

1 **Attributing the *Bixby Letter* using n-gram tracing**

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15 **Abstract**

16 There is a long-standing debate around the authorship of the *Bixby Letter*, one of the most
17 famous pieces of correspondence in American history. Despite being signed by President
18 Abraham Lincoln, some historians have claimed that its true author was John Hay, Lincoln's
19 personal secretary. Analyses of the letter have been inconclusive in part because the text
20 totals only 139 words and is thus far too short to be attributed using standard methods. To
21 test whether Lincoln or Hay wrote this letter, we therefore introduce and apply a new
22 technique for attributing short texts called *n-gram tracing*. After demonstrating that our
23 method can distinguish between the known writings of Lincoln and Hay with a very high
24 degree of accuracy, we use it to attribute the *Bixby Letter*, concluding that the text was
25 authored by John Hay – rewriting this one episode in the history of the United States and
26 offering a solution to one of the most persistent problems in authorship attribution.

27

28 **Keywords:** American History, Authorship Attribution, Computational Social Science, Corpus
29 Linguistics, Forensic Linguistics, John Hay, Abraham Lincoln, Stylistics, Stylometry

30

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35 **Attributing the Bixby Letter using n-gram tracing**

36

37 **1. Introduction**

38 On the 21st of November 1864, only five months before he was assassinated, Abraham
 39 Lincoln, the 16th President of the United States, sent a short letter of condolence to Lydia
 40 Bixby of Boston, a widow whose five sons were believed to have died in the Civil War. The
 41 original letter was lost, but the Adjutant General of Massachusetts, who had requested the
 42 letter from the Department of War on the widow's behalf, also sent a copy to the *Boston*
 43 *Evening Transcript*, who published the letter on the 24th of November (see Table 1). The
 44 *Bixby Letter* would go on to become one of America's most famous pieces of
 45 correspondence, praised for its sentiment and style and counted among Lincoln's greatest
 46 texts along with the *Gettysburg Address*, the *Second Inaugural Address*, and the
 47 *Emancipation Proclamation*. The authorship of the letter, however, has long been the subject
 48 of debate, with some historians arguing that its true author was John Hay – Lincoln's young
 49 assistant and the future Secretary of State under William McKinley and Theodore Roosevelt.

50 **Table 1 The *Bixby Letter* (*Boston Evening Transcript*, 25 November 1864)**

*EXECUTIVE MANSION,
 WASHINGTON, NOV. 21, 1864.
 Dear Madam,—*

I have been shown in the files of the War Department a statement of the Adjutant General of Massachusetts, that you are the mother of five sons who have died gloriously on the field of battle.

I feel how weak and fruitless must be any words of mine which should attempt to beguile you from the grief of a loss so overwhelming. But I cannot refrain from tendering to you the consolation that may be found in the thanks of the Republic they died to save.

I pray that our Heavenly Father may assuage the anguish of your bereavement, and leave you only the cherished memory of the loved and lost, and the solemn pride that must be yours, to have laid so costly a sacrifice upon the altar of Freedom.

Yours, very sincerely and respectfully,

MRS. BIXBY.

A. LINCOLN.

51

52 A wide range of external evidence has been presented in favour of both Lincoln (e.g.
53 Barton, 1926; Basler, 1953; Randall & Current, 1955; Bullard, 1946, 1951; Emerson, 2006,
54 2008) and Hay (e.g. Butler, 1940; Wakefield, 1948; Burlingame, 1995, 1999). Hay is
55 generally acknowledged to have written much of Lincoln's correspondence, as this was the
56 task for which he was hired by John George Nicolay, Lincoln's other personal secretary,
57 after Lincoln had secured the Republican presidential nomination in May 1860 (Kushner,
58 1974). Furthermore, several reliable sources – including Nicholas Murray Butler, the
59 president of Columbia University, and Spencer Eddy, Hay's personal secretary later in life –
60 claimed that Hay had confided in them that he had written the letter. In addition, Hay kept
61 scrapbooks containing extensive records of his achievements, which included the *Bixby*
62 *Letter*, as well as references to many texts he had certainly written, including his 1883 novel
63 *The Bread Winners* and a series of letters sent to newspapers across the country in support
64 of Lincoln, both of which were initially published anonymously (Kushner & Hummel, 1977).
65 Alternatively, aside from the fact that the letter bears his name, perhaps the most convincing
66 evidence that Lincoln wrote the *Bixby Letter* is that Hay never publicly took credit for its
67 authorship, although he did take credit for other letters sent by the President. Hay and
68 Nicolay even attributed the letter to Lincoln in their biography of the President (1890) and
69 Hay's children said that their father never claimed authorship in private. Furthermore,
70 although Hay authored much of Lincoln's correspondence at that time, Lincoln did write
71 some letters, including letters of condolence, and he might have been especially likely to
72 have written this letter, as he had lost three sons himself. His one surviving son, Robert
73 Todd Lincoln, who was Hay's close friend, also asserted that his father had written the *Bixby*
74 *Letter* and that Hay had confirmed as much to him personally.

75 In addition to external evidence, internal evidence related to the style of the *Bixby*
76 *Letter* has been presented in support of both Lincoln and Hay. In 1943, Basler remarked on
77 the quality of the letter and its similarity to Lincoln's style (Burlingame, 1995); ten years later,
78 he included the letter in his *Collected Works of Abraham Lincoln*. Similarly, Bullard (1946)
79 argued that the letter was generally a better match for Lincoln's style than Hay's. A more

80 thorough analysis was presented by Nickell (1989), who identified several distinctive words,
81 phrases, and rhythms in the letter, for which he could only find analogues in Lincoln's
82 writings, including the use of alliteration and the word 'tender'. Nickell also argued that
83 Lincoln wrote in a more traditional and formal style, whereas the younger Hay wrote in a
84 more contemporary and informal style. For example, Nickell claimed that the use of the word
85 'beguile' in the letter is used with its traditional sense of 'diverting', as opposed to the more
86 modern sense of 'enticing', which is how Hay used the word in a letter Nickell quotes.
87 Burlingame (1999), however, who has been one of the strongest proponents of Hay's
88 authorship, found that Hay used 'beguile' at least 30 times in his writings, including in a
89 collection of unpublished letters, while he could find no record of Lincoln ever having used
90 the word. Burlingame (1995) also argued that various other words were indicative of Hay,
91 including 'gloriously', 'cherish', 'republic', and 'Heavenly Father'.

92 The stylistic evidence is far from definitive. Burlingame and others have claimed that
93 more passages in the *Bixby Letter* resemble Hay's known writings, while Nickell and others
94 have claimed that more resemble Lincoln's. Emerson (2006: 2) dismissed this type of
95 internal evidence outright, stating that 'one can find as many arguments in favour of
96 Lincoln's literary style as one can find for Hay's.' Developing objective methods for
97 attributing authorship, however, is the focus of considerable research in *stylometry* (Koppel
98 et al., 2009; Stamatatos, 2009), where questioned documents are attributed, for example, by
99 comparing the frequencies of common words or common word and character sequences in
100 the text to their frequencies in writing samples from each possible author. The *Bixby Letter*
101 has never been subjected to thorough stylometric analysis, at least in part, because it only
102 contains 139 words; short texts are difficult to attribute using stylometric techniques because
103 the relative frequencies of linguistic features in a text can only be trusted to approximate
104 their values in an author's writings more generally if that text is long enough to contain
105 numerous tokens of those features. For example, the word 'beguile' occurs once in the *Bixby*
106 *Letter*, but we should not assume its author used this word on average about once every

107 139 words. Similarly, the word 'by' does not occur in the letter, but we should not assume its
108 author never used this word at all.

109 The problem of text length has received considerable attention in stylometry, with
110 Stamatatos (2009: 553) calling it 'the most important' methodological issue in the field. Eder
111 (2015) conducted the most thorough assessment of the effect of questioned document
112 length in authorship attribution and recommended a minimum length of 5,000 words; this is a
113 very conservative limit, at least in part because his tests involved between 6 and 21 possible
114 authors, as opposed to the basic problem of 2 authors, which requires less data.
115 Alternatively, many studies have been able to successfully attribute texts of around 1,000
116 (e.g. Stamatatos et al., 2001; Burrows, 2002; Juola, 2006; Stamatatos, 2009) or 500 words
117 (e.g. Gamon, 2004; Grieve, 2007; Koppel, Schler & Argamon, 2011). Few studies have
118 attributed shorter texts, although some promising results have been achieved in the 200- to
119 500-word range (e.g. Forsyth & Holmes, 1996; Koppel et al., 2011), especially based on the
120 frequencies of relatively common parts-of-speech (e.g. Chaski, 2005; Hirst & Feiguina,
121 2007). The attribution of texts shorter than 200 words has received very little attention,
122 limited mostly to a small number of recent studies of Twitter data. Most notably, Layton et al.
123 (2010) were able to attribute posts based primarily on references to usernames, while
124 Schwartz et al. (2013) were able to attribute posts based on character and word sequences
125 that are used by only one author in their corpus. Although both methods worked well for
126 classifying posts that contained these features, a substantial proportion of posts resisted
127 attribution. Better results were achieved by Brocardo et al. (2013), who proposed a method
128 for short-text *authorship verification* – which involves testing whether an author wrote a text,
129 as opposed to *authorship attribution*, which involves selecting the most likely author from a
130 set of candidates, as in the case of the *Bixby Letter*. Their method is based on the number of
131 character sequences in the questioned document that also occur in the known writings of an
132 author. Crucially, all three of these studies measured the presence and absence of linguistic
133 features as opposed to their relative frequencies, whose value is limited in short texts.

134 Totalling only 139 words, the *Bixby Letter* is far too short to be attributed using
135 standard stylometric techniques. Short documents, however, are common in a forensic
136 context (Coulthard, 2004; Coulthard et al., 2017). For example, the mean length of texts
137 received by the German Federal Criminal Police Office between 2002 and 2005 was 248
138 words, with two thirds of incriminating texts containing fewer than 200 words (Ehrhardt,
139 2007). A common method for attributing texts of any length in forensic stylistics is to
140 manually identify features of interest in the questioned document and to then search for
141 those features in the possible author writing samples to see if they are used predominantly
142 by one suspect (e.g. McMenamin, 1993, 2002). This approach is based on the reasonable
143 assumption that the repetition of features across texts is evidence of shared authorship (see
144 Coulthard, 2004). Still feature selection is usually left to the judgment of the forensic linguist,
145 limiting the reliability of this approach in practice, although forensic linguists have recently
146 begun to apply more objective selection criteria (e.g. Wright 2017). Most notably, in terms of
147 short texts, Grant (2013) attributed a series of text messages in a murder investigation
148 through a systematic analysis of the occurrence of creative spellings (see also MacLeod &
149 Grant, 2012; Silva et al. 2011). Similarly, Nini (2018) measured the similarity of short letters
150 connected to the Jack the Ripper case based on shared word sequences. Once again, like
151 the stylometric research on short texts reviewed above, these studies focus on the
152 occurrence of features as opposed to their relative frequencies.

153 Because no generally applicable method for attributing short texts exists in
154 stylometry or forensic stylistics, in this paper, we attribute the *Bixby Letter* by applying a new
155 quantitative approach to short-text authorship attribution that we call *n-gram tracing*, which
156 builds on recent research in both fields. Our method involves first extracting all sequences of
157 linguistic forms (i.e. characters and words) that occur in the questioned document and then
158 finding the possible author who uses the highest percentage of these forms. In the
159 remainder of this paper, we describe our process of data collection, introduce and exemplify
160 *n-gram tracing* through the analysis of the *Gettysburg Address*, test the method on the
161 known writings of Abraham Lincoln and John Hay, and use the method to attribute the *Bixby*

162 *Letter*, showing that the text is far more likely to have been written by Hay. Finally, we
 163 conclude this paper by considering the historical, methodological, and theoretical
 164 significance of our study.

165

166 **2. Data**

167 For years, historians believed the original *Bixby Letter* was held in the collection of
 168 Brasenose College in Oxford, but in 1925 an investigation by the *New York Times* revealed
 169 that the College had no record of ever possessing the document (Emerson, 2006). A futile
 170 search for the letter ensued, but eventually it was accepted that the original must have been
 171 lost. Some historians even speculated that the letter had been destroyed by the Widow
 172 Bixby – a woman of purportedly dubious character, who had in fact lost two as opposed to
 173 five sons in the Civil War, and who was rumoured to have been a brothel owner and a
 174 Confederate sympathiser (Burlingame, 1999). Because there is no original, different
 175 versions of the letter are in circulation today. Variation between these versions is minimal –
 176 often relating to punctuation and spacing, especially in the salutation and valediction as
 177 opposed to the body of the letter – but there are some disagreements in the main text, most
 178 notably involving ‘any word of mine’ vs. ‘any words of mine’ and ‘tendering you’ vs.
 179 ‘tendering to you’. Given these inconsistencies, it is necessary to select a specific version of
 180 the *Bixby Letter* to attribute. We chose to analyse the version printed in *Boston Evening*
 181 *Transcript*, because it is the first known copy of the letter and because the original is
 182 accessible online¹ (see Table 1). In our analysis, we focused on the main body of the letter,
 183 which contains 3 paragraphs, 4 sentences, and 139 words.

184 To compile a corpus of Lincoln’s writings, we downloaded a digitised version of
 185 Balser’s 1953 *The Collected Works of Abraham Lincoln*, which is provided online by The
 186 Abraham Lincoln Association through the University of Michigan Library². The collection
 187 contains over 6,500 texts, including letters, bills, notes, notices, petitions, speeches,

¹ <http://news.google.com/newspapers?nid=sArNgO4T4MoC&dat=18641125>

² <http://quod.lib.umich.edu/l/lincoln/>

188 receipts, and resolutions, dated between the 26th of May 1830 and the 14th of April 1865.
189 The collection is divided into 8 volumes and organised chronologically, aside from Volume 1,
190 which contains some of Lincoln's most important writings. After downloading the documents
191 individually, we inspected each by hand, as they often contain information in addition to the
192 main text, including dates, place names, notes, and annotations by the editors. Close
193 reading of these annotations also revealed that a number of texts were only co-authored or
194 signed by Lincoln. Any document for which we had any doubt that Lincoln was the primary
195 author was therefore removed from the corpus, including the *Bixby Letter*, leaving 5,601
196 documents totalling approximately 650,000 words. These documents were then semi-
197 automatically cleaned to remove text that was not part of the main body, including
198 salutations and valedictions from letters. In addition, because Hay became Lincoln's
199 personal secretary following his presidential nomination by the Republican Party on the 18th
200 of May 1860, we removed all texts from that date onward as they were potentially written by
201 Hay. The final Lincoln corpus used to attribute the *Bixby Letter* therefore only contains texts
202 written by Lincoln up to this date, totalling 1,085 texts and 400,747 words, with texts ranging
203 in length from 5 to 17,003 words and with a median length of 125 words. Notably, average
204 text length rises from around 100 words in Lincoln's complete corpus to 350 words in
205 Lincoln's early corpus because the complete corpus includes a large number of telegraphs
206 and short letters from his time in office.

207 To compile a corpus of Hay's writings, we downloaded a digitized version of Volume
208 I³ and II⁴ of *The Life and Letters of John Hay*, edited by William Roscoe Thayer, which was
209 originally published in 1915. The collection is organised chronologically, and includes letters,
210 prose, poems, and diary entries spanning Hay's entire life. The collection does not contain a
211 copy of the *Bixby Letter*. As opposed to the Lincoln collection, where each text could be
212 downloaded individually, the Hay texts were grouped into chapters, interspersed with
213 extensive commentary from the editor, as well as extracts from texts written by other

³ http://archive.org/stream/lifeandlettersof007751mbp/lifeandlettersof007751mbp_djvu.txt

⁴ http://archive.org/stream/lifelettersofjoh02inthay/lifelettersofjoh02inthay_djvu.txt

214 authors. After downloading the chapters, we therefore carefully inspected each file by hand
215 and manually divided the text into individual documents. Documents of unclear provenance
216 or that were co-authored by others were excluded from the corpus. In addition, we obtained
217 other texts written by Hay from Project Gutenberg, including short stories⁵, poems⁶, a 1901
218 novel (*The Bread Winners*)⁷, and a 1903 collection of essays (*Castilian Days*)⁸. We divided
219 the two book-length texts into chapters. In total, the Hay corpus contains 577 texts totalling
220 261,126 words, with texts ranging in length from 9 to 8,954 words and a median of 159
221 words per text.

222

223 3. N-gram Tracing

224 In forensic linguistics, short texts are often attributed by manually selecting linguistic features
225 from the questioned document that appear to be relatively distinctive or rare and by then
226 searching for these forms in the writing samples of each possible author. Although this
227 method is logical and is regularly applied in casework, there are at least three potential
228 issues with its application. First, it is unclear how to select an exhaustive or at least an
229 unbiased feature set, as the debate around the style of the *Bixby Letter* illustrates: different
230 analysts can identify different sets of seemingly distinctive features and consequently come
231 to different attributions of the same questioned document. Second, it is unclear how to
232 control for variation in the amount of material in the possible author writing samples, which
233 often varies tremendously, as is the case here: if more text is available for one of the
234 possible authors, then the forms extracted from the questioned document have an increased
235 chance of being found in that author's sample regardless of authorship. Third, it is unclear
236 how to judge whether differences in the use of forms in the possible author writing samples
237 are sufficient in the aggregate to attribute the questioned document: because this approach

⁵ <http://www.gutenberg.org/cache/epub/11392/pg11392.txt>

⁶ <http://www.gutenberg.org/cache/epub/6062/pg6062.txt>

⁷ <http://www.gutenberg.org/cache/epub/16321/pg16321.txt>

⁸ <http://www.gutenberg.org/cache/epub/7470/pg7470.txt>

238 relies on the judgment of the analyst and therefore cannot be consistently or mechanically
239 applied, it is difficult to systematically evaluate the reliability of such methods.

240 Based on this general approach to forensic authorship analysis, but keeping these
241 three limitations in mind, we have developed a new method for attributing short texts in a
242 replicable manner that we refer to as *n-gram tracing*. The method takes the n-gram as its
243 unit of analysis, where an n-gram is defined a sequence of one or more linguistic forms (e.g.
244 1-grams, 2-grams) at any level of linguistic analysis (e.g. words, characters). For example,
245 n-grams of various types extracted from the first line of the *Bixby Letter* are presented in
246 Table 2. The basic idea behind n-gram tracing is to calculate the percentage of n-grams that
247 occur in a questioned document that also occur at least once in a possible author writing
248 sample. This process is repeated for each possible author and the text is then attributed to
249 the possible author whose writing sample contains the highest percentage of the n-grams
250 from the questioned document.

251

252

253

254 **Table 2** N-gram examples from the first sentence of the *Bixby Letter*

Level	Length	Example
Word	1	<i>i, have, been, shown, in, the, files, of, war, ..., field, battle</i>
	2	<i>I have, have been, been shown, shown in, ..., of battle</i>
	3	<i>I have been, have been shown, ..., field of battle</i>
Character	1	<i>i, _, h, a, v, e, b, n, s, o, w, t, ..., c, y</i>
	2	<i>i_, _h, ha, av, ve, e_, _b, be, ..., ba, tl</i>
	3	<i>i_h, _ha, hav, ave, _be, bee, ..., ttl, tle</i>

255

256 Our method is grounded in two key insights. The first is that we extract the complete
 257 set of n-grams that occur in the questioned document, so as to obtain a broad and unbiased
 258 feature set. The second is that we only consider the presence or absence of these n-grams
 259 in the questioned document and the possible author writing samples, as opposed to their
 260 relative frequencies, so as to avoid examining relative frequencies in a very short text.

261 Instead, we measure the percentage of the n-gram types found in the questioned document
 262 that also occur at least once in equal-sized samples of texts drawn from each possible
 263 author writing sample. Specifically, for each possible author, a random sample of texts is
 264 analysed that is roughly equal in length to the total number of words in the possible author
 265 writing sample with the fewest words. The author who uses a higher percentage of the n-
 266 grams in these comparable samples – or equivalently the author that uses a larger number
 267 of unique n-grams – is then selected as the most likely author of the questioned document.

268 To summarise, our algorithm for conducting a basic n-gram tracing analysis for
 269 authorship attribution involves the following four steps:

- 270 1. Extract all n-grams of a particular length and level from the questioned document.
- 271 2. Take a random sample of texts of equal size from each possible author writing
 272 sample.
- 273 3. Measure the percentage of n-gram types found in the questioned document that
 274 also occur at least once in each possible author writing sample.

275 4. Attribute the questioned document to the possible author who uses the highest
276 percentage of these n-grams.

277 In general, n-gram tracing should be run across as many different types of n-grams as
278 possible, including both word and character-level n-grams up to a length where only a small
279 number of n-grams are occurring in the possible author writing samples. In addition, the
280 analysis can be repeated for different random samples of texts, allowing for the average
281 percentages of n-grams seen to be calculated and compared.

282 More formally, n-gram tracing involves measuring and comparing the similarity
283 between the set of n-grams occurring in a questioned document and the set of n-grams
284 occurring in each possible author writing sample. Specifically, we use the *Overlap*
285 *Coefficient* (Vijaymeena & Kavitha, 2016; Oakes, 2014), which measures the similarity
286 between two sets (X, Y) by dividing size of the intersection of those two sets (i.e. the number
287 of shared elements) by the size of the smaller set (i.e. the total number of elements):

$$288 \frac{|X \cap Y|}{\min(|X|, |Y|)}$$

289 In the context of n-gram tracing, this amounts to dividing the number of linguistic features, in
290 our case n-grams, shared by the questioned document (Q) and a possible author writing
291 sample (A) by the number of features in the questioned document, which should always be
292 considerably smaller than in the number of features in the possible author writing sample.

$$293 \frac{|Q \cap A|}{|Q|}$$

294 This process is then repeated for all possible authors, using comparable writing samples,
295 and the questioned document is then attributed to the possible author with the highest
296 *Overlap Coefficient*.

297 Although the *Overlap Coefficient* is rarely used in stylometry (although see Brocardo
298 et al., 2013), the closely related *Jaccard Index*, which uses the size of the union of the two
299 sets as the denominator as opposed to the size of the smaller set, has been applied in
300 numerous recent authorship studies especially by forensic linguists (e.g. Grant, 2013;

301 Wright, 2017; Nini, 2018). We prefer the Overlap Coefficient primarily because it provides a
302 more meaningful metric of stylistic difference, directly measuring the percentage of the
303 features in the questioned document that also occur in the possible author writing sample.
304 Alternatively, the Jaccard Index measures the percentage of features shared by the
305 questioned document and the possible author writing sample, which is less interpretable, as
306 writing samples are usually far longer than questioned documents.

307 The results of n-gram tracing can also be visualised by calculating the cumulative
308 percentage of n-grams seen as texts are drawn at random from each possible author's
309 writing sample and by plotting these percentages against the total number of words in these
310 texts. In this way, it is possible to graph how the percentage of n-grams seen increases for
311 each possible author as the amount of data seen increases. To ensure the results are not
312 dependent on the random sampling of texts, this analysis can be repeated several times on
313 many different random sequences of texts and the average cumulative percentages of n-
314 grams seen can then be calculated and plotted at regular intervals of total words seen (e.g.
315 up to 5,000 words, up to 10,000 words, etc.). In general, these traces will rise rapidly at first
316 and often overlap, but as more texts are analysed, the traces will flatten out, as fewer new n-
317 grams will be encountered (see Zipf, 1935), and a clear and consistent distinction between
318 the authors should become apparent. In essence, the basic n-gram tracing algorithm
319 described above involves comparing the traces for each of the possible authors at the point
320 when the curve for the author with the smallest writing sample is exhausted; however,
321 plotting these values across sample sizes provides additional information about the use of
322 the set of n-grams in the possible author corpora. Most important, inspecting these graphs
323 allows for the definitiveness of the attribution to be judged, both by comparing the degree of
324 difference between the possible authors and the consistency of the analysis as more data is
325 analysed.

326 Although n-gram tracing was inspired by the qualitative approach to authorship
327 analysis commonly applied in forensic linguistic casework, it also builds on recent
328 quantitative research in stylometry and forensic linguistics. The multivariate analysis of word

329 and character n-grams, as broadly defined here, is the standard approach in stylometry (e.g.
330 Kešelj et al., 2003; Grieve, 2007; Luyckx & Daelemans, 2008), but the more distinctive
331 aspect of our approach is that we only consider the presence and absence of these features
332 rather than their relative frequencies. A similar approach has been taken in a small number
333 of recent studies (e.g. Brocardo et al., 2013; Grant, 2013; Schwartz et al., 2013; Wright,
334 2017; Nini, 2018). Our method is most similar to the approach for short-text authorship
335 verification proposed in Brocardo et al. (2013), which is based on the analysis of the
336 occurrence of all 3-5 alphabetic character n-grams in the questioned document using the
337 Overlap Coefficient. The main difference between these two techniques are that our method
338 is designed for attribution as opposed to verification and is based on a much larger and
339 more principled feature set, including both word and character-level n-grams. Our method is
340 also similar to the approach for authorship attribution proposed in Wright (2017), where the
341 occurrence of all 2-6 word n-grams in the questioned document and the possible author
342 writing samples are compared using the Jaccard Index (see also Johnson & Wright, 2014).
343 The main differences between these two techniques are that our method is designed
344 especially for short texts, controls for the size of the possible author writing sample, is based
345 on the Overlap Coefficient as opposed to the Jaccard Index, and is based on a much larger
346 feature space. In addition, our approach to visualisation is entirely new.

347

348 **4. Demonstration: *Gettysburg Address***

349 To illustrate how n-gram tracing works, we present an analysis of the *Gettysburg Address*,
350 which was delivered by Abraham Lincoln on the 19th of November 1863 at the site of the
351 bloodiest battle of the Civil War. We selected this text because it is one of Lincoln's most
352 famous texts, drafts prove it was written by Lincoln, and it is a relatively short text (272
353 words) that postdates May 1860, like the *Bixby Letter*. There are five final versions of the
354 *Gettysburg Address* written in Lincoln's hand, which differ slightly from each other. In this
355 case, we chose to analyse the *Bliss Copy*, as it is generally considered the standard – the
356 only version signed and dated by Lincoln and the version etched into the Lincoln Memorial.

357 We then compared the *Gettysburg Address* to the texts in our Hay and Lincoln corpora using
358 a series of n-gram tracing analyses.

359 We began by extracting all 2-word n-grams from the *Gettysburg Address*, of which
360 there are 239 distinct types when we ignore case and punctuation and prohibit n-grams from
361 spanning sentences. For example, the first 2-word n-gram in the *Address* is 'four score',
362 while the last is 'the earth'. We then measured the percentage of these 2-word n-grams in
363 the complete Hay corpus (261,126 total words) and in a random sample of texts drawn from
364 the Lincoln corpus totalling 260,954 words. We found that Hay used 55% of the n-grams,
365 whereas Lincoln used 60% (64% of the n-grams occur in Lincoln's complete 400,747 word
366 corpus). Because the 2-word n-gram overlap with the Lincoln corpus is greater, this analysis
367 correctly attributes the *Gettysburg Address* to Lincoln. We also repeated the 2-word n-gram
368 tracing analysis for Lincoln with 50 different random samples of his texts, which agreed with
369 our first analysis, with a mean percentage of n-grams seen at 260,000 words of 60%.

370 To visualise the 2-word n-gram analysis, we first extracted a random sequence of
371 texts from each possible author corpus and computed the cumulative percentage of the 239
372 2-word n-grams that had been seen as each additional text was added to the analysis. We
373 then plotted these cumulative percentages of n-grams seen against the total number of
374 words seen, as presented in Figure 1. The figure contains two traces: the longer line on top
375 plots the percentage of the 239 n-grams seen for Lincoln, which reaches 64% at 400,000
376 words, while the shorter line below plots the same value for Hay, which reaches 55% at
377 260,000 words. Individual texts are marked with a cross. Notably, both traces are monotonic
378 because adding new texts can only result in new n-grams being seen. Furthermore, both
379 traces show plateaus because at times numerous texts are added to the analyses that do
380 not contain any new n-grams. As the basic analysis found, the trace for Lincoln is higher at
381 the point where Hay's trace ends around 260,000 words, but the visualisation offers further
382 support for this attribution by showing that there is a clear and consistent difference in the
383 percentage of n-grams used by the two authors after approximately 100,000 words from
384 each had been seen.

385 We also extracted 50 random sequences of texts for each author and plotted the
386 cumulative percentage of the 239 2-word n-grams that were seen as each additional text
387 was added to the analysis. All 100 traces are presented together in Figure 2 in the same
388 way as Figure 1, except that marks for individual texts have been omitted for clarity.
389 Although each trace takes a different path, Lincoln always outstrip Hay over time, confirming
390 that the attribution does not depend substantially on the randomisation procedure. In
391 addition to presenting 100 traces on the same graph, we reduced the 50 traces for each
392 author to a single aggregated trace by taking the average cumulative percentage of n-grams
393 seen across all analyses every 5,000 words. The results of this analysis are presented in the
394 second cell of Figure 3, which shows the same overall pattern as Figures 1 and 2, with
395 Lincoln once again clearly using a higher percentage of the 2-word n-grams in the
396 *Gettysburg Address* than Hay.

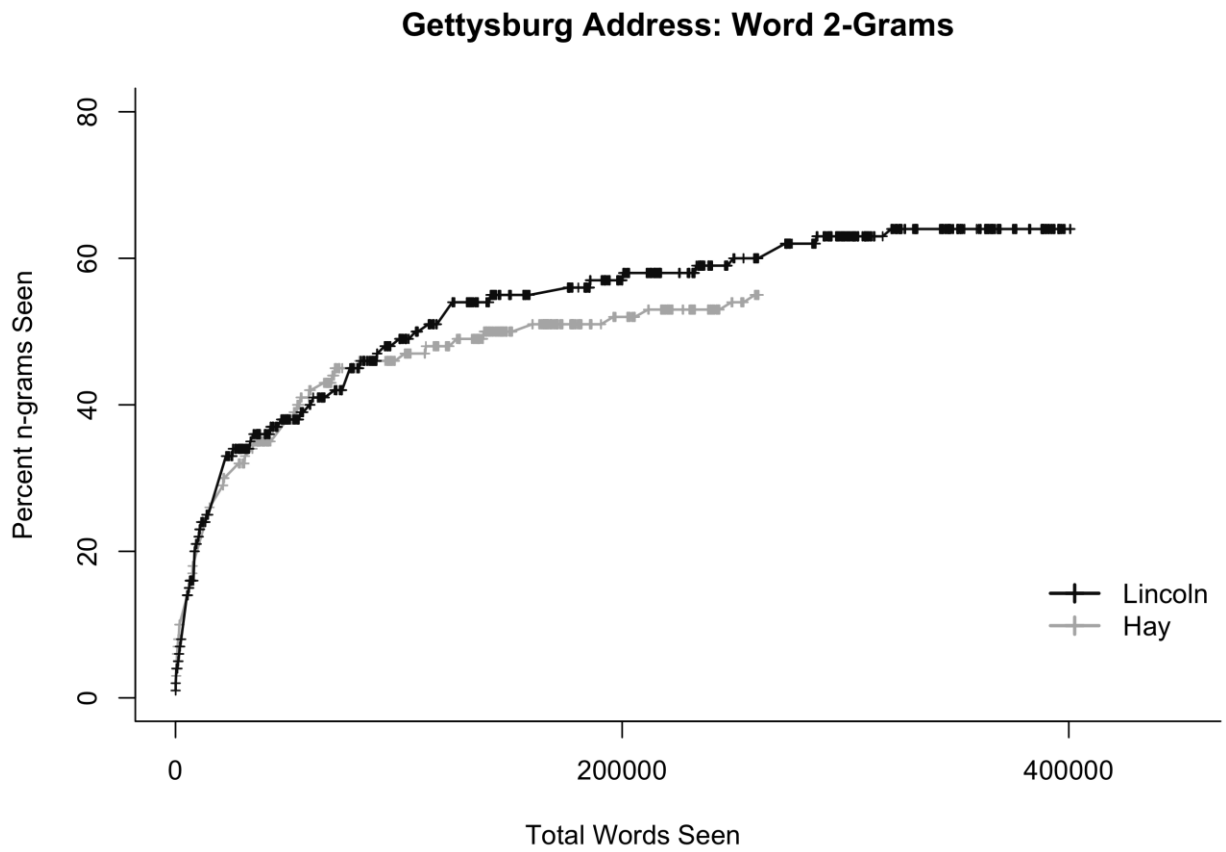
397 In addition to 2-word n-grams, we also analysed 1-, 3- and 4-word n-grams, based
398 on the average percentage of n-grams seen in 50 random 260,000-word samples of texts.
399 The analysis was only run up to 4-word n-grams because from this point onward the Hay
400 corpus contains none of the n-grams found in the *Gettysburg Address*. The 3- and 4-word n-
401 gram analyses also correctly attributed the *Gettysburg Address* to Lincoln: 18% of 3-grams
402 for Lincoln vs. 14% for Hay and 2% of 4-grams for Lincoln vs. 0% for Hay. The 1-word n-
403 gram analysis, however, incorrectly attributed the *Gettysburg Address* to Hay. Figure 3
404 presents the aggregated n-gram traces for all analyses. Notably, the 2-, 3- and 4-word n-
405 gram analyses, which correctly attributed the document to Lincoln, appear to be far more
406 definitive than the incorrect 1-word n-gram analysis.

407 Finally, we analysed 1- to 20-character n-grams, where an n-gram could be
408 composed of any case-insensitive sequence of characters, including not only letters and
409 numbers, but punctuation marks and spaces, allowing word boundaries to be preserved,
410 although once again we did not allow n-grams to span sentences. This analysis was run for
411 n-grams of up to 20 characters in length because after this point the Hay corpus contains
412 none of the n-grams found in the *Gettysburg Address*. From 3-character n-grams onward the

413 analysis correctly attributes the document to Lincoln; the 1- and 2-character n-gram
414 analyses were inconclusive as both authors use 100% of these n-grams by 260,000 words.
415 The first 15 analyses are visualised in Figure 4, showing that the attribution becomes
416 especially clear from 7-characters onward and that the 1- and 2-character analyses both
417 reach 100% of n-grams seen almost immediately.

418 N-gram tracing therefore correctly identifies Lincoln as the author of the *Gettysburg*
419 *Address*. Overall, 21 of the 24 analyses we ran attributed the document to Lincoln, while in 2
420 of the remaining 3 cases, the analysis is inconclusive. The only analysis that incorrectly
421 attributes the *Address* to Hay is based on 1-word n-grams. To assess the degree to which
422 such misattributions affect the ability of n-gram tracing to distinguish between Lincoln and
423 Hay, we conducted a systematic evaluation of the method on the known writings of these
424 two authors.

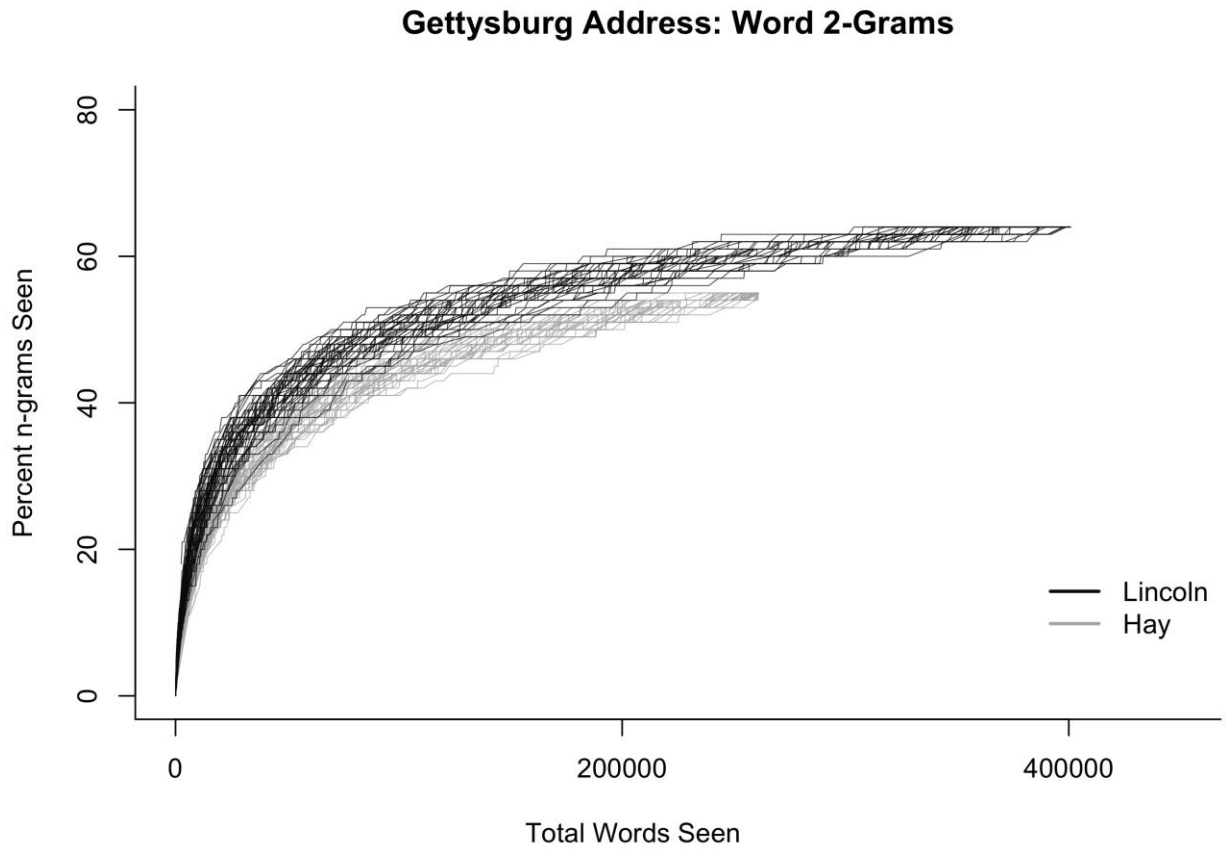
425 **Figure 1** One *Gettysburg Address* 2-word n-gram traces



426

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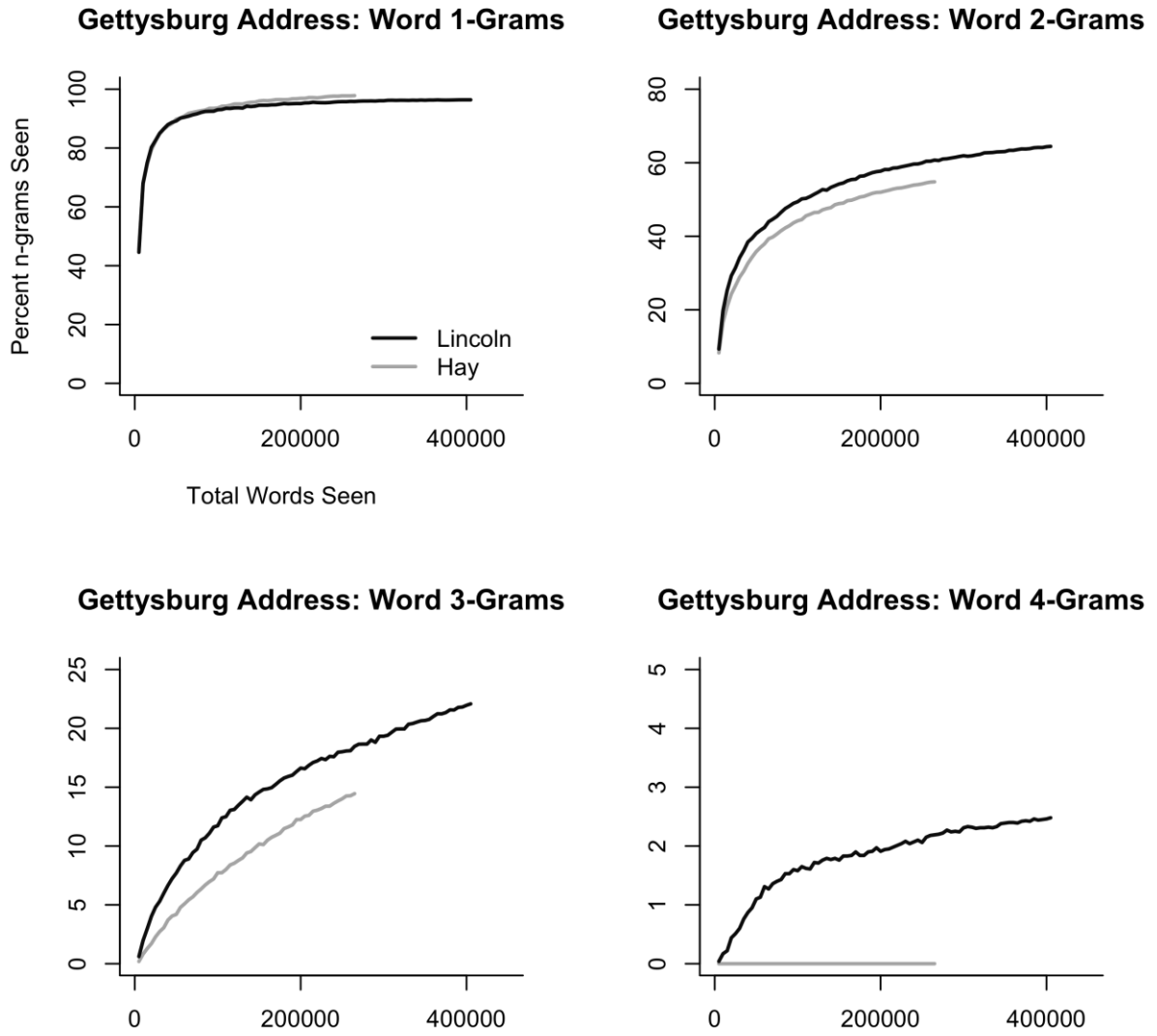
428 **Figure 2** Fifty *Gettysburg Address* 2-word n-gram traces



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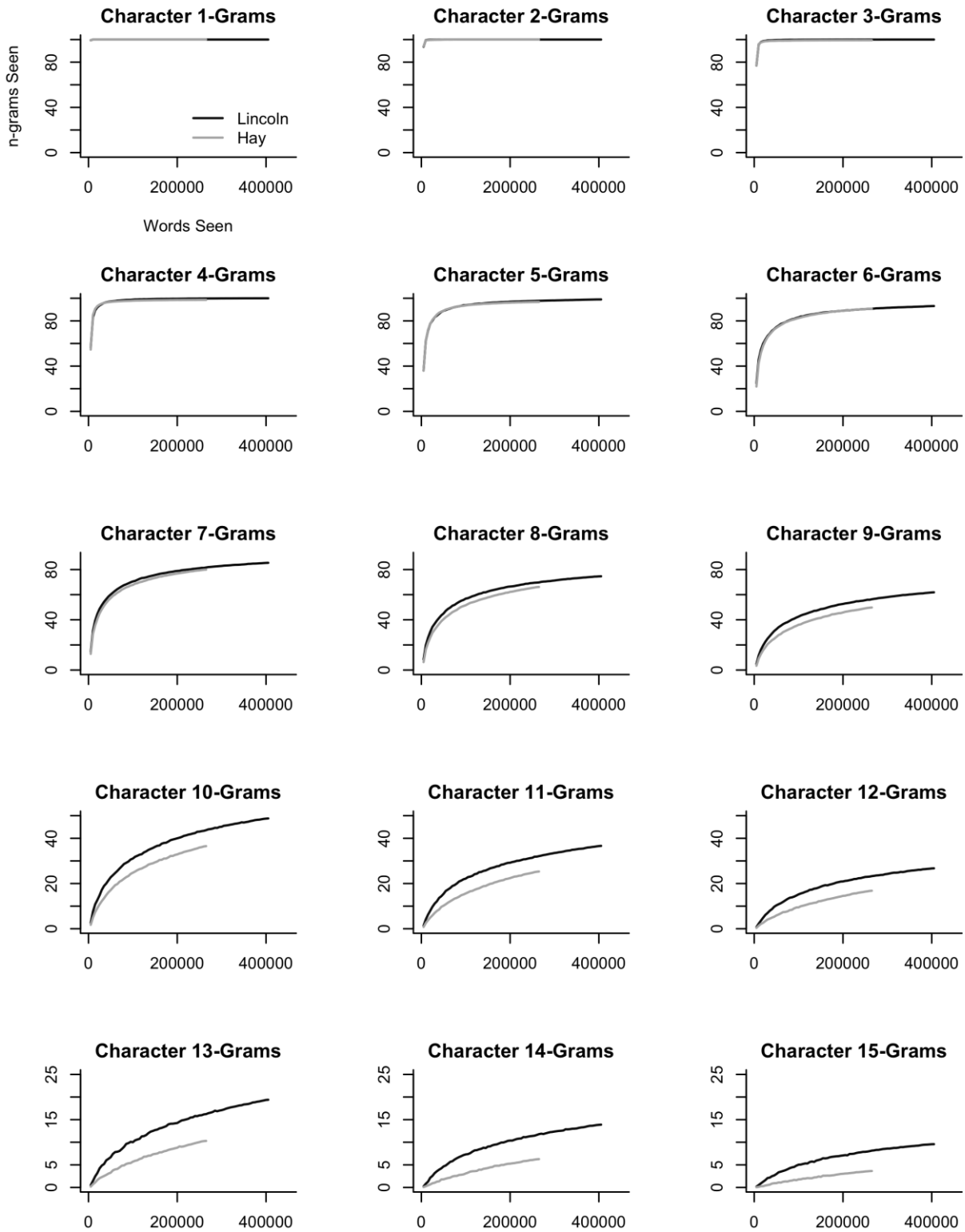
431 **Figure 3** *Gettysburg Address* word-level aggregated n-gram traces



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433

434 **Figure 4** *Gettysburg Address* character-level aggregated n-gram traces



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438 5. Evaluation

439 Before any method for authorship attribution can be used to resolve a case of disputed
440 authorship, it must be shown that the method can distinguish between the writings of the
441 possible authors under consideration with a reasonable degree of accuracy. If the method
442 can correctly classify the known writings of those authors, then it can be used to attribute the
443 questioned document, assuming its true author is one of the authors under consideration.
444 This is the approach taken here: in this section, we show that n-gram tracing is capable of
445 distinguishing between the writings of Lincoln and Hay with a very high degree of accuracy;
446 in the next section, we use n-gram tracing to attribute the *Bixby Letter*. We do not assess or
447 assume the general applicability of n-gram tracing. This is the subject of future research, but
448 it is not a prerequisite for the application of a method to a specific case of disputed
449 authorship (see Grant 2013).

450 To evaluate the suitability of n-gram tracing for attributing the *Bixby Letter*, we used
451 our method to attribute each text in our corpus of possible authors following a leave-one-out
452 approach to cross-validation (Zhang & Yang, 2015). In other words, we removed each of the
453 1,662 texts from our corpus one at a time (1,085 for Lincoln, 577 for Hay), and then
454 attributed that text by comparing it to the remaining texts in the corpus using n-gram tracing.
455 For each text, we compared 25 different n-gram types, including 1- to 5-word and 1- to 20-
456 character n-grams, aggregating each analysis over 10 randomised sequences of texts per
457 author, selecting the author who used the higher percentage of n-grams at 260,000 words.

458 We measured the accuracy of our attributions in various ways. For each n-gram type
459 and for each author, we calculated both the *recall* (i.e. the percentage of texts written by that
460 author that were attributed to him) and the *precision* (i.e. the percentage of texts attributed to
461 that author that were written by him), in addition to a summary F_1 score, which is essentially
462 an average of precision and recall. For each n-gram type, we also calculated the percentage
463 of texts attributed correctly across the entire analysis, although this overall measure of
464 accuracy is imbalanced, as there are nearly twice as many Lincoln texts than Hay texts in
465 the corpus. Across all analyses, we counted ties, where Lincoln and Hay had the same

466 percentage of n-grams seen at 260,000 words (often 0% or 100%), as incorrect attributions
467 for both authors. In addition, we measured the accuracy of two aggregated analyses, where
468 we selected the author returned by the majority of a series of the best performing word- and
469 character-level analyses.

470 We found tracing character-level n-grams to be an especially good way to attribute
471 the writings of Lincoln and Hay (Table 3). Overall, all analyses based on between 5- and 10-
472 grams achieved F_1 scores ≥ 0.95 for both authors, with the best results obtained using 7-
473 and 8-grams. In addition, when we selected the author chosen by a majority of the analyses
474 based on between 4- and 10-grams (i.e. the author returned by at least 4 of these 7
475 analyses), we correctly identified the author of all 1,662 texts. These results clearly attest to
476 the power of n-gram tracing for distinguishing between this set of possible authors and are
477 especially remarkable given the brevity of many of the texts, a majority of which contain
478 fewer than 200 words and 10% of which contain no more than 50 words.

479 We also found tracing word-level n-grams to be good way to attribute the writings of
480 Lincoln and Hay (Table 4), although it was not as accurate as the character-level analysis.
481 Overall, analyses based on between 1- and 3-grams achieved F_1 scores ≥ 0.90 for both
482 authors, with the best results obtained using 2-grams. In addition, when we selected the
483 author chosen by a majority of the analyses based on between 1- and 3-word n-grams (i.e.
484 the author returned by at least 2 of these 3 analyses), we achieved F_1 scores ≥ 0.95 for both
485 authors.

486 **Table 3** Character n-gram Evaluation results

n	Hay			Lincoln			Acc
	Rec	Pre	F ₁	Rec	Pre	F ₁	
1	.43	.96	.59	.12	.99	.21	.23
2	.62	.93	.74	.56	.95	.70	.58
3	.93	.86	.89	.80	.98	.88	.85
4	.98	.91	.94	.93	.99	.96	.95
5	.99	.91	.95	.94	1	.97	.96
6	.99	.93	.96	.96	.99	.97	.97
7	.97	.96	.96	.98	.98	.98	.98
8	.95	.98	.96	.99	.98	.98	.98
9	.94	.98	.96	.99	.97	.98	.97
10	.92	.99	.95	.99	.96	.97	.97
11	.91	.98	.94	.99	.95	.97	.96
12	.89	.98	.93	.99	.94	.96	.96
13	.86	.98	.92	.99	.93	.96	.94
14	.83	.97	.89	.99	.92	.95	.93
15	.79	.97	.87	.99	.90	.94	.92
16	.77	.97	.86	.98	.90	.94	.91
17	.72	.97	.83	.98	.88	.93	.89
18	.68	.95	.79	.96	.89	.92	.86
19	.63	.92	.75	.94	.88	.91	.83
20	.58	.90	.71	.92	.88	.90	.80
4-10	1	1	1	1	1	1	1

487

488

489 **Table 4** Word n-gram Evaluation results

n	Hay			Lincoln			Acc
	Rec	Pre	F ₁	Rec	Pre	F ₁	
1	.96	.91	.93	.93	.98	.95	.94
2	.91	.97	.94	.99	.96	.97	.96
3	.85	.97	.91	.98	.93	.95	.93
4	.69	.94	.80	.94	.90	.92	.85
5	.41	.83	.55	.82	.89	.85	.68
1-3	.93	.98	.95	.99	.97	.98	.97

490

491

492 In addition to identifying the most reliable n-gram types upon which to base our
493 attribution of the *Bixby Letter*, it is important to consider why our analyses of other n-gram
494 types were less accurate. Analyses based on 1- and 2-character n-grams are problematic
495 because these features are far too common in the corpus of possible authors, resulting in a
496 large number of 100% ties, as reflected by the low recall scores for both authors. We
497 therefore excluded 1- and 2- character n-grams from our main analysis of the *Bixby Letter*.
498 Alternatively, analyses based on the longest word and character n-grams are problematic
499 because these features are far too uncommon in the corpus of possible authors. For
500 example, it is entirely possible that only one 5-word n-gram in a questioned document will
501 reoccur anywhere in the corpus of possible authors; in such cases, the attribution will be
502 driven entirely by this one text, potentially leading to unreliable results. We therefore
503 restricted our main analysis of the *Bixby Letter* to n-gram types where at least 5% of the n-
504 grams found in the letter are also found in the writings of Lincoln or Hay

505 We also considered how the performance of n-gram tracing was affected by text
506 length by comparing the length of texts that were successfully and unsuccessfully attributed
507 by each analysis using a series of Wilcoxon signed-rank tests. All n-gram tracing analyses
508 for each author were found to be less successful on shorter texts ($p < 0.001$). For example,
509 the median length of Hay's texts that were successfully attributed by the 7-character n-gram
510 analysis was 160 words, whereas the median length of texts that were unsuccessfully
511 attributed was 115 words. Similarly, the median length of Lincoln's texts that were
512 successfully attributed was 127 words, whereas the median length of texts that were
513 unsuccessfully attributed was 70 words. Despite these differences, n-gram tracing still
514 attributes very short texts written by Lincoln and Hay with a very high degree of accuracy, as
515 our evaluation has shown. For example, attributing texts containing fewer than 100 words
516 using a 7-character n-gram analysis still achieves 0.94 recall for Hay (vs. 0.98 recall for
517 Hay's texts that contain 100 words or more) and 0.96 recall for Lincoln (vs. 0.99 recall for
518 Lincoln's texts that contain 100 words or more). Furthermore, by this standard, the *Bixby*
519 *Letter* is a relatively long text.

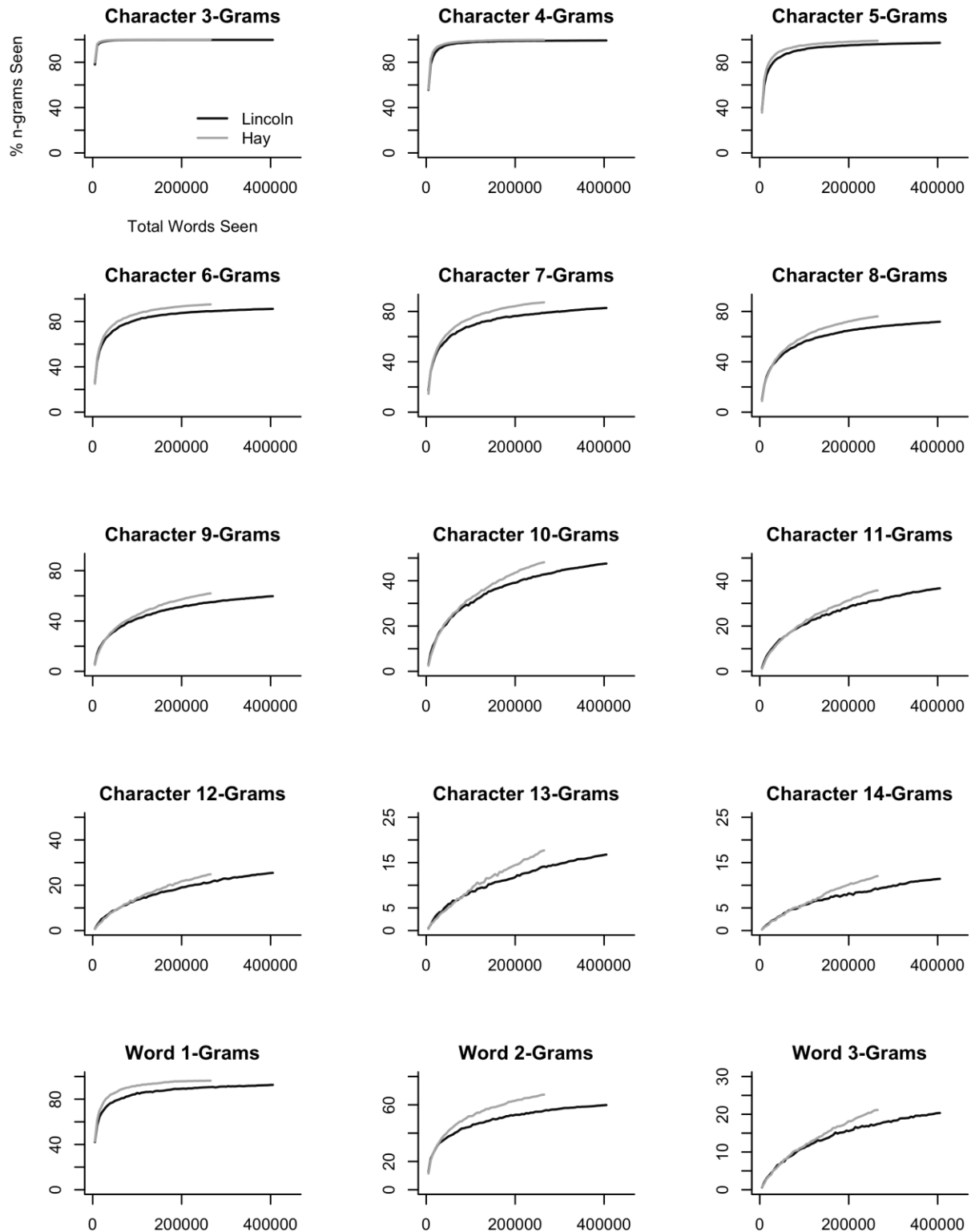
520 In summary, we found that n-gram tracing, based on a range of different n-gram
521 types, is able to distinguish between the known writings of Lincoln and Hay with a very high
522 degree of accuracy, including texts containing fewer than 100 words. We found that the
523 analysis of 4- to 12-character n-grams and 1- to 3-word n-grams was especially useful for
524 distinguishing between Lincoln and Hay. We also found that selecting the author chosen by
525 the majority of the 4- to 10-character analyses attributed all 1,662 texts in our corpus of
526 possible authors perfectly. Based on the results of our evaluation, we are therefore confident
527 using n-gram tracing to investigate whether Lincoln or Hay is more likely to have written the
528 *Bixby Letter*.

529

530 **6. Results**

531 To attribute the *Bixby Letter*, we used n-gram tracing to compare all 1- to 3-word n-grams
532 and all 3- to 16-character n-grams in the *Bixby Letter* to our Lincoln and Hay writing samples
533 based on random samples of approximately 260,000 words. Longer n-gram types were
534 excluded from our analysis because fewer than 5% of the n-grams were found to occur in
535 the Hay and Lincoln corpora. Overall, all 17 of these analyses identify Hay as the author of
536 the *Bixby Letter*. Each of these n-gram tracing analyses (excluding the 15- and 16-character
537 n-gram analyses, which are very similar to traces for the other analyses) are also visualised
538 in Figure 5, based on 50 random sequences of texts for each author, aggregated in
539 increments of 5,000 words. These traces show that clear and consistent differences
540 between Hay and Lincoln are identified by 100,000 words for all word-level analyses and for
541 all character-level analyses from 5 characters onward. The n-gram tracing analysis therefore
542 clearly attributes the *Bixby Letter* to John Hay, providing very strong stylistic evidence
543 against the standard attribution of the letter to Abraham Lincoln.

544 **Figure 5** *Bixby Letter* aggregated n-gram traces



545

546 Although we excluded longer character n-grams from our main attribution, n-gram

547 tracing analyses based on these additional feature sets also attribute the *Bixby Letter* to

548 Hay, as does the 4-word n-gram analysis. The 5-word n-gram analysis, however, attributes

549 the *Bixby Letter* to Lincoln. This attribution is made because ‘may be found in the’ is the only
 550 5-word n-gram out of the 115 unique 5-word n-grams in the *Bixby Letter* that occurs
 551 anywhere in our corpus of possible authors, specifically in a single speech delivered by
 552 Lincoln on the 11th of January 1837 at the Illinois State Assembly:

553 *If any gentleman be entitled to stock in the Bank, which he is kept out of possession*
 554 *of by others, let him assert his right in the Supreme Court, and let him or his*
 555 *antagonist, whichever may be found in the wrong, pay the costs of suit.*

556 This example illustrates the problem that arises when tracing very rare n-gram types: the
 557 entire attribution can be based on a single phrase in a single text, leading to unreliable
 558 results. In light of the preponderance of evidence for Hay, this one result should not diminish
 559 our confidence in the attribution, especially because the meaning of ‘found’ in this passage
 560 is different than in the *Bixby Letter*, where it means ‘discovered’ as opposed to ‘judged’. In
 561 fact, ‘may be found in’ is used twice by Hay, both times with the ‘discovered’ meaning, once
 562 in an 1863 diary entry (‘After every battle Lee may be found in his tent’) and once in *Castilian*
 563 *Days* (‘This custom, more or less modified, may be found in most cities of Europe’).

564 Finally, the n-grams in the *Bixby Letter* that are only used by Lincoln or Hay are
 565 presented in Table 5, of which there are notably fewer for Lincoln despite being drawn from
 566 a much larger corpus. Although their discriminatory value was found to be weaker, it is more
 567 instructive to consider unique word-level n-grams rather than unique character-level n-
 568 grams, because word-level n-grams are less common, more distinctive, and more
 569 interpretable. Thematically, Hay’s unique word sequences appear more evocative and
 570 emotive than Lincoln’s more mundane sequences – the types of constructions one might
 571 expect to find in official letters sent from the Office of the President. For example, Hay’s
 572 unique n-grams often reference emotion (e.g. *anguish, grief*) and religion (e.g. *altar, pray*),
 573 whereas Lincoln’s often reference governmental bureaucracy (e.g. *war department, files*).
 574 Grammatically, Hay’s word sequences tend to contain more forms related to the construction
 575 of complex noun phrases. For example, 66% of Hay’s sequences contain nouns, compared
 576 to 50% for Lincoln, and 49% of Hay’s sequences contain determiners, compared to 32% for

577 Lincoln. Alternatively, Lincoln's word sequences tend to contain more forms related to the
 578 construction of complex verb phrases. For example, 32% of Lincoln's sequences contain
 579 verbs, compared to 14% for Hay, and 18% of Lincoln's sequences contain auxiliaries,
 580 compared to 9% for Hay. Furthermore, 23% of Lincoln's sequences contain pronouns, while
 581 only 9% of the Hay sequences do. Overall, these patterns imply that Hay's style tends to be
 582 more formal than Lincoln's (see Biber 1988). Overall, while far from definitive, this closer
 583 analysis of the tone and structure of the unique n-grams used by each author helps us
 584 obtain a subtler understanding of the basic differences in style detected and revealed
 585 through n-gram tracing.

586 **Table 5** *Bixby Letter* unique word-level n-grams

n	Unique Hay n-grams	Unique Lincoln n-grams
1	<i>adjutant, altar, anguish, beguile, costly</i> (5)	<i>bereavement, tendering</i> (2)
2	<i>a loss, altar of, anguish of, any words, been shown, consolation that, feel how, grief of, have laid, I pray, pride that, sons who, thanks of, the altar, the anguish, the cherished, the consolation, the thanks, weak and</i> (19)	<i>a sacrifice, and fruitless, cannot refrain, father may, files of, mine which, shown in, the loved, war department, yours to</i> (10)
3	<i>and the solemn, but I cannot, from the grief, gloriously on the, thanks of the, the altar of, the anguish of, the consolation that, the grief of, the thanks of, you from the</i> (11)	<i>a statement of, and leave you, and lost and, cannot refrain from, I cannot refrain, of mine which, shown in the, statement of the, the files of, the war department</i> (10)

587

588 7. Conclusion

589 The historical significance of our attribution is clear. The *Bixby Letter* is one of the most
 590 famous and beautiful letters in the history of the United States and, despite on-going
 591 academic debate, it has generally been attributed to Abraham Lincoln, both by historians
 592 and the media. We have demonstrated, however, that the *Bixby Letter* was far more likely to
 593 have been authored by his 26-year-old assistant, John Hay. Assuming that only these two

594 men could have written the *Bixby Letter*, our analysis shows that John Hay was almost
595 certainly its primary author, providing strong linguistic support for the attributions made by
596 Burlingame (1995, 1999) and other historians based primarily on external evidence.

597 Although we believe that our finding should finally lead to the official reattribution of
598 this famous letter to John Hay, it could not detract from Abraham Lincoln's record, which
599 was built upon far greater achievements than the *Bixby Letter*. Nevertheless, this short text
600 is of considerable cultural, historical, and literary significance, and it is therefore important
601 that we can now finally attribute the *Bixby Letter* with confidence to its true author. This study
602 not only rights the historical record, but it should help historians better understand the inner
603 workings of the Lincoln White House, arguably the most important presidency in the history
604 of the United States. In addition, this result should remind us that John Hay was a great
605 writer and a singular statesman, whose unwillingness to take credit for such a famous letter
606 testifies to his humility and his love for Abraham Lincoln. Our attribution might even go some
607 way to repairing the reputation of Mrs Lydia Bixby, for even if she was a Copperhead and a
608 procuress, it is certainly better to have torn up a letter written by a secretary than by the
609 President.

610 In addition to the historical significance of this study, the method introduced in this
611 paper for attributing short texts represents a major step forward for authorship attribution.
612 Short text attribution is considered to be one of the most important and difficult problems in
613 stylometry, and n-gram tracing is a powerful solution to this problem. Our method has been
614 used here not only to attribute the *Bixby Letter*, which contains only 139 words, but over
615 1,600 texts of known authorship in both the Hay and Lincoln cannon, a majority of which are
616 shorter than 200 words and some of which are as short as 5 words. Furthermore, given that
617 n-gram tracing successfully attributed texts from various different genres without taking this
618 information into consideration, it appears that our method may also provide a solution to the
619 problem of cross-genre attribution, another fundamental challenge in stylometry and forensic
620 stylistics. Testing whether or not these types of results can be replicated over other sets of
621 possible authors is the goal of future research, in addition to testing the maximum number of

622 authors between which the method can distinguish and the minimum amount of data needed
623 for each. This is the main limitation of n-gram tracing: to reliably attribute short texts, the
624 method requires access to substantial amounts of training data for each possible author,
625 which is not always possible in historical and forensic contexts. Nevertheless, it seems clear
626 that the method could have resolved this case of disputed authorship based on far less data,
627 as many of the aggregated traces presented in Figure 5 and 6 diverge by 25,000 words.

628 More generally, the success of our method, which is rooted in forensic authorship
629 analysis, shows how insights from forensic linguistics can inform computational research on
630 authorship attribution. At the same time, our results should give forensic linguists pause.
631 This study has shown that manually selecting features, especially rare features, can lead to
632 misleading results. For example, the unique word sequences listed in Table 3 would seem to
633 be good markers of authorship, but this list, and the number of unique n-grams used by each
634 author, is only informative because it is exhaustive, especially as there are almost as many
635 unique forms for Lincoln as there are for Hay. One analyst, like Nickell, might consider the
636 word ‘tendering’, while another analyst, like Burlingame, might consider the word ‘beguile’,
637 and each will honestly come to a different conclusion, while an analyst who considers both
638 forms would come to no conclusion at all. When analysing authorship, it is therefore
639 extremely important to select a representative sample of features that is truly capable of
640 distinguishing between the authors under comparison. We have essentially taken the
641 simplest solution to this problem in this paper, attributing a text by extracting all the features
642 of a particular type that occur within it.

643 Finally, our study offers evidence in support of two theories of language use, outlined
644 in Coulthard (2004), which provide a theoretical foundation for much research in authorship
645 analysis and forensic linguistics. The first is the theory of the *uniqueness of the utterance*,
646 which claims that as sequences of words (or characters) become longer, they become less
647 likely to be repeated. This claim is supported by the results of this study, which shows that
648 the likelihood that a sequence of words or characters found in the *Bixby Letter*, or any of the
649 1,662 texts over which we evaluated our method, is repeated in the possible author writing

650 samples falls as the length of these sequences increases. In particular, n-gram tracing is
651 most successful when it focuses on n-grams of middling lengths, because sequences that
652 are too short tend to be reused by all authors, while sequences that are too long tend to be
653 reused by none. Furthermore, n-gram tracing successfully distinguishes between the
654 writings of Lincoln and Hay precisely because the likelihood of repetition falls at a slower
655 rate for the true author of these texts than for the other author. The second is the theory of
656 *idiolectal co-selection*, which states that an individual's *idiolect* – their underlying system of
657 linguistic knowledge – manifests itself during language production through the unique co-
658 selection of a variety of linguistic features. In other words, although the use of a single
659 linguistic feature is unlikely to be distinctive on its own, the co-occurrence of many features
660 will generally distinguish the linguistic output of individual authors. These co-occurrence
661 patterns are exactly the information upon which n-gram tracing is based, and our
662 unambiguous attribution of the *Bixby Letter* therefore also supports this theory of idiolectal
663 co-selection.

664 Of course, a systematic analysis of the writings of many authors and many registers
665 is needed to demonstrate that the uniqueness of the utterance and idiolectal co-selection
666 hold across the population. These are research questions we are currently pursuing, but the
667 results presented in this paper nevertheless offers initial empirical support for both of these
668 claims. Furthermore, n-gram tracing provides a replicable technique for measuring the
669 distinctiveness of linguistic forms and authorial styles. In addition to offering a solution to the
670 short text attribution problem, n-gram tracing may therefore finally provide linguists with a
671 way for judging the reality of the linguistic individual – a question of central theoretical
672 importance not only to forensic linguistics and stylometry, but many other domains of
673 linguistic inquiry.

674

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