50 30-	-200E-9 -	L1 8-13 L2 8-12 L3 11 LT 10 R1 11-13 R2 10-12	BEA(M) SCA1 PWBA5 PWBABTR	RBS EMPL EFFICIEN MEASURED METAL TA A1 BACKI RADIATIV BRANCHIN MEASURED	CY RGET ON NG. E DECAY G RATIOS
30NG78	3.0	THIN		LT 9	BEA(G3)	RBS EMPLO EFFICIEN Measured Metal tai Carbon B	RGET ON ACKING.
TABLE I	BII	EXPERIMEN	TAL IONIZAT	ION CROSS S	SECTIONS		
THIN T	RGET						
ENERGY	<u>L1</u>	L2	L3	L1/L2	L1/L3	TOTAL	REF
MeV		BARNS				BARNS	
.50 1.00 1.50 2.00 2.50	.068 .320 .63 .87 1.65	.025 .410 1.86 4.40 7.4	.100 1.68 6.6 14.2 23.6	2.70 .79 .340 .200 .220	.66 .190 .096 .061 .070	.200 2.42 9.1 19.4 33.0	LEIC77
3.00	4.50	13.0 24.3	35.0	.350	.129	42.7 53 80	LEIC77

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